Total Marks:80

**Duration: 3Hrs** 

- NB 1. Question No.I is compulsory.
  - 2. Attempt any **three** from the remaining six questions.
  - 3. Figures to the right indicate full marks.

Q1a. If 
$$L\{tsin\omega t\} = \frac{2\omega s}{(s^2 + \omega^2)^2}$$
, find  $L\{\omega tcos\omega t + sin\omega t\}$  [20]

- b. If  $f(z) = (x^2 + axy + by^2) + i(cx^2 + dxy + y^2)$  is analytic, find a,b,c and d
- c. **Find** the Fourier series expansion of  $f(x) = x^3 (-\pi, \pi)$
- d. If the two regression equations are 4x 5y + 33 = 0, 20x 9y 107 = 0 find i) the mean values of x and y
  - ii) the Correlation Coefficient iii) Standard deviation of y if variance of x is 9
- Q2 a. Show that the function is Harmonic and find the Harmonic Conjugate

$$u = cosx coshy - 2xy$$
 [6]

b. Evaluate 
$$\int_0^\infty e^{-t} \left( \int_0^t u^2 \sinh u \cosh u \, du \right) dt$$
 ) using Laplace Transform. [6]

c. Find Fourier Series expansion of 
$$f(x) = x$$
  $-1 < x < 0$   $= x + 2$   $0 < x < 1$  [8]

Q3 a. Find the Analytic function 
$$f(z) = u + iv$$
 if  $u - v = e^x(cosy - siny)$  [6]

b. Find Inverse Z transform of 
$$\frac{5z}{(2z-1)(z-3)}$$
  $\frac{1}{2} < |z| < 3$  [6]

c. Solve the Differential Equation using Laplace transform

$$(D^2 - 2D + 1)y = e^t, y(0) = 2, y'(0) = -1$$
 [8]

- Q4 a. Find the Complex Form of Fourier Series for  $f(x) = \cos \alpha x \ (-\pi, \pi)$  [6]
  - b. Find the Spearman's Rank correlation coefficient between *X* and *Y*. [6]

X	68	64	3758	50	64	80	75	40	55	64
EY	62	58	68	45	81	60	68	48	50	70

c. Find the inverse Laplace transform of i) 
$$\frac{s-1}{s^2+2s+2}$$
 ii)  $\frac{e^{-\pi s}}{s^2(s^2+1)}$  [8]

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Q5 a. Find the 
$$Z\{f(k)\}$$
 where  $f(k) = 4^k$ ,  $k < 0$   
=  $3^k$ ,  $k \ge 0$ 

b. Show that  $\{cosx, cos2x, cos3x, \dots \}$  is orthogonal set over the interval  $[0,2\pi]$ . Construct the corresponding orthonormal set.

[6]

c. Find the bilinear transformation which maps the points z = 1, i, -1 into the points w = i, 0, -i, Hence find the image of |z| < 1.

[8]

Q6 a. Fit a straight line to the given data

[6]

X	10	12	2 15	23	20
Y	14	317	23	25	21

b. Find Inverse Laplace Transform using Convolution theorem  $\frac{1}{(s-2)^3(s+3)}$  [6]

c. Find Half Range Cosine Series for f(x) = sinx in  $(0,\pi)$  and hence deduce that

$$\frac{\pi^2 - 8}{16} = \frac{1}{1^2 \cdot 3^2} + \frac{1}{3^2 \cdot 5^2} + \frac{1}{5^2 \cdot 7^2} + \dots \dots \dots$$
 [8]



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