Numerical Anaylasis Proj 4

Prolem 1: Find the polynomial of degree 10 that interpolates the function arctan x at 11 equally spaced points in the interval [1,6]. Print the coefficients in the Newton form of the polynomial. Compute and print the difference between the polynomial and the function at 33 equally spaced points in the interval [0,8]. What conclusion can be drawn?

Prolem 1: Print the coefficients in the Newton form of the polynomial.

```
In [4]:
```

```
#import sympy
from sympy import *
import sympy as sym
import numpy as npy
import math
#using init printing
sym.init printing(use latex="mathjax")
init printing(use unicode=True,)
# # Function to find the root
def arctan(x):
    return npy.arctan(x)
def populateDatapoints matrix(f,x,y,a,b,n):
t = (b-a)/n
an=a
 for i in range(n):
    y[i,0] = f(an)
    x.append(an)
    an=an+t
def productTerm(i, value, x):
   product = 1
    for j in range(0,i):
        product = product * (value - x[j])
    return product
def dividedDiffTable matrix(x, y, n):
    for i in range(1,n):
        for j in range(0, n-i):
            y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (x[j] - x[i+j])
```

```
def NewtonDividedDifference(value,x,y,n):
    sum = y[0,0]
    for i in range(1, n):
        sum = sum + (productTerm(i, value, x) * y[0,i])
    return sum
# construct table polynomial 11
b=6
x=[]
x array=[]
n=11
ymatrix= sym.Matrix.zeros(n,n)
xmatrix= sym.Matrix.zeros(n)
populateDatapoints matrix(arctan,x,ymatrix,a,b,n)
dividedDiffTable matrix(x, ymatrix, n)
xmatrix=ymatrix.row(0)
print(xmatrix)
Matrix([[0.785398163397448, 0.402843797977465, -0.153274974082992, 0.0
458491398368293, -0.0110733536933921, 0.00216313869198317, -0.00032906
3209962730, 3.26938070460224e-5, 5.03927839154818e-7, -1.2198780505844
6e-6, 3.70644555184973e-7]])
Prolem 1: Find the polynomial of degree 10 that interpolates the function arctan x at 11 equally spaced
In [2]:
from sympy import *
init printing(use latex=True)
```

points in the interval [1,6]

```
#import sympy
from sympy import *
import sympy as sym
import numpy as npy
import math
#using init printing
sym.init printing(use latex="mathjax")
init_printing(use_unicode=True,)
x=symbols('x')
def populateDatapoints matrix(f,w,y,a,b,n):
t = (b-a)/n
# print('t',t)
# print('a',a)
```

```
# print('b',b)
 an=a
 for i in range(n):
    y[i,0] = f(an)
    w.append(an)
    an=an+t
def arctan(w):
    return npy.arctan(w)
def productTerm string(i, w):
    for j in range(0,i):
        temp=w[j]
        s= s + '('+ str(x-temp)+')'
        if(i != i-1):
            s=s+"*"
    #print('s product term:',s)
    return s
def dividedDiffTable matrix(w, y, n):
    for i in range(1,n):
        for j in range(0,n-i):
            y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (w[j] - w[i+j])
def NewtonDividedDifference_string(w,y,n):
    sum = y[0,0]
    s=''
    s=str(y[0,0])
    p=''
    for i in range(1, n):
        temp=y[0,i]
        p=productTerm_string(i,w)
        s = s + "+" + p + '(' + str(temp) + ')'
    return s
# #polynomial
a2 = 1
b2 = 6
n2 = 11
w=[]
ymatrix= sym.Matrix.zeros(n2,n2)
populateDatapoints_matrix(arctan,w,ymatrix,a2,b2,n2)
dividedDiffTable_matrix(w, ymatrix, n2)
# #string
x=symbols('x')
r= NewtonDividedDifference string(w,ymatrix,n2)
expand(r)
```

```
\# L2 = (x-0)*(x-3)/((2-0)*(2-3))
\# L3 = (x-0)*(x-2)/((3-0)*(3-2))
\# p = 1*L1 + 3*L2 + 0*L3
# expand(p)
Out[2]:
3.70644555184973 \cdot 10^{-7}x^{10} - 1.2507689503945 \cdot 10^{-5}x^9 + 0.000182979893808116x^8
      -0.0184140900756385x^5 - 0.00039789220117583x^4 + 0.18168736652767x^3
                                                     -0.0936294988557575
Prolem 1: Compute and print the difference between the polynomial and the function at 33 equally
spaced points in the interval [0,8]
In [3]:
# # Function to find the root
def arctan(x):
    return npy.arctan(x)
def NewtonDividedDifference string(w,y,n):
    sum = y[0,0]
    s=str(y[0,0])
    p=''
    for i in range(1, n):
         temp=y[0,i]
         p=productTerm_string(i,w)
         s = s + "+" + p + '(' + str(temp) + ')'
    return s
def productTerm string(i, w):
    for j in range(0,i):
         temp=w[j]
         s= s + '('+ str(x-temp)+')'
         if(i != i-1):
             s=s+"*"
    #print('s product term:',s)
```

