

# Basic Overview of ML

## ◆ SML has an Interactive compiler: *read-eval-print*

- Expressions are type checked, compiled and executed
- Compiler infers type before compiling or executing

## ◆ Examples

- (5+3)-2;

> val it = 6 : int      "it" is an id bound to the value of last exp

- if 5>3 then "Big" else "Small";

> val it = "Big" : string

- val greeting = "Hello";

> val greeting = "Hello" : string

- See Pucella 1.6. "Getting started"
- Note: to read in a file with sml code  
– use "filename.sml";

- ◆ Can also use \_ in declarations if we don't care about the value being matched

- fun hd(x::xs) = x ;  
- fun hd(x::\_) = x ;

- ◆ Patterns
- ◆ Declarations
- ◆ Functions
- ◆ Type declarations
- ◆ Reference Cells
- ◆ Polymorphism
- ◆ Overloading
- ◆ Exceptions

# Overview by Type

- ◆ Basic Types
  - Unit (unit)
  - Booleans (bool)
  - Integers (int)
  - Strings (string)
  - Characters (char)
  - Reals (real)
  - Tuples
  - Lists
  - Records

## ◆ Booleans

- true, false : bool
- if ... then ... else ... types must match; "else" is mandatory

## ◆ Integers

- 0, 1, 2, ... ~1, ~2, ... : int .
- +, -, \*, div ... : int \* int → int .
- =, <, <=, >, <= : int \* int -> bool .
- (op >) turns the infix operator > into a function: 1 < 5 but (op <)(1,5)

## ◆ Strings

- "Universitetet i Oslo" : string
- "Universitetet" ^ " i " ^ "Oslo"

## ◆ Char

- #"a"

## ◆ Reals

- 1.0, 2.2, 3.14159, ... decimal point used to disambiguate
- No '=' operator for reals 1.0 = 1.0 → Error
- Cannot combine reals and ints, no coercion. 1.0 + 2 → Error

# Overview by Type

## ◆ Unit

- `() : unit` similar to void in C

## ◆ Tuples

- `(1, 2) : int * int ;`
- `(4, 5, "ha det!") : int * int * string;`
- `#3(4, 5, "ha det!")`  
`> val it = "ha det" : string`

## ◆ Records

- Are tuples with labeled fields:
- `{name="Jones", age=34} : {name: string, age: int};`
- `#name({name="Jones", age=34}); > val it = "Jones" : string`
- **Order does not matter:**  
`{name="Jones", age=34} = {age=34, name="Jones"}; → true`  
`("Jones",34) = (34,"Jones") → Error.`

## ◆ Lists

- `nil;`
- `1 :: nil ;`
- `1::(2::(3::(4::nil)))`
- `1 :: [2, 3, 4];` infix cons notation  
`> val it = [1,2,3,4] : int list`
- `[1,2] @ [3,4]` append  
`> val it = [1,2,3,4] : int list`

## ◆ Basic Types

- Unit (unit)
- Booleans (bool)
- Integers (int)
- Strings (string)
- Characters (char)
- Reals (real)
- Tuples
- Lists
- Records

# Declarations (Value)

## ◆ val keyword, type annotations

- val mypi = 3.1415;     > val mypi = 3.1415 : real
- val name : string = "Gerardo";     > val name = "Gerardo" : string

## ◆ Patterns can be used in place of identifiers (more later)

<pat> ::= <id> | <tuple> | <cons> | <record> | <constr>

## ◆ Value declarations

- General form : val <pat> = <exp>
- Examples:
  - val myTuple = ("Carlos", "Johan");
  - val (x,y) = myTuple;
  - val myList = [1, 2, 3, 4];
  - val x::rest = myList;
- Local declarations
  - let val x = 2+3 in x\*4 end;
  - > val it = 20 : int

# Functions

## ◆ Function declaration

- Functions are as other values:
  - `fn x => x * 2 ;` "anonymous function"
  - > `val it = fn : int -> int`
  - `val dbl = fn x => x * 2 ;` > `val dbl = fn : int -> int`
- But we have a special syntax for defining functions:
  - `fun dbl x = x * 2 ;` > `val dbl = fn : int -> int`

## ◆ Function declaration, general form

- `fun f (<pattern>) = <expr>`
  - `fun f (x,y) = x+y;` Must match pattern (x,y)
- `fn <pattern> => <expr>`
  - `fn (x,y) => x+y;` Anonymous function

