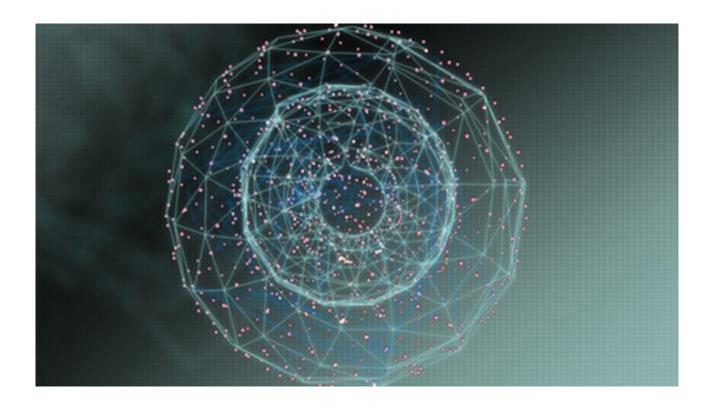
PATTERN DISCOVERY IN DATA MINING

Concepts and challenges in pattern discovery and analysis.

Pattern evaluation, mining and classification

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1 Lecture 2: Pattern Discovery Basic Concepts

1.1 Frequent Itemsets (Patterns)

X = itemset

- (absolute) support (count) of X: Frequency or the number of occurrences of an itemset X
- **(relative) support, s:** The fraction of transactions that contains X (i.e., the probability that a transaction contains X)
- An itemset X is **frequent** if the support of X is no less than a minsup threshold (denoted as σ): $sup(X) \geqslant \sigma$.

1.2 Association Rules

Association rules: $X \to Y(s, c)$:

• **Support** (s): the probability that a transaction contains $X \cup Y$:

$$\sup(X \to Y) = P(X \cup Y)$$

• **Confidence** (c): the conditional probability that a transaction containing X also contains Y:

$$c = \mathrm{P}(Y \mid X) = \frac{\sup(X \cup Y)}{\sup(X)}$$

1.3 Expressing Patterns in Compressed Form

Definition. Closed patterns: A pattern (itemset) X is closed if X is frequent, and there exists no super-pattern $Y \supset X$, with the same support as X.

Closed pattern is a lossless compression of frequent patterns.

Definition. Max-patterns: A pattern X is a max-pattern if X is frequent and there exists no frequent super-pattern $Y \supset X$.

Max-pattern is a lossy compression!

1.4 Recommended readings

- R. Agrawal, T. Imielinski, and A. Swami, «Mining association rules between sets of items in large databases», in Proc. of SIGMOD'93
- R. J. Bayardo, «Efficiently mining long patterns from databases», in Proc. of SIG-MOD'98
- N. Pasquier, Y. Bastide, R. Taouil, and L. Lakhal, «Discovering frequent closed itemsets for association rules», in Proc. of ICDT'99
- J. Han, H. Cheng, D. Xin, and X. Yan, «Frequent Pattern Mining: Current Status and Future Directions», Data Mining and Knowledge Discovery, 15(1): 55-86, 2007

2 Lecture 3. Efficient Pattern Mining Methods

2.1 The Downward Closure Property of Frequent Patterns

The downward closure (also called «Apriori») property of frequent patterns: **Any subset of a frequent itemset must be frequent**. Apriori pruning principle: **If there is any itemset which is infrequent, its superset should not even be generated!**

Scalable mining Methods: Three major approaches

- · Level-wise, join-based approach: Apriori (2.2)
- Vertical data format approach: Eclat (2.4)
- Frequent pattern projection and growth: FPgrowth (2.5)

2.2 The Apriori Algorithm

2.2.1 Algorithm pseudocode

```
C_k: Candidate itemset of size k F_k: Frequent itemset of size k TDB = transactional database
```

Algorithm 1 The Apriori Algorithm

```
k := 1 F_k := \text{frequent items} \qquad \qquad \text{\# frequent 1-itemset} while F_k \neq \emptyset do C_{k+1} := \text{candidates generated from } F_k \qquad \qquad \text{\# candidate generation} Derives F_{k+1} by counting candidates in C_{k+1} with respect to TDB at minsup k := k+1 end while \text{return } \cup_k F_k \qquad \qquad \text{\# return } F_k \text{ generated at each level}
```

2.2.2 How to generate candidates?

```
• Step1: self-joining F<sub>k</sub>
```

• Step2: pruning

Algorithm 2 Step1: self-joining F_k

```
insert into C_k select p.item<sub>1</sub>, p.item<sub>2</sub>, ..., p.item<sub>k-1</sub>, q.item<sub>k-1</sub> from F_{k-1} as p, F_{k-1} as q where p.item<sub>1</sub>= q.item<sub>1</sub>, ..., p.item<sub>k-2</sub> = q.item<sub>k-2</sub>, p.item<sub>k-1</sub> < q.item<sub>k-1</sub>
```

Algorithm 3 Step2: pruning

```
for all itemsets c in C<sub>k</sub> do
  for all (k-1) subsets s of c do
    if s is not in F<sub>k-1</sub> then
        delete c from C<sub>k</sub>
    end if
  end for
end for
```

2.3 Extensions or Improvements of Apriori

- · Reduce passes of transaction database scans
 - Partitioning
 - Dynamic itemset counting
- Shrink the number of candidates
 - Hashing
 - Pruning by support lower bounding
 - Sampling
- Exploring special data structures
 - Tree projection
 - H-miner
 - Hypecube decomposition

2.3.1 Partitioning

Theorem. Any itemset that is potentially frequent in TDB must be frequent in at least one of the partitions of TDB

Method: Scan Database Only Twice:

- Scan 1: Partition database (how?) and find local frequent patterns
- Scan 2: Consolidate global frequent patterns (how to?)

2.3.2 Direct Hashing and Pruning (DHP)

Observation: A k-itemset whose corresponding hashing bucket count is below the threshold cannot be frequent

2.4 Vertical Data Format

ECLAT - Equivalence Class Transformation

Frequent patterns are derived based on vertical intersections. To accelerate data mining you can use **diffset**: only keep track of differences of tids.