L1 = (x-2)*(x-3)/((0-2)*(0-3))

def populateDatapoints matrix(f,x,y,a,b,n):

t = (b-a)/n

```
an=a
 for i in range(n):
    y[i,0] = f(an)
    x.append(an)
    an=an+t
def fillactual(f,a,b,n,r,v):
    t = (b-a)/n
    an=a
    for i in range(n):
#
          print('an',an)
        r.append(f(an))
        v.append(an)
        an=an+t
def getdifs expr(f,expr,a,b,n,diff):
    xvalues=[]
    realyvalues=[]
    fillactual(f,a,b,n,realyvalues,xvalues)
    for i in range(n):
        x=xvalues[i]
        aprox = eval(expr)
        d=aprox - realyvalues[i]
        diff.append(d)
def productTerm(i, value, x):
    product = 1
    for j in range(0,i):
        product = product * (value - x[j])
    return product
def dividedDiffTable matrix(x, y, n):
    for i in range(1,n):
        for j in range(0, n-i):
            y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (x[j] - x[i+j])
def NewtonDividedDifference(value,x,y,n):
    sum = y[0,0]
    for i in range(1, n):
        sum = sum + (productTerm(i, value, x) * y[0,i])
    return sum
def main():
#
      print('hello world')
    #assumption polynomial is degree the one constructed with 11 terms [0,6]
    #difference between the polynomial and the function at 33 equally spaced points
    #polynomial
    a2 = 1
    b2 = 6
    n2 = 11
    xvalues=[]
    ymatrix= sym.Matrix.zeros(n2,n2)
```

```
populateDatapoints matrix(arctan,xvalues,ymatrix,a2,b2,n2)
    dividedDiffTable matrix(xvalues, ymatrix, n2)
    expr = NewtonDividedDifference string(xvalues,ymatrix,n2)
    # diffs populate 33 equally spaced points
    a=0
    b=8
    n = 33
    diff=[]
    getdifs_expr(arctan,expr,a,b,n,diff)
    print("diffs:",diff)
    return 0
main()
diffs: [-0.093629498855757498, -0.029016435273853586, -0.0067801695146
522678, -0.0010229027955719339, -2.5396883236328271e-05, 2.55266510980
06781e-05, -6.6613381477509392e-16, -2.6693240513520067e-06, 2.4169797
874229459e-07, 5.5808495758036258e-07, -1.3803247878030334e-07, -1.925
1866367753223e-07, 9.620486629557945e-08, 1.0016641982524277e-07, -9.2
020687292304615e-08, -7.4547628070575911e-08, 1.2560967577179838e-07,
7.5609929428566147e-08, -2.5561252270378532e-07, -9.2090330472416326e-
08, 8.4102444475320226e-07, 2.2204460492503131e-16, -5.400587742121487
6e-06, 4.3794718580514314e-06, 0.00014443095242966386, 0.0007986653675
1249662, 0.0029723490323052548, 0.0089380159803891246, 0.02333339871953
71719, 0.054929600456944394, 0.11933704277219559, 0.24302732121823101,
0.469098352659870881
Out[3]:
```

