



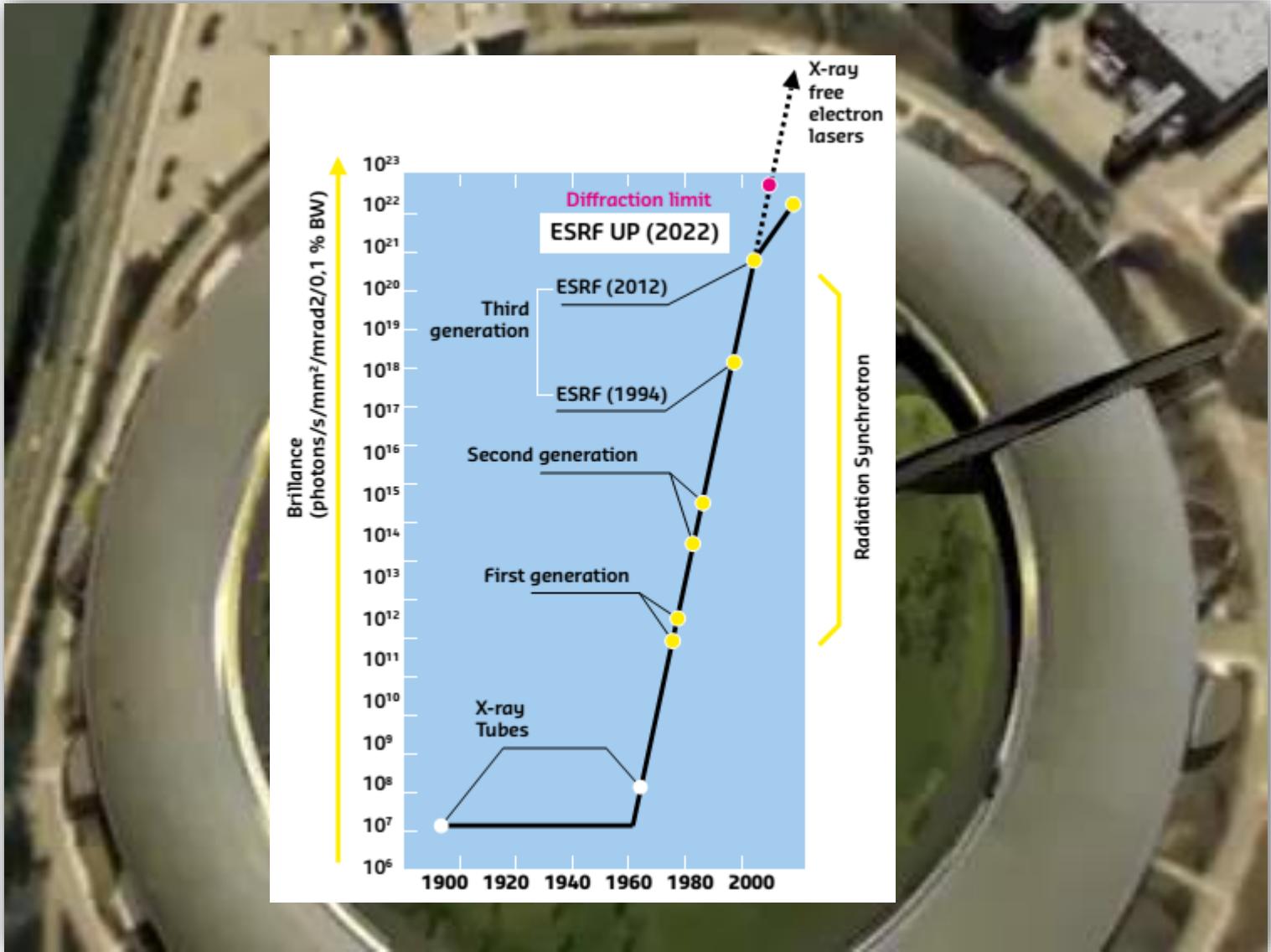


- ***Synchrotron radiation***
- ***Principles of X-ray optics***
- ***Mirrors***
- ***Diffractive optics***
- ***X-ray micro-/nano-focusing***
- ***Summary***

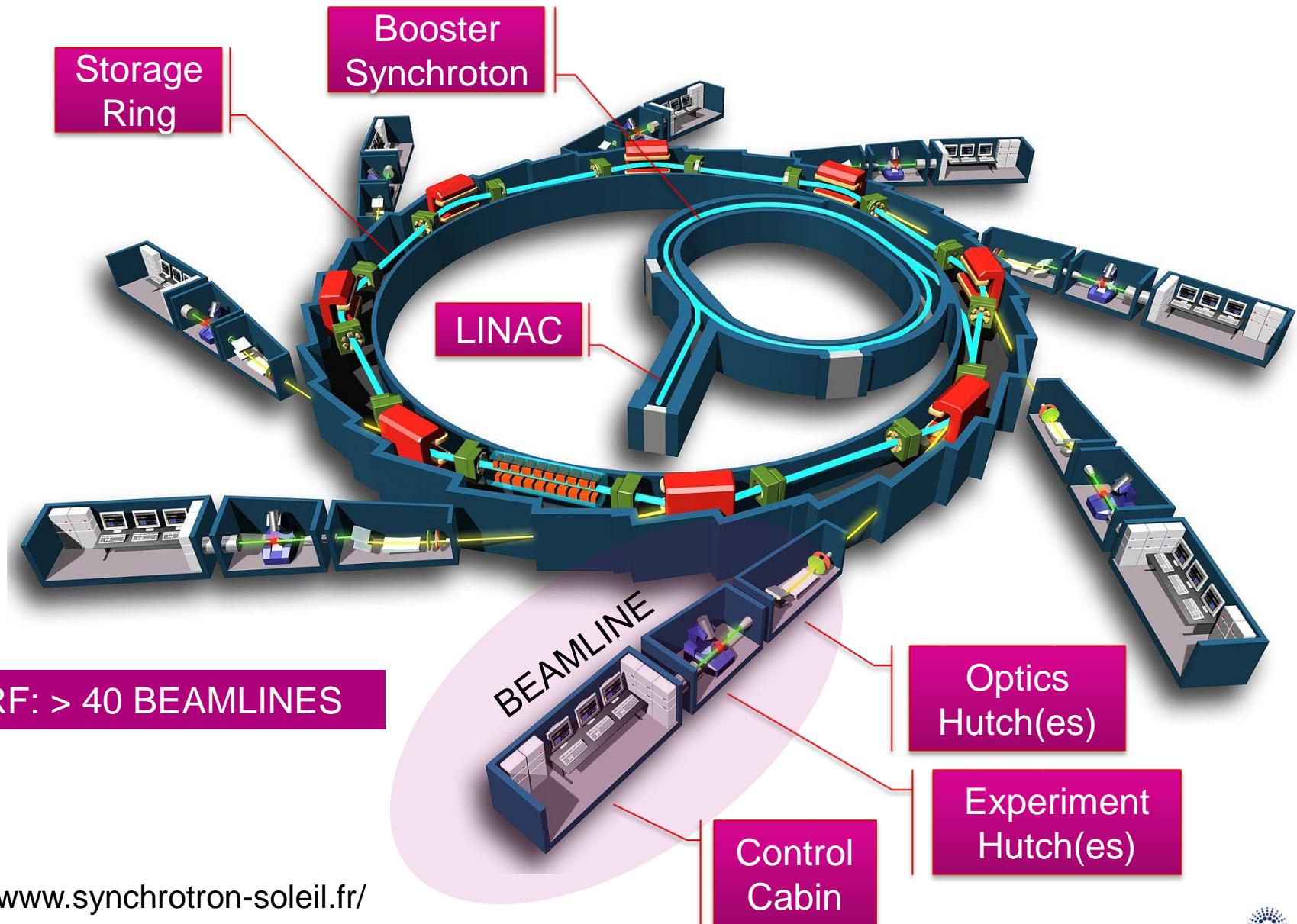
Ray Barrett  
*X-ray Optics Group Leader*  
*European Synchrotron Radiation Facility*  
*Grenoble, France*

[barrett@esrf.fr](mailto:barrett@esrf.fr)

# A STORAGE RING BASED SYNCHROTRON SOURCE

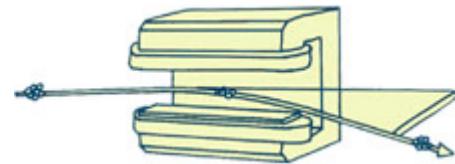
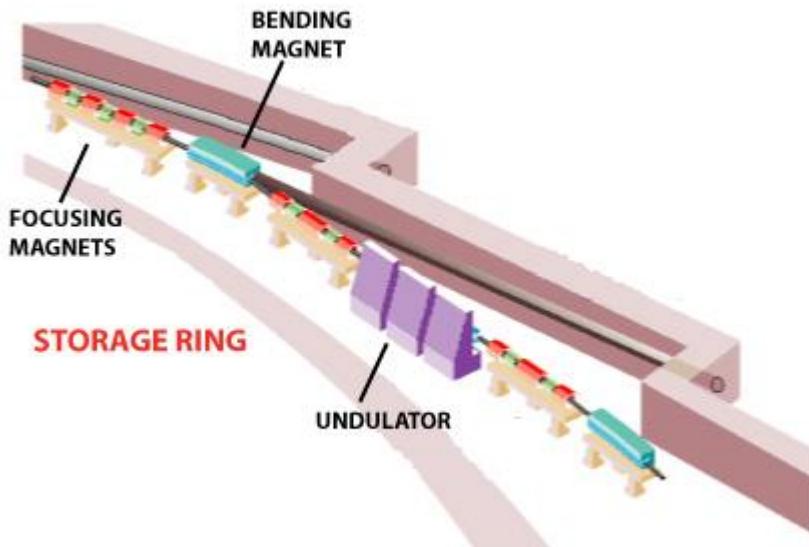


