

Linear Search

```
#include <iostream>
using namespace std;

int main() {
    // Input array
    int arr[] = {3, 5, 7, 9, 11};
    int target = 7; // Element to search
    int n = sizeof(arr) / sizeof(arr[0]); // Calculate array size

    // Iterate through array to find the target
    for (int i = 0; i < n; i++) {
        if (arr[i] == target) {
            cout << "Found at index " << i << endl; // Element found
            break; // Exit loop once found
        }
    }

    return 0;
}

/*
Time Complexity: O(n) - we may have to check each element
Space Complexity: O(1) - no extra space used
*/
```

Binary Search

```
#include <iostream>
using namespace std;

int main() {
    // Array must be sorted for Binary Search
    int arr[] = {2, 4, 6, 8, 10};
    int target = 6;
    int low = 0, high = 4; // Start and end indexes

    // Continue until search space is valid
    while (low <= high) {
        int mid = (low + high) / 2; // Find mid index
        if (arr[mid] == target) {
            cout << "Found at index " << mid << endl;
            break;
        } else if (arr[mid] < target) {
            low = mid + 1; // Search in right half
        } else {
            high = mid - 1; // Search in left half
        }
    }

    return 0;
}
```

```
/*
Time Complexity:  $O(\log n)$  - halving the search space each step
Space Complexity:  $O(1)$ 
*/
```

Bubble Sort

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {5, 3, 8, 4};
    int n = sizeof(arr) / sizeof(arr[0]);    // total elements

    /* ----- Outer loop -----
       After each full pass, the largest
       remaining element "bubbles" to the end */
    for (int i = 0; i < n; ++i) {

        /* ----- Inner loop -----
           Compare pairs (j, j+1) that
           are still unsorted ( $\leq n-i-2$ ) */
        for (int j = 0; j < n - i - 1; ++j) {

            // If current element is bigger than next, swap them
            if (arr[j] > arr[j + 1]) {
                swap(arr[j], arr[j + 1]);
            }
        }

        // Print sorted array
        for (int num : arr) cout << num << " ";
        return 0;
    }

    /*
    (two nested loops over n) Time Complexity:  $O(n^2)$ 
    (in-place swapping) Space Complexity:  $O(1)$ 
    */
```

Selection Sort

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {64, 25, 12, 22, 11};
    int n = sizeof(arr) / sizeof(arr[0]);
```

```

/* Outer loop: step through each index i,      *
 * assuming that position i should hold the    *
 * smallest remaining element in the suffix.   */
for (int i = 0; i < n; ++i) {
    int minIdx = i; // candidate index for minimum

    // Scan the unsorted suffix to find real minimum
    for (int j = i + 1; j < n; ++j) {
        if (arr[j] < arr[minIdx]) {
            minIdx = j;
        }
    }

    // Put the found minimum into correct spot i
    swap(arr[i], arr[minIdx]);
}

for (int num : arr) cout << num << " ";
return 0;
}

/*
(two nested loops)    Time Complexity: O(n²)
(in-place)             Space Complexity: O(1)
*/

```

Insertion Sort

```

#include <iostream>
using namespace std;

int main() {
    int arr[] = {12, 11, 13, 5, 6};
    int n = sizeof(arr) / sizeof(arr[0]);

    /* Treat arr[0..i-1] as a sorted sub-array;      *
     * insert arr[i] into its correct position.      */
    for (int i = 1; i < n; ++i) {
        int key = arr[i]; // element to be inserted
        int j = i - 1;    // last index of sorted part

        // Shift elements right until the spot for key is found
        while (j >= 0 && arr[j] > key) {
            arr[j + 1] = arr[j];
            --j;
        }
        arr[j + 1] = key; // place key
    }

    for (int num : arr) cout << num << " ";
    return 0;
}

```

```

/*
Time Complexity:  $O(n^2)$  worst,  $O(n)$  best (already sorted)
Space Complexity:  $O(1)$ 
*/

```

Merge Sort

```

#include <iostream>
#include <vector>
using namespace std;

/* ----- Helper: merge two sorted halves ----- */
void merge(vector<int>& arr, int l, int m, int r) {
    /* Create temp arrays:
       Left  = arr[l .. m]
       Right = arr[m+1 .. r]
    */
    int n1 = m - l + 1, n2 = r - m;
    vector<int> L(n1), R(n2);
    for (int i = 0; i < n1; ++i) L[i] = arr[l + i];
    for (int j = 0; j < n2; ++j) R[j] = arr[m + 1 + j];

    // Merge back into arr
    int i = 0, j = 0, k = l;
    while (i < n1 && j < n2) {
        arr[k++] = (L[i] <= R[j]) ? L[i++] : R[j++];
    }
    // Copy leftovers (one of these loops will execute 0 times)
    while (i < n1) arr[k++] = L[i++];
    while (j < n2) arr[k++] = R[j++];
}

/* ----- Recursive merge-sort ----- */
void mergeSort(vector<int>& arr, int l, int r) {
    if (l < r) {
        int m = l + (r - l) / 2;    // safe midpoint
        mergeSort(arr, l, m);      // sort left half
        mergeSort(arr, m + 1, r);  // sort right half
        merge(arr, l, m, r);       // merge halves
    }
}

int main() {
    vector<int> arr = {12, 11, 13, 5, 6, 7};

    mergeSort(arr, 0, arr.size() - 1);

    for (int x : arr) cout << x << " ";
    return 0;
}

/*
Time Complexity:  $O(n \log n)$  (divide-and-conquer)
Space Complexity:  $O(n)$  extra (temporary arrays or recursion stack)
*/

