Guide for the Quantum-Circuit Package

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ABSTRACT

Quantum-Circuit is a library for creating quantum circuit diagrams in Typst.

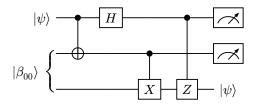
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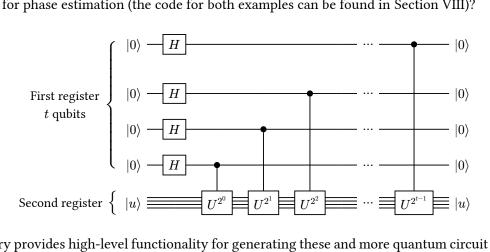
I Introduction

Section IV features a gallery of many gates that are possible to use with this library and how to create them. In Section VIII, you can find a variety of example figures along with the code.

Would you like to create quantum circuits directly in Typst? Maybe a circuit for quantum teleportation?



Or rather for phase estimation (the code for both examples can be found in Section VIII)?



This library provides high-level functionality for generating these and more quantum circuit diagrams.

For those who work with the LaTeX packages qcircuit and quantikz, the syntax will be somewhat familiar. The wonderful thing about Typst is that the changes can be viewed instantaneously which makes it ever so much easier to design a beautiful quantum circuit. The syntax also has been updated a little bit to fit with concepts of the Typst language and many things like styling content is much simpler than with quantikz since it is directly supported in Typst.

II Basics

A basic circuit can be created by calling the quantum-circuit() command with a number of circuit elements:

```
#quantum-circuit(
   1, gate($H$), phase($theta.alt$), meter(), 1
)
```

A quantum gate is created using the gate() command. Unlike qcircuit and quantikz, the math environment is not automatically entered for the content of the gate which allows to pass in any type of content (even images or tables). Use displaystyle math (for example \$ U_1 \$ instead of \$U_1\$) to enable appropriate scaling of the gate for more complex mathematical expressions like double subscripts etc.

Consecutive gates are automatically joined with wires. Plain integers can be used to indicate a number of cells with just wire and no gate (where you would use a lot of &'s and qw's in quantikz):

```
#quantum-circuit(
  1, gate($H$), 4, meter()
H
```

A new wire can be created by breaking the current wire with $[\ \]$:

```
#quantum-circuit(
   1, gate($H$), ctrl(1), 1, [\],
   2, targ(), 1
)
```

We can create a cx-gate by calling ctrl(0) and passing the relative distance to the desired wire, e.g., 1 to the next wire, 2 to the second-next one or -1 to the previous wire. Per default, the end of the vertical wire is just joined with the target wire without any decoration at all. Here, we make the gate a cx-gate by adding a targ() symbol on the second wire.

Let's look at a quantum bit-flipping error correction circuit. Here we encounter our first multi-qubit gate as well as wire labels:

Multi-qubit gates have a dedicated command mqgate() which takes the content as well as the number of qubits. Wires can be labelled at the beginning or the end with the lstick() and rstick() commands respectively.

In many circuits, we need classical wires. This library generalizes the concept of quantumm classical and bundled wires and provides the setwire() command that allows all sorts of changes to the current wire setting. You may call setwire() with the number of wires to display:

The setwire command produces no cells and can be called at any point on the wire. When a new wire is started, the default wire setting is restored automatically (quantum wire with default wire style, see Section III on how to customize the default). Calling setwire(0) removes the wire altogether until setwire is called with different arguments. More than two wires are possible and it lies in your hands to decide how many wires still look good. The distance between wires can also be specified:

```
#quantum-circuit(
  setwire(4, wire-distance: 1.5pt), 1, gate($U$), meter()
```

III CIRCUIT STYLING

The quantum-circuit() command provides several options for styling the entire circuit. The parameters row-spacing and column-spacing allow changing the optical density of the circuit by adjusting the spacing between circuit elements vertically and horizontically.

```
#quantum-circuit(
   row-spacing: 5pt,
   column-spacing: 5pt,
   1, gate($A$), gate($B$), 1, [\],
   1, 1, gate($S$), 1
)
```