# SCHEMATIC OF A SYNCHROTRON RADIATION (SR) LIGHT SOURCE

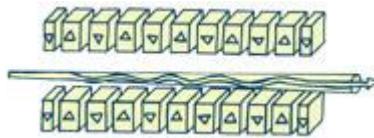


<http://www.synchrotron-soleil.fr/>

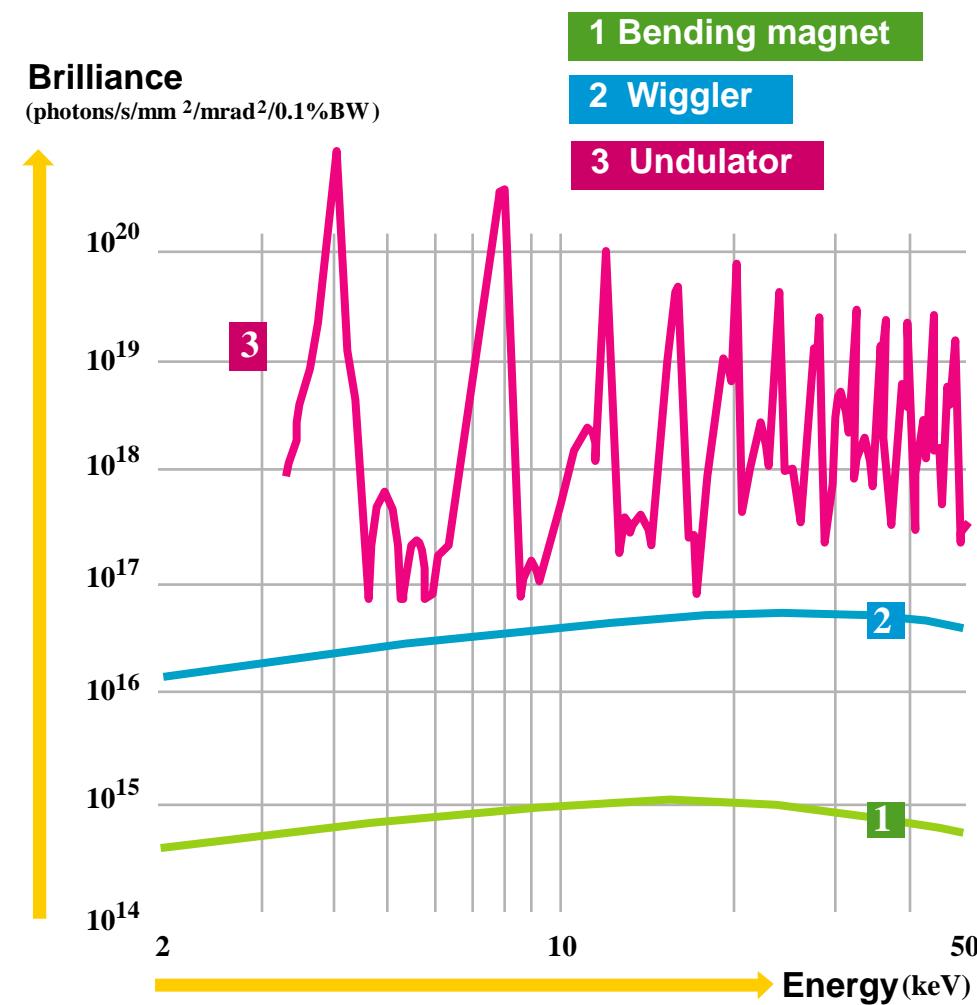
# THE X-RAY SOURCES OF A SYNCHROTRON LIGHT FACILITY



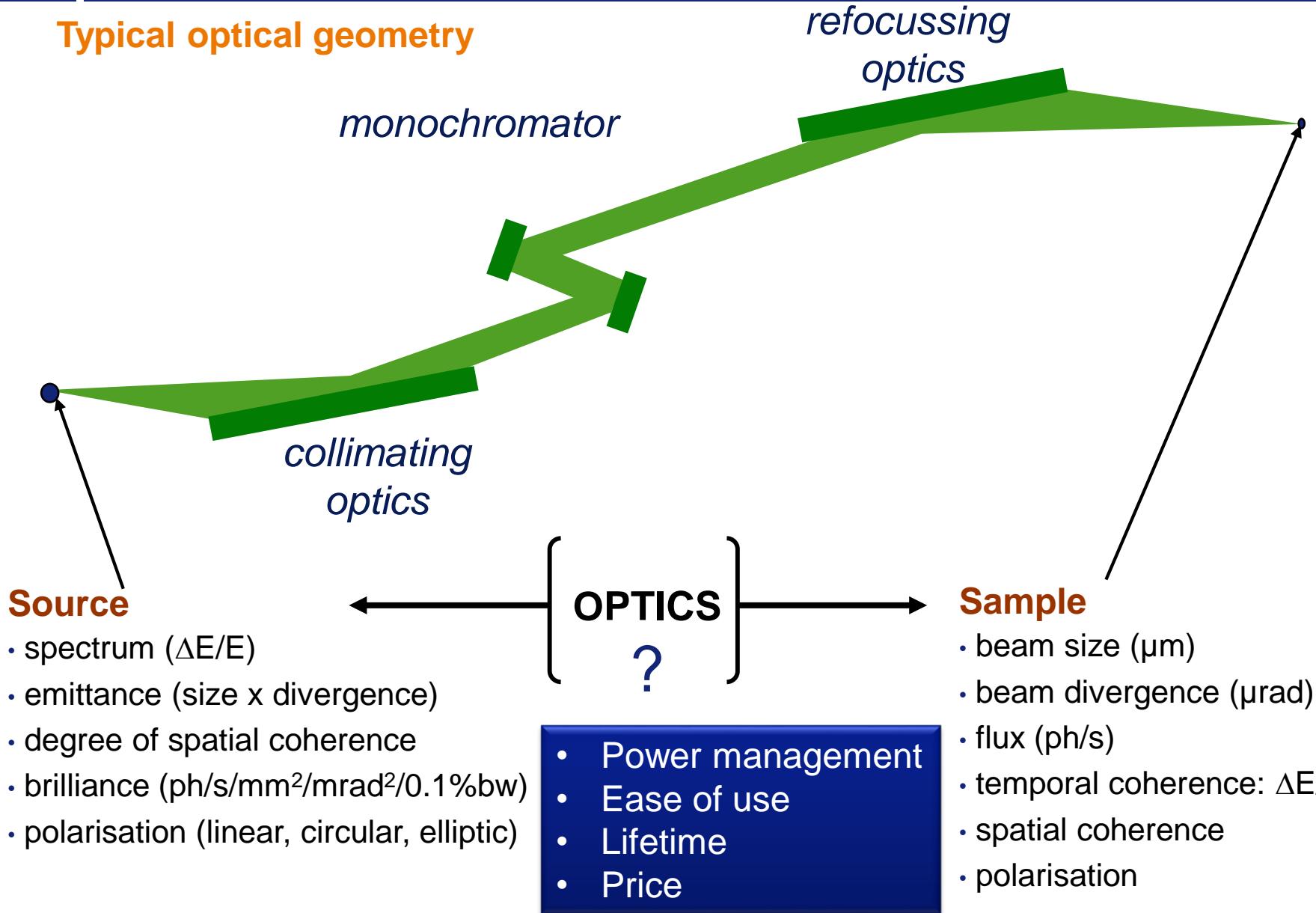
Bending magnet



Undulator/wiggler



- Beam size
  - Unfocused: few mm to few cm (source is weakly divergent)
  - Focused beam: < 100 nm to ~10's  $\mu\text{m}$
- Energy range/tunability
  - $0.1\text{ eV} < E < 0.5 \text{ MeV}$  but mostly 2-100 keV
- Energy bandwidth ( $\Delta E/E$ ):
  - $10^{-2}$  to  $10^{-8}$  at sample, typically  $\Delta E \sim \text{few eV} @ 20\text{keV}$
- Polarized radiation
  - 100% linear or circular or elliptical
- Pulsed radiation
  - 50 ps pulses every ns
- Power
  - several kW total power, several  $100 \text{ W/mm}^2$  power density (white beam)
- High degree of coherence
- Photon Flux
  - Brilliance:  $10^{22} \text{ ph/sec/mrad}^2/\text{mm}^2/0.1\%\text{bw}$  ( $10^{11}$  higher than conventional sources)  $\Rightarrow$  photon flux (@  $\Delta E/E = 10^{-4}$ ):  $10^9\text{-}10^{14} \text{ ph/s}$
  - Extremely variable photon rates on detectors (< 1 ph/s to full beam flux)





- ***Synchrotron radiation***
- ***Principles of X-ray optics***
- ***Mirrors***
- ***Diffractive optics***
- ***X-ray micro-/nano-focusing***
- ***Summary***

# VISIBLE LIGHT OPTICS

## Refractive lenses



## Polarising Optics



## Fresnel lenses



## Fibre optics/ waveguides

## Diffractive optics



## Mirrors

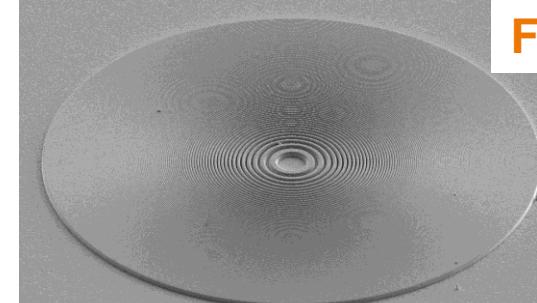
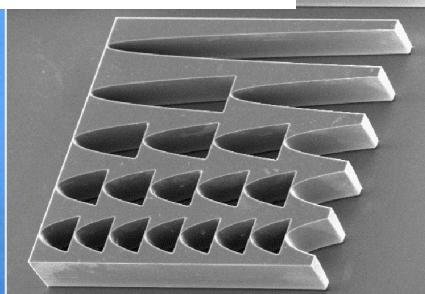


## Filters

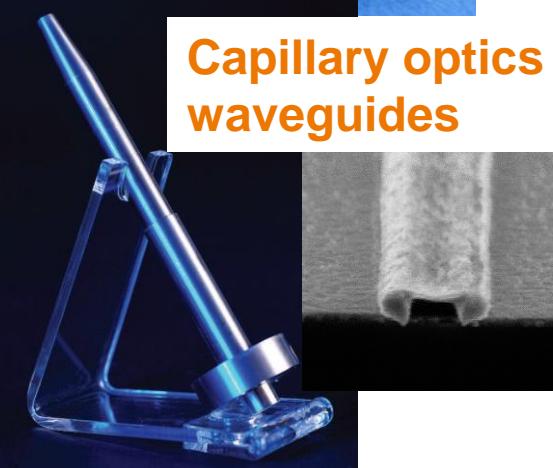
+ interferometers, ...



Refractive lenses



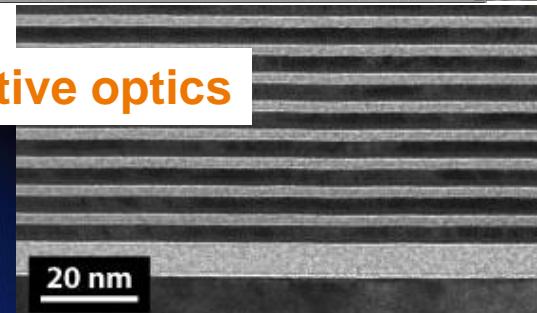
Fresnel lenses



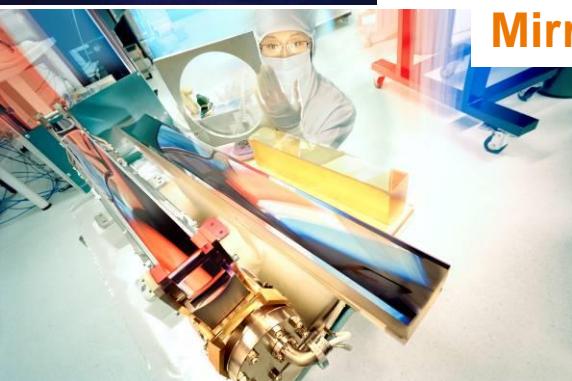
Capillary optics  
waveguides



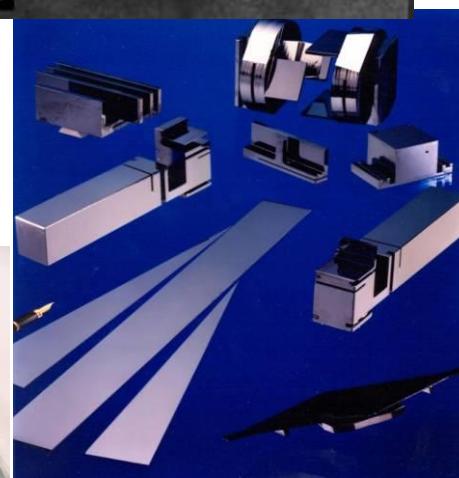
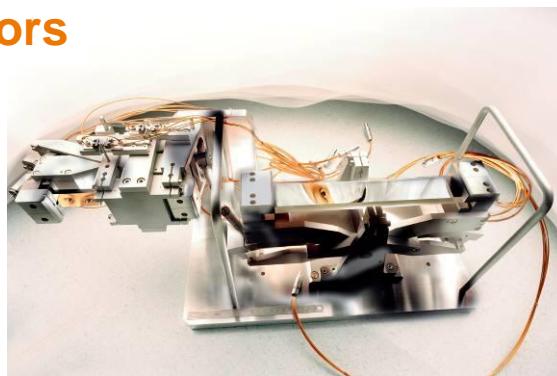
Diffractive optics



Filters



Mirrors



+ polarising optics,  
interferometers, ...

## plane wave in vacuum:

$$\Psi(z) = \Psi_0 \exp(-ik_0 z) \text{ where } k_0 = 2\pi/\lambda$$

## wave in medium ( $n=1-\delta-i\beta$ ):

$$\Psi(z) = \Psi_0 \exp(-ink_0 z)$$

$$= \Psi_0 \exp(-ik_0 z) \exp(i\delta k_0 z) \exp(-\beta k_0 z)$$

$\delta$ : phase change

$\beta$ : attenuation

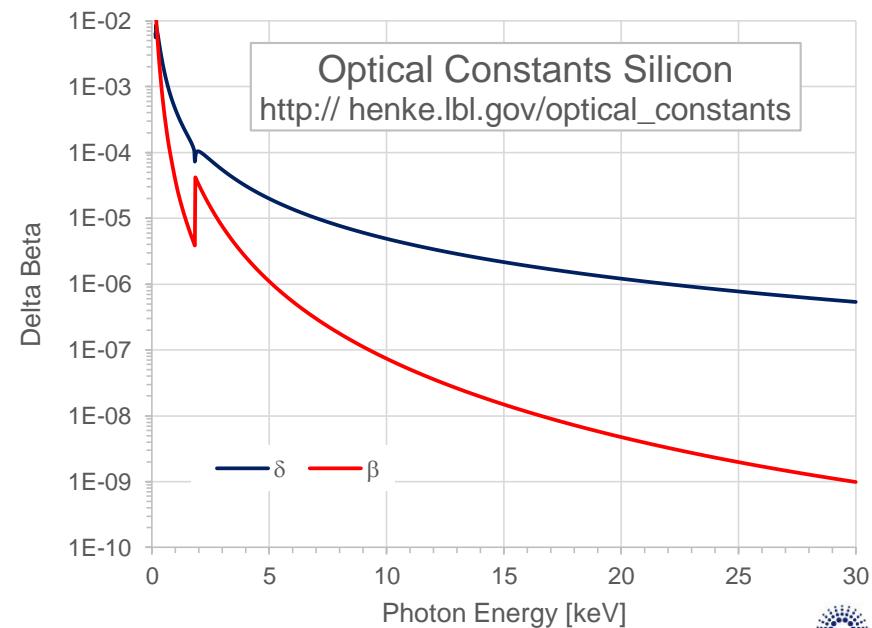
## intensity: $|\Psi(z)|^2$

$$I/I_0 = \exp(-2\beta k_0 z) = \exp(-\mu z)$$

## phase change in distance $z$ :

$$\varphi(z) = 2\pi\delta z/\lambda$$

e.g. Kirz et al., *Quart. Rev. Biophys* 28, [1] (1995): 33–130.  
doi:10.1017/S0033583500003139.



