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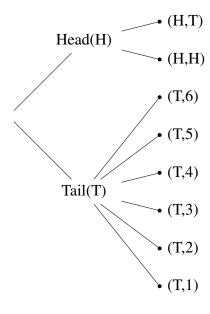
Assignment 6

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Question: Consider the experiment of tossing a coin. If the coin shows head, toss it again but if it shows tail, then throw a die. Find the conditional probability of the event that 'the die shows a number greater than 4' given that 'there is at least one tail'.

Solution:

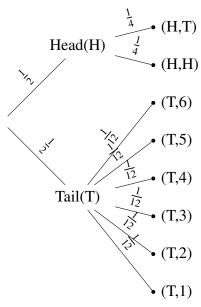
The outcomes of the experiment can be represented in following diagrammatic manner called the 'tree diagram'.



The sample space of the experiment may be described as

$$S = \{(H,H), (H,T), (T,1), (T,2), (T,3), (T,4), (T,5), (T,6)\}$$

Thus, the probabilities assigned to the 8 elementary events (H, H), (H, T), (T, 1), (T, 2), (T, 3) (T, 4), (T, 5), (T, 6) are $\frac{1}{4}$, $\frac{1}{4}$, $\frac{1}{12}$, $\frac{1}{12}$, $\frac{1}{12}$, $\frac{1}{12}$, $\frac{1}{12}$ respectively which is clear from the below given tree diagram.



Let F be the event that 'there is at least one tail' and E be the event 'the die shows a number greater than 4'.

Then

$$F = (H, T), (T, 1), (T, 2), (T, 3), (T, 4), (T, 5), (T, 6)$$
(1)

$$E = (T,5), (T,6) \text{ and } E \cap F = (T,5), (T,6)$$
 (2)

Now

$$P(F) = \sum_{i=1}^{6} P((T, i))$$

$$= \frac{1}{4} + \frac{1}{4} + \frac{1}{12} = \frac{3}{4}$$
(4)

And

$$P(E \cap F)a = P((T,5)) + P((T,6))$$
 (5)

$$=\frac{1}{12} + \frac{1}{12} = \frac{1}{6} \tag{6}$$

hence

$$P(E|F) = \frac{P(E \cap F)}{P(F)} = \frac{\frac{1}{6}}{\frac{3}{4}} = \frac{2}{9}$$
 (7)