

$$\{0^n 1^m : n \leq m \leq 2n\}$$

011

0111

1 — 0?

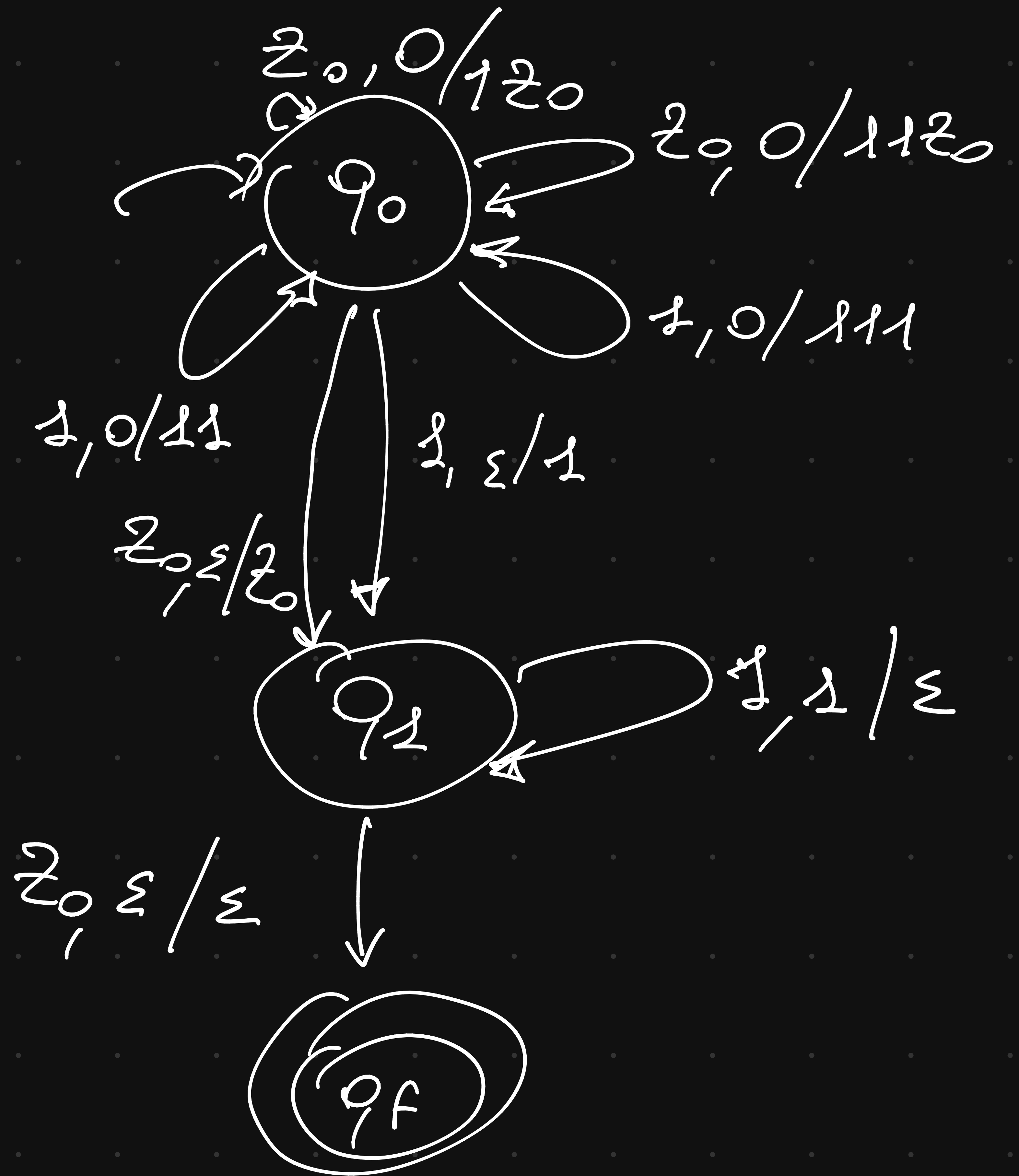
1 — 0?

1 — 0?

1 — 0?

1 — 0?

1



$L$  è regolare allora  $\exists m_0 > 0$  : per ogni parola  $w \in L$   
 sufficientemente lunga, esiste  $w = xyz$   
 t.c.  $|xy| \leq m_0$  e  $\forall i \geq 0 \quad xy^i z \in L$

$\exists 0^n 1^m : m \geq 0$

$\forall k, \exists w(k), |w(k)| \geq k, \forall$  decomposizione  $w = xyz$   
 t.c.  $|xy| \leq k$  e  $|y| \neq \varepsilon, \exists i : xy^i z \notin L$

$w(k) = 0^k 1^k \quad \forall w = xyz \quad x = 0^i \quad y = 0^j \quad z = 0^{k-i-j} 1^k$