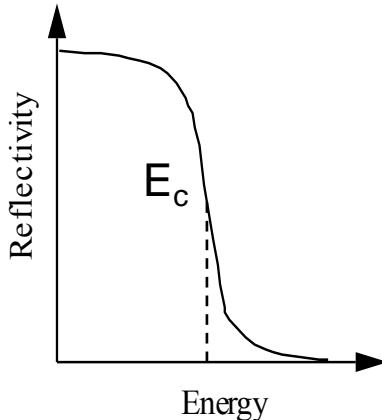
# X-RAY OPTICS: MANY APPROACHES

“... The refractive index.... cannot be more than 1.05 at most....  
....X-rays cannot be concentrated by lenses...”

W.C. Röntgen  
Über eine neue art von Strahlen.  
Phys.-Med. Ges., Würzburg, 137, p. 41,  
(1895)  
English translation in Nature 53, p. 274

$$n=1-\delta-i\beta \text{ with } \delta, \beta \ll 1$$

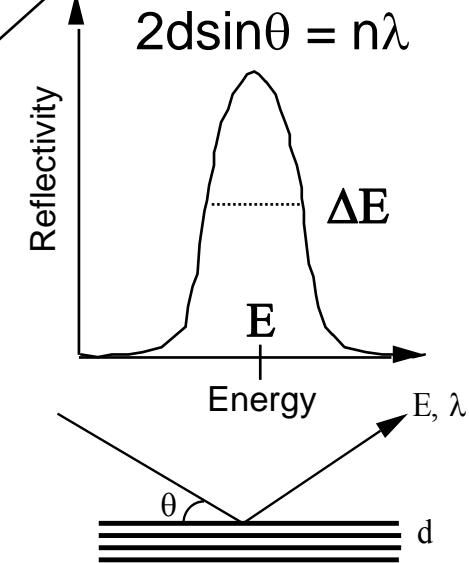
## REFLECTION



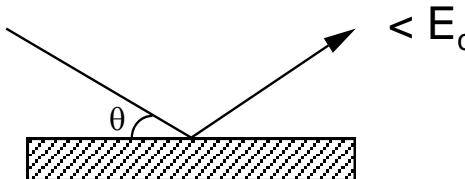
$\delta$  (phase-shift),  $\beta$  (absorption), materials  
(and energy) dependent optical constants

- Very weak refraction
- Quite high absorption

## DIFFRACTION



## REFRACTION



- X-ray mirrors
- Capillaries
- Waveguides

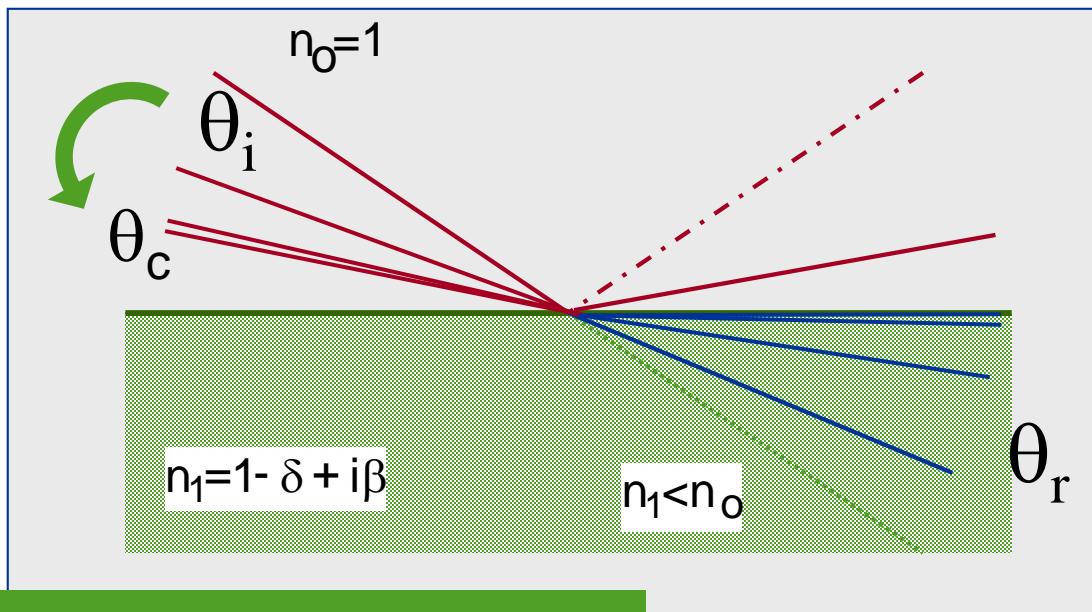
- Refractive lenses

- Crystals & multilayers
- X-ray gratings
- Fresnel zone plates
- Bragg-Fresnel lens

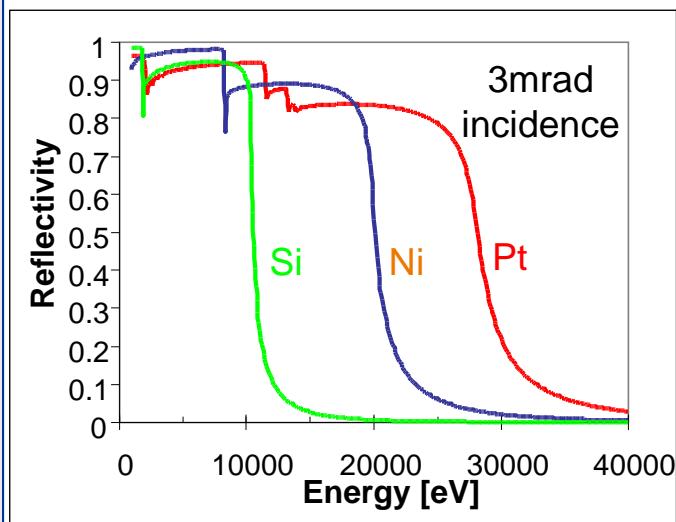


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# TOTAL EXTERNAL REFLECTION: X-RAY MIRRORS



'real' materials



Snell's Law (Descartes' law) :

$$n_o \cos \theta_i = n_1 \cos \theta_r$$

for  $\delta \ll 1$  and  $\beta \ll \delta$

$$\theta_{c[mrad]} E_{c[keV]} = 19.83 \sqrt{\rho_{[g/cm^3]}}$$

$$\theta_c \approx \sqrt{2\delta} \propto \lambda \sqrt{Z}$$

The critical angle for total external reflection.

E=10keV

- Gold 9 mrad
- Nickel 6 mrad
- Silicon 3 mrad

## • Deflection

beam steering (different experiments, Bremsstrahlung)

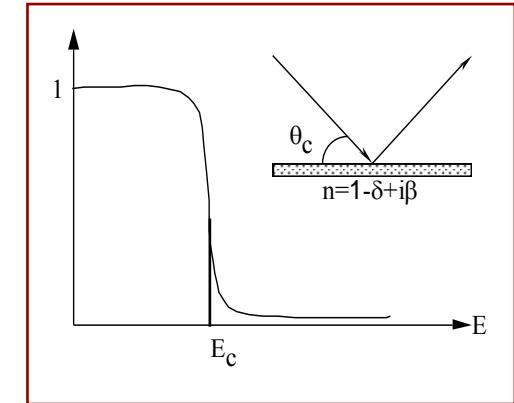
## • Power filter

lower incident power on sensitive optical components

## • Spectral shaper

energy low-pass filter (harmonic rejection)

mirror+filter = spectral window



## • Focusing

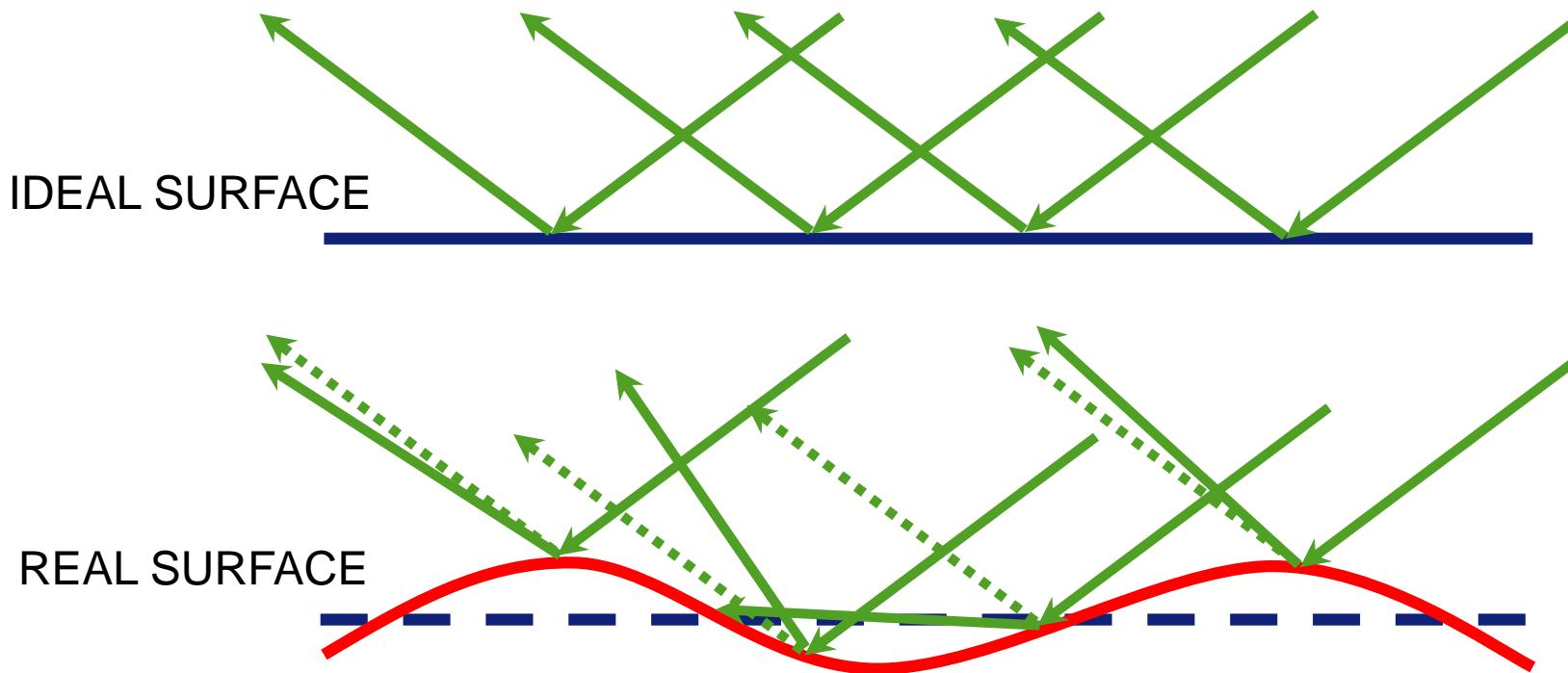
wiggler & bending magnet : spherical, cylindrical, and toroidal mirrors

microscopy & microprobe : source demagnification (ellipsoidal mirror, KB .....