## ◆ Multiple-clause definition

- `fun <name> <pat1> = <exp1> | ...`  
| `<name> <patn> = <expn>`
  - `fun length (nil) = 0`  
| `length (x::s) = 1 + length(s);`  
> `val length = fn 'a list -> int`
  - `length ["J", "o", "n"]` > `val it = 3 : int`

### Insert an element in an ordered list:

```
fun insert (e, nil) = [e]
| insert (e, x::xs) = if e>x then x :: insert(e,xs)
                      else e::(x::xs);
- insert (3,[1,2,5]) ;
> val it = [1,2,3,5] : int list
```

### Append lists:

```
fun append(nil, ys) = ys
| append(x::xs, ys) = x :: append(xs, ys);
- append ([3,4],[1,2]) ;
>val it = [3,4,1,2] : int list
```

# Declarations (Type)

## ◆ Enumeration types

- `datatype color = Red | Yellow | Blue;`
  - elements are: `Red, Yellow, Blue` <- Constructors!

## ◆ Tagged union types

- `datatype value = I of int | R of real | S of string;`
  - elements are: `I(9) , R(8.3) , S("hello") ...`
- `datatype keyval = StrVal of string * string | IntVal of string * int ;`
  - elements are: `StrVal("foo","bar") , IntVal("foo",55) ...`
- `datatype mylist = Nil | Cons of value * mylist`
  - elements are: `Nil , Cons (I(8) ,Nil) , Cons (R(1.0), Cons (I (8), Nil))`

## ◆ General form

`datatype <name> = <clause> | ... | <clause>`  
`<clause> ::= <constructor> | <constructor> of <type>`

## ◆ We use *datatype* to define new types, and *type* to define an alias for a type:

- `type int_pair = int * int ;`

## ◆ And we can force to use the type alias:

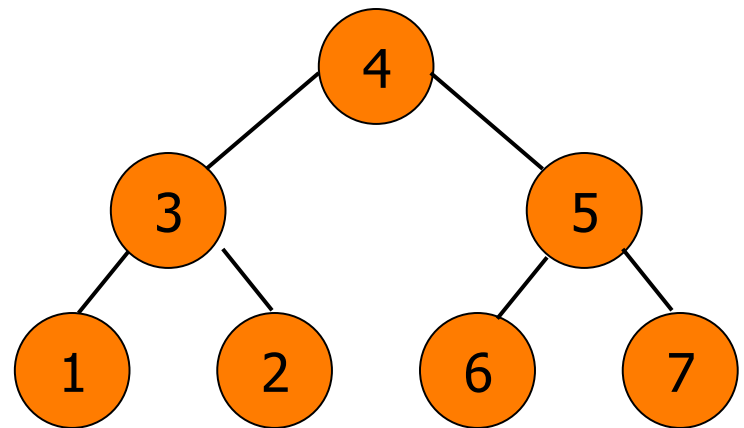
- |  |  |
|--|--|
| - <code>val a = (3,5);</code>            | - <code>val a : int_pair = (3,5);</code> |
| > <code>val a = (3,5) : int * int</code> | > <code>val a = (3,5) : int_pair</code>  |

# Datatype & Pattern matching

## ◆ Recursively defined data structure

- datatype tree = Leaf of int | Node of int\*tree\*tree;

```
Node(4, Node(3,Leaf(1), Leaf(2)),  
      Node(5,Leaf(6), Leaf(7))  
)
```



## ◆ Recursive function (sum)

- fun sum (Leaf n) = n

| sum (Node(n,t1,t2)) = n + sum(t1) + sum(t2);

# Case expression

## ◆ Datatype

- datatype exp = Num of int | Var of var | Plus of exp\*exp;

## ◆ Case expression

case e of Num(i) => ... |

Var(v) => .... |

Plus(e1,e2) => ...

