



Exploring coefficients

across models

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77 models

6 Belgium $\langle \text{tibble } [52 \times 6] \rangle \langle \text{S3: lm} \rangle$



Regression coefficients

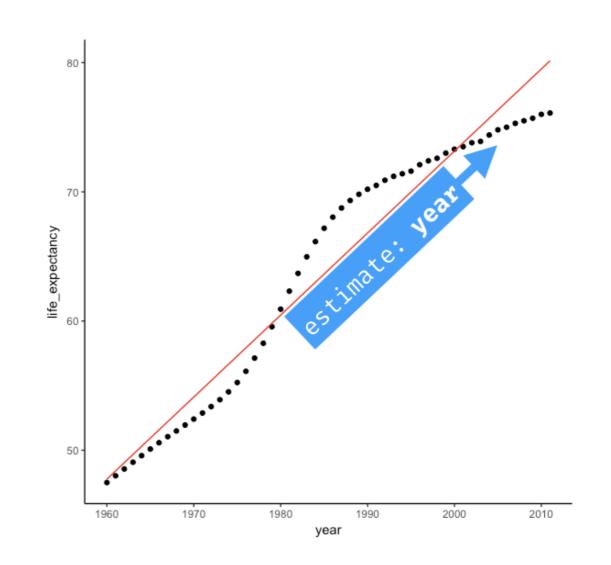
$$y = \alpha + \beta x$$



Regression coefficients

$$y = \alpha + \beta x$$

$$\frac{\text{Life}}{\text{Expectancy}} = \frac{\text{Term:}}{\text{(intercept)}} + \frac{\text{Term:}}{\text{year}} \text{ Year}$$





Coefficients of multiple models

```
gap models %>%
 mutate(coef = map(model, \sim tidy(.x))) %>%
 unnest (coef)
# A tibble: 154 x 6
  country term estimate std.error statistic p.value
  <fct> <chr> <dbl> <dbl>
                                          <dbl> <dbl>
                               39.9
                                          -30.0 1.32e^{-3.3}
1 Algeria (Intercept) -1197
                 0.635 0.0201 31.6 1.11e^{-34}
2 Algeria year
3 Argentina (Intercept) - 372 7.91 -47.0 4.66e^{-4_3}
                0.223 0.00398 56.0 8.78e<sup>-47</sup>
4 Argentina year
                                          -45.8 	 1.71e^{-4_2}
5 Australia (Intercept) - 429 9.37
                 0.254 0.00472 53.9 5.83e<sup>-46</sup>
6 Australia
           year
                                          -51.6 5.07e^{-45}
          (Intercept) - 415 8.04
7 Austria
                0.246 0.00405
                                       60.8 1.48e<sup>-48</sup>
8 Austria
           year
```





Let's practice!





Evaluating the fit of many models

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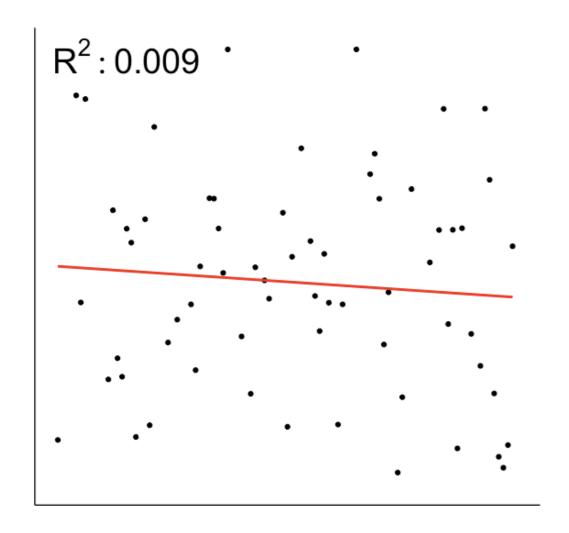


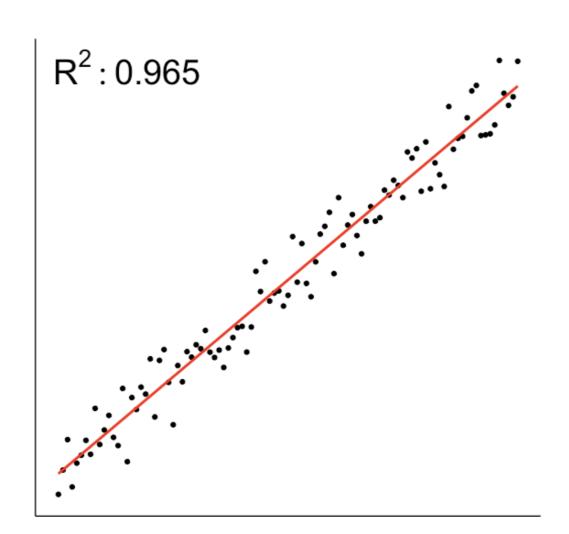
The fit of our models

$$R^2 = rac{\% \ variation \ explained \ by \ the \ model}{\% \ total \ variation \ in \ the \ data}$$