## • Collimation

parabolic mirror : matching the monochromator angular acceptance with the beam divergence

J. Susini, Optical Engineering, 34(2), (1995)



Topography of surface typically described by:

- 1) Slope error (orientation of local surface compared with ideal surface). Distinguish between meridional/tangential (along mirror) and sagittal slope error. **Usual units for X-ray mirrors:  $\mu$ radian or arcsecs ( $1'' \approx 5 \mu\text{rad}$ )**
- 2) Figure error (height of local surface compared with ideal surface). **Usual units for X-ray mirrors: nm.**

## • Typical Requirements

*micro-roughness < 3Å rms and slope error < 1 µrad rms for blur 10% source size*

Ultra-precise shaping, figuring and super-polishing

Very accurate and stable mechanical mounting, bending mechanisms, UHV environment

Efficient cooling scheme

## ■ Technically limiting parameters

- gravity sag

$$\Delta_g \propto \frac{5g}{32} \frac{L^3}{t^2} \frac{\rho}{E}$$



$\frac{\rho}{E}$   $E \frac{\alpha}{\kappa}$   $\frac{\alpha}{\kappa}$

- vibration

$$f_o \propto \sqrt{\frac{E}{\rho}}$$

- thermal deformation

$$\Delta_t \propto \frac{\alpha}{\kappa} P_s$$

- thermal bending

$$F_b \propto E \frac{\alpha}{\kappa} P_t w t^3$$

+

“Polishability”

Most SR Mirrors are  
manufactured from  
Si

Grazing incidence => rectangular optical aperture

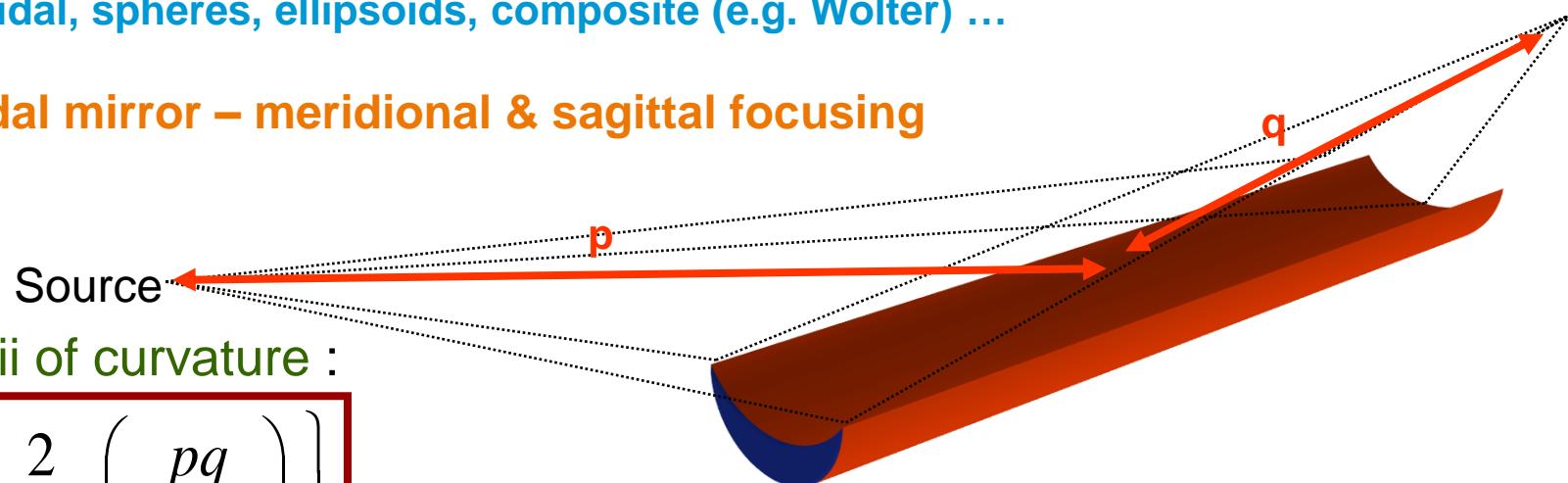
Long mirrors (up to 1.5m): gravity sag

Typically Si with surface coatings (Rh, Pt, ...) to tailor X-ray reflectivity,  $E_c$

Intense X-ray beams: thermal deformation, cooling

Use of curved surfaces: focusing, collimation: flat, sagittal/meridional cylinders, Focus toroïdal, spheres, ellipsoids, composite (e.g. Wolter) ...

e.g. toroïdal mirror – meridional & sagittal focusing



Radii of curvature :

$$R_m = \frac{2}{\sin \theta_i} \left( \frac{pq}{p+q} \right)$$

$$R_s = 2 \sin \theta_i \left( \frac{pq}{p+q} \right)$$

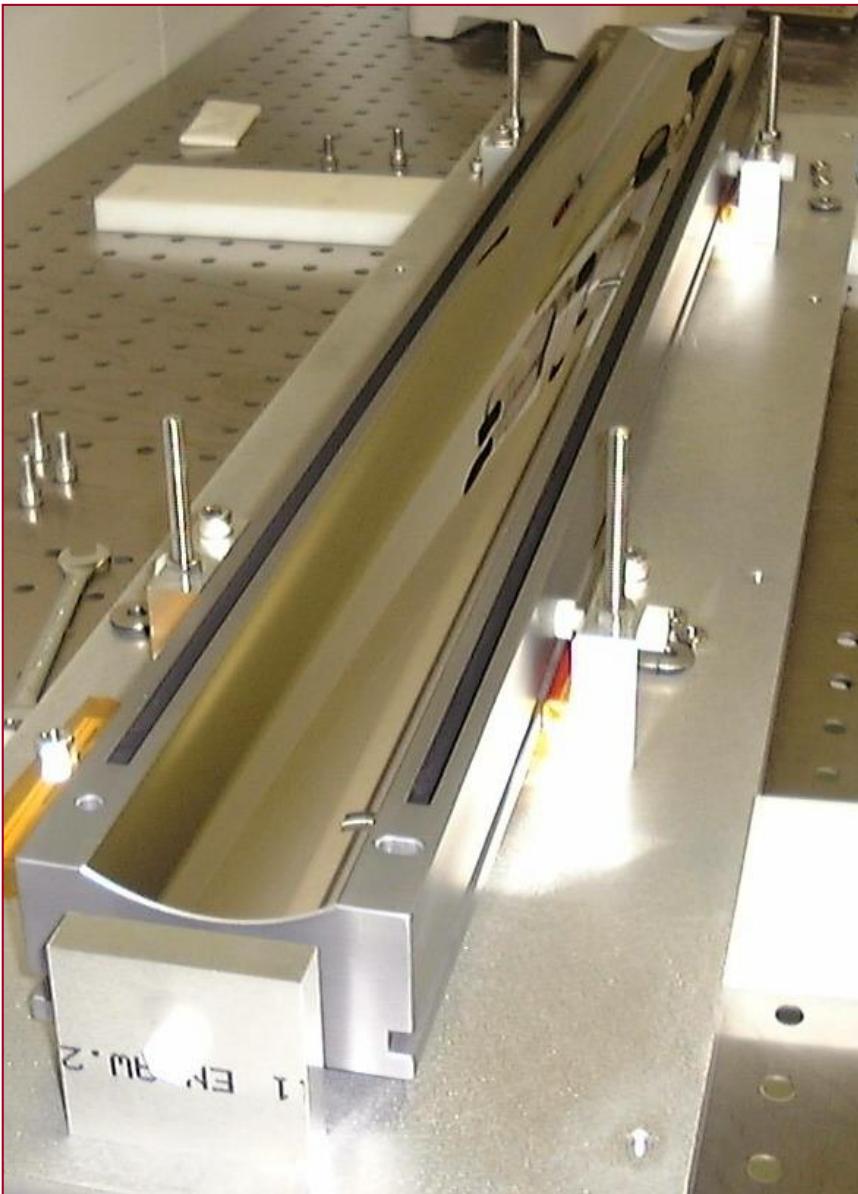
$$R_s \approx R_m \theta^2$$

$$\theta = 10 \text{ mrad}$$

$$R_s \sim \text{mm}$$

$$R_m \sim \text{km}$$

May be obtained by bending



Material-coating: Silicon-Pt

Supplier: SESO (France)

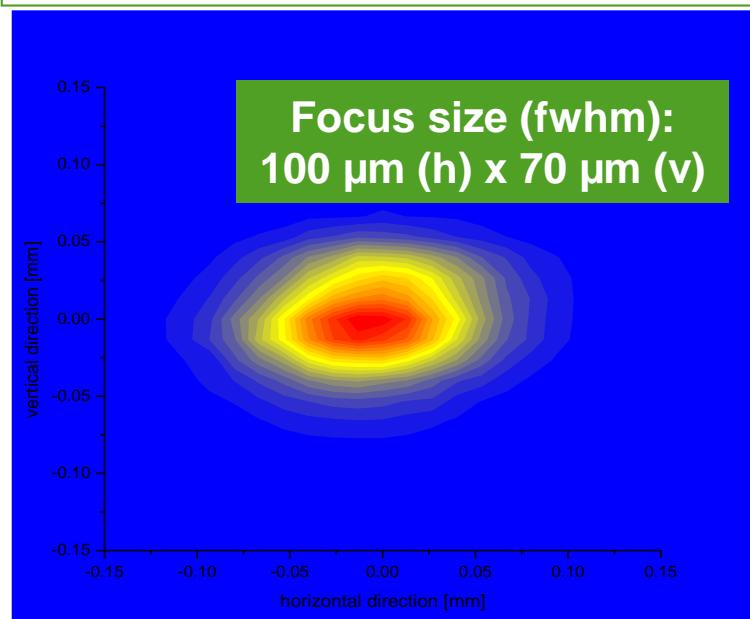
Roughness  $\leq 2\text{\AA}$  rms

Radii of curvature:

- Sagittal: 71.60 mm
- Meridional: 25 km

Slope error (RMS)

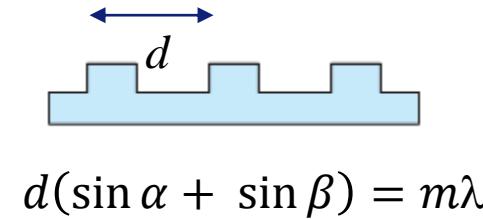
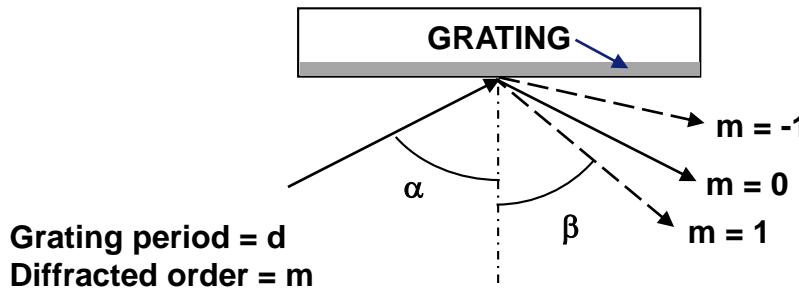
- 0.7  $\mu\text{rad}$  over 450 mm
- 1.0  $\mu\text{rad}$  over 900 mm



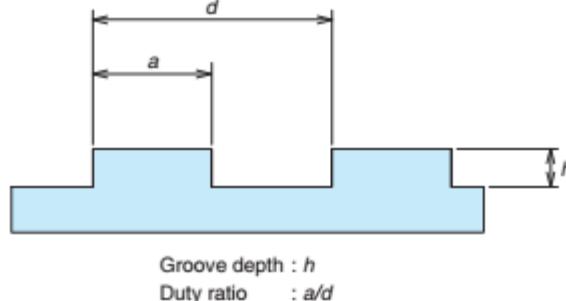


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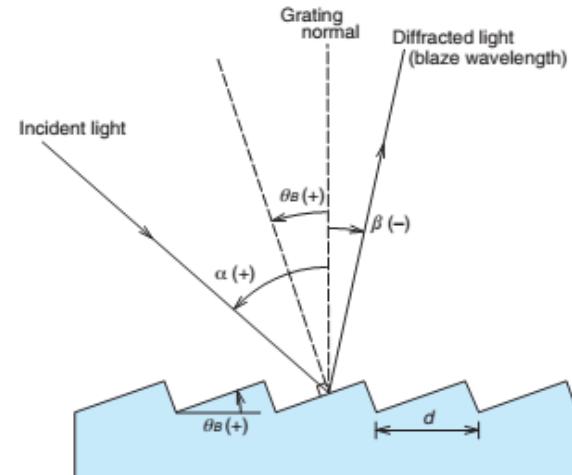
surface reflection and diffraction to disperse X-rays according to energy:



- surface grating structures - mechanical ruling or masked etching
- monochromators or energy analysers
- Grating line densities (lines/mm) either constant or variable (VLS – variable line spacing) - latter have a focusing effect
- Substrates flat, spherical, (toroidal)
- Groove profile important for efficiency