The wire, color and fill options provide means to customize line strokes and colors. This allows us to easily create "dark-mode" circuits:

```
#box(fill: black, quantum-circuit(
  wire: .7pt + white, // Wire and stroke color
  color: white, // Default foreground and text color
  fill: black, // Gate fill color
  1, gate($X$), ctrl(1), rstick([*?*]), [\ ],
  1,1, targ(), meter(),
))
```

Furthermore, a common task is changing the total size of a circuit by scaling it up or down. Instead of tweaking all the parameters like font-size, padding, row-spacing etc. you can specify the scale-factor option which takes a percentage value:

```
#quantum-circuit(
    scale-factor: 60%,
    1, gate($H$), ctrl(1), gate($H$), 1, [\ ],
    1, 1, targ(), 2
)
```

Note, that this is different than calling Typst's builtin scale() function on the circuit which would scale it without affecting the layout, thus still reserving the same space as if unscaled!

For an optimally layout, the height for each row is determined by the gates on that wire. For this reason, the wires can have different distances. To better see the effect, let's decrease the row-spacing:

```
#quantum-circuit(
    row-spacing: 2pt, min-row-height: 4pt,
    1, gate($H$), ctrl(1), gate($H$), 1, [\],
    1, gate($H$), targ(), gate($H$), 1, [\],
    2, ctrl(1), 2, [\],
    1, gate($H$), targ(), gate($H$), 1
```

Setting the option equal-row-heights to true solves this problem (manually spacing the wires with lengths is still possible, see Section V):

```
#quantum-circuit(
    equal-row-heights: true,
    row-spacing: 2pt, min-row-height: 4pt,
    1, gate($H$), ctrl(1), gate($H$), 1, [\],
    1, gate($H$), targ(), gate($H$), 1, [\],
    2, ctrl(1), 2, [\],
    1, gate($H$), targ(), gate($H$), 1
)
```

There is another option for quantum-circuit() that has a lot of impact on the looks of the diagram: gate-padding. This at the same time controls the default gate box padding and the distance of lstick's and rstick's to the wire. Need really wide or tight circuits?

```
#quantum-circuit(
    gate-padding: 2pt,
    row-spacing: 5pt, column-spacing: 7pt,
    lstick($|0)$, num-qubits: 3), gate($H$), ctrl(1),
        ctrl(2), 1, rstick("GHZ", num-qubits: 3), [\],
    1, gate($H$), ctrl(0), 1, gate($H$), 1, [\],
    1, gate($H$), 1, ctrl(0), gate($H$), 1, [\],
}
```

IV GATE GALLERY

Normal gate	—[H]—	gate(\$H\$)	Round gate	<u>—(X)</u> —	gate(\$X\$, radius: 100%)
D gate	<u>-</u> Y	<pre>gate(\$Y\$, radius: (right: 100%))</pre>	Meter		meter()
Meter with label	±> 	<pre>meter(label: \$lr(±>)\$)</pre>	Phase gate	<u>α</u>	phase(\$α\$)
Control	-•-	ctrl(0)	Open control		ctrl(0, open: true)
Target		targ()	Swap target	-×-	targX()
Permutation gate		permute(2,0,1)	Multiqubit gate		mqgate(\$U\$, 3)
lstick	$ \psi angle \$	lstick(\$ psi>\$)	rstick	$ \ket{\psi}$	rstick(\$ psi>\$)
Multi-qubit lstick	$ \psi angle \; \left\{ \begin{array}{c} \end{array} ight.$	lstick(\$ psi>\$, num-qubits: 2)	Multi-qubit rstick	$egin{array}{c} \ \ \end{bmatrix} \ket{\psi}$	<pre>rstick(\$ psi\s, num-qubits: 2, brace: "]")</pre>
midstick	— yeah —	midstick("yeah")	Wire bundle		nwire(5)
Controlled z-gate		ctrl(1) + ctrl(0)	Controlled x-gate	—	ctrl(1) + targ()
Swap gate	- * -	swap(1) + targX()	Controlled Hadamard		controlled(\$H\$, 1) + ctrl(0)
Meter to classical		meter(target: 1) + ctrl(0)			

V FINE-TUNING

The quantum-circuit() command allows not only gates as well as content and string items but only length parameters which can be used to tweak the appearance of the circuit. Inserting a length value between gates adds a **horizontal space** of that length between the cells:

```
#quantum-circuit( gate(X), gate(Y), 10pt, gate(Z) X Y Z
```

In the background, this works like a grid gutter that is set to 0pt by default. If a length value is inserted between the same two columns on different wires/rows, the maximum value is used for the space. In the same spirit, inserting multiple consecutive length values result in the largest being used, e.g., a 5pt, 10pt, 6pt results in a 10pt gutter in the corresponding position.