- fun eval(e) = case e of Num(i) => i  
| Var(v) => lookUp(v)  
| Plus(e1,e2) => eval(e1) + eval(e2)

## ◆ Case matching is done in order

## ◆ Use \_ to catch all missing

- fun bintoString(i) = case i of 0 => "zero"  
| 1 => "one"  
| \_ => "illegal value";

> val bintoString = fn : int -> string



# insert: Three “different” declarations

1. 

```
fun insert (e, ls) =  
  case ls of nil => [e]  
           | x::xs => if e>x then x::insert(e, xs) else  
e::ls ;
```
2. 

```
fun insert (e, nil)  = [e]  
  | insert (e, x::xs) = if e>x then x::insert(e, xs)  
                        else e::(x::xs) ;
```
3. 

```
fun insert (e: int, ls: int list) : int list =  
  case ls of nil  => [e]  
           | x::xs => if e>x then x::insert(e, xs) else  
e::ls ;
```

# ML imperative constructs

## ◆ None of the constructs seen so far have side effects

- An expression has a value, but evaluating it does not change the value of any other expression

## ◆ Assignment

- Different from other programming languages:

To separate side effects from pure expressions as much as possible

- Restricted to *reference cells*

# Variables and assignment

## ◆ General terminology: L-values and R-values

- Assignment (pseudocode, not ML!)  $y := x+3;$ 
  - Identifier on left refers to a *memory location*, called L-value
  - Identifier on right refers to *contents*, called R-value

## ◆ Variables

- Most languages
  - A variable names a storage location
  - Contents of location can be read, can be changed
- ML reference cell (L-value)
  - A reference cell has a different type than a value
  - Explicit operations to read contents or change contents
  - Separates naming (declaration of identifiers) from “variables”

# ML reference cells

## ◆ Different types for location and contents

<code>x : int</code>	non-assignable integer value
<code>y : int ref</code>	location whose contents must be integer

## ◆ Operations

<code>ref x</code>	expression creating new cell containing value x
<code>!y</code>	returns the contents (value) of location y
<code>y := x</code>	places value x in reference cell y

## ◆ Examples

- `val x = ref 0 ;` create cell x with initial value 0
- > `val x = ref 0 : int ref`
- `x := x+3;` place value of x+3 in cell x; requires `x:int`
- > `val it = () : unit` (type is "unit" since it is an expression with side effects)
- `x := !x + 3;` add 3 to contents of x and store result in location x
- > `val it = () : unit`
- `!x;` > `val it = 6 : int`

# ML examples

## ◆ Create cell and change contents

- `val x = ref "Bob";`
- `x := "Bill";`



## ◆ Create cell and increment

- `val y = ref 0;`
- `y := !y + 1;`
- `y := y + 1`      **Error!**



## ◆ In summary:

- `x : int`      not assignable (like constant in other PL)
- `y : int ref`      assignable reference cell

# Imperative programming in ML

```
val i = ref 0;  
while !i < 5 do  
  (i := !i + 1 ;  
   print("i is :" ^ Int.toString(!i) ^ "\n")  
  );
```

## ◆ References

## ◆ In ML you evaluate a **series of expressions**

- By evaluating  $(e_1; e_2; \dots; e_n)$ , the expressions  $e_1$  to  $e_n$  are evaluated from left to right
- The result is the value of  $e_n$ . The other values are discarded

## ◆ While command : while e1 do e2

- **while e1 do e2**  $\equiv$  **if e1 then (e2; while e1 do e2) else () ;**

## ◆ **print : string -> unit**

- print returns **it : ()** but has a side effect.

# More on list functions

- ◆ Writing a recursive function is not difficult, but what about efficiency?

- ◆ Example: Reverse a list  
(remember  $[1,2] @ [3,4] = [1,2,3,4]$ )

```
fun rev [] = []  
  | rev (x::xs) = (rev xs) @ [x] ;
```