2.5 A Pattern Growth Approach

FP-tree - frequent pattern tree

TID	Items in the Transaction	Ordered, frequent items
100	$\{f,a,c,d,g,i,m,p\}$	$\{f, c, a, m, p\}$
200	$\{a,b,c,f,l,m,o\}$	$\{f,c,a,b,m\}$
300	$\{b,f,h,j,o,w\}$	{f, b}
400	$\{b,c,k,s,p\}$	$\{c,b,p\}$
500	$\{a,f,c,e,l,p,m,n\}$	$\{f, c, a, m, p\}$

Figure 1: Transactional DB

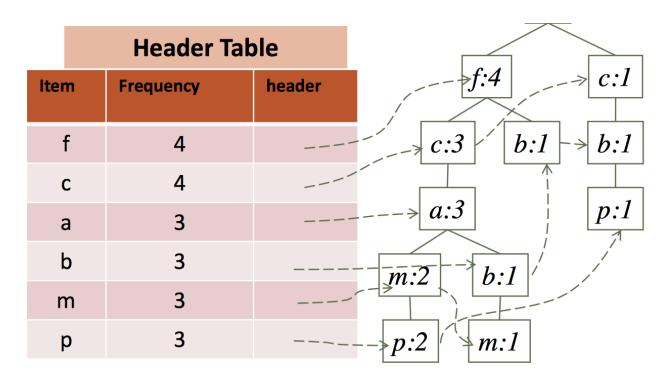


Figure 2: FP-tree

2.6 CLOSET+: Mining Closed Itemsets by Pattern-Growth

Itemset merging: If Y appears in every occurrence of X, then Y is merged with X

2.7 Recommended readings

- R. Agrawal and R. Srikant, «Fast algorithms for mining association rules», VLDB'94
- A. Savasere, E. Omiecinski, and S. Navathe, «An efficient algorithm for mining association rules in large databases», VLDB'95
- J. S. Park, M. S. Chen, and P. S. Yu, «An effective hash-based algorithm for mining association rules», SIGMOD'95

- S. Sarawagi, S. Thomas, and R. Agrawal, «Integrating association rule mining with relational database systems: Alternatives and implications», SIGMOD'98
- M. J. Zaki, S. Parthasarathy, M. Ogihara, and W. Li, «Parallel algorithm for discovery of association rules», Data Mining and Knowledge Discovery, 1997
- J. Han, J. Pei, and Y. Yin, «Mining frequent patterns without candidate generation», SIGMOD'00
- M. J. ZakiandHsiao, «CHARM: An Efficient Algorithm for Closed Itemset Mining», SDM'02
- J. Wang, J. Han, and J. Pei, «CLOSET+: Searching for the Best Strategies for Mining Frequent Closed Itemsets», KDD'03
- C. C. Aggarwal, M.A., Bhuiyan, M. A. Hasan, «Frequent Pattern Mining Algorithms: A Survey», in Aggarwal and Han (eds.): Frequent Pattern Mining, Springer, 2014

3 Lecture 4: Pattern Evaluation

3.1 Interestingness Measures: Lift and χ^2

3.1.1 Interestingness Measure: Lift

Lift - measure of dependent/correlated events:

$$lift(B,C) = \frac{c(B \to C)}{s(C)} = \frac{s(B \cup C)}{s(B) \times s(C)}$$

Lift(B, C) may tell how B and C are correlated:

- Lift(B, C) = 1: B and C are independent
- Lift(B, C) > 1: positively correlated
- Lift(B, C) < 1: negatively correlated

3.1.2 Interestingness Measure: χ^2

$$\chi^2 = \sum \frac{(Observed - Expected)^2}{Expected}$$

General rules:

- $\chi^2 = 0$: independent
- $\chi^2 > 0$: correlated, either positive or negative, so it needs additional test

Too many null transactions may lead to invalid correlation result!

3.2 Null Invariance Measures

$$\operatorname{AllConf}(A,B) = \frac{s(A \cup B)}{\max\{s(A), s(B)\}}$$

$$\operatorname{Jaccard}(A,B) = \frac{s(A \cup B)}{s(A) + s(B) - s(A \cup B)}$$

$$\operatorname{Cosine}(A,B) = \frac{s(A \cup B)}{\sqrt{s(A) \times s(B)}}$$

$$\operatorname{Kulczynsky}(A,B) = \frac{1}{2} \left(\frac{s(A \cup B)}{s(A)} + \frac{s(A \cup B)}{s(B)} \right)$$

$$\operatorname{MacConf}(A,B) = \max \left\{ \frac{s(A)}{s(A \cup B)}, \frac{s(B)}{s(A \cup B)} \right\}$$

3.3 Imbalance Ratio

IR (Imbalance Ratio): measure the imbalance of two itemsets A and B in rule implications:

$$IR(A, B) = \frac{|s(A) - s(B)|}{s(A) + s(B) - s(A \cup B)}$$

Kulczynski and Imbalance Ratio (IR) together present a clear picture

3.4 Recommended Readings

- C. C. Aggarwal and P. S. Yu. A New Framework for Itemset Generation. PODS'98
- S. Brin, R. Motwani, and C. Silverstein. Beyond market basket: Generalizing association rules to correlations. SIGMOD'97
- M. Klemettinen, H. Mannila, P. Ronkainen, H. Toivonen, and A. I. Verkamo. Finding interesting rules from large sets of discovered association rules. CIKM'94
- E. Omiecinski. Alternative Interest Measures for Mining Associations. TKDE'03
- P.-N. Tan, V. Kumar, and J. Srivastava. Selecting the Right Interestingness Measure for Association Patterns. KDD'02
- T. Wu, Y. Chen and J. Han, Re-Examination of Interestingness Measures in Pattern Mining: A Unified Framework, Data Mining and Knowledge Discovery, 21(3):371-397, 2010

4 Lecture 4: Mining Diverse Patterns

4.1 Mining Multi-Level Associations

Items often form hierarchies. How to set min-support thresholds? **Level-reduced min-support**: items at the lower level are expected to have lower support.

Efficient mining: **shared** multi-level mining. Use the lowest min-support to pass down the set of candidates.

Redundancy¹ filtering: some rules may be redundant due to «ancestor»² relationships between items. A rule is **redundant** if:

- its support is close to the «expected» value, according to its «ancestor» rule
- it has a similar confidence as its «ancestor».

It is necessary to have customized min-support settings for different kinds of items: group-based «individualized» min-support.

4.2 Mining Multi-Dimensional Associations

Rules can be single-dimensional or multi-dimensional:

• Single-dimentional:

$$\operatorname{buys}(X, \operatorname{wnilk}) \Rightarrow \operatorname{buys}(X, \operatorname{wbread})$$

• Inter-dimension association rule:

$$age(X, \mathbf{<18-25}) \land occupation(X, \mathbf{$$

• Hybrid-dimension association rules:

$$age(X, \text{\tt ``al8-25"}) \land buys(X, \text{\tt ``popcorn"}) \Rightarrow buys(X, \text{\tt ``coke"})$$

Attributes can be categorical or numerical

4.3 Mining Quantitative Associations

Methods:

- Static discretization based on predefined concept hierarchies
- · Dynamic discretization based on data distribution
- Clustering: distance-based association
- Deviation analysis

4.4 Mining Negative Correlations

- Rare patterns = very low support but interesting
- Negative patterns = negatively correlated, unlikely to happen together

A support-based definition: if itemsets A and B are both frequent but rarely occur together, i.e., $\sup(A \cup B) << \sup(A) \times \sup(B)$ then A and B are negatively correlated.

The support-based definition is not null-invariant!