Putting a a length after the wire break item [\] produces a **vertical space** between the corresponding wires:

VI Annotations

Quantum-Circuit provides a way of making custom annotations through the annotate() interface. An annotate() object may be placed anywhere in the circuit, the position only matters for the draw order in case several annotations would overlap.

The annotate() command allows for querying cell coordinates of the circuit and passing in a custom draw function to draw globally in the circuit diagram.

Let's look at an example:

```
#quantum-circuit(
  1, ctrl(1), gate($H$), meter(), [\ ],
  1, targ(), 1, meter(),
                                                                                                 Readout circuit
  annotate(0, (2, 4),
    (y, (x1, x2)) \Rightarrow \{
      let brace = math.lr($#box(height: x2 - x1)}$)
      place(dx: x1, dy: y, rotate(brace, -90deg, origin: top))
      let content = [Readout circuit]
      style(styles => {
        let size = measure(content, styles)
        place(dx: x1 + (x2 - x1)/2 - size.width/2, dy: y - .6em - size.height,
content)
      })
  })
)
```

First, the call to annotate() asks for the y coordinate of the zeroth row (first wire) and the x coordinates of the second and forth column. The draw callback function then gets the corresponding coordinates as arguments and uses them to draw a brace and some text above the cells.

Note, that the circuit does not know how large the annotation is. If it goes beyond the circuits bounds, you may want to adjust the parameter circuit-padding of quantum-circuit() appropriately.

Another example, here we want to obtain coordinates for the cell centers. We can achieve this by adding 0.5 to the cell index. The fractional part of the number represents a percentage of the cell width/height.

VII Function Documentation

```
gate(
  content-type string,
  arg: string none auto boolean
  a: integer symbol function float
)
```

This section contains a complete reference for every function in **quantum-circuit**.

Gates

- gate()
- mqgate()
- <u>meter()</u>
- permute()
- phantom()
- <u>targ()</u>
- targX()
- phase()
- controlled()
- <u>swap()</u>
- <u>ctrl()</u>

Decorations

- <u>lstick()</u>
- rstick()
- nwire()
- setwire()
- gategroup()
- <u>slice()</u>
- annotate()

Quantum Circuit

• quantum-circuit()

gate

Basic command for creating gates. Use this to create a simple gate, e.g. gate(\$X\$). For special gates, many other dedicated gate commands exist.

Note, that many of the parameters listed here are mostly used for derived gate function and do not need to be touched in all but very few cases.

Parameters

```
gate(
  content: content,
  fill: none color,
  radius: length dictionary,
  box: boolean,
  floating: boolean,
  multi: dictionary,
  size-hint: function,
  draw-function: function,
  gate-type,
  args: dictionary
)
```

content content

What to show in the gate (none for special gates).

fill none or color

Gate backgrond fill color.

Default: none

radius length or dictionary

Gate rectangle border radius. Allows values like the builtin rect() function.

Default: Opt

box boolean

Whether this is a boxed gate (determines whether the outgoing wire will be drawn all through the gate (box: false) or not).

Default: true

floating boolean

Whether the content for this gate will be shown floating (i.e. no width is reserved).

Default: false

multi dictionary

Information for multi-qubit and controlled gates (see mqgate().

Default: none

size-hint function

Size hint function.

Default: default-size-hint

draw-function function

Drawing function that produces the displayed content. Signature: (gate, draw-params).

 $Default: {\tt draw-boxed-gate}$

args dictionary

Optional additional arguments. When using a custom draw-function , you may store extra information here.

Default: (:)

mqgate

Basic command for creating multi-qubit or controlled gates. For the latter, you usually want to go for something like ctrl(), swap(), or <a href="mailto:controlled().