$i=0 \quad xy^0 z = 0^i 0^{k-i-j} 1^k = 0^{k-j} 1^k$

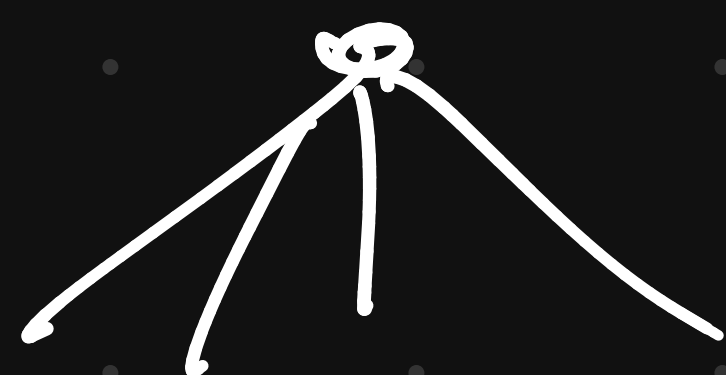
# Pumping Lemma per CFL

Se  $L \in \text{CFL}$ ,  $\exists n_0$  t.c. per ogni parola  $w$ ,  $|w| \geq n_0$

per ogni decomposizione  $w = uvxyz$   
t.c.  $|vxy| \leq n_0$ ,  $vy \neq \varepsilon$

Allora

$$uv^i xy^i z \in L \quad \forall i \geq 0$$



# Forme Normali per CFG

Forme normali di Chomsky

$$A \rightarrow BC$$

$$A \rightarrow \epsilon$$

$A, B, C$  variabili  
 $\epsilon$  terminale

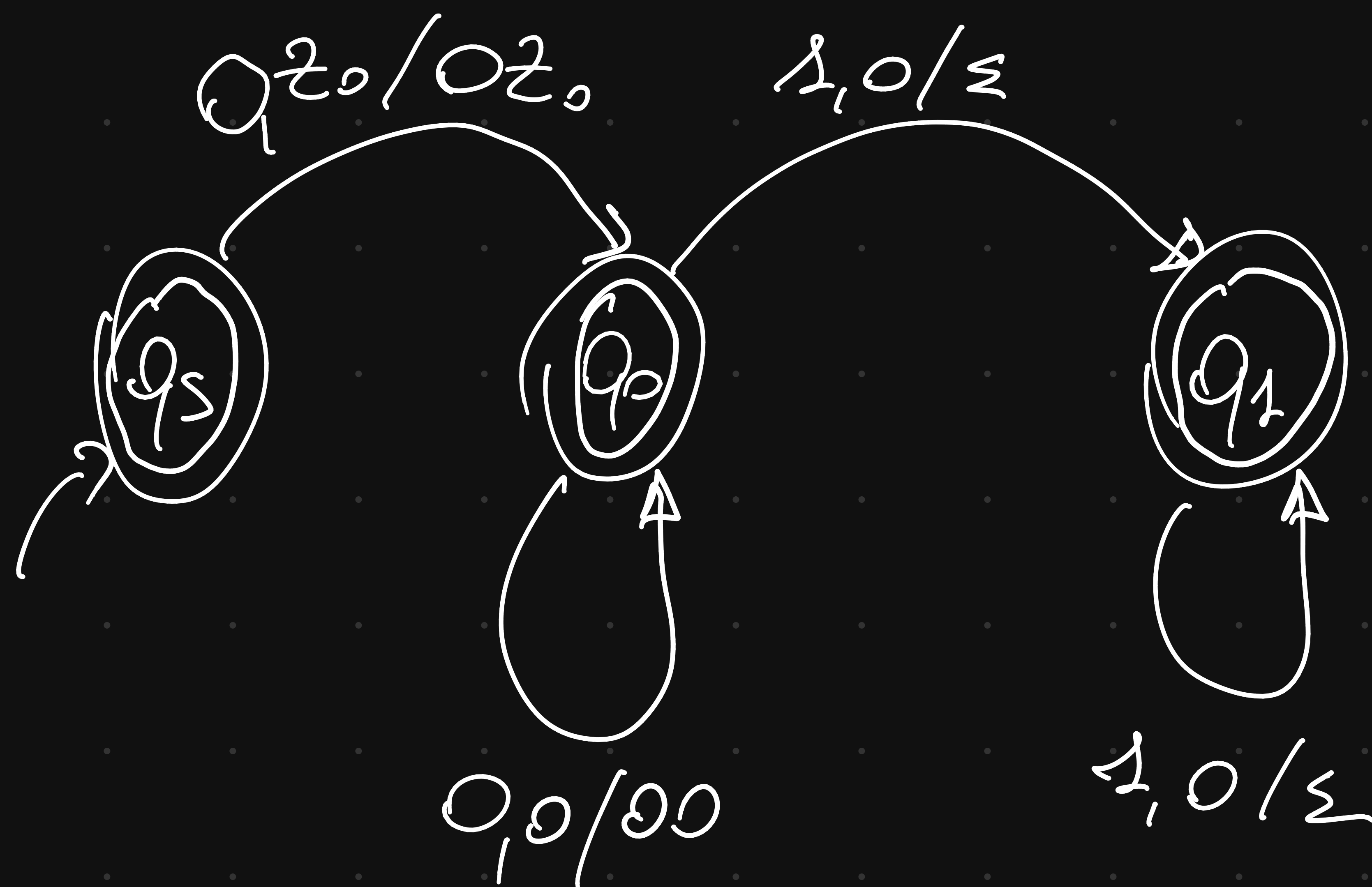
Forme normali di Greibach

$$A \rightarrow \epsilon x$$

$x$  terminale

✓ forme sentenziale

$\{0^n 1^m : n \geq m\}$  descrivere un DPDA che lo riconosce



$11 \notin L$   
 $0101 \notin L$