A Kulczynski measure-based definition: if itemsets A and B are frequent but $\frac{P(A|B)+P(B|A)}{2} < \varepsilon$, where ε is a negative pattern threshold, then A and B are negatively correlated.

¹Redundancy - избыточность

²Ancestor – предок

4.5 Mining Compressed Patterns

4.5.1 Mining Compressed Patterns

Pattern distance measure:

$$Dist(P_1, P_2) = 1 - \frac{|T(P_1) \cap T(P_2)|}{|T(P_1) \cup T(P_2)|}$$

δ-clustering. For each pattern P, find all patterns which can be expressed by P and whose distance to P is within δ (δ-cover). All patterns in the cluster can be represented by P = compressed patterns.³

4.5.2 Redundancy-Aware Top-k Patterns

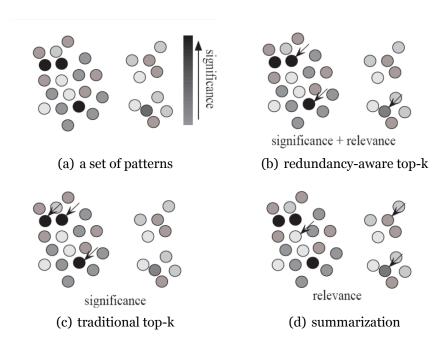


Figure 3: Desired patterns: high significance & low redundancy

Use **MMS (Maximal Marginal Significance)** for measuring the combined significance of a pattern set.⁴

4.6 Mining Colossal Patterns

4.6.1 Pattern-Fusion

Pattern fusion strategy: fuse small patterns together in one step to generate new pattern candidates of significant sizes.

Subpatterns α_1 to α_k cluster tightly around the colossal pattern α by sharing a similar support. Such subpatterns are **core patterns** of α . A colossal pattern can be generated by merging a set of core patterns.

³Method for efficient, direct mining of compressed frequent patterns: Xin et al., VLDB'05.

⁴Xin et al., Extracting Redundancy-Aware Top-K Patterns, KDD'06.

4.6.2 Robustness of Colossal Patterns

Definition. For a frequent pattern α , a subpattern β is a τ -core pattern of α if β shares a similar support set with α , i.e.,

$$\frac{|D_{\alpha}|}{|D_{\beta}|} \geqslant \tau, 0 < \tau \leqslant 1,$$

where τ is called the **core ratio**.

Definition. (d, τ)-robustness⁵: a pattern α is (d, τ) -robust if d is the maximum number of items that can be removed from α for the resulting pattern to remain a τ -core pattern of α :

$$d = \max_{\beta} \{ |\alpha| - |\beta| \mid \beta \subseteq \alpha, \text{ and } \beta \text{ is a } \tau\text{-core pattern of } \alpha \}$$

For a pattern α let C_{α} be the set of all its core patterns for a specified τ :

$$C_{\alpha} = \{\beta \mid \beta \subseteq \alpha, \frac{|D_{\alpha}|}{|D_{\beta}|} \geqslant \tau\}$$

Theorem. For a (d, τ) -robust pattern α :

$$|C_{\alpha}| \geqslant 2^d$$

Robustness of Colossal Patterns: a colossal pattern tends to have much more core patterns than small patterns. Such core patterns can be clustered together to form «dense balls» based on pattern distance defined by

$$Dist(\alpha, \beta) = 1 - \frac{|D_{\alpha} \cap D_{\beta}|}{|D_{\alpha} \cup D_{\beta}|}$$

Theorem. For two patterns $\beta_1, \beta_2 \in C_{\alpha}$

$$Dist(\beta_1, \beta_2) \leqslant r(\tau)$$
, where $r(\tau) = 1 - \frac{1}{2/\tau - 1}$

4.6.3 The Pattern-Fusion Algorithm

- Initialization (Creating initial pool): Use an existing algorithm to mine all frequent patterns up to a small size, e.g., 3
- Iteration (Iterative Pattern Fusion):
 - At each iteration, K seed patterns are randomly picked from the current pattern pool
 - For each seed pattern thus picked, we find all the patterns within a bounding ball centered at the seed pattern
 - All these patterns found are fused together to generate a set of super-patterns
 - All the super-patterns thus generated form a new pool for the next iteration
- Termination: when the current pool contains no more than K patterns at the beginning of an iteration

⁵Robustness - прочность

4.7 Recommended Readings

- R. Srikant and R. Agrawal, «Mining generalized association rules», VLDB'95
- Y. Aumann and Y. Lindell, «A Statistical Theory for Quantitative Association Rules», KDD'99
- D. Xin, J. Han, X. Yan and H. Cheng, «On Compressing Frequent Patterns», Knowledge and Data Engineering, 60(1): 5-29, 2007
- D. Xin, H. Cheng, X. Yan, and J. Han, «Extracting Redundancy-Aware Top-K Patterns», KDD'06
- F. Zhu, X. Yan, J. Han, P. S. Yu, and H. Cheng, «Mining Colossal Frequent Patterns by Core Pattern Fusion», ICDE'07
- J. Han, H. Cheng, D. Xin, and X. Yan, «Frequent Pattern Mining: Current Status and Future Directions», Data Mining and Knowledge Discovery, 15(1): 55-86, 2007

5 Constraint-Based Pattern Mining

5.1 Meta-Rule Guided Mining

In general, (meta) rules can be in the form of

$$P_1 \wedge P_2 \wedge ... \wedge P_l \Rightarrow Q_1 \wedge Q_2 \wedge ... \wedge Q_r$$

Method to find meta-rules:

- Find frequent (l + r) predicates (based on min-support)
- Push constraints deeply when possible into the mining process
- Also, push min_conf, min_correlation, and other measures as early as possible (measures acting as constraints)

5.2 Kinds of Constraints

- · Pattern space pruning constraints
 - Anti-monotonic: If constraint c is violated, its further mining can be terminated
 - Monotonic: If c is satisfied, no need to check c again
 - Succinct⁶: if the constraint c can be enforced by directly manipulating the data
 - Convertible: c can be converted to monotonic or anti-monotonic if items can be properly ordered in processing
- Data space pruning constraints
 - Data succinct: Data space can be pruned at the initial pattern mining process
 - Data anti-monotonic: If a transaction t does not satisfy c, then t can be pruned to reduce data processing effort

Anti-monotonic constraints have more pruning power than monotonic constraints.

⁶Succinct - краткий

5.2.1 Pattern space pruning constraints

Constraint c is **anti-monotone**: if an itemset S violates constraint **c**, so does any of its superset. That is, mining on itemset S can be terminated. For example, constraint $\sup(S) \geqslant \sigma$ is anti-monotone.

A constraint c is **monotone**: if an itemset S satisfies the constraint **c**, so does any of its superset. That is, we do not need to check **c** in subsequent mining. For example, constraints $sum(S.price) \ge v$ or $min(S.price) \le v$ are monotone.