Parameters

```
mqgate(
  content: content,
  num-qubits: integer,
  fill: none color,
  radius: length dictionary,
  box: boolean,
  label: content,
  control: boolean,
  wire-count: integer,
  extent: auto length,
  size-all-wires: none boolean,
  draw-function,
  args
)
```

num-qubits integer

Number of qubits (or relative wire count for controlled gates).

```
fill none or color

Gate backgrond fill color.
```

Default: none

radius length or dictionary

Gate rectangle border radius. Allows values like the builtin rect() function.

Default: Opt

box boolean

Whether this is a boxed gate (determines whether the outgoing wire will be drawn all through the gate (box: false) or not)

Default: true

label content

Optional label on the vertical wire.

Default: none

```
control boolean
```

If true, this gate draws a vertical control wire.

Default: false

wire-count integer

Wire count for control wires.

Default: 1

```
extent auto or length
```

How much to extent the gate beyond the first and last wire, default is to make it align with an X gate (so [size of x gate] / 2).

Default: auto

```
size-all-wires none or boolean
```

A single-qubit gate affects the height of the row it's being put on. For multi-qubit gate there are different possible behaviours:

- Affect size on only the first and last qubit (false)
- Affect the size of all qubits (true)
- Affect the size on no qubit (none)

Default: false

meter

Draw a meter box representing a measurement.

Parameters

```
meter(
  target: none integer,
  wire-count: integer,
  label: content
)
```

```
target none or integer
```

Default: none

wire-count integer

Wire count for the control wire.

Default: 2

label content

Label to show above the meter.

```
Default: none
```

permute

Create a viualized permutation gate which maps the qubits q_k,q_{k+1},\dots to the qubits $q_{p(k)},q_{p(k+1)},\dots$ when placed on qubit k. The permutation map is given by the qubits argument.

Example:

permute(1, 0) when placed on the second wire swaps the second and third wire.

```
permute(2, 0, 1) when placed on wire 0 maps (0,1,2)\mapsto (2,0,1)
```

Note, that the wiring is not very sophisticated and will probably look best for relatively simple permutations. Furthermore, it only works with quantum wires.

• ..qubits (array): Qubit permutation specification.

Parameters

phantom

Create an invisible (phantom) gate for reserving space. If content is provided, the height and width parameters are ignored and the gate will take the size it would have if gate(content) was called.

Instead specifying width and/or height will create a gate with exactly the given size (without padding).

Parameters

```
phantom(
    content: content,
    width: length,
    height: length
)

content content

Content to measure for the phantom gate size.

Default: none

width length
```

Width of the phantom gate (ignored if $% \left(1\right) =\left(1\right) =\left(1\right)$ content is not none).

Default: Opt

height length

Height of the phantom gate (ignored if $\,$ content $\,$ is not none).

Default: Opt

targ

Target element for controlled x operations (\oplus).

Parameters

```
fill: none color boolean,
    size: length
)
fill none or color or boolean
Fill color for the target circle. If set to true, the target
```

is filled with the circuits background color.

Default: none

size length

Size of the target symbol.

Default: 4.3pt

targX

Target element for swap operations (\times) without vertical wire).

Parameters

```
targX(size: length)
```

```
size length
Size of the target symbol.
Default: 7pt
```

phase

Create a phase gate shown as a point on the wire together with a label.

Parameters

```
phase(
  label: content,
  open: boolean,
  fill: none color,
  size: length
label
          content
Angle value to display.
open
           boolean
Whether to draw an open dot.
Default: false
fill
        none or color
Fill color for the circle or stroke color if open: true.
Default: none
size
         length
Size of the circle.
Default: 2.3pt
```

rstick

Basic command for labelling a wire at the end.

Parameters

```
rstick(
  label: content,
  num-qubits: content,
  brace: auto none string
)
```

label content

Label to display, e.g. \$10>\$.

```
num-qubits content
```

How many qubits the rstick should span.

Default: 1

```
brace auto or none or string
```

If brace is auto , then a default } brace is shown only if num-qubits > 1 . A brace is always shown when explicitly given, e.g., "}" , "[" or "|" . No brace is shown for brace: none .