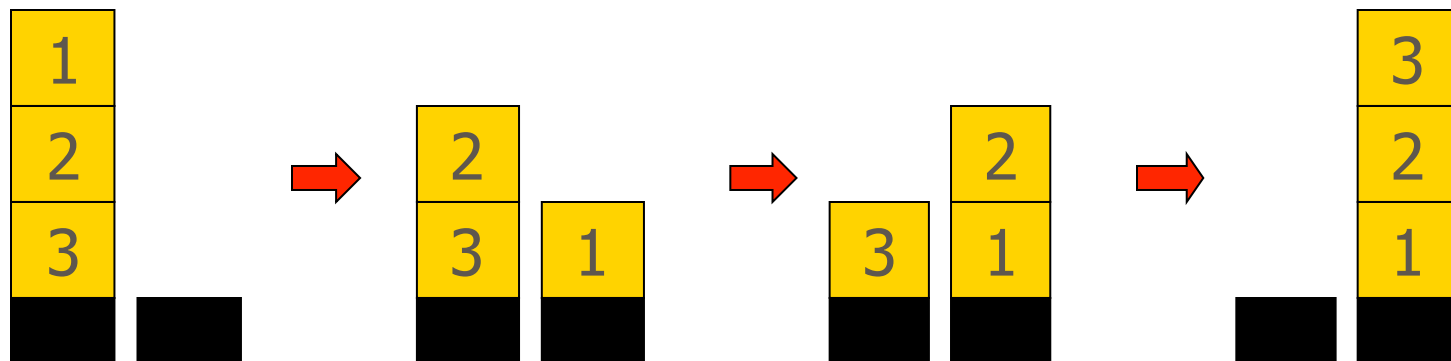
- ◆ Questions
  - How efficient is reverse?
  - Can you do this with only one pass through list?

# More efficient reverse function

```
fun revAppend ([],ys) = ys  
  | revAppend (x::xs,ys) = revAppend(xs,(x::ys)) ;
```

```
fun rev xs = revAppend(xs,[]);
```

Tail recursive function!





# Two factorial functions

## ◆ Standard recursion

- fun fact n =  
    if n = 0 then 1 else n \* fact(n-1) ;

## ◆ Tail recursive (iterative)

- fun facti(n,p) =  
    if n = 0 then p else facti(n-1,n\*p) ;
- fun fact n = facti(n,1) ;

## ◆ More examples in Pucella sec. 2.7

# Monomorphism vs. Polymorphism

- ◆ *Monomorphic* means “having only one form”, as opposed to *Polymorphic*
- ◆ A type system is **monomorphic** if each constant, variable, etc. has unique type
- ◆ Variables, expressions, functions, etc. are **polymorphic** if they “allow” more than one type

Example. In ML, the *identity* function `fn x => x` is polymorphic: **it has infinitely many types!**

- `fn x => x`

> `val it = fn : 'a -> 'a`

**Warning!** The term “polymorphism” is used with different specific technical meanings (more on this in ML-lecture 3)

# Higher-order functions (functionals)

- ◆ In ML functions are computational values ("first-class objects")
  - can be constructed during execution
  - stored in data structures
  - passed as arguments to other functions
  - returned as values

*A functional is a function that operates on other functions*

- ◆ Programs are more concise and clear when using functionals
- ◆ Functionals on lists have been very popular in Lisp
- ◆ The use of functionals is a powerful tool for *modularisation* which is what gives FPLs one of its conceptual advantages (Hughes 1984)

# Higher-order functions (functionals)

## ◆ Map: apply a function to every element in a list

- fun map (f, nil) = nil


| map (f, x::xs) = f(x) :: map (f,xs);

> val map = fn : ('a -> 'b) \* 'a list -> 'b list

- fun incr x = x+1 ;

> val incr = fn : int -> int

- map (incr, [1,2,3]);            [2,3,4]

- map (fn x => x\*x, [1,2,3]);            [1,4,9]

# Higher-order functions (functionals)

## ◆ Map: apply a function to every element in a list

- fun map (f, nil) = nil

| map (f, x::xs) = f(x) :: map (f,xs);

> val map = fn : ('a -> 'b) \* 'a list -> 'b list

- fun bintoString(i) =

case x of 0 => "zero"

| 1 => "one"

| \_ => "illegal value";

> val bintoString = fn : int -> string

- map (bintoString , [1,0,2,0]);

> val it = ["one","zero","illegal value","zero"] : string list

# Higher-order functions (functionals)

◆ **filter**: apply a predicate to every element of list

- fun filter (p, nil) = nil

| filter (p, (x::xs)) = if p(x) then x :: (filter (p,xs))  
else filter (p,xs) ;

- val odd = fn : int -> bool

- val mylist = [1,2,3,4,5,6,7,8];

- filter (odd, mylist);

> val it = [1,3,5,7] : int list

- map (fn x => x\*x, (filter(odd,mylist)));

> val it = [1,9,25,49] : int list

- val pairs = [(1,2),(4,3),(8,9),(0,9),(0,0),(5,1)] ;

- filter ((op <) , pairs);