5.2.2 Data space pruning constraints

A constraint **c** is **data anti-monotone**: if a data entry **t** cannot satisfy a pattern **p** under constraint **c**, **t** cannot satisfy **p**'s superset either. That's why, data entry **t** can be pruned.

Succinctness: if the constraint **c** can be enforced by directly manipulating the data.

Convertible constraints: convert tough⁷ constraints into (anti-)monotone by proper ordering of items in transactions. For example, ordering items in value-descending order makes the constraint avg(S.profit) > 20 anti-monotone if the patterns grow in the right order.

5.3 Recommended Readings

- R. Srikant, Q. Vu, and R. Agrawal, «Mining association rules with item constraints», KDD'97
- R. Ng, L.V.S. Lakshmanan, J. Han & A. Pang, Exploratory mining and pruning optimizations of constrained association rules», SIGMOD'98
- G. Grahne, L. Lakshmanan, and X. Wang, «Efficient mining of constrained correlated sets», ICDE'00
- J. Pei, J. Han, and L. V. S. Lakshmanan, «Mining Frequent Itemsets with Convertible Constraints», ICDE'01
- J. Pei, J. Han, and W. Wang, «Mining Sequential Patterns with Constraints in Large Databases», CIKM'02
- F. Bonchi, F. Giannotti, A. Mazzanti, and D. Pedreschi, «ExAnte: Anticipated Data Reduction in Constrained Pattern Mining», PKDD'03
- F. Zhu, X. Yan, J. Han, and P. S. Yu, «gPrune: A Constraint Pushing Framework for Graph Pattern Mining», PAKDD'07

6 Sequential Pattern Mining

6.1 Sequential Pattern

Sequence \rightarrow Element \rightarrow Item or Event (items within an element are unordered)

⁷Tough - жесткий

The Apriori property still holds: if a subsequence s_1 is infrequent, none of s_1 's supersequences can be frequent.

Algorithms:

• Generalized Sequential Patterns: GSP

• Vertical format-based mining: SPADE

• Pattern-growth methods: **PrefixSpan**

• Mining closed sequential patterns: CloSpan

6.2 GSP: Apriori-Based Sequential Pattern Mining

```
Algorithm 4 GSP

k = 1

repeat

find length=k frequent sequences

Apriori: remove candidates with sup < min_sup

length=k frequent sequences ⇒ length=(k+1) candidate sequences

k = k + 1

until no frequent sequences or candidates
```

6.3 SPADE: Sequential Pattern Mining in Vertical Data Format

SPADE = **S**equential **Pa**ttern **D**iscovery using **E**quivalent Class

SID	Sequence
1	<a(<u>abc)(a<u>c</u>)d(cf)></a(<u>
2	<(ad)c(bc)(ae)>
3	<(ef)(<u>ab</u>)(df) <u>c</u> b>
4	<eg(af)cbc></eg(af)cbc>
	min_sup = 2

Figure 4: A sequence database

SID	EID	Items
1	1	a
1 1	2	abc
1	3	ac
1	4	$^{\mathrm{d}}$
1 2 2 2 2	5	cf
2	1	ad
2	2	\mathbf{c}
2	3	\mathbf{bc}
	4	ae
3	1	$\mathbf{e}\mathbf{f}$
3	2	ab
3	3	$\mathrm{d}\mathrm{f}$
3	4	\mathbf{c}
3	5	b
4	1	\mathbf{e}
4	2	g
4	3	af
4	4	c
4	5	b
4	6	\mathbf{c}

\mathbf{a}		1	b	
SID	EID	$_{ m SID}$	EID	10.00
1	1	1	2	
1	2	2	3	
1	3	3	2	
2	1	3	5	
2	4	4	5	
3	2			
4	3			

	$^{\mathrm{ab}}$			ba	
SID	EID (a)	EID(b)	SID	EID (b)	EID(a)
1	1	2	1	2	3
2	1	3	2	3	4
3	2	5			
4	3	5			

aba				
SID	EID (a)	EID(b)	EID(a)	1.11
1	1	2	3	
2	1	3	4	

Figure 5: SPADE algorithm

6.4 PrefixSpan: A Pattern-Growth Approach

PrefixSpan = Prefix-projected Sequential pattern mining

SID	Sequence
10	<a(<u>abc)(a<u>c</u>)d(cf)></a(<u>
20	<(ad)c(bc)(ae)>
30	<(ef)(<u>ab</u>)(df) <u>c</u> b>
40	<eg(af)cbc></eg(af)cbc>

Prefix	Suffix (Projection)	
<a>	<(abc)(ac)d(cf)>	
<aa></aa>	<(_bc)(ac)d(cf)>	
<ab></ab>	<(_c)(ac)d(cf)>	
*		

Figure 6: SPADE algorithm

PrefixSpan Mining: Prefix Projections

- Step 1: Find length-1 sequential patterns: <a>, , etc.
- Step 2: Divide search space and mine each projected DB: <a>-projected DB, -projected DB, etc.

6.5 CloSpan: Mining Closed Sequential Patterns

Definition. A closed sequential pattern α : there exists no superpattern β such that β and α have the same support:

$$CS = \{ \alpha \mid \alpha \in FS \text{ and } \nexists \beta \in FS \text{, such that } \alpha \subseteq \beta \text{ and } sup(\alpha) = sup(\beta) \}$$

CloSpan is based on this property: if $s \supset s_1$ then s is closed only if two project DBs have the same size. So redundant search space can be pruned using **Backward Subpattern** and **Backward Superpattern** pruning.

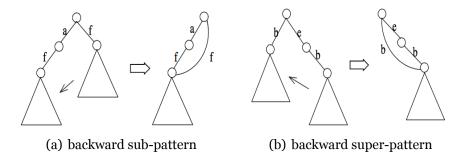


Figure 7: CloSpan pruning algorithm

6.6 Constraint-Based Sequential-Pattern Mining

- Anti-monotonic: If S violates c, the super-sequences of S also violate c
- Monotonic: If S satisfies c, the super-sequences of S also do so
- **Data anti-monotonic**: If a sequence s1 with respect to S violates c3, s1 can be removed
- **Succinct**: Enforce constraint c by explicitly manipulating data
- Convertible: Projection based on the sorted value not in sequence order

6.6.1 Timing-Based Constraints

- **Order constraint**: Some items must happen before the other. Anti-monotonic: constraint-violating sub-patterns pruned
- **Min-gap/max-gap constraint**: Confines two elements in a pattern. Succinct: enforced directly during pattern growth
- **Max-span constraint**: Maximum allowed time difference between the 1st and the last elements in the pattern. Succinct: enforced directly when the 1st element is determined
- **Window size constraint**: Time window allows a group of consecutive elements of a data-sequence to be merged and treated as a single element as long as their timestamps are within the user-specified window-size.