Default: auto

lstick

Basic command for labelling a wire at the start.

Parameters

```
lstick(
  label: content,
  num-qubits: content,
  brace: auto none string
)
```

label content

Label to display, e.g. \$10>\$.

num-qubits content

How many qubits the lstick should span.

Default: 1

brace auto or none or string

If brace is auto , then a default { brace is shown only if num-qubits > 1 . A brace is always shown when explicitly given, e.g., "}" , "[" or "|" . No brace is shown for brace: none .

Default: auto

nwire

Creates a symbol similar to \qwbundle on quantikz. Annotates a wire to be a bundle of quantum or classical wires.

• n(integer):

Parameters

nwire(n)

controlled

Create a controlled gate. See also ctrl(). This function however may be used to create controlled gates where a gate box is at both ends of the control wire.

Example: controlled(\$H\$, 2).

Parameters

```
controlled(
  content: content,
  relative-qubit: integer,
  wire-count: integer,
  draw-function,
   ..args
)
```

content

content

Gate content to display.

relative-qubit integer

Target qubit relative to this one.

wire-count integer

Wire count for the control wire.

- draw-function (function). See gate() .
- ..args (array): Optional, additional arguments to be stored in the gate.

Default: 1

swap

Creates a SWAP operation with another qubit.

Parameters

```
swap(
  relative-qubit: integer,
  size: length
)
```

relative-qubit integer

Target qubit relative to this one.

size length

Size of the target symbol.

Default: 7pt

ctrl

Creates a control with a vertical wire to another qubit.

Parameters

```
ctrl(
  relative-qubit: integer,
  wire-count: integer,
  open: boolean,
  fill: none color,
  size: length
)
```

relative-qubit integer

Target qubit relative to this one.

wire-count integer

Wire count for the control wire.

Default: 1

```
open boolean
```

Whether to draw an open dot.

Default: false

```
fill none or color
```

Fill color for the circle or stroke color if open: true.

Default: none

size length

Size of the control circle.

Default: 2.3pt

setwire

Set current wire mode (0: none, 1 wire: quantum, 2 wires: classical, more are possible) and optionally the stroke style.

The wire style is reset for each row.

Parameters

```
setwire(
  wire-count: integer,
  stroke: none stroke,
  wire-distance: length
)
```

wire-count integer

Number of wires to display.

stroke none or stroke

When given, the stroke is applied to the wire. Otherwise the current stroke is kept.

Default: none

wire-distance length

Distance between wires.

Default: 1pt

gategroup

Highlight a group of circuit elements by drawing a rectangular box around them.

Parameters

```
gategroup(
  wires: integer,
```

```
steps: integer,
padding: length dictionary,
stroke: stroke,
fill: color,
radius: length dictionary
)
```

wires integer

Number of wires to include.

steps integer

Number of columns to include.

padding length or dictionary

Padding of rectangle. May be one length for all sides or a dictionary with the keys left, right, top, bottom and default. Not all keys need to be specified. The value for default is used for the omitted sides or Opt if no default is given.

Default: Opt

stroke stroke

Stroke for rectangle.

Default: .7pt

fill color

Fill color for rectangle.

Default: none

radius length or dictionary

Corner radius for rectangle.

Default: Opt

slice

Slice the circuit vertically, showing a separation line between columns.

Parameters

```
slice(
  wires: integer,
  label: content,
  stroke: stroke,
  dx,
  dy
)
```

```
wires integer

Number of wires to slice.
```

Default: 0

label content

Label for the slice.

Default: none

```
stroke stroke
```

Line style for the slice.

```
Default: (paint: red, thickness: .7pt, dash: "dashed")
```

annotate

Lower-level interface to the cell coordinates to create an arbitrary annotatation by passing a custom function.

This function is passed the coordinates of the specified cell rows and columns.

