

```

1  # coding: utf-8
2
3  import numpy as np
4  import math
5
6  def Leg_pol(n,x):
7      if n < 0:
8          print 'n cannot be less than 0!!!'
9          return None
10     elif n == 0: return 1
11     elif n == 1: return x
12     else:
13         P_0 = 1; P_1 = x; P_2 = 0
14         for i in range(1,n):
15             P_2 = (P_1 * x * (2*i + 1) - P_0 * i) / float(i + 1)
16             P_0 = P_1; P_1 = P_2
17         return P_2
18
19  def Leg_pol_list(n,x):
20      tmp = [1, x]
21      for i in range(1,n+1):
22          tmp.append(((2*i+1) * x * tmp[i] - tmp[i-1] * i) / float(i + 1))
23      return tmp
24
25  def Leg_pol_der(n,x):
26      P = Leg_pol_list(n,x)
27      return n / (1 - x**2) * (P[n-1] - x * P[n])
28
29  def Leg_roots(n):
30      roots = [math.cos(math.pi * (4*i-1) / float(4*n+2)) for i in range(1,n+1)]
31      norm0 = 0; norm = np.linalg.norm(roots)
32      while abs(norm - norm0) > 0.000000001:
33          norm0 = norm
34          roots = [item - Leg_pol(n,item)/Leg_pol_der(n,item) for item in roots]
35          norm = np.linalg.norm(roots)
36      return roots
37
38  def Gauss_weights(n):
39      roots = Leg_roots(n)
40      weights = [2/((1 - roots[i])**2)*(Leg_pol_der(n,roots[i]))**2) for i in range(n)]
41      return weights
42
43  def Gauss_integr(n,function):
44      roots = Leg_roots(n)
45      weights = Gauss_weights(n)
46      res = 0
47      for i in range(n):
48          res += weights[i] * function(roots[i])
49      return res
50
51  def Gauss_integr_ar(n,array):
52      if (n != len(array)):
53          print 'array length is not equal to the number of nodes!'
54          return None
55      weights = Gauss_weights(n)
56      res = 0
57      for i in range(n):
58          res += weights[i] * array[i]
59      return res

```