6.7 Recommended Readings

• M. N. Garofalakis, R. Rastogi, K. Shim: Mining Sequential Patterns with Regular Expression Constraints. IEEE Trans. Knowl. Data Eng. 14(3), 2002

- H. Mannila, H. Toivonen, and A. I. Verkamo, "Discovery of frequent episodes in event sequences", Data Mining and Knowledge Discovery, 1997
- J. Pei, J. Han, B. Mortazavi-Asl, J. Wang, H. Pinto, Q. Chen, U. Dayal, and M.-C. Hsu, "Mining Sequential Patterns by Pattern-Growth: The PrefixSpan Approach", IEEE TKDE, 16(10), 2004
- J. Pei, J. Han, and W. Wang, "Constraint-based sequential pattern mining: the pattern-growth methods", J. Int. Inf. Sys., 28(2), 2007
- R. Srikant and R. Agrawal, "Mining sequential patterns: Generalizations and performance improvements", EDBT'96
- X. Yan, J. Han, and R. Afshar, "CloSpan: Mining Closed Sequential Patterns in Large Datasets", SDM'03
- M. Zaki, "SPADE: An Efficient Algorithm for Mining Frequent Sequences", Machine Learning, 2001

7 Lecture 8. Graph Pattern Mining

7.1 Frequent (Sub)Graph Patterns

Given a labeled graph dataset $D=\{G_1,G_2,...,G_n\}$, the supporting graph set of a subgraph g is $D_g=\{G_i\mid g\subseteq G_i,G_i\in D\}$:

$$support(g) = \left| D_g \right| / |D|$$

A (sub)graph g is frequent if $support(g) \ge min_sup$.

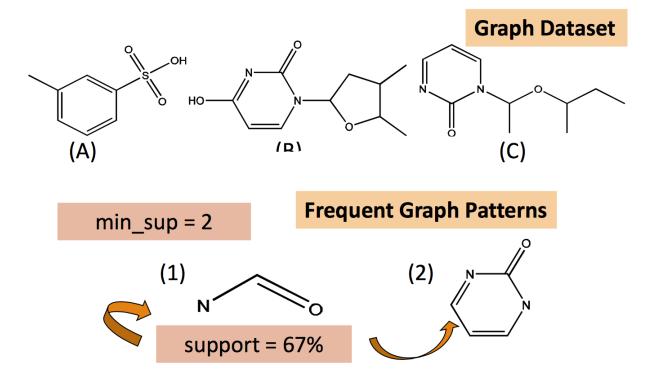


Figure 8: Example: Chemical structures

7.2 Apriori-Based Approach

The Apriori property (anti-monotonicity): a size-k subgraph is frequent if and only if all of its subgraphs are frequent.

Candidate generation: a candidate size-(k+1) edge/vertex subgraph is generated if its corresponding two k-edge/vertex subgraphs are frequent:

- AGM Generating new graphs with one more vertex
- FSG Generating new graphs with one more edge (more efficient)

Iterative mining process: Candidate-generation \rightarrow candidate pruning \rightarrow support counting \rightarrow candidate elimination.

7.3 gSPAN: Graph Pattern Growth

Depth-first growth of subgraphs from k-edge to (k+1)-edge, then (k+2)-edge subgraphs generates many duplicate subgraphs.

Right-most path extension in subgraph pattern growth reduces generation of duplicate subgraphs: *take the path from root to the right-most leaf (choose the vertex with the smallest index at each step)*. The Enumeration of graphs using right-most path extension is complete.

DFS Code: flatten a graph into a sequence using depth-first search

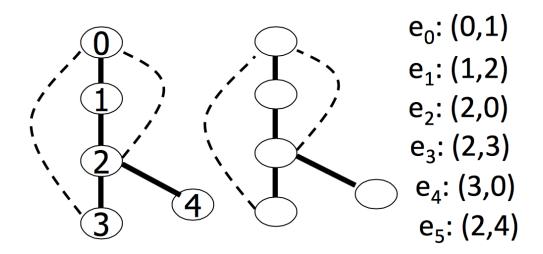


Figure 9: gSPAN

7.4 Mining Closed Graph Patterns

A frequent graph G is closed if there exists no supergraph of G that carries the same support as G.

CloseGraph algorithm: mining closed graph patterns by extending gSpan. Suppose G and G_1 are frequent, and G is a subgraph of G_1 . If in any part of the graph in the dataset where G occurs, G_1 also occurs, then we need not grow G (except some special, subtle cases), since *none of G's children will be closed except those of G*₁.

7.5 gIndex: A Graph Indexing Method

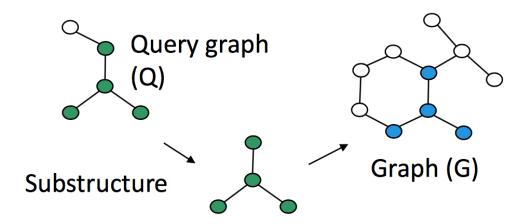


Figure 10: Graph query

- use frequent substructures for indexing
- discriminative substructures: reduce index size by removing similar (not discriminative) substructures from the index

Definition. Fragment x is **discriminative** with respect to feature set F if $D_x \ll \bigcap_{f \in F \land f \subseteq x} D_f$, where D_x is the set of graphs containing x.

Selection: Given a set of indexing features $f_1, f_2, ... f_n$, and a new structure x (x should be either redundant or discriminative), the extra indexing power is measured by occurrence probability

$$Pr(x \mid f_1, f_2, ... f_n) = \frac{\left|\bigcap_{f \in F \land f \subseteq x} D_f\right|}{\left|D_x\right|}$$

When $Pr(x \mid f_1, f_2, ...f_n) \ll 1$, x is a discriminative structure and should be included in the index.

7.6 SpiderMine: Mining Top-K Large Structural Patterns in a Massive Network

SpiderMine: mine top-K largest frequent substructure patterns whose diameter is bounded by $_{Dmax}$ with a probability at least $1 - \varepsilon$. General idea: large patterns are composed of a number of small components («spiders») which will eventually connect together after some rounds of pattern growth.

An r-spider is a frequent graph pattern P such that there exists a vertex u of P, and all other vertices of P are within distance r from u.