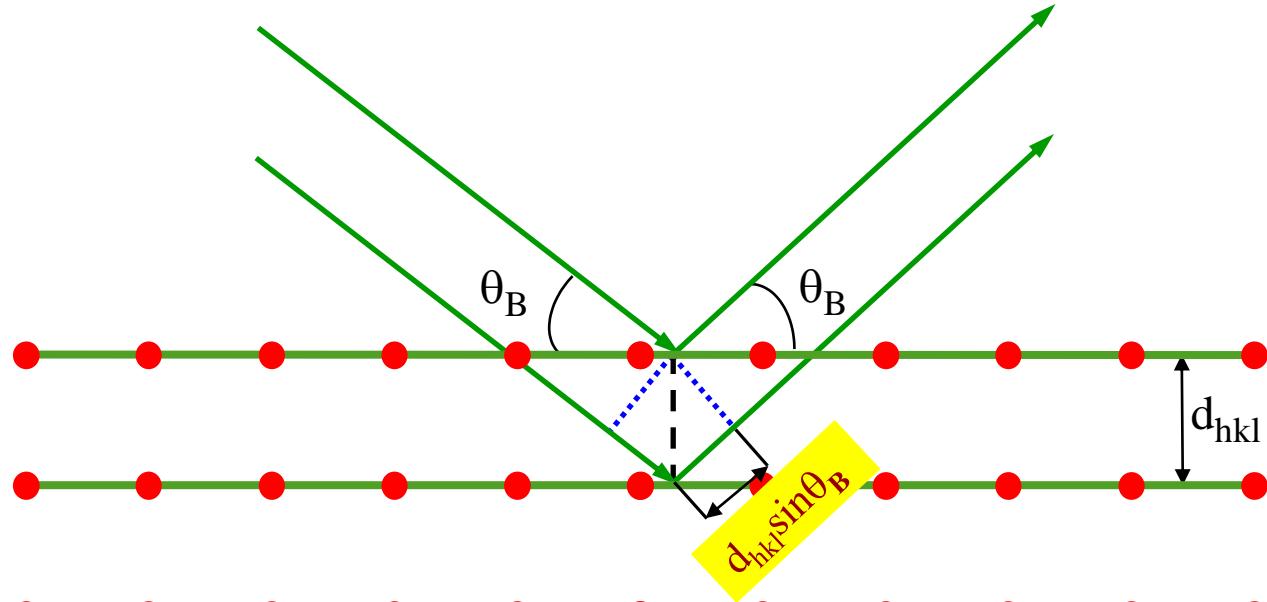


Laminar: rectangular grooves



Blazed: saw-tooth grooves

X-ray diffraction results from elastic scattering of X-rays from structures with long-range order. For X-ray optics generally concerned with **highly perfect single crystals** (typically Silicon) *cf* neutron mosaic crystals



$$\text{Bragg equation: } 2d_{hkl} \sin\theta_B = n\lambda$$

- Incident X-rays are “reflected” at atomic planes in the crystal lattice (bulk effect)
- Path difference** of the rays  $2d_{hkl} \sin\theta_B$
- Constructive interference if the path difference amounts to  $\lambda$  ( $n \lambda$ ?)
- Use of curved, elastically deformed crystals allows focusing

## CRYSTAL MONOCHROMATORS

Energy, E, determined by incidence angle,  $\theta_B$ , of X-ray beam onto crystal planes according to Bragg equation:

$$E = \frac{hc}{\lambda} = \frac{hc}{2d_{hkl} \sin \theta_B}$$

c = light velocity  
h = Plancks constant

Energy resolution depends upon type of crystal and reflecting planes used (described by angular Darwin width  $\omega_s$ ) & divergence of incident beam,

$$\frac{\Delta E}{E} = \frac{\Delta \lambda}{\lambda} = \sqrt{\omega_s^2 + \psi_0^2} \cot \theta_B$$

e.g. **Si 111 reflexion**,

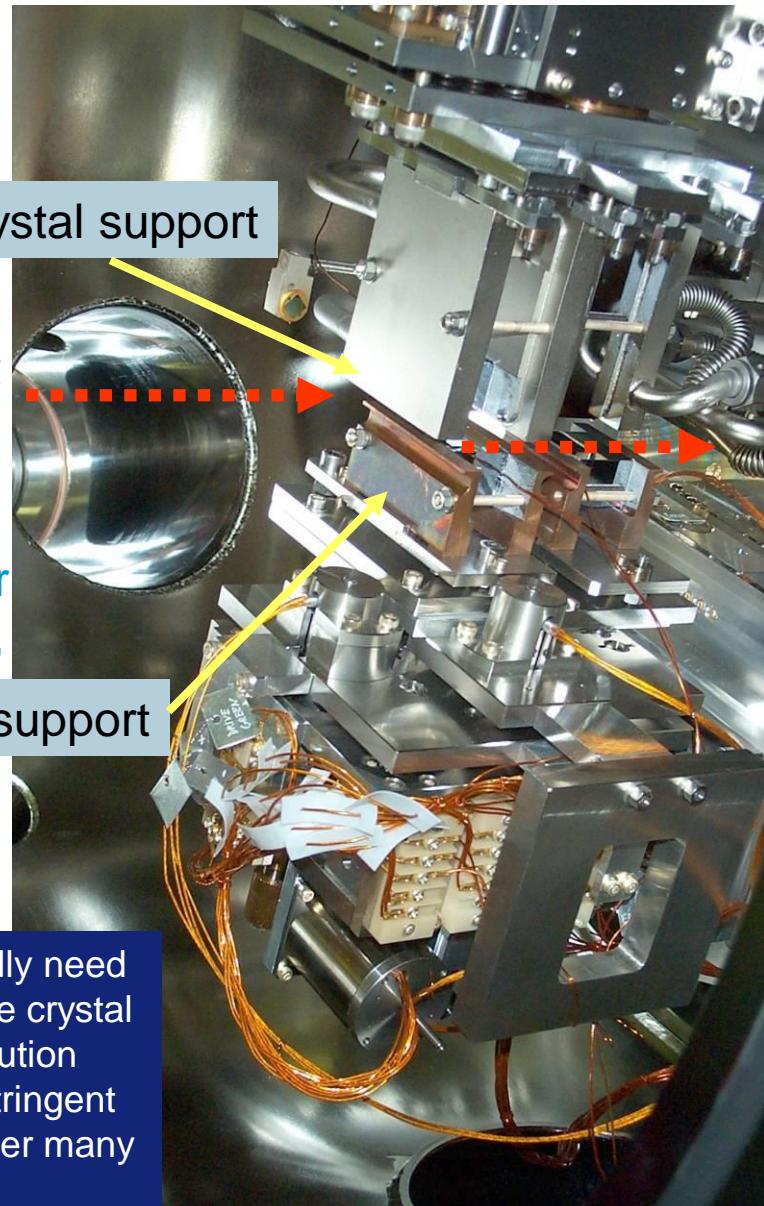
$d_{hkl} = 3.1355 \text{ \AA}$

$\omega_s = 10.7 \mu\text{rad}$  (@ 8keV):

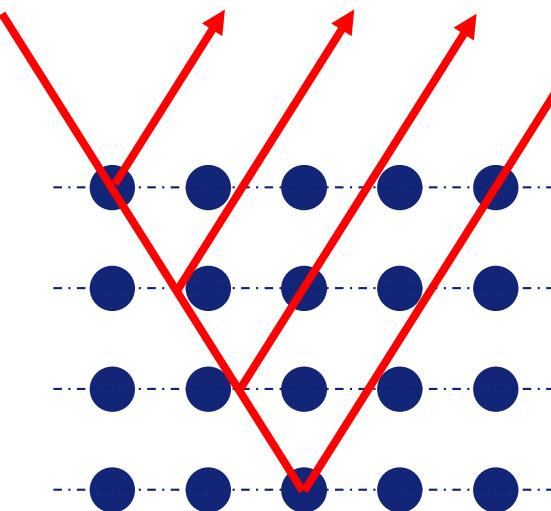
$\theta_B = 14^\circ$

with a parallel incident beam:

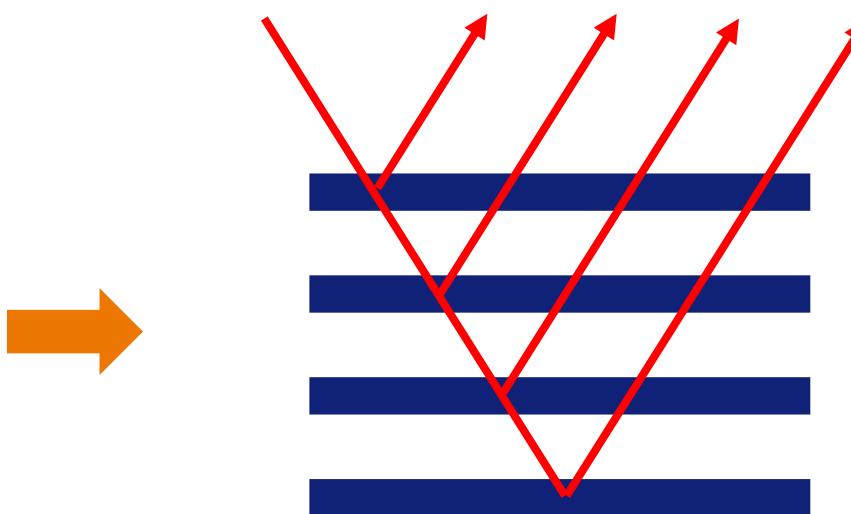
$\Delta E/E = 1.4 \cdot 10^{-4}, \Delta E = 1.1 \text{ eV}$



## X-RAY MULTILAYERS

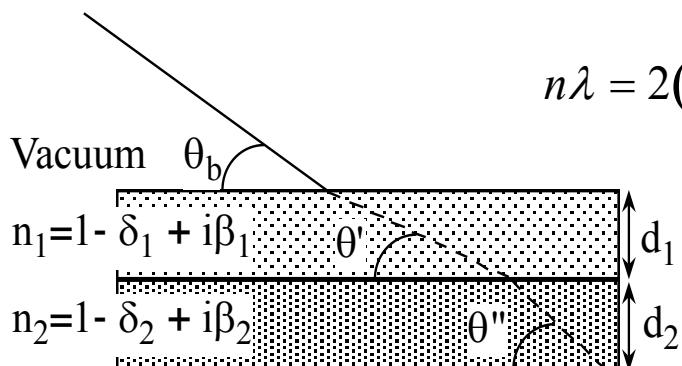


Crystal  
(3-dimensional)



Multilayer (Synthetic crystal)  
(1-dimensional)

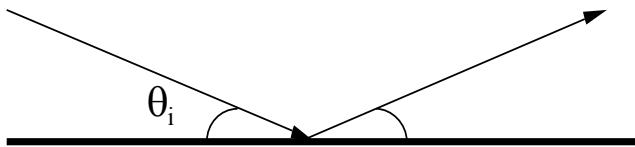
X-region : *inside the multilayer, as a result of refraction, modified Bragg's law needed*



$$n\lambda = 2(d_1 + d_2) \sqrt{1 - \frac{\bar{\delta}}{\sin^2 \theta_b}} \sin \theta_b$$

$$\left\{ \begin{array}{l} \gamma = d_1 / (d_1 + d_2) \\ \bar{\delta} = \gamma \delta_1 + (1 - \gamma) \delta_2 \\ \bar{\beta} = \gamma \beta_1 + (1 - \gamma) \beta_2 \\ P(\theta_b) = 1(s) \text{ or } \cos(2\theta_b)(p) \end{array} \right.$$

high reflectivity x-ray mirrors...  
or 'synthetic crystals'



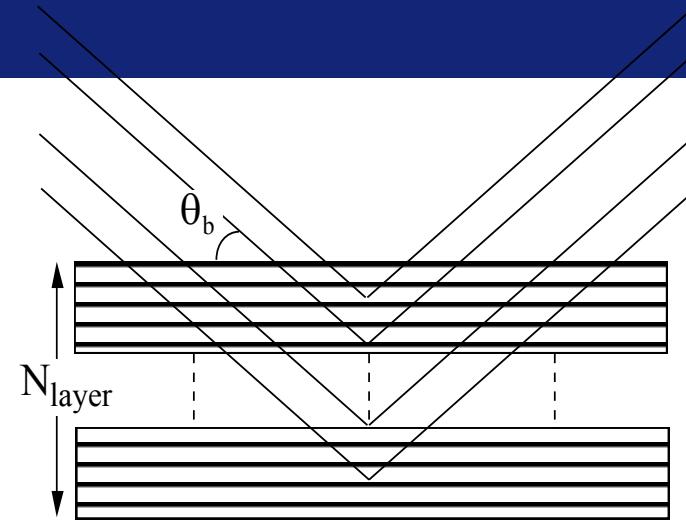
### single boundary

For  $\theta_i > \theta_c$

$E_r = rE_0$  where  $E_r, E_0$  are reflected and incident wave amplitudes,  $r$  is the amplitude reflectivity