> val it = [(1,2),(8,9),(0,9)] : (int \* int) list

# Curried functions

- ◆ A function can have only one argument
  - tuples are used for more than one argument
- ◆ Multiple arguments may be realized by giving a function as a result
  - *Currying* -> after the logician Haskell B. Curry
- ◆ A function over pairs has type
$$'a * 'b \rightarrow 'c$$
while a curried function has type
$$'a \rightarrow ('b \rightarrow 'c)$$
- ◆ A curried function allows *partial application*: applied to its 1st argument (of type  $'a$ ), it results in a function of type  $'b \rightarrow 'c$

# Curried functions

## ◆ Example: function to add two numbers

```
- fun pluss (x,y) = x + y ;  
> val pluss = fn : int * int -> int  
- pluss (2,3) ;  
➤ val it = 5 : int
```

## ◆ Curried version of the same function

```
- fun cPluss x y = x + y ;  
> val cPluss = fn : int -> int -> int  
- cPluss 2 3 ;  
> val it = 5 : int  
- val addTwo = cPluss 2 ;  
> val addTwo = fn : int -> int  
- addTwo 5 ;  
> val it = 7 : int
```



# Curried functions

## ◆ Curry and uncurry

- fun curry f x y = f (x,y) ;

> val curry = fn : ('a \* 'b -> 'c) -> 'a -> 'b -> 'c

- fun uncurry f (x,y) = f x y ;

> val uncurry = fn : ('a -> 'b -> 'c) -> 'a \* 'b -> 'c

# Example: the map function

- ◆ Recall that map can be defined as

```
fun map (f, nil) = nil
```

```
| map (f, x::xs) = f(x) :: map (f,xs);
```

```
> val map = fn : ('a -> 'b) * 'a list -> 'b list
```

```
- map (fn x => x+1, [1,2,3]);
```

```
> val it = [2,3,4] : int list
```

- ◆ By currying it, we can define map as

```
fun map f nil = nil
```

```
| map f (x::xs) = (f x) :: map f xs;
```

```
> val map = fn : ('a -> 'b) -> 'a list -> 'b list
```

```
- map (fn x => x+1) [1,2,3];
```

```
> val it = [2,3,4] : int list
```

# More on the map function

- ◆ We can have a function having as argument a function which has another function as an argument
- ◆ Thanks to currying, we can combine functionals to work on lists of lists

Example:

```
- map (map (fn x => x+1)) [[1], [1,2], [1,2,3]];
```

```
→ [ map (fn x => x+1) [1], map (fn x => x+1)[1,2], map (fn x => x+1)[1,2,3]]
```

```
→ [ [2], [2,3], [2,3,4]]
```

What does it give as a result?

```
> val it = [[2],[2,3], [2,3,4]] : int list list
```

# Equality

- ◆ Equality in (S)ML is defined for many types but not all – E.g., it is defined for:
  - Integers
  - Booleans
  - Strings
  - Characters
- ◆ What about floating points (reals), compound types (tuples, records, lists), functions, abstract data types, etc?

# Equality

## ◆ When are two expressions equal?

- The so-called *Leibniz's Principle of the Identity of Indiscernables*:

"e1 and e2 are **equal** iff they cannot be distinguished by any operation in the language"

"e1 and e2 are **distinct** iff there is some way to tell them apart"

## ◆ What is difficult about Leibniz's Principle?

# Problems with Equality

- ◆ Equality, as defined by Leibniz's principle, is **undecidable**

**In general, there is no program which determines whether two expressions are equal in Leibniz's sense.**

Also:

- ◆ Problems with reference cells (aliasing)

```
- val s = ref 1 ; val t = ref 1 ;  
- s = t ;                > false  
- !s = !t                > true  
- val s = t ;  
- s = t ;                > true
```

- ◆ Polymorphic equality complicates the compiler

# Equality Types

- ◆ An **equality type** is a type admitting equality test
- ◆ Types admitting equality in (S)ML
  - *int, bool, char, string*
  - *tuples* and *records*, if all their components admit equality
  - *datatypes*, if every constructor's parameter admits equality
  - *lists* admit equality if the underlying element type admits equality
    - Two lists are equal if they have the same length and the same elements in corresponding positions

# Equality Types (cont.)

## ◆ Do **not** admit equality in (S)ML

- *reals*
- *functions*
- *tuples, records and datatypes* not mentioned in the previous slide
- *abstract data types*

## ◆ Equality type variable: "a

- fun equals (x,y) = if x = y then true else false ;
- > stdIn:7.25 Warning: calling polyEqual
- val equals = fn : "a \* "a -> bool



# Equality: Examples

- ◆ Equality tests on functions is not computable since
$$f = g \text{ iff for all } x, f(x) = g(x)$$
- ◆ No “standard” notion of equality for an abstract type
  - What is supposed to be the equality on *trees*? Is it defined structurally? Is it over the list of their elements? By DFS or BFS?