The SpiderMine Algorithm

- Mine the set S of all the r-spiders
- · Randomly draw M r-spiders

- Grow these M r-spiders for $t=D_{max}/2$ iterations, and merge two patterns whenever possible
- Discard unmerged patterns
- · Continue to grow the remaining ones to maximum size
- Return the top-K largest ones in the result

SpiderMine general ideas:

- Small patterns are much less likely to be hit in the random draw
- Even if a small pattern is hit, it is even less likely to be hit multiple times
- The larger the pattern, the greater the chance it is hit and saved

7.7 Recommended Readings

- C. Borgelt and M. R. Berthold, «Mining molecular fragments: Finding relevant substructures of molecules», ICDM'02
- J. Huan, W. Wang, and J. Prins. «Efficient mining of frequent subgraph in the presence of isomorphism», ICDM'03
- A. Inokuchi, T. Washio, and H. Motoda. «An apriori-based algorithm for mining frequent substructures from graph data», PKDD'00
- M. Kuramochi and G. Karypis. «Frequent subgraph discovery», ICDM'01
- S. Nijssen and J. Kok. A quickstart in frequent structure mining can make a difference. KDD'04
- N. Vanetik, E. Gudes, and S. E. Shimony. «Computing frequent graph patterns from semistructured data», ICDM'02
- X. Yan and J. Han, «gSpan: Graph-Based Substructure Pattern Mining», ICDM'02
- X. Yan and J. Han, «CloseGraph: Mining Closed Frequent Graph Patterns», KDD'03
- X. Yan, P. S. Yu, and J. Han, «Graph Indexing: A Frequent Structure-based Approach», SIGMOD'04
- F. Zhu, Q. Qu, D. Lo, X. Yan, J. Han, and P. S. Yu, «Mining Top-K Large Structural Patterns in a Massive Network», VLDB'11

8 Lecture 9. Pattern-Based Classification

8.1 Classification: Basic Concepts

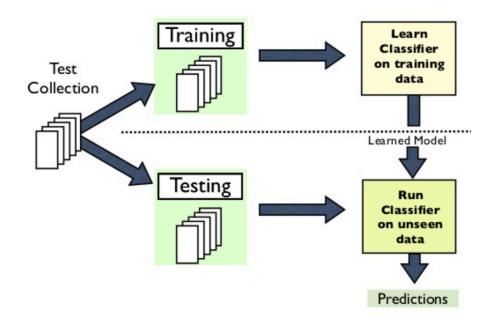


Figure 11: Classification

Typical Classification Methods:

- Support Vector Machines
- · Decision Tree
- · Neural Network
- Bayesian Network

8.2 Pattern-based classification methods

- CBA [Liu, Hsu & Ma, KDD'98]: Use high-conf., high-support class association rules to build classifiers
- Emerging patterns [Dong & Li, KDD'99]: Patterns whose support changes significantly between the two classes
- CMAR [Li, Han & Pei, ICDM'01]: Multiple rules in prediction
- CPAR [Yin & Han, SDM'03]: Beam search on multiple prediction rules
- RCBT [Cong et al., SIGMOD'05]: Build classifier based on mining top-k covering rule groups with row enumeration (for high-dimensional data)
- Lazy classifier [Veloso, Meira & Zaki, ICDM'06]: For a test t, project training data D on t, mine rules from D_t , predict on the best rule
- Discriminative pattern-based classification [Cheng et al., ICDE'07]

8.3 CBA: Classification Based on Associations

- Mine high-confidence, high-support class association rules
- LHS: conjunctions of attribute-value pairs); RHS: class labels $p_1 \wedge p_2 ... \wedge p_l \to \left[A_{class-label} = C\right]$
- Rank rules in descending order of confidence and support
- Classification: Apply the first rule that matches a test case; otherwise apply the default rule

8.4 CMAR: Classification Based on Multiple Association Rules

Rule pruning whenever a rule is inserted into the tree:

- Given two rules, R_1 and R_2 , if the antecedent⁸ of R_1 is more general than that of R_2 and $conf(R_1) \geqslant conf(R_2)$, then prune R_2
- Prunes rules for which the rule antecedent and class label are not positively correlated, based on the χ^2 test of statistical significance

Classification based on generated/pruned rules:

- If only one rule satisfies tuple X, assign the class label of the rule
- If a ruleset S satisfies X
 - Divide S into groups according to class labels
 - Use a weighted χ^2 measure to find the strongest group of rules, based on the statistical correlation of rules within a group
 - Assign X the class label of the strongest group

8.5 Discriminative Pattern-Based Classification

Principle: Mining discriminative frequent patterns as high-quality features and then apply any classifier.

Framework (PatClass):

- Feature construction by **frequent itemset mining**
- Feature selection (e.g., using Maximal Marginal Relevance (MMR))
 - Select **discriminative features** (i.e., that are relevant but minimally similar to the previously selected ones)
 - Remove redundant or closely correlated features
- Model learning: apply a general classifier, such as SVM or C4.5, to build a classification model

⁸Antecedent - предшественник

8.5.1 On the Power of Discriminative Patterns

K-itemsets are often more informative than single features (1-itemsets) in classification. Computation on real datasets shows: the discriminative power of k-itemsets (for k > 1 but often ≤ 10) is higher than that of single features.

Computation on real datasets shows: pattern frequency (but not too frequent) is strongly tied with the discriminative power (information gain). Information gain upper bound monotonically increases with pattern frequency.

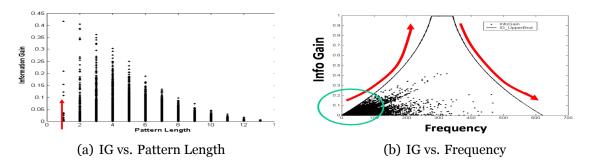


Figure 12: Information Gain

Information gain formula:

$$IG(C\mid X)=H(C)-H(C\mid X)\text{, where}$$

$$H(C)=-\sum_{i=1}^m p_i\log_2(p_i)\text{ - entropy of given data}$$

$$H(C\mid X)=\sum_j P(X=x_j)H(Y\mid X=x_j)\text{ - conditional entropy of study focus}$$

8.6 DDPMine: Direct Mining of Discriminative Patterns

General methodology:

- Input: A set of training instances D and a set of features F
- Iteratively perform feature selection based on the **«sequential coverage»** paradigm
 - Select the feature f_i with the highest discriminative power
 - Remove instances D_i from D covered by the selected feature f_i

Implementation:

- Integration of branch-and-bound search with FP-growth mining
- Iteratively eliminate training instances and progressively shrink the FP-tree

8.6.1 Branch-and-Bound Search

- The discriminative power (information gain) of a low frequency pattern is upper bounded by a small value
- During FPGrowth mining we record the most discriminative itemset discovered so far and its information gain value g_{best}

- Before constructing a conditional FP-tree, we first estimate the upper bound of information gain based on the conditional DB
- If the upper bound value $\leqslant g_{best}$, skip this conditional FP-tree and its subsequent trees