$r < 10^{-2}$  and  $R = |r|^2 < 10^{-4}$

$$R \propto \frac{1}{\sin^4 \theta_i}$$



### multiple boundaries

ideally  $|r| \times N_{layer} \Rightarrow R \rightarrow 1$

$n_1 = 1 - \delta_1 + i\beta_1$  and  $n_2 = 1 - \delta_2 + i\beta_2$

$$R \propto \frac{\Delta\delta^2 + \Delta\beta^2}{4} \frac{N_{layer}^2}{\sin^4 \theta_b}$$

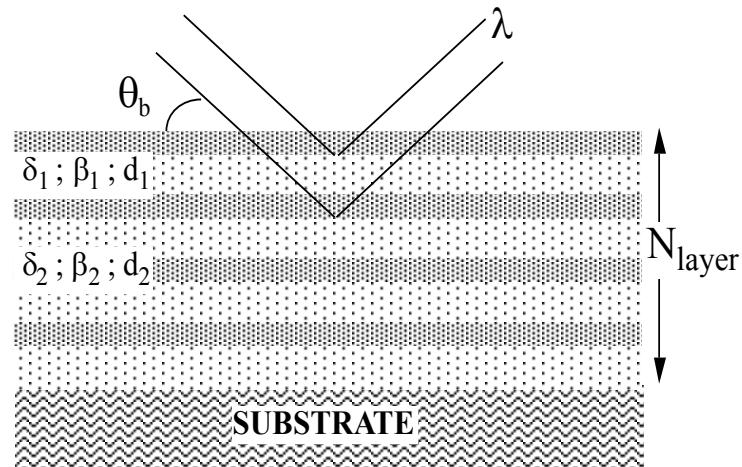
## 1 - Materials : *highest contrast*

$$R \propto \frac{\Delta\delta^2 + \Delta\beta^2}{4} \frac{1}{\sin^4 \theta_b}$$

## 2 - Gamma parameter : *order suppression*

$$\gamma = \frac{d_1}{(d_1 + d_2)}$$

$$\gamma = \frac{1}{n} \quad \Rightarrow \quad \cancel{\text{order } n}$$



## 3 - Number of layers : *energy resolution*

$$FWHM = \frac{0.888 \lambda}{N_{layer} d \cos \theta_b} \quad \Rightarrow \quad \frac{\Delta E}{E} = \frac{1.776}{N_{layer}}$$

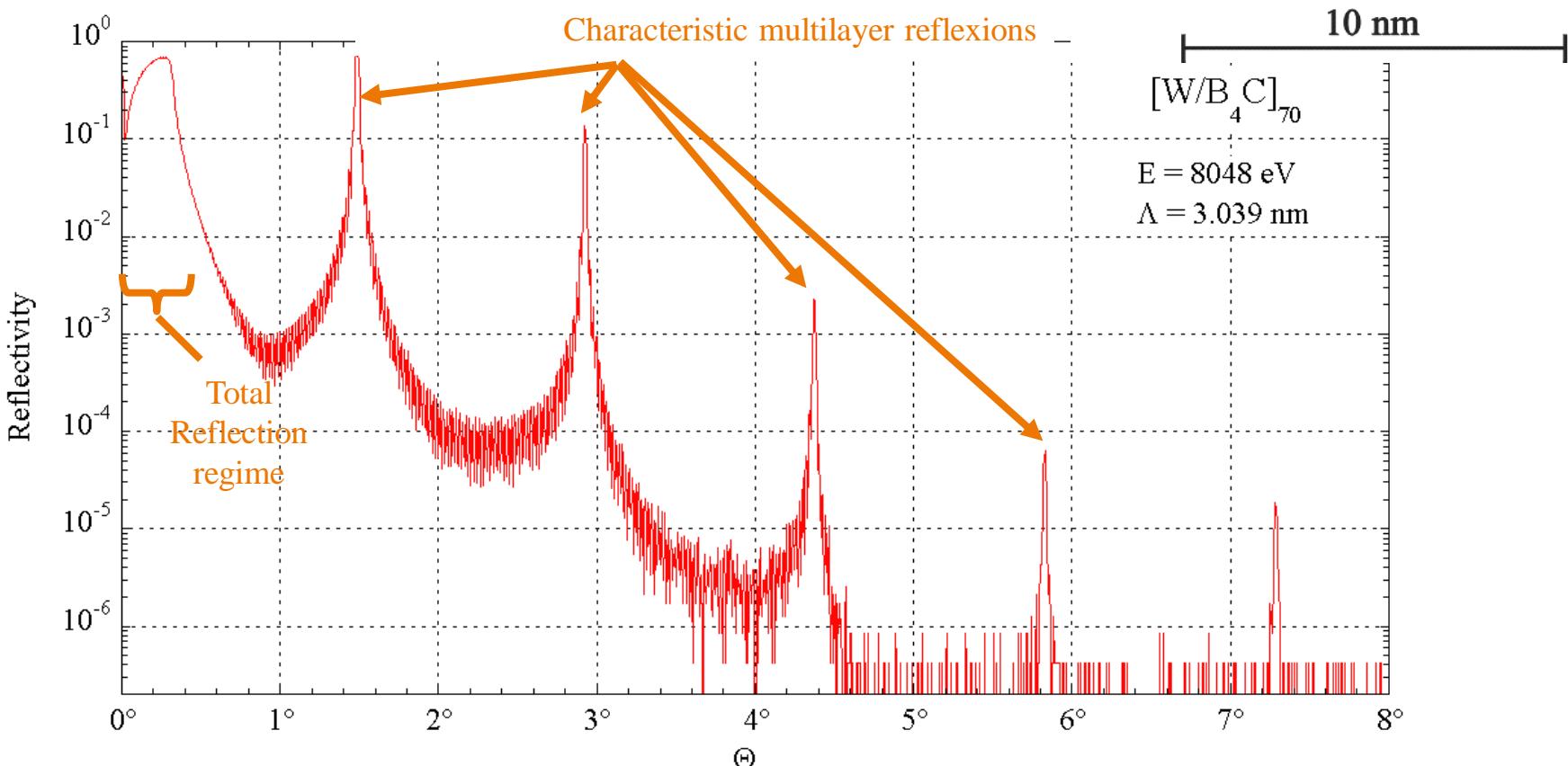
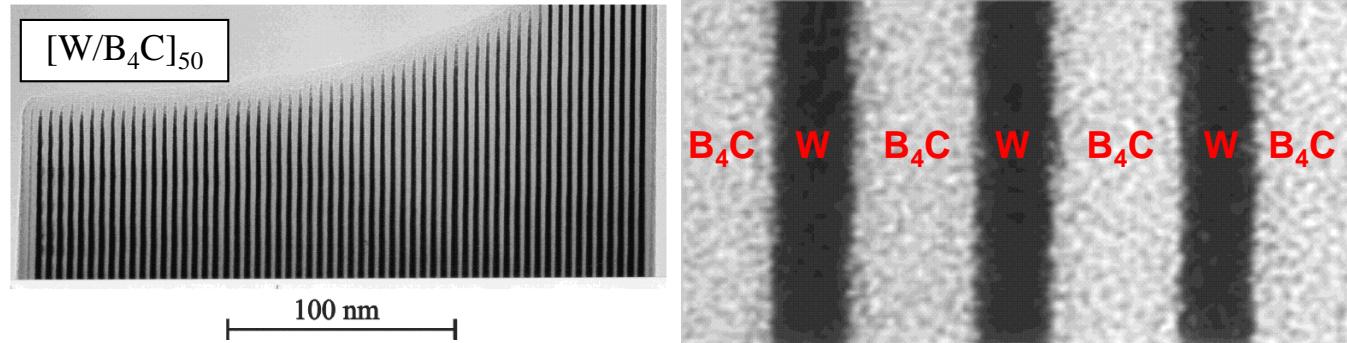
$$N_{layer} \text{ limited by } N_{max} = \frac{\sin^2 \theta_b}{2 \pi \beta} = \frac{2 \sin^2 \theta_b}{\lambda \mu}$$

Typically  $N_{layer/max} \sim 100$

$$\Rightarrow \quad \frac{\Delta E}{E} \sim 10^{-2}$$

# X-RAY MULTILAYER CHARACTERIZATION

Typical X-ray reflectivity scan of a multilayer



### ❖ Power filter

- $\theta_b$  multilayer  $\ll \theta_b$  crystal  $\rightarrow$  crystal length  $\ll$  multilayer length
- lower power density

### ❖ Wide band-pass monochromator - analyser

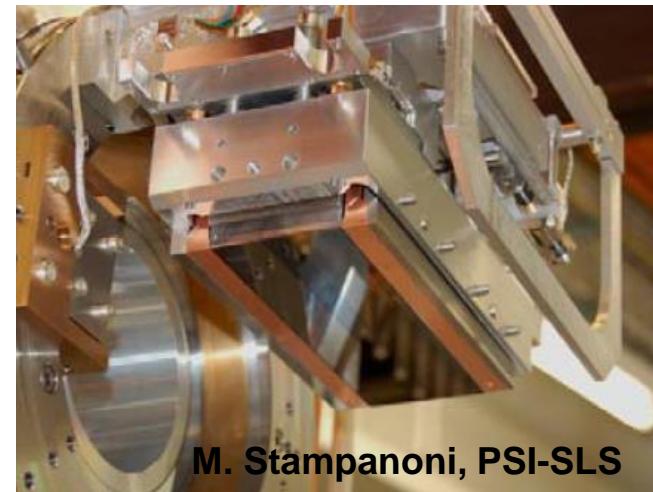
- $5 \cdot 10^{-3} < \Delta E/E < 5 \cdot 10^{-1}$

### ❖ Harmonic rejection

- $\gamma = 1/n$

### ❖ Monochromator for soft(er) X-rays

- d-spacing  $> 2\text{nm}$  cf  $3\text{-}4\text{\AA}$  for radiation hard crystals



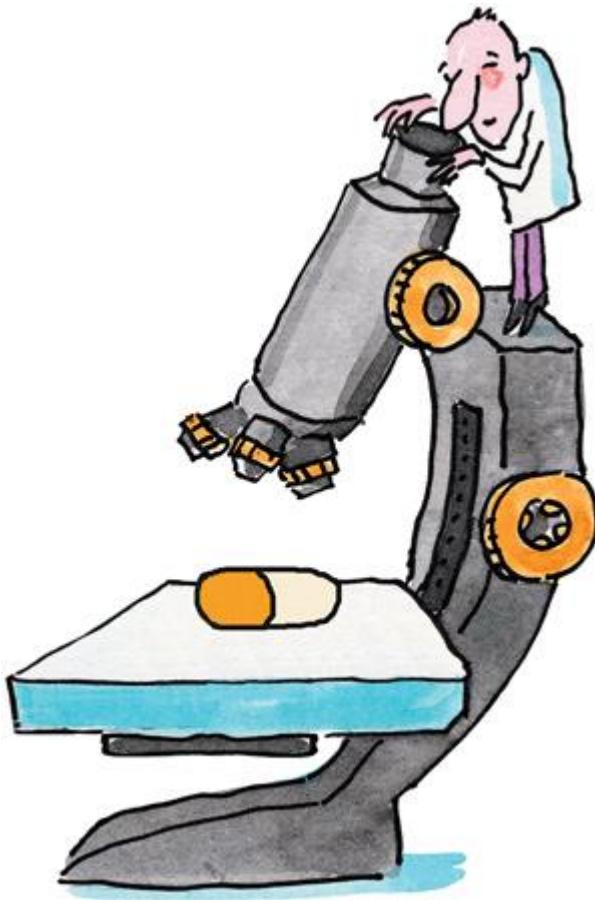
M. Stampanoni, PSI-SLS

### ❖ Focussing

- $\theta_b$  multilayer  $>> \theta_c$  mirror  $\rightarrow$  multilayer length  $\ll$  mirror length
- lower spherical aberrations ( $\sim L^2$ ), increased numerical aperture

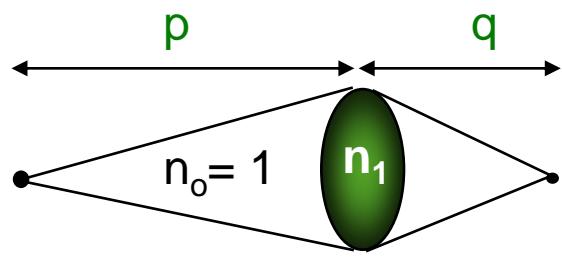
### ❖ Super-mirror (depth graded ML) : extending total reflection

- $R > 40\%$  at  $60\text{keV}$  : not possible with a mirror



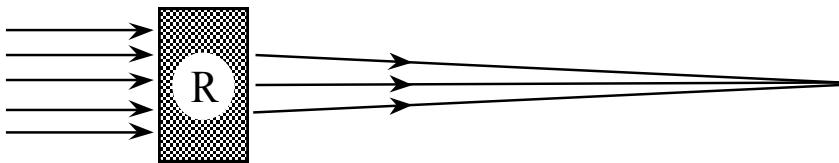
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## COMPOUND REFRACTIVE LENS

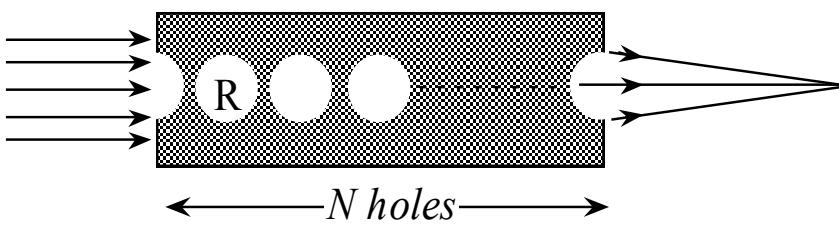


$$\text{Gaussian lens equation: } \frac{1}{f} = \frac{2(n_1 - 1)}{R}$$

$$\text{Thin lens equation : } \frac{1}{f} = \frac{1}{p} + \frac{1}{q}$$



$$\frac{1}{f} = \frac{2\delta}{R}$$



$$\frac{1}{f} = N \frac{2\delta}{R}$$

$$\text{X-rays : } n = 1 - \delta + i\beta$$

$n_1 < 1$  : concave lens

Typically Be or Al lenses –e.g.