Parameters

```
annotate(
  rows: integer array,
  columns: integer array,
  callback: function
)
```

```
rows integer or array
```

Row indices for which to obtain coordinates.

```
columns integer or array
```

Column indices for which to obtain coordinates.

callback function

Function to call with the obtained coordinates. The signature should be with signature (row-coords, col-coords) => {} . This function is expected to display the content to draw in absolute coordinates within the circuit.

quantum-circuit

Create a quantum circuit diagram. Content items may be

- Gates created by one of the many gate commands (gate(), mqgate(), meter(),...)
- [\] for creating a new wire/row

- Commands like setwire() or gategroup()
- Integers for creating cells filled with the current wire setting
- Lengths for creating space between rows or columns
- Plain content or strings to be placed on the wire
- lstick, midstick or rstick for placement next to the wire

Parameters

```
quantum-circuit(
  wire: stroke,
  row-spacing: length,
  column-spacing: length,
  min-row-height: length,
  min-column-width: length,
  gate-padding: length,
  equal-row-heights: boolean,
  color: color,
  fill: color,
  font-size: length,
  scale-factor: relative length,
  baseline: length content string,
  circuit-padding: dictionary ,
  ..content
)
```

wire stroke

Style for drawing the circuit wires. This can take anything that is valid for the stroke of the builtin line function.

Default: .7pt + black

row-spacing length

Spacing between rows.

Default: 12pt

column-spacing length

Spacing between columns.

Default: 12pt

min-row-height length

Minimum height of a row (e.g. when no gates are given).

Default: 10pt

min-column-width

length

Minimum width of a column.

Default: Opt

gate-padding length

General padding setting including the inset for gate boxes and the distance of lstick and co. to the wire.

Default: .4em

equal-row-heights boolean

If true, then all rows will have the same height and the wires will have equal distances orienting on the highest row.

Default: false

color color

Foreground color, default for strokes, text, controls etc. If you want to have dark-themed circuits, set this to white for instance and update wire and fill accordingly.

Default: black

fill color

Default fill color for gates.

Default: white

font-size length

Default font size for text in the circuit.

Default: 10pt

scale-factor relative length

Total scale factor applied to the entire circuit without changing proportions

Default: 100%

baseline length or content or string

Set the baseline for the circuit. If a content or a string is given, the baseline will be adjusted auto-matically to align with the center of it. One useful application is "=" so the circuit aligns with the equals symbol.

Default: Opt

circuit-padding dictionary

Padding for the circuit (e.g., to accomodate for annotations) in form of a dictionary with possible keys left, right, top and bottom. Not all of those need to be specified.

This setting basically just changes the size of the bounding box for the circuit and can be used to increase it when labels or annotations extend beyond the actual circuit.

• ..content (array): Items, gates and circuit commands (see description).

Default: none

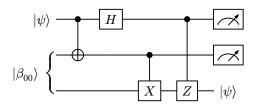
VIII DEMO

This section demonstrates the use of the **quantum-circuit** library by reproducing some figures from the famous book *Quantum Computation and Quantum Information* by Nielsen and Chuang [1].

VIII.a Quantum teleportation

Quantum teleportation circuit reproducing the Figure 4.15 in [1].

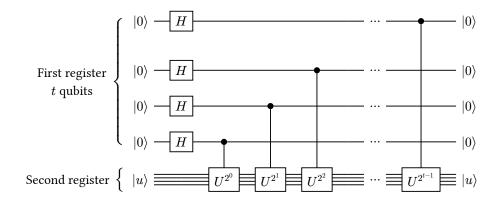
```
#quantum-circuit(
  lstick($|psi\$), ctrl(1), gate($H\$), 1, ctrl(0), meter(), [\ ],
  lstick(\$|beta_00\$, num-qubits: 2), targ(), 1, ctrl(0), 1, meter(), [\ ],
  3, controlled(\$X\$, -1), controlled(\$Z\$, -2), midstick(\$|psi\$)
)
```