What conclusion can be drawn? Numerically we can see that the interpolation can be very accurate within the range that the interpolating polynomial is constructed and becomes increasingly un-accurate outside the bound in which it was constructed

Problem 2 (3 pts) Let f (x) = $max\{0, 1, -x\}$. Sketch the function f. Then find interpolating polynomials p of degrees 2, 4, 8, 16, and 32 to f on the interval [-4,4], using equally spaced nodes. Calculate the discrepancy f(x) - p(x) at 64 equally spaced points for each p and plot it. Then redo the problem using Chebyshev nodes. Compare.

Problem 2: Let $f(x) = max\{0, 1, -x\}$. Sketch the function $f(x) = max\{0, 1, -x\}$.

```
In [29]:
```

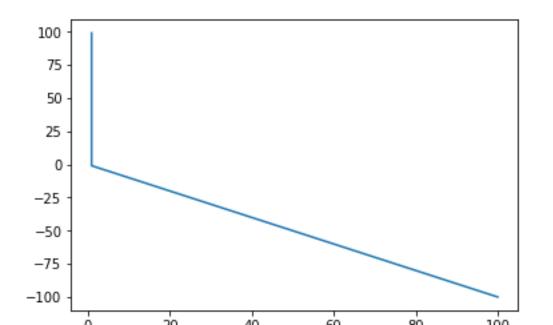
0

```
import matplotlib.pyplot as plt
from sympy import *
init printing(use latex=True)
```

```
#import sympy
from sympy import *
import sympy as sym
import numpy as npy
import math
#using init printing
sym.init printing(use latex="mathjax")
init printing(use unicode=True,)
x=symbols('x')
def populateDatapoints matrix(f,w,y,a,b,n):
t = (b-a)/n
# print('t',t)
# print('a',a)
# print('b',b)
an=a
 for i in range(n):
    y[i,0] = f(an)
   w.append(an)
    an=an+t
def arctan(w):
    return npy.arctan(w)
def productTerm string(i, w):
    s=''
    for j in range(0,i):
        temp=w[j]
        s= s + '('+ str(x-temp)+')'
        if(i != i-1):
            s=s+"*"
    #print('s product term:',s)
    return s
def dividedDiffTable_matrix(w, y, n):
    for i in range(1,n):
        for j in range(0,n-i):
            y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (w[j] - w[i+j])
def NewtonDividedDifference string(w,y,n):
    sum = y[0,0]
    s=''
    s=str(y[0,0])
    p=''
    for i in range(1, n):
        temp=y[0,i]
        p=productTerm string(i,w)
        s = s + "+" + p + '(' + str(temp) + ')'
    return s
```

def f(x):

```
x=x*(-1)
    return max(0, 1, x)
k=[]
y=[]
for i in range (-100,100):
    k.append(f(i))
    y.append(i)
 \#plot(p,(x,0,4),xlabel='x',ylabel='y',title='Interpolating polynomial for (0,-2), (
plt.plot(k, y)
plt.show()
```



find interpolating polynomials p of degrees 2, 4, 8, 16, and 32 to f on the interval