Aluminium @ 10keV       $\delta = 5.5 \cdot 10^{-6}$

1 hole 100  $\mu\text{m}$  radius :       $f = 9 \text{ m}$

15 holes 100  $\mu\text{m}$  radius:       $f = 60 \text{ cm}$

A. Snigirev et al. Nature, 384 (1996)

### Advantages

- simplicity and low cost
- low sensitivity to heat load

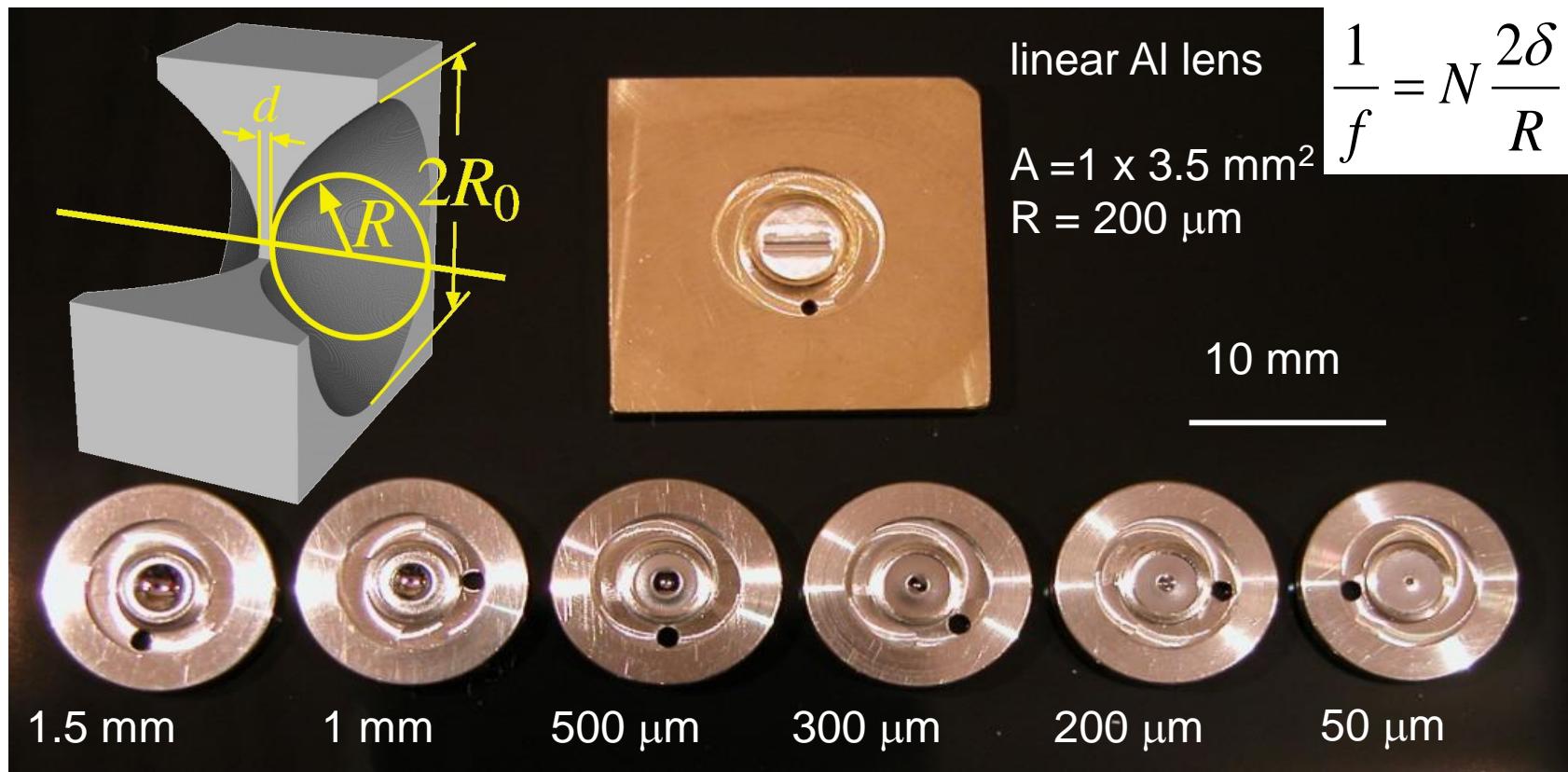
### Disadvantages

- efficiency limited by absorption
- small aperture (limited resolution)
- strong chromatic aberrations

## PARABOLOIDAL & PARABOLIC CYLINDER X-RAY LENSES

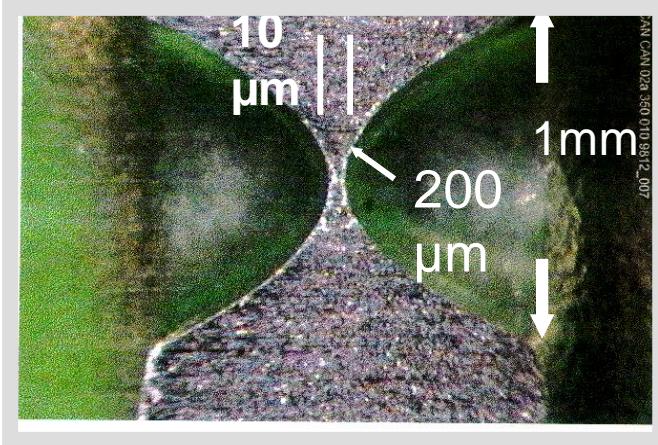
- Parabol-ic/oidal profile  $\Rightarrow$  no spherical aberration
- Be ~2-40 keV  $\Rightarrow$  absorption $\downarrow$
- Al ~40-80 keV
- Ni ~80-150 keV

Typical parameters :  
 $R = 50$  to  $1500 \mu\text{m}$   
 $2R_0 = 0.45$  to  $2.5 \text{ mm}$   
 $d < 30 \mu\text{m}$

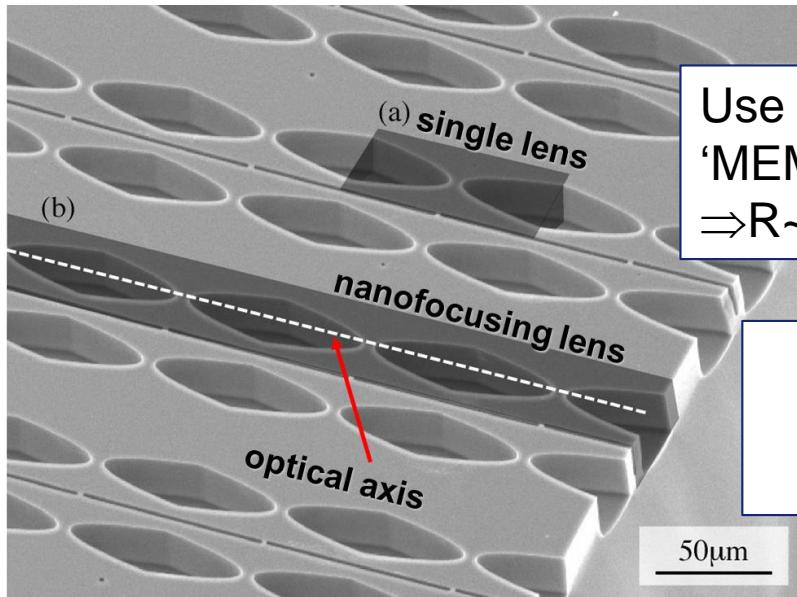
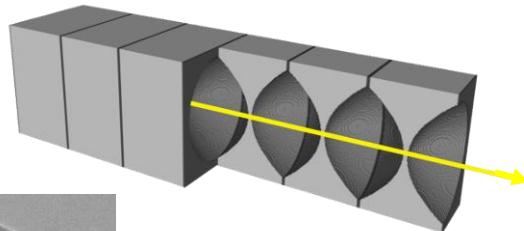


Be / Al parabolic lenses (Aachen) courtesy Prof. B. Lengeler

# PARABOLIC REFRACTIVE LENSES

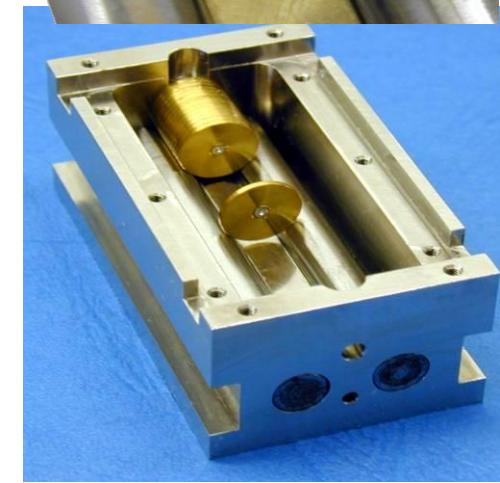
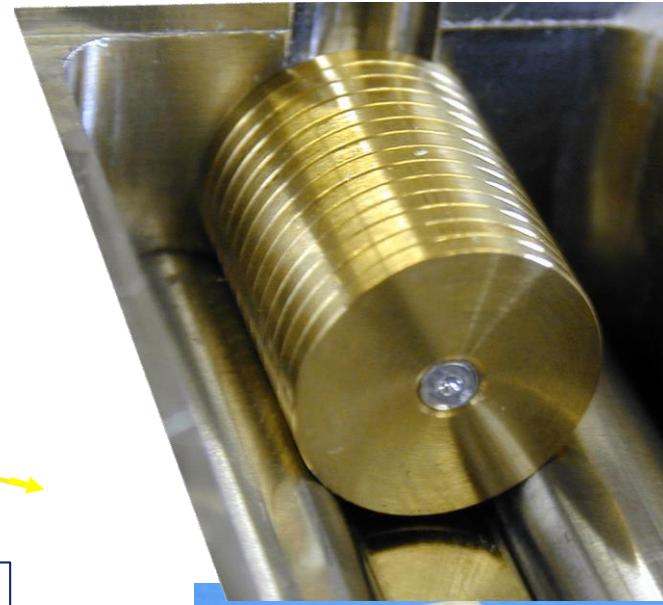