```

Quick Sort]

```
#include <iostream>
#include <vector>
using namespace std;

/* Lomuto partition: chooses last element as pivot and
   places it in correct spot, so  $\text{left} \leq \text{pivot} < \text{right}$  */
int partition(vector<int>& a, int low, int high) {
    int pivot = a[high];
    int i = low - 1;    // tracks "last index of smaller element"

    for (int j = low; j < high; ++j) {
        if (a[j] <= pivot) { // belongs on the left
            ++i;
            swap(a[i], a[j]);
        }
    }
    swap(a[i + 1], a[high]); // place pivot
    return i + 1;           // pivot index
}

void quickSort(vector<int>& a, int low, int high) {
    if (low < high) {
        int pi = partition(a, low, high);
        quickSort(a, low, pi - 1); // sort left subarray
        quickSort(a, pi + 1, high); // sort right subarray
    }
}

int main() {
    vector<int> arr = {10, 7, 8, 9, 1, 5};
    quickSort(arr, 0, arr.size() - 1);

    for (int x : arr) cout << x << " ";
    return 0;
}

/*
Time Complexity: average  $O(n \log n)$ , worst  $O(n^2)$  (when pivot poorest)
Space Complexity:  $O(\log n)$  expected (recursion), worst  $O(n)$ 
*/
```

Two-Pointers Technique

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {1, 2, 3, 4, 6};
```

```

int n = sizeof(arr) / sizeof(arr[0]);
int target = 6;

int left = 0, right = n - 1;    // two ends of the sorted array

// Move inward until pointers cross
while (left < right) {
    int sum = arr[left] + arr[right];

    if (sum == target) {        // pair found
        cout << arr[left] << " " << arr[right] << endl;
        break;
    } else if (sum < target) {    // need bigger sum → move left
        ++left;
    } else {                    // need smaller sum → move right
        --right;
    }
}
return 0;
}

/*
Time Complexity: O(n)
Space Complexity: O(1)
*/

```

Sliding Window

```

#include <iostream>
using namespace std;

int main() {
    int arr[] = {1, 4, 2, 10, 23, 3, 1, 0, 20};
    int n = sizeof(arr) / sizeof(arr[0]);
    int k = 3;                                // window size

    // Compute sum of first window [0..k-1]
    int windowSum = 0;
    for (int i = 0; i < k; ++i) windowSum += arr[i];

    int maxSum = windowSum;                   // initialize answer

    // Slide window: add next element, subtract exiting element
    for (int i = k; i < n; ++i) {
        windowSum += arr[i] - arr[i - k];
        maxSum = max(maxSum, windowSum);    // track best
    }

    cout << maxSum << endl;
    return 0;
}

/*
Time Complexity: O(n)

```

```
Space Complexity: O(1)
*/
```

Kadane's Algorithm

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {-2, 1, -3, 4, -1, 2, 1, -5, 4};
    int n = sizeof(arr) / sizeof(arr[0]);

    int maxEndingHere = arr[0];    // best subarray ending at index i
    int maxSoFar = arr[0];        // best subarray seen overall

    for (int i = 1; i < n; ++i) {
        // Extend previous subarray or start new at i
        maxEndingHere = max(arr[i], maxEndingHere + arr[i]);
        maxSoFar = max(maxSoFar, maxEndingHere);
    }

    cout << maxSoFar << endl;    // maximum subarray sum
    return 0;
}

/*
Time Complexity: O(n)
Space Complexity: O(1)
*/
```

Prefix Sum

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {1, 2, 3, 4, 5};
    int n = sizeof(arr) / sizeof(arr[0]);

    int prefix[n + 1];    // prefix[0] = 0, prefix[i] = sum up to i-1
    prefix[0] = 0;

    // Build prefix array
    for (int i = 0; i < n; ++i) {
        prefix[i + 1] = prefix[i] + arr[i];
    }

    // Example: sum of subarray [1, 3] (2 + 3 + 4) = prefix[4] - prefix[1]
    cout << prefix[4] - prefix[1] << endl;    // prints 9
    return 0;
}
```

```

/*
Time Complexity: O(n) to build, O(1) per range query
Space Complexity: O(n) for prefix array
*/

```

Flood Fill (DFS)

```

#include <iostream>
using namespace std;

const int ROW = 3, COL = 3;

/* Recursive DFS: recolor connected components that match origColor */
void floodFill(int grid[ROW][COL], int r, int c,
               int newColor, int origColor) {

    // Out-of-bounds OR cell doesn't match original color → stop
    if (r < 0 || c < 0 || r >= ROW || c >= COL || grid[r][c] != origColor)
        return;

    grid[r][c] = newColor;           // paint current cell

    // Recurse 4-directionally (up, down, left, right)
    floodFill(grid, r + 1, c, newColor, origColor);
    floodFill(grid, r - 1, c, newColor, origColor);
    floodFill(grid, r, c + 1, newColor, origColor);
    floodFill(grid, r, c - 1, newColor, origColor);
}

int main() {
    int grid[ROW][COL] = { {1, 1, 1},
                           {1, 1, 0},
                           {1, 0, 1} };

    int startR = 1, startC = 1;
    floodFill(grid, startR, startC, 2, grid[startR][startC]);

    // Print result
    for (int i = 0; i < ROW; ++i) {
        for (int j = 0; j < COL; ++j) cout << grid[i][j] << " ";
        cout << endl;
    }
    return 0;
}

/*
Time Complexity: O(n×m) – visits every cell at most once
Space Complexity: O(n×m) worst (recursion stack in deepest cases)
*/

```