8.7 Recommended Readings

- H. Cheng, X. Yan, J. Han & C.-W. Hsu, Discriminative Frequent Pattern Analysis for Effective Classification, ICDE'07
- H. Cheng, X. Yan, J. Han & P. S. Yu, Direct Discriminative Pattern Mining for Effective Classification, ICDE'08
- G. Cong, K. Tan, A. Tung & X. Xu. Mining Top-k Covering Rule Groups for Gene Expression Data, SIGMOD'05
- M. Deshpande, M. Kuramochi, N. Wale & G. Karypis. Frequent Substructure-based Approaches for Classifying Chemical Compounds, TKDE'05
- G. Dong & J. Li. Efficient Mining of Emerging Patterns: Discovering Trends and Differences, KDD'99
- W. Fan, K. Zhang, H. Cheng, J. Gao, X. Yan, J. Han, P. S. Yu & O. Verscheure. Direct Mining of Discriminative and Essential Graphical and Itemset Features via Model-based Search Tree, KDD'08
- W. Li, J. Han & J. Pei. CMAR: Accurate and Efficient Classification based on Multiple Class-association Rules, ICDM'01
- B. Liu, W. Hsu & Y. Ma. Integrating Classification and Association Rule Mining, KDD'98
- J. Wang and G. Karypis. HARMONY: Efficiently Mining the Best Rules for Classification, SDM'05
- X. Yin & J. Han. CPAR: Classification Based on Predictive Association Rules, SDM'03

9 Lecture 10. Exploring Pattern Mining Applications

Frequent Pattern Mining for Text Data — Phrase Mining and Topic Modeling:

- Strategy 1: Simultaneously Inferring Phrases and Topics
 - Generate bag-of-words → generate sequence of tokens
 - Bigram topical model [Wallach'06], topical n-gram model [Wang, et al.'07], phrase discovering topic model [Lindsey, et al.'12]
- Strategy 2: Post Topic Modeling Phrase Construction
 - Post bag-of-words model inference, visualize topics with n-grams
 - Label topic [Mei et al.'07], TurboTopic [Blei & Lafferty'09], KERT [Danilevsky, et al.'14]
- Strategy 3: First Phrase Mining then Topic Modeling

- Prior bag-of-words model inference, mine phrases and impose on the bag-of-words model
- ToPMine [El-kishky, et al.'15]

9.1 Strategy 1: Simultaneously Inferring Phrases and Topics

- Bigram Topic Model [Wallach'06]
 - Probabilistic generative model that conditions on previous word and topic when drawing next word
- Topical N-Grams (TNG) [Wang, et al.'07]
 - Probabilistic model that generates words in textual order
 - Create n-grams by concatenating successive bigrams (a generalization of Bigram Topic Model)
- Phrase-Discovering LDA⁹ (**PDLDA**) [Lindsey, et al.'12]
 - Viewing each sentence as a time-series of words, PDLDA posits that the generative parameter (topic) changes periodically
 - Each word is drawn based on previous m words (context) and current phrase topic

9.2 Strategy 2: Post Topic Modeling Phrase Construction

9.2.1 TurboTopics

TurboTopics [Blei & Lafferty'09] – Phrase construction as a post-processing step to Latent Dirichlet Allocation

- Perform Latent Dirichlet Allocation on corpus to assign each token a topic label
- Merge adjacent unigrams with the same topic label by a distribution-free permutation test on arbitrary-length back-off model
- End recursive merging when all significant adjacent unigrams have been merged

9.2.2 KERT

KERT [Danilevsky et al.'14] – Phrase construction as a post-processing step to Latent Dirichlet Allocation

- Perform frequent pattern mining on each topic
- · Perform phrase ranking based on four different criteria

Framework of KERT:

- Run bag-of-words model inference and assign topic label to each token
- Extract candidate keyphrases within each topic (frequent pattern mining)
- Rank the keyphrases in each topic

⁹LDA - Latent Dirichlet Allocation

- Popularity: «information retrieval» vs. «cross-language information retrieval»
- Discriminativeness: only frequent in documents about topic t
- Concordance: «active learning» vs. «learning classification»
- Completeness: «vector machine» vs. «support vector machine»

9.3 Strategy 3: First Phrase Mining then Topic Modeling

The **ToPMine** (Topical Phrase Mining) Framework [El-Kishky et al. VLDB'15]:

- Perform frequent contiguous pattern mining to extract candidate phrases and their counts
- Perform agglomerative merging of adjacent unigrams as guided by a significance score— This segments each document into a "bag-of-phrases"
- The newly formed bag-of-phrases are passed as input to PhraseLDA, an extension of LDA, that constrains all words in a phrase to each sharing the same latent topic

9.3.1 Phrase Mining: Frequent Pattern Mining + Statistical Analysis

Significance score:

$$\alpha(P_1,P_2) \approx \frac{f(P_1 \bullet P_2) - \mu_0(P_1,P_2)}{\sqrt{f(P_1 \bullet P_2)}}$$

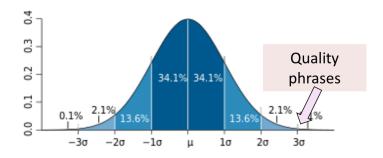


Figure 13: Significance score

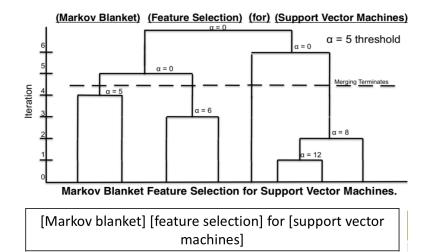


Figure 14: Phrase Mining

9.4 Recommended Readings

- M. Danilevsky, C. Wang, N. Desai, X. Ren, J. Guo, J. Han. «Automatic Construction and Ranking of Topical Keyphrases on Collections of Short Documents», SDM'14
- X. Wang, A. McCallum, X. Wei. Topical n-grams: Phrase and topic discovery, with an application to information retrieval, ICDM'07
- R. V. Lindsey, W. P. Headden, III, M. J. Stipicevic. A phrase-discovering topic model using hierarchical pitman-yor processes, EMNLP-CoNLL'12.
- Q. Mei, X. Shen, C. Zhai. Automatic labeling of multinomial topic models, KDD'07
- D. M. Blei and J. D. Lafferty. Visualizing Topics with Multi-Word Expressions, arXiv:0907.1013, 2009
- M. Danilevsky, C. Wang, N. Desai, J. Guo, J. Han. Automatic Construction and Ranking of Topical Keyphrases on Collections of Short Documents, SDM'14
- A. El-Kishky, Y. Song, C. Wang, C. R. Voss, J. Han. Scalable Topical Phrase Mining from Text Corpora, VLDB'15
- K. Church, W. Gale, P. Hanks, D. Hindle. Using Statistics in Lexical Analysis. In U. Zernik (ed.), Lexical Acquisition: Exploiting On-Line Resources to Build a Lexicon. Lawrence Erlbaum, 1991