degree 2

[-4,4], using equally spaced nodes

```
In [107]:
```

```
import matplotlib.pyplot as plt
init printing(use latex=True)
import sympy as sym
import numpy as npy
import math
#using init printing
sym.init printing(use latex="mathjax")
init_printing(use_unicode=True,)
x=symbols('x')
def populateDatapoints matrix(f,w,y,a,b,n):
t = (b-a)/n
 an=a
 for i in range(n):
    y[i,0] = f(an)
    w.append(an)
    an=an+t
def arctan(w):
    return npy.arctan(w)
def productTerm string(i, w):
    s=''
    for j in range(0,i):
        temp=w[j]
        s= s + '('+ str(x-temp)+')'
        if(i != i-1):
            s=s+"*"
    #print('s product term:',s)
    return s
def dividedDiffTable matrix(w, y, n):
    for i in range(1,n):
        for j in range(0, n-i):
            y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (w[j] - w[i+j])
def NewtonDividedDifference_string(w,y,n):
    sum = y[0,0]
    s=''
    s=str(y[0,0])
    for i in range(1, n):
```

```
temp=y[0,i]
        p=productTerm string(i,w)
        s = s + "+" + p + '(' + str(temp) + ')'
    return s
def fw(w):
    w=w*(-1)
    return max(0, 1, w)
#Then find interpolating polynomials p of degrees 2, 4, 8, 16, and 32 to f on the in
# using equally spaced nodes.
#degrees 2
#---polynomial
a2 = -4
b2 = 4
n2=2
w2 = []
ymatrix= sym.Matrix.zeros(n2,n2)
populateDatapoints matrix(arctan,w2,ymatrix,a2,b2,n2)
dividedDiffTable matrix(w2, ymatrix, n2)
#---printing degrees 2
r2= NewtonDividedDifference string(w2,ymatrix,n2)
expand(r2)
Out[107]:
```

```
0.331454415917008x + 1.99840144432528 \cdot 10^{-15}
```

degree 4

In [6]:

```
import matplotlib.pyplot as plt
init_printing(use_latex=True)
import sympy as sym
import numpy as npy
import math
#using init printing
sym.init_printing(use_latex="mathjax")
init_printing(use_unicode=True,)
x=symbols('x')
def populateDatapoints_matrix(f,w,y,a,b,n):
t = (b-a)/n
```

```
# print('a',a)
# print('b',b)
 for i in range(n):
    y[i,0] = f(an)
    w.append(an)
    an=an+t
def arctan(w):
    return npy.arctan(w)
def productTerm_string(i, w):
    s=''
    for j in range(0,i):
        temp=w[j]
        s= s + '('+ str(x-temp)+')'
        if(i != i-1):
            s=s+"*"
    #print('s product term:',s)
    return s
def dividedDiffTable_matrix(w, y, n):
    for i in range(1,n):
        for j in range(0,n-i):
            y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (w[j] - w[i+j])
def NewtonDividedDifference_string(w,y,n):
    sum = y[0,0]
    s=''
    s=str(y[0,0])
    p=''
    for i in range(1, n):
        temp=y[0,i]
        p=productTerm string(i,w)
        s = s + "+" + p + '(' + str(temp) + ')'
    return s
def fw(w):
    w=w*(-1)
    return max(0, 1, w)
#Then find interpolating polynomials p of degrees 2, 4, 8, 16, and 32 to f on the in
# using equally spaced nodes.
#degrees 4
a2 = -4
b2 = 4
```

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n2=4 w4=[]

ymatrix= sym.Matrix.zeros(n2,n2)

```
populateDatapoints_matrix(iw,w4,ymatrix,a2,b2,n2)
dividedDiffTable_matrix(w4, ymatrix, n2)
#---printing degrees 4
r4= NewtonDividedDifference_string(w4,ymatrix,n2)
expand(r4)
Out[6]:
0.125x^2 - 0.25x + 1.0
degree 8
In [7]:
import matplotlib.pyplot as plt
init printing(use latex=True)
import sympy as sym
import numpy as npy
import math
#using init printing
sym.init printing(use latex="mathjax")
init_printing(use_unicode=True,)
x=symbols('x')
def populateDatapoints matrix(f,w,y,a,b,n):
 t = (b-a)/n
# print('t',t)
# print('a',a)
# print('b',b)
 an=a
 for i in range(n):
    y[i,0] = f(an)
    w.append(an)
    an=an+t
def arctan(w):
    return npy.arctan(w)
def productTerm_string(i, w):
    s=''
    for j in range(0,i):
        temp=w[j]
        s= s + '('+ str(x-temp)+')'
        if(i != i-1):
            s=s+"*"
    #print('s product term:',s)
    return s
def dividedDiffTable_matrix(w, y, n):
```