The fit of our models







Glance across your models

```
model_perf <- gap_models %>%
  mutate(coef = map(model, \sim glance(.x))) %>%
  unnest (coef)
model perf
# A tibble: 77 x 14
   country data model r.squared adj.r.squared sigma statistic
   <fct> <fct> 
                                    <dbl> <dbl> <dbl> <dbl>
                       <dbl>
                       0.952
                                0.951
 1 Algeria <tib... <S3:...
                                           2.18
                                                     996
                       0.984
                                0.984
                                           0.431 3137
 2 Argenti... <tib... <S3:...
                        0.983
                                           0.511
 3 Austral... <tib... <S3:...
                                0.983
                                                    2905
 4 Austria <tib... <S3:...
                        0.987
                                0.986
                                           0.438 3702
                                0.947 1.83
 5 Banglad... <tib... <S3:...
                        0.949
                                                   921
 6 Belgium <tib... <S3:...
                         0.990
                                      0.990
                                           0.331 5094
 # ... with 71 more rows
```



Best & worst fitting models

```
model_perf %>%
  top_n(n = 2, wt = r.squared)

# A tibble: 2 x 14
  country data model r.squared adj.r.squared sigma statistic
  <fct> </to>  <dbl> <dbl> <dbl> <dbl> <dbl> 1 Canada <tib... <S3:... 0.995 0.995 0.231 10117
2 Italy <tib... <S3:... 0.997 0.997 0.226 15665</pre>
```





Let's practice!





Visually inspect the fit of your models

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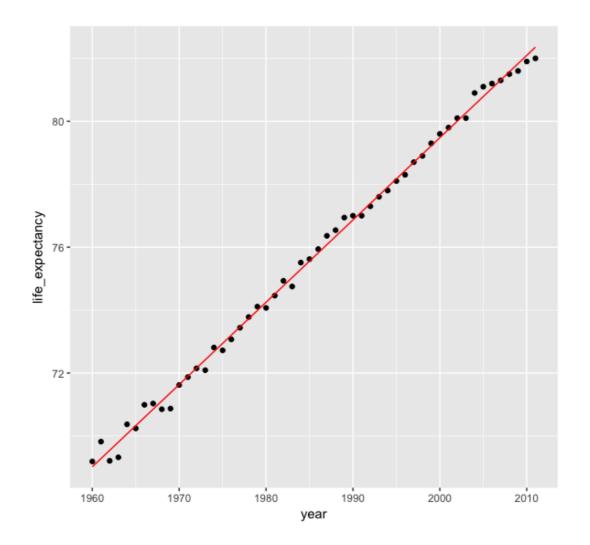


Building augmented datframes

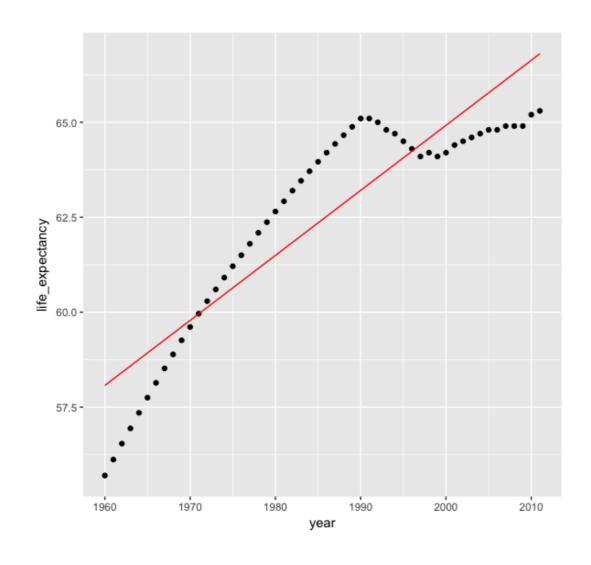
```
> augmented models
# A tibble: 4,004 x 10
  country life expectancy year .fitted .se.fit .resid .hat .sigma
  <fct>
                   <dbl> <int>
                                 <dbl> <dbl> <dbl> <dbl> <dbl> <
                    47.5 1960
                                47.8
                                        0.595 - 0.266 \ 0.0747
1 Algeria
                    48.0 1961
2 Algeria
                                48.4 0.578 -0.381 0.0705
                                                             2.20
                                                             2.20
 3 Algeria
                    48.6 1962
                                49.0
                                       0.561 -0.486 0.0664
 4 Algeria
                                49.7
                                                             2.20
                    49.1 1963
                                       0.544 -0.600 0.0625
 5 Algeria
                    49.6 1964
                                50.3 0.527 -0.725 0.0587
                                                             2.20
                    50.1 1965
                                 50.9 0.511 -0.850 0.0551
                                                             2.20 ...
 6 Algeria
```