VIII.b Quantum phase estimation

Quantum phase estimation circuit reproducing the Figure 5.2 in [1].

```
#quantum-circuit(
    setwire(0), lstick(align(center)[First register\ $t$ qubits], num-qubits: 4), lstick($|0\$),
    setwire(1), gate($H$), 4, midstick($ dots $), ctrl(4), rstick($|0\$), [\ ], 10pt,
    setwire(0), phantom(width: 13pt), lstick($|0\$), setwire(1), gate($H$), 2, ctrl(3), 1,
        midstick($ dots $), 1, rstick($|0\$), [\ ],
    setwire(0), 1, lstick($|0\$), setwire(1), gate($H$), 1, ctrl(2), 2,
        midstick($ dots $), 1, rstick($|0\$), [\ ],
    setwire(0), 1, lstick($|0\$), setwire(1), gate($H$), ctrl(1), 3, midstick($ dots $), 1,
        rstick($|0\$), [\ ],
    setwire(0), lstick([Second register], num-qubits: 1, brace: "{"}, lstick($|u\$),
        setwire(4, wire-distance: 1.3pt), 1, gate($ U^2^0 $), gate($ U^2^1 $), gate($ U^2^2 $),
        1, midstick($ dots $), gate($ U^2^(t-1) $), rstick($|u\$)
}
```



VIII.c Quantum Fourier transform:

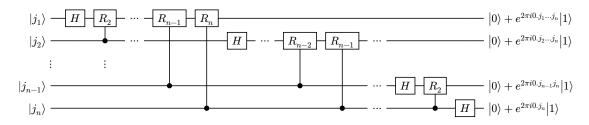
Circuit for performing the quantum Fourier transform, reproducing the Figure 5.1 in [1].

```
#quantum-circuit(
    scale-factor: 85%,
    row-spacing: 5pt,
    column-spacing: 8pt,
    lstick($|j_1\$), gate($H$), controlled($R_2\$, 1), midstick($ dots $),
        controlled($R_[n-1)\$, 3), controlled($R_n\$, 4), 8, rstick($|0)+e^(2pi i 0.j_1 dots j_n)|1\$),[\],
    lstick($|j_2\$), 1, ctrl(0), midstick($ dots $), 2, gate($H$), midstick($ dots $),
        controlled($R_[n-2)\$, 2), controlled($R_[n-1)\$, 3), midstick($ dots $),
        rstick($|0)+e^(2pi i 0.j_2 dots j_n)|1\$), [\],

setwire(0), midstick($dots.v\$), 1, midstick($dots.v\$), [\],

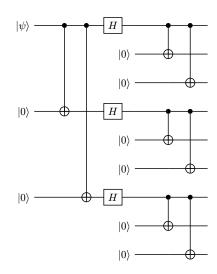
lstick($|j_(n-1)\$), 3, ctrl(0), 3, ctrl(0), 1, midstick($ dots $), gate($H\$), controlled($R_(2)\$, 1),
    1, rstick($|0)+e^(2pi i 0.j_[n-1)j_n)|1\$), [\],

lstick($|j_n\$), 4, ctrl(0), 3, ctrl(0), midstick($ dots $), 1, ctrl(0), gate($H\$),
    rstick($|0)+e^(2pi i 0.j_n)|1\$)
)
```



VIII.d Shor Nine Qubit Code

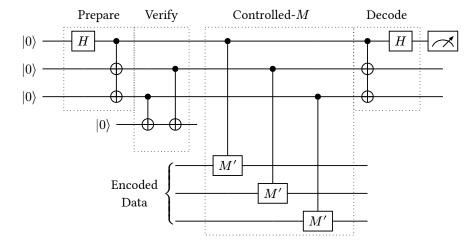
Encoding circuit for the Shor nine qubit code. This diagram repdoduces Figure 10.4 in [1]



