

Probability and Random Variables

Assignment

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Question 8(B)

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The vertices of a triangle ABC are A(3,8), B(-1,2) and C (6,-6). Find:

- Slope of BC
- Equation of a line perpendicular to BC and passing through A.

ANSWER:

PART(1)

Let (x_2, y_2) be the co-ordinates of point B(-1,2),
So,

$$x_2 = -1$$

$$y_2 = 2$$

Let (x_3, y_3) be the co-ordinates of point C(6,-6),

So,

$$x_3 = 6$$

$$y_3 = -6$$

To find the slope between two points, we use the slope point formula. For two points, (x_2, y_2) and (x_3, y_3) , the point-slope formula is given by:

$$\text{Slope} = \frac{(y_3 - y_2)}{(x_3 - x_2)}$$

Therefore, the slope of line BC will be given as:

$$\begin{aligned} \text{Slope} &= \frac{(-6) - 2}{(6 - (-1))} \\ &= \frac{-8}{7} \end{aligned}$$

The slope of line BC is $\frac{-8}{7}$.
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PART(2)

Let slope of line perpendicular to BC be Slope(2),
and let slope of line BC be Slope(1)

we know that,

$$\text{Slope}(2) = - \frac{1}{\text{Slope}(1)}$$

$$= \frac{1}{\frac{-8}{7}}$$

$$= 7/8$$

In general case, for a line passing through a point (x_1, y_1) and having a slope m can be given by the equation : $(y - y_1) = m(x - x_1)$

Therefore, the equation of a line passing through The point A(3,8) and having a slope of 7/8 will be given as : $(y - 8) = 7/8(x - 3)$

$$8(y - 8) = 7(x - 3)$$

$$8y - 64 = 7x - 21$$

$$8y - 7x = 43$$

The equation of line perpendicular to BC and passing through A(3,8) is $8y - 7x = 43$