Model for Italy $R^2:0.99$

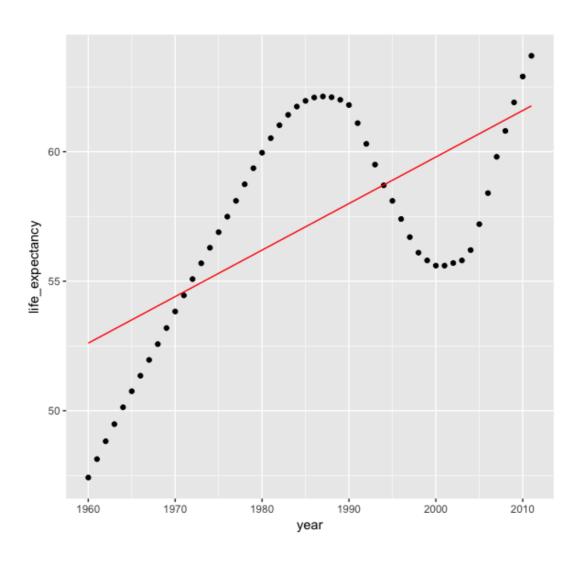
```
augmented_model %>% filter(country == "Italy") %>%
  ggplot(aes(x = year, y = life_expectancy)) +
  geom_point() +
  geom_line(aes(y = .fitted), color = "red")
```



Model for Fiji $\mathbb{R}^2:0.82$



Model for Kenya $\mathbb{R}^2:0.42$







Let's practice!





Improve the fit of your models

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Multiple Linear Regression model

$$y = \alpha + \beta_1 x_1 + \beta_2 x_2 + \dots$$

$$\frac{\text{Life}}{\text{Expectancy}} = \frac{\text{Term:}}{\text{(intercept)}} + \frac{\text{Term:}}{\text{year}} + \frac{\text{Term:}}{\text{population}} + \frac{\text{Term:}}{\dots} \dots$$

Available Features: year, population, infant mortality, fertility, gdpPercap



Using all features

Simple Linear Model: life_expectancy ~ year

```
gap_models <- gap_nested %>%
  mutate(model = map(data, ~lm(formula = life_expectancy ~ year, data = .x)))
```

Multiple Linear Model: life_expectancy ~ year + population + ...

Multiple Linear Model: **life_expectancy ~ .**

```
gap_fullmodels <- gap_nested %>%
  mutate(model = map(data, ~lm(formula = life_expectancy ~ ., data = .x)))
```



Using broom with Multiple Linear Regression models

```
tidy(gap fullmodels$model[[1]])
                    estimate std.error statistic
                                                    p.value
      (Intercept) -1.830195e+03 1.502271e+02 -12.182848 5.325478e-16
           year 9.814091e-01 7.800580e-02 12.581232 1.693870e-16
 infant mortality -1.603504e-01 4.021732e-03 -39.870986 2.525847e-37
      fertility -2.600935e-01 1.648652e-01 -1.577614 1.215074e-01
      population -1.611437e-06 1.704374e-07 -9.454716 2.347590e-12
       qdpPercap -1.797662e-03 4.878209e-04 -3.685086 6.008755e-04
augment(gap fullmodels$model[[1]])
  life expectancy year infant mortality fertility population ... .fitted
          48.02 1961 148.1 7.65 11404859 ... 48.35078
   48.55 1962 148.2 7.65 11690152 ... 49.26449
glance(gap fullmodels$model[[1]])
 r.squared adj.r.squared sigma statistic p.value df logLik ...
1 0.9990732 0.9989724 0.3160595 9917.133 1.562325e-68 6 -10.70225 ...
```



Adjusted R^2

```
glance(gap_fullmodels$model[[1]])

r.squared adj.r.squared sigma statistic p.value df logLik ...
1 0.9990732 0.9989724 0.3160595 9917.133 1.562325e-68 6 -10.70225 ...
```





Let's practice!