for i in range(1,n):

```
for j in range(0, n-i):
            y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (w[j] - w[i+j])
def NewtonDividedDifference string(w,y,n):
    sum = y[0,0]
    s=''
    s=str(y[0,0])
    p=''
    for i in range(1, n):
        temp=y[0,i]
        p=productTerm_string(i,w)
        s = s + "+" + p + '(' + str(temp) + ')'
    return s
def fw(w):
    w=w*(-1)
    return max(0, 1, w)
#Then find interpolating polynomials p of degrees 2, 4, 8, 16, and 32 to f on the in
# using equally spaced nodes.
#degrees 8
a2 = -4
b2 = 4
n2 = 8
w4 = []
ymatrix= sym.Matrix.zeros(n2,n2)
populateDatapoints matrix(fw,w4,ymatrix,a2,b2,n2)
dividedDiffTable_matrix(w4, ymatrix, n2)
#---printing degrees 8
r4= NewtonDividedDifference_string(w4,ymatrix,n2)
expand(r4)
Out[7]:
```

 $-0.00198412698412698x^7 - 0.00555555555555555553x^6 + 0.036111111111111111x^5 + 0.0$

 $-0.06388888888888888876x^2 + 0.18809523809524$

```
degree 16
```

In [104]:

```
import matplotlib.pyplot as plt
init_printing(use_latex=True)
import sympy as sym
import numpy as npy
import math
```

```
#using init_printing
sym.init_printing(use_latex="mathjax")
init printing(use unicode=True,)
x=symbols('x')
def populateDatapoints matrix(f,w,y,a,b,n):
t = (b-a)/n
# print('t',t)
# print('a',a)
# print('b',b)
an=a
 for i in range(n):
    y[i,0] = f(an)
    w.append(an)
    an=an+t
def arctan(w):
    return npy.arctan(w)
def productTerm_string(i, w):
    s=''
    for j in range(0,i):
        temp=w[j]
        s= s + '('+ str(x-temp)+')'
        if(i != i-1):
            s=s+"*"
    #print('s product term:',s)
    return s
def dividedDiffTable_matrix(w, y, n):
    for i in range(1,n):
        for j in range(0,n-i):
            y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (w[j] - w[i+j])
def NewtonDividedDifference string(w,y,n):
    sum = y[0,0]
    s=''
    s=str(y[0,0])
    p=''
    for i in range(1, n):
        temp=y[0,i]
        p=productTerm string(i,w)
        s = s + "+" + p + '(' + str(temp) + ')'
    return s
def fw(w):
    w=w*(-1)
    return max(0, 1, w)
#Then find interpolating polynomials p of degrees 2, 4, 8, 16, and 32 to f on the il
```