10 Lecture 11: Advanced Topics on Pattern Discovery

10.1 Frequent Pattern Mining in Data Streams

10.1.1 Lossy Counting Algorithm

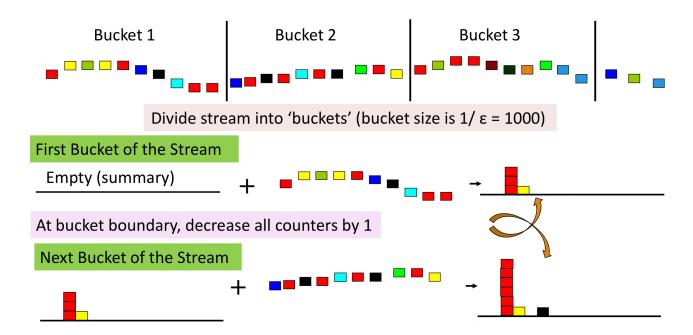


Figure 15: Lossy Counting Algorithm

Given:

- support threshold = σ
- error threshold = ε
- stream length = N

Output: items with frequency counts exceeding $(\sigma - \varepsilon) \times N$

$$f$$
requency $count\ error \leqslant number\ of\ buckets = rac{N}{bucket\ size} = rac{N}{1/arepsilon} = arepsilon N$

Approximation guarantee:

- · No false negatives
- False positives have true frequency count at least $(\sigma \varepsilon) \times N$
- Frequency count underestimated by at most εN

10.1.2 Recommended Readings

- G. Manku and R. Motwani, «Approximate Frequency Counts over Data Streams», VLDB'02
- A. Metwally, D. Agrawal, and A. El Abbadi, «Efficient Computation of Frequent and Top-k Elements in Data Streams», ICDT'05

10.2 Spatiotemporal and Trajectory Pattern Mining

10.2.1 Mining Relative Movement Patterns

- **Flock**: At least m entities are within a circular region of radius r and move in the same direction
- Convoy: Uses density-based clustering at each timestamp; no need to be a rigid circle
- **Swarm**: Moving objects may not be close to each other for all the consecutive time stamps

10.2.2 Recommended Readings

- Y. Huang, S. Shekhar, H. Xiong, Discovering colocation patterns from spatial data sets: A general approach, IEEE Trans. on Knowledge and Data Engineering, 16(12), 2004
- K. Koperski, J. Han, «Discovery of Spatial Association Rules in Geographic Information Databases», SSD'95
- Z. Li, B. Ding, J. Han, R. Kays, «Swarm: Mining Relaxed Temporal Moving Object Clusters», VLDB'10
- Z. Li, B. Ding, J. Han, Roland Kays, Peter Nye, «Mining Periodic Behaviors for Moving Objects», KDD'10
- C. Zhang, J. Han, L. Shou, J. Lu, T. La Porta, «Splitter: Mining Fine-Grained Sequential Patterns in Semantic Trajectories», VLDB'14
- Y. Zheng and X. Zhou, Computing with Spatial Trajectories, Springer, 2011

10.3 Pattern Discovery for Software Bug Mining

10.3.1 Typical Software Bug Detection Methods

- Mining rules from source code
 - Bugs as deviant behavior (e.g., by statistical analysis)
 - Mining programming rules (e.g., by frequent itemset mining)
 - Mining function precedence protocols (e.g., by frequent subsequence mining)
 - Revealing neglected conditions (e.g., by frequent itemset/subgraph mining)
- Mining rules from revision histories
 - By frequent itemset mining
- Mining copy-paste patterns from source code
 - Find copy-paste bugs (e.g., CP-Miner [Li et al., OSDI'04])
 - Reference: Z. Li, S. Lu, S. Myagmar, Y. Zhou, «CP-Miner: A Tool for Finding Copypaste and Related Bugs in Operating System Code», OSDI'04

10.3.2 Mining Copy-and-Paste Bugs

```
void init prom meminit(void)
                                                              Hash values
  for (i=0; i<n; i++) {
                                                                    65
                                                                             for (i=0; i<n; i++) {
     total[i].adr = list[i].addr;
                                                                                total[i].adr = list[i].addr;
                                                                    16
     total[i].bytes = list[i].size;
                                                                    16
                                                                                total[i].bytes = list[i].size;
     total[i].more = &total[i+1];
                                                                    71
                                                                                total[i].more = &total[i+1];
  }
                                      Code copy-and-
                                      pasted but forget
for (i=0; i<n; i++) {
                                      to change "id"!
                                                                             for (i=0; i<n; i++) {
                                                                    65
     taken[i].adr = list[i].addr;
                                                                                taken[i].adr = list[i].addr;
                                                                    16
     taken[i].bytes = list[i].size
                                                                    16
                                                                               taken[i].bytes = list[i].size;
     taken[i].more = &total[i+1];
                                                                                taken[i].more = &total[i+1];
                                                                    71
  }
                 (a) code with a bug
                                                                                    (b) sequence
```

Figure 16: Copy-and-Paste Bugs

- Map each statement to number
- · Tokenize each component
 - Different operators, constants, keywords = different tokens
 - Same type of identifiers = same token
- Program = long sequence
 - Cut the long sequence by blocks.

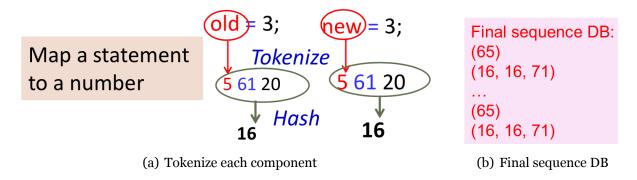


Figure 17: Building Sequence Database from Source Code

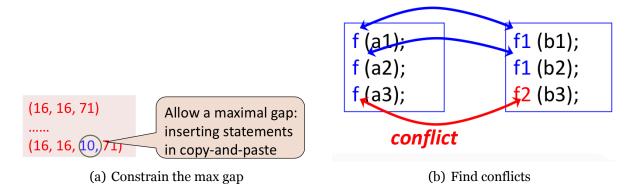


Figure 18: Detecting «Forget-to-Change» Bugs

- Modification to the sequence pattern mining algorithm
 - Constrain the max gap
- Composing Larger Copy-Pasted Segments
 - Combine the neighboring copy-pasted segments repeatedly
- Find conflicts: Identify names that cannot be mapped to the corresponding ones
 - If 0 < unchanged ratio < threshold, then report it as a bug

10.4 Pattern Discovery for Image Analysis

10.4.1 Recommended Readings

- Hongxing Wang, Gangqiang Zhao, Junsong Yuan, Visual pattern discovery in image and video data: a brief survey, Wiley Interdisciplinary Review: Data Mining and Knowledge Discovery 4(1): 24-37 (2014)
- Hongxing Wang, Junsong Yuan, Ying Wu, Context-Aware Discovery of Visual Co-Occurrence Patterns. IEEE Transactions on Image Processing 23(4): 1805-1819 (2014)
- Gangqiang Zhao, Junsong Yuan, Discovering Thematic Patterns in Videos via Cohesive Sub-graph Mining. ICDM 2011: 1260-1265
- Junsong Yuan, Ying Wu, Ming Yang, From frequent itemsets to semantically meaningful visual patterns. KDD 2007: 864-873