◆ Ex:

```
fun find x nil = false
  | find x (y :: ys) = x = y orelse find x ys ;
```

```
> = stdIn:30.31 Warning: calling polyEqual
val find = fn : "a -> "a list -> bool
```

(don't worry, only a performance issue)

# Modularity: Basic Concepts

## ◆ Component

- Meaningful program unit
  - Function, data structure, module, ...

## ◆ Interface

- Types and operations defined within a component that are visible outside the component

## ◆ Specification

- Intended behavior of component, expressed as property observable through interface

## ◆ Implementation

- Data structures and functions inside component

# Example: Function Component

## ◆ Component

- Function to compute square root

## ◆ Interface

- function `sqrt (float x)` returns float

## ◆ Specification

- If  $x > 1$ , then  $\text{sqrt}(x) * \text{sqrt}(x) \approx x$ .

## ◆ Implementation

```
float sqroot (float x){  
    float y = x/2; float step=x/4; int i;  
    for (i=0; i<20; i++){if ((y*y)<x) y=y+step; else y=y-step; step = step/2;}  
    return y;  
}
```

# Something on ML Modules

- ◆ Signatures and structures are part of the standard *ML module system*
- ◆ An ML structure is a module, which is a collection of:
  - Types
  - Values
  - Structure declarations
- ◆ Signatures are module interfaces
  - Kind of “type” for a structure

# Example: Point

## ◆ Signature definition (Interface)

```
signature POINT =  
sig  
  type point  
  val mk_point : real * real -> point (*constructor*)  
  val x_coord : point -> real          (*selector*)  
  val y_coord : point -> real          (*selector*)  
  val move_p : point * real * real -> point  
end;
```

# Example: Point (cont.)

## ◆ Structure definition (Implementation)

```
structure pt : POINT =  
  struct  
    type point = real * real  
    fun mk_point(x,y) = (x,y)  
    fun x_coord(x,y) = x  
    fun y_coord(x,y) = y  
    fun move_p((x,y):point,dx,dy) = (x+dx, y+dy)  
  end;
```

- ## ◆ To be able to use the implementation:
- open pt;

# Example: Point (cont.)

**Open the structure by writing open <structname>**

```
- open pt;
```

...

**After that you may use the struct operations**

```
- val p1 = mk_point(4.3, 6.56);  
> val p1 = (4.3,6.56) : point  
- y_coord (p1);  
> val it = 6.56 : real  
- move_p (p1, 3.0, ~1.0);  
> val it = (7.3,5.56) : point
```

**You may use the struct without opening it by prefixing a function with the struct name.**

```
- pt.mk_point(1.0,1.0);  
> val it = (1.0,1.0) : point
```

**E.g. we would like to use the min function to get the smallest of two ints.**

```
- min(1,2);  
> stdIn:1.1-1.4 Error: unbound variable or constructor: min
```

**The function is defined in the Int struct so we must use Int as a prefix**

```
- Int.min(1,2);  
> val it = 1 : int
```

See: <http://www.smlnj.org/doc/basis/pages/sml-std-basis.html> for an overview of the structures and signatures in The Standard ML Basis Library. Follow the link: [Top-level Environment](#) to see which functions are available in the top level environment, i.e. which you can use without prefixes.