using equally spaced nodes.

```
#degrees 16
a2 = -4
b2 = 4
n2 = 16
w16=[]
ymatrix= sym.Matrix.zeros(n2,n2)
populateDatapoints matrix(fw,w16,ymatrix,a2,b2,n2)
dividedDiffTable matrix(w16, ymatrix, n2)
#---printing degrees 16
r16= NewtonDividedDifference string(w16,ymatrix,n2)
expand(r16)
Out[104]:
       1.61249685059209 \cdot 10^{-5}x^{15} + 4.6514332228618 \cdot 10^{-5}x^{14} - 0.0006186406180
+0.00937053070386402x^{11} +0.0197354497354495x^{10} -0.0718682287729915x^9 -0.
  +0.293641975308649x^6 -0.616966490299811x^5 -0.241865079365044x^4 +0.4672
                                      -0.0825896325895933x + 1.00000000000000
degree 32
In [13]:
import matplotlib.pyplot as plt
```

```
init printing(use latex=True)
import sympy as sym
import numpy as npy
import math
#using init printing
sym.init printing(use latex="mathjax")
init_printing(use_unicode=True,)
x=symbols('x')
def populateDatapoints matrix(f,w,y,a,b,n):
t = (b-a)/n
an=a
 for i in range(n):
    y[i,0] = f(an)
    w.append(an)
    an=an+t
def arctan(w):
    return npy.arctan(w)
def productTerm string(i, w):
    for j in range(0,i):
        temp=w[j]
        s = s + '(' + str(x-temp) + ')'
        if(i != i-1):
```

```
s=s+"*"
    return s
def dividedDiffTable matrix(w, y, n):
    for i in range(1,n):
         for j in range(0, n-i):
             y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (w[j] - w[i+j])
def NewtonDividedDifference_string(w,y,n):
    sum = y[0,0]
    s=str(y[0,0])
    p=''
    for i in range(1, n):
        temp=y[0,i]
        p=productTerm string(i,w)
        s = s + "+" + p + '(' + str(temp) + ')'
    return s
def fw(w):
    w=w*(-1)
    return max(0, 1, w)
#Then find interpolating polynomials p of degrees 2, 4, 8, 16, and 32 to f on the il
# using equally spaced nodes.
#degrees 32
a2 = -4
b2 = 4
n2 = 32
w32=[]
ymatrix= sym.Matrix.zeros(n2,n2)
populateDatapoints matrix(fw,w32,ymatrix,a2,b2,n2)
dividedDiffTable matrix(w32, ymatrix, n2)
#---printing degrees 32
r32= NewtonDividedDifference string(w32,ymatrix,n2)
expand(r32)
Out[13]:
      4.85087465772575 \cdot 10^{-9}x^{31} + 1.42598987783145 \cdot 10^{-8}x^{30} - 3.912212489505
      + 1.40464334535301 \cdot 10^{-5}x^{27} + 3.66401543325998 \cdot 10^{-5}x^{26} - 0.0002967737
+0.00410931699787995x^{23} +0.00901396325067296x^{22} -0.0393033127915205x^{21} -
```

 $+0.452866228986612x^{18} - 1.29534019295516x^{17} - 1.85135278530192x^{16} + 4.4666228986612x^{18} - 1.29534019295516x^{18} - 1.85135278530192x^{16} + 4.4666228986612x^{18} - 1.29534019295516x^{18} - 1.85135278530192x^{16} + 4.46662x^{18} - 1.46662x^{18} - 1.46666x^{18} - 1.46666x^{1$

 $-10.9959026817321x^{13} - 9.67916314376179x^{12} + 18.3688323680897x^{11} + 11$

 $-7.86432852663257x^8 + 12.9152231861739x^7 + 2.79778448621379x^6 - 4.42$

 $+0.65422122705294x^3 + 0.0172139869253196x^2 - 0.0264694521$

Calculate the discrepancy f(x) - p(x) at 64 equally spaced points for each p and plot it.

```
f(x) - p2(x)
```

```
In [29]:
import matplotlib.pyplot as plt
init_printing(use_latex=True)
import sympy as sym
import numpy as npy
import math
#using init_printing
sym.init printing(use latex="mathjax")
init_printing(use_unicode=True,)
x=symbols('x')
sym.init_printing(use_latex="mathjax")
init printing(use unicode=True,)
def populateDatapoints matrix(f,w,y,a,b,n):
t = (b-a)/n
 an=a
 for i in range(n):
   y[i,0] = f(an)
    w.append(an)
    an = an + t
#(arctan,w,ymatrix,a,b,ndegree_poly)
def populateDatapoints matrix Chebyshev(f,nodes,y,a,b,n):
 for j in range(n):
     nodes.append(npy.cos((2*(j+1)-1)/(2*n)*npy.pi))
 for i in range(n):
    y[i,0] = f(nodes[i])
def arctan(w):
    return npy.arctan(w)
def productTerm string(i, w):
    s=''
    for j in range(0,i):
        temp=w[j]
        s = s + '(' + str(x-temp) + ')'
        if(i != i-1):
            s=s+"*"
    #print('s product term:',s)
    return s
```