VIII.e Fault-Tolerant Measurement

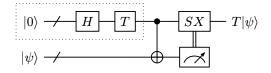
Circuit for performing fault-tolerant measurement (as Figure 10.28 in [1]).

```
#let mark(text, col1, col2) = annotate(0, (col1, col2),
  (y, (x1, x2)) \Rightarrow style(styles \Rightarrow {
    let size = measure(text, styles)
    place(dx: x1 + (x2 - x1)/2 - size.width/2, dy: y - .6em - size.height, text)
#let group = gategroup.with(stroke: (dash: "dotted", thickness: .5pt))
#quantum-circuit(
  row-spacing: 6pt,
  circuit-padding: (top: 2em),
  lstick(\$|0)\$), 10pt, group(3, 2), gate(\$H\$), ctrl(2), 3pt, group(4, 2), 3, group(7, 3),
    ctrl(4), 2, 10pt, group(3, 2), ctrl(2), gate($H$), meter(), [\],
  lstick($|0)$), 1, targ(), 1, ctrl(2), 2, ctrl(4), 1, targ(), 2, [\],
  lstick(\$|0\rangle\$), 1, targ(), ctrl(1), 4, ctrl(4), targ(), 2, [\],
  setwire(0), 2, lstick(\$|0\rangle\$), setwire(1), targ(), targ(), 1, [\ ], 10pt,
  setwire(0), 4, lstick(align(center)[Encoded\ Data], num-qubits: 3), setwire(1), 1,
    gate($M'$), 3, [\],
  setwire(0), 5, setwire(1), 2, gate($M'$), 2, [\],
  setwire(0), 5, setwire(1), 3, gate($M'$), 1,
mark("Prepare", 1, 3),
 mark("Verify", 3, 5),
  mark([Controlled-$M$], 5, 9),
  mark("Decode", 9, 11)
)
```

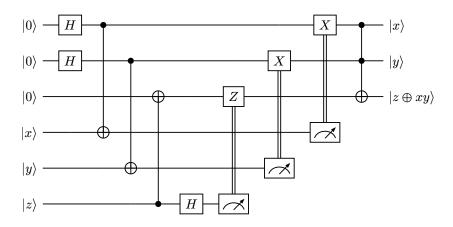


VIII.f Fault-Tolerant Gate Construction

The following two circuits reproduce figures from Exercise 10.66 and 10.68 on construction fault-tolerant $\frac{\pi}{8}$ and Toffoli gates in [1].

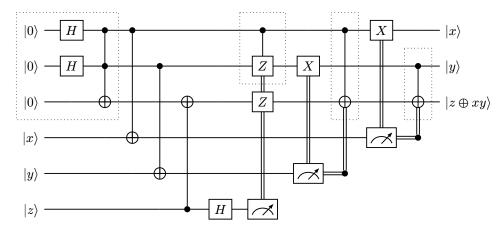


```
#quantum-circuit(
  lstick($|0>$), gate($H$), ctrl(3), 5, gate($X$), ctrl(2), rstick($|x>$), [\ ],
  lstick($|0>$), gate($H$), 1, ctrl(3), 3, gate($X$), 1, ctrl(0), rstick($|y>$), [\ ],
  lstick($|0>$), 3, targ(), 1, gate($Z$), 2, targ(), rstick($|z plus.circle x y>$), [\ ],
  lstick($|x>$), 1, targ(), 5, meter(target: -3), [\ ],
  lstick($|y>$), 2, targ(), 3, meter(target: -3), [\ ],
  lstick($|z>$), 3, ctrl(-3), gate($H$), meter(target: -3)
)
```



```
#let group = gategroup.with(stroke: (dash: "dotted", thickness: .5pt))

#quantum-circuit(
    group(3, 3, padding: (left: 1.5em)), lstick($|0)$), gate($H$), ctrl(2), ctrl(3), 3,
        group(2, 1),ctrl(1), 1, group(3, 1), ctrl(2), gate($X$), 1, rstick($|x)$), [\],
    lstick($|0)$), gate($H$), ctrl(0), 1, ctrl(3), 2, gate($Z$), gate($X$), 2, group(2, 1),
    ctrl(1), rstick($|yy$), [\],
    lstick($|0)$), 1, targ(), 2, targ(), 1, gate($Z$), 1, targ(fill: true), 1, targ(fill: true),
    rstick($|0)$), 1, targ(), 2, targ(), 1, gate($Z$), 1, targ(fill: true), 2, targ(fill: true),
    rstick($|x)$, 2, targ(), 6, meter(target: -3), setwire(2), ctrl(-1, wire-count: 2), [\],
    lstick($|yy$), 3, targ(), 3, meter(target: -3), setwire(2), ctrl(-2, wire-count: 2), [\],
    lstick($|z)$), 4, ctrl(-3), gate($H$), meter(target: -4)
}
```



BIBLIOGRAPHY

[1] M. A. Nielsen, and I. L. Chuang, *Quantum Computation and Quantum Information*, 2nd ed., Cambridge University Press, 2022.