# Type

A **type** is a collection of computational entities sharing some common property

## ◆ Examples

- Integers
- $[1 \dots 100]$
- Strings
- $\text{int} \rightarrow \text{bool}$
- $(\text{int} \rightarrow \text{int}) \rightarrow \text{bool}$

## ◆ “Non-examples”

- $\{3, \text{true}, 5.0\}$
- Even integers
- $\{f:\text{int} \rightarrow \text{int} \mid \text{if } x > 3 \text{ then } f(x) > x * (x + 1)\}$

Distinction between types and non-types is language dependent



# Uses for types

## ◆ Program organization and documentation

- Separate types for separate concepts
  - E.g., customer and accounts (banking program)
- Types can be checked, unlike program comments

## ◆ Identify and prevent errors

- Compile-time or run-time checking can prevent meaningless computations such as `3 + true` - “Bill”

## ◆ Support optimization

- Short integers require fewer bits
- Access record component by known offset

# Type errors

## ◆ Hardware error

- Function call `x()` (where `x` is not a function) may cause jump to instruction that does not contain a legal op code
  - If `x = 512`, executing `x()` will jump to location 512 and begin execute “instructions” there

## ◆ Unintended semantics

- `int_add(3, 4.5)`: Not a hardware error, since bit pattern of float 4.5 can be interpreted as an integer

# General definition of type error

- ◆ A *type error* occurs when execution of program is not faithful to the intended semantics
- ◆ Type errors depend on the concepts defined in the language; **not** on **how** the program is executed on the underlying software
- ◆ All values are stored as sequences of bits
  - Store 4.5 in memory as a floating-point number
    - Location contains a particular bit pattern
  - To interpret bit pattern, we need to know the type
  - If we pass bit pattern to integer addition function, the pattern will be interpreted as an integer pattern
    - Type error if the pattern was intended to represent 4.5

# Subtyping

- ◆ **Subtyping** is a relation on types allowing values of one type to be used in place of values of another
  - **Substitutivity:** If  $A$  is a subtype of  $B$  ( $A <: B$ ), then any expression of type  $A$  may be used without type error in any context where  $B$  may be used
- ◆ In general, if  $f: A \rightarrow B$ , then  $f$  may be applied to  $x$  if  $x: A$ 
  - Type checker: If  $f: A \rightarrow B$  and  $x: C$ , then  $C = A$
- ◆ In languages with subtyping
  - Type checker: If  $f: A \rightarrow B$  and  $x: C$ , then  $C <: A$

Remark: **No subtypes in ML!**

# Type safety

- ◆ A Prog. Lang. is *type safe* if no program can violate its type distinction
  - E.g. use an integer as a function
  - Access memory not allocated to the program.
- ◆ Examples of not type safe language features:
  - Type casts (a value of one type used as another type)
    - Use integers as functions (jump to a non-instruction or access memory not allocated to the program) (C)
  - Pointer arithmetic
    - $*(p)$  has type A if p has type A\*
    - $x = *(p+i)$  what is the type of x?
  - Explicit deallocation and dangling pointers
    - Allocate a pointer p to an integer, deallocate the memory referenced by p, then later use the value pointed to by p

# Relative type-safety of languages

- ◆ **Not safe:** BCPL family, including C and C++
  - Casts; pointer arithmetic
- ◆ **Almost safe:** Algol family, Pascal, Ada.
  - Explicit deallocation; dangling pointers
    - No language with explicit deallocation of memory is fully type-safe
- ◆ **Safe:** Lisp, ML, Smalltalk, Java, Haskell
  - Lisp, Smalltalk: dynamically typed
  - ML, Haskell, Java: statically typed

# Compile-time vs. run-time checking

- ◆ Lisp uses run-time type checking
  - (car x)    check first to make sure x is list
- ◆ ML uses compile-time type checking
  - f(x)       must have  $f : A \rightarrow B$  and  $x : A$
- ◆ Basic tradeoff
  - Both prevent type errors
  - Run-time checking slows down execution (compiled ML code, up to 4 times faster than Lisp code)
  - Compile-time checking restricts program flexibility
    - Lisp list: elements can have different types
    - ML list: all elements must have same type
- ◆ Combination of Compile/Run-time eg. Java
  - Static type checking to distinguish arrays and integers
  - Run-time checking to detect array bounds errors

# Compile-time type checking

- ◆ **Sound** type checker: no program with error is considered correct
- ◆ **Conservative** type checker: some programs without errors are considered to have errors
- ◆ Static typing is always conservative
  - if (possible-infinite-run-expression)
  - then (expression-with-type-error)
  - else (expression-with-type-error)

Cannot decide at compile time if run-time error will occur  
(from the undecidability of the Turing machine's halting problem)