dof divided Difference matrix/w w

```
der dividedbilitable matrix(w, y, m).
   for i in range(1,n):
       for j in range(0,n-i):
           y[j,i] = (y[j,i-1] - y[j+1,i-1]) / (w[j] - w[i+j])
def NewtonDividedDifference_string(w,y,n):
   sum = y[0,0]
   s=''
   s=str(y[0,0])
   p=''
   for i in range(1, n):
       temp=y[0,i]
       p=productTerm string(i,w)
       s = s + "+" + p + '(' + str(temp) + ')'
   return s
# fillactual(fw,a2,b2,n2,realvalues,w2)
def fillactual(f,a,b,n,r,v):
   t = (b-a)/n
   an=a
   for i in range(n):
#
         print('an',an)
       r.append(f(an))
       v.append(an)
       an=an+t
def getdifs expr(f,expr,a,b,n,diff,xvalues):
   realyvalues=[]
   fillactual(f,a,b,n,realyvalues,xvalues)
   for i in range(n):
       x=xvalues[i]
       aprox = eval(expr)
       diff.append(d)
def fw(w):
   w=w*(-1)
   return max(0, 1, w)
def NewtonDividedDifference(value,w,y,n):
   sum = y[0,0]
   for i in range(1, n):
       sum = sum + (productTerm(i, value, w) * y[0,i])
   return sum
def difplot(ndegree poly,nPlaces):
   a=-4
   b=4
   n=2
   W = []
   createxvalues=[]
   diff=[]
   print('difference Poly Degree', ndegree poly, "Red is without Chebyshev nodes and
```

```
ymacrix- sym.Macrix.Zeros(ndegree_pory,ndegree_pory)
    populateDatapoints matrix(arctan,w,ymatrix,a,b,ndegree poly)
    dividedDiffTable_matrix(w, ymatrix, ndegree_poly)
    expr= NewtonDividedDifference string(w,ymatrix,n)
    getdifs expr(fw,expr,a,b,nPlaces,diff,createxvalues)
    plt.plot(createxvalues,diff,color='red')
                                                        #plot1
    #plt.show()
    title=str(ndegree_poly)+' diff without Chebyshev nodes'
    plt.savefig(title)
    plt.close()
    w=[]
    createxvalues=[]
    diff=[]
    ymatrix= sym.Matrix.zeros(ndegree poly,ndegree poly)
    populateDatapoints matrix Chebyshev(arctan,w,ymatrix,a,b,ndegree poly)##che
    dividedDiffTable matrix(w, ymatrix, ndegree poly)
    expr= NewtonDividedDifference_string(w,ymatrix,n)
    getdifs expr(fw,expr,a,b,nPlaces,diff,createxvalues)
    plt.plot(createxvalues, diff, color='green')
#
      plt.show()
    title=str(ndegree_poly)+' diff with Chebyshev nodes'
    plt.savefig(title)
    plt.close()
ndegree poly2=2
ndegree poly4=4
ndegree poly8=8
ndegree poly16=16
ndegree poly32=32
nPlaces=64
difplot(ndegree poly2,nPlaces)
difplot(ndegree_poly4,nPlaces)
difplot(ndegree poly8,nPlaces)
difplot(ndegree poly16,nPlaces)
difplot(ndegree poly32,nPlaces)
```

```
difference Poly Degree 2 Red is without Chebyshev nodes and green is w ith Chebyshev nodes
difference Poly Degree 4 Red is without Chebyshev nodes and green is w ith Chebyshev nodes
difference Poly Degree 8 Red is without Chebyshev nodes and green is w ith Chebyshev nodes
difference Poly Degree 16 Red is without Chebyshev nodes and green is with Chebyshev nodes
difference Poly Degree 32 Red is without Chebyshev nodes and green is with Chebyshev nodes
```

In []:		