

## Problem 1: Recursion in the International Math Olympiad!

### Problem Number: P1

In 2017, one of the problems in the prestigious International Math Olympiad had the following recurrence relation:

$$a_{n+1} = \begin{cases} \sqrt{a_n} & \text{if } \sqrt{a_n} \text{ is an integer} \\ a_n + 3 & \text{otherwise} \end{cases}$$

They had to find all values of  $a_0 > 1$  such that the sequence eventually becomes cyclic.

Your problem however, is to simply give  $a_n$  given  $a_0$  and  $n$ .

Input:

The input starts with one line  $t \leq 100$ , denoting the number of test cases.

For each test case, there are two integers  $0 \leq a_0, n \leq 10^6$ .

Output:

For each test case, output  $a_n$

Sample Input	Sample Output
1	1
1 100	17
2 5	

Note: You do not have to use recursion as a solution, but using recursion works.

## Problem 2: Cell Multiplication

### Problem Number: P2

The cells in the superhuman body multiply over time. Let  $w_t, r_t, s_t$  be the number of white blood cells, red blood cells, and supercells at time  $t$ .

Scientists have recently discovered that there is a relationship between the cells, in that we have the following system of equations:

$$\begin{cases} w_{t+1} = w_t + s_t \\ r_{t+1} = r_t + 2w_t + 2s_t \\ s_{t+1} = 3s_t + 3r_t + 3w_t \end{cases}$$

The superhuman cells grow very fast, but fortunately, there is enough space in a superhuman body to have enough space.

Your task as AMC125 students is to find the number of each cell there is at time  $t$  modulo 100, since the number of cells may be too big after a while.

#### Input:

The input starts with one line  $n \leq 100$ , denoting the number of test cases.

For each test case, there is are four integers  $0 \leq t, w_0, r_0, s_0 \leq 10^9$ .

#### Output:

For each test case, output the number of white blood cells, red blood cells, and supercells at time  $t$ .

Sample Input	Sample Output
1 1 1 1 1	2 5 9