**Materials:**  
low Z, high  
density  
**Al, Be, B, Si, ...**



Use of planar  
'MEMS' technologies  
⇒ R~2μm

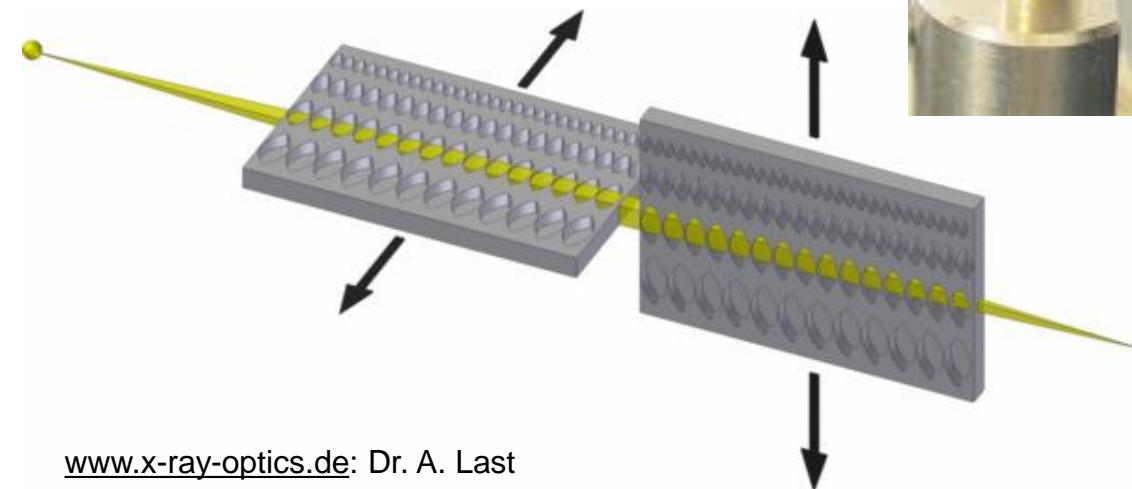
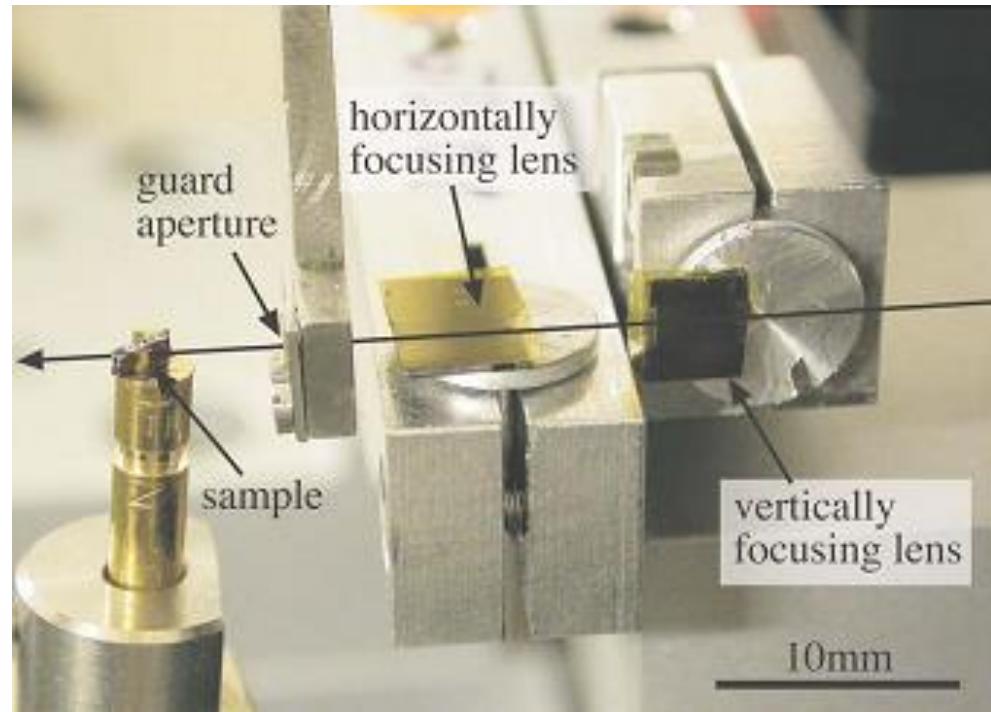
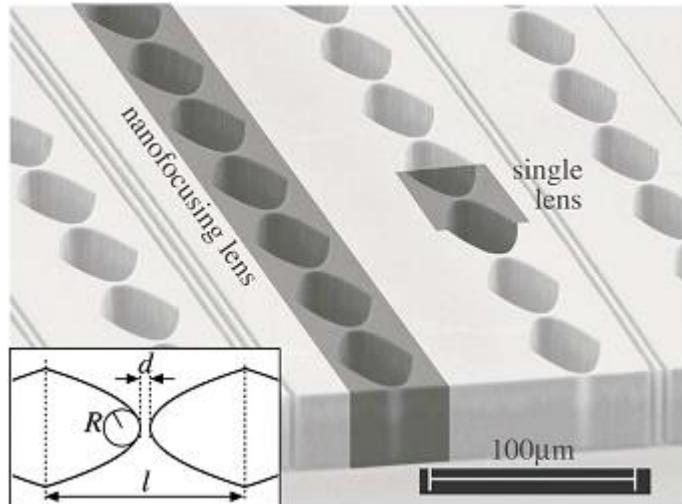
Si lens (e-beam  
lithography &  
deep trench RIE



B. Lengeler, C. Schroer, M. Richwin,  
C. Schroer et al, *Applied Physics Letters*, 82(9), 2003    RWTH, Aachen, Germany



## 2D FOCUSING WITH PLANAR REFRACTIVE LENSES

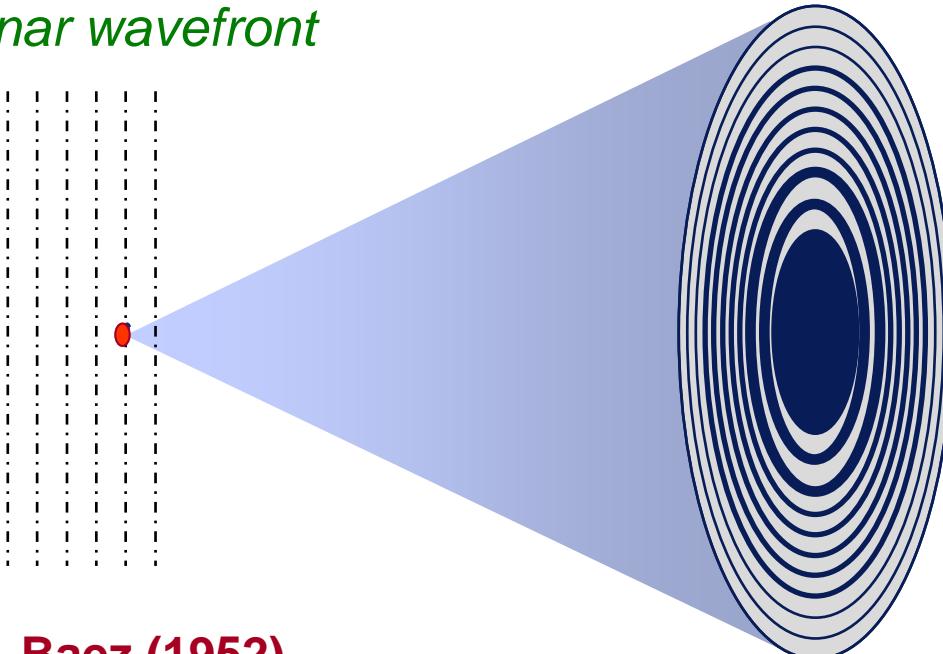


[www.x-ray-optics.de](http://www.x-ray-optics.de): Dr. A. Last

47 x 55 nm<sup>2</sup> beam focus  
@21keV  
Schroer et al., Appl. Phys. Lett.  
87, 124103 (2005)  
Aperture limited by absorption

## Hologram (Fresnel Zones)

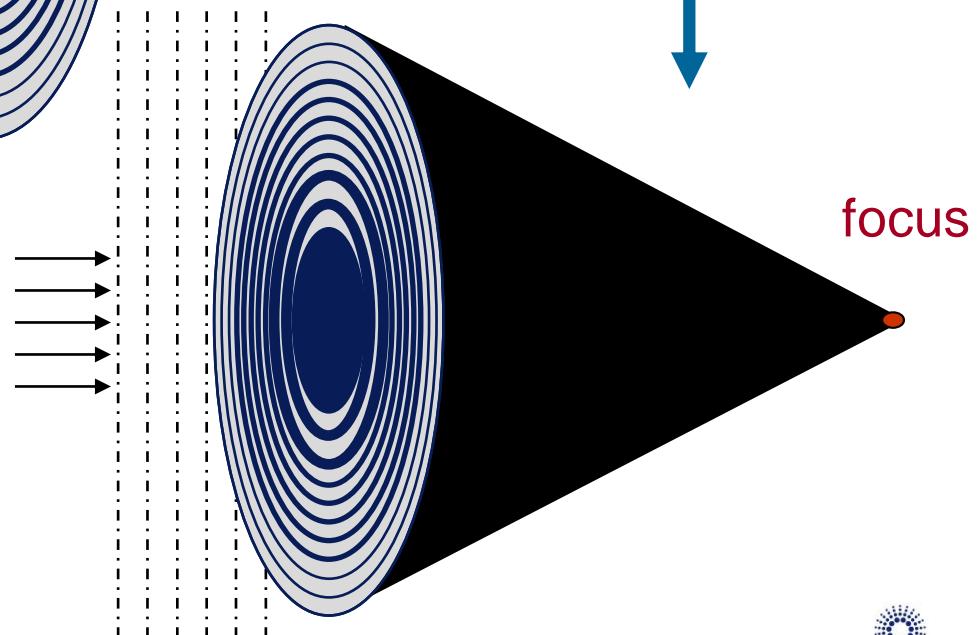
*Planar wavefront*



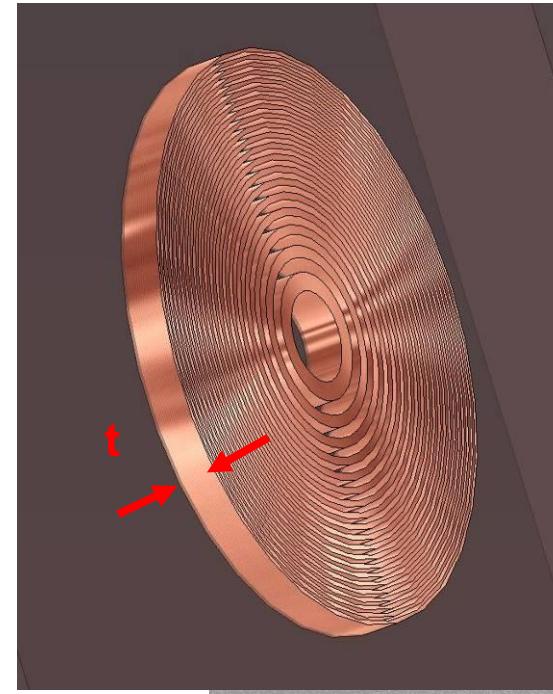
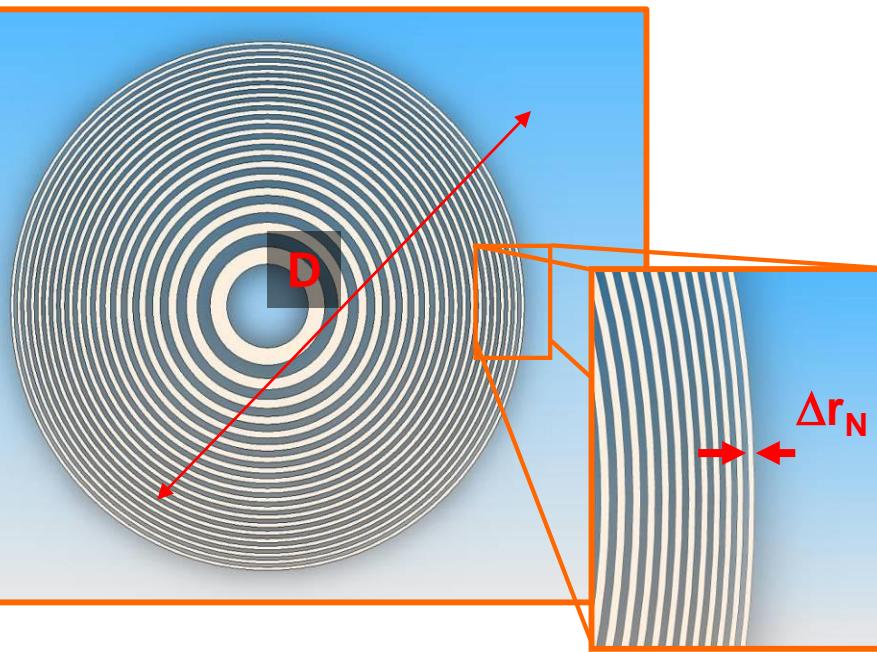
Baez (1952)  
Schmahl (1969)  
Kirz (1971)  
Niemann (1974)

Gabor hologram of a point object

*Reconstruction  
by  
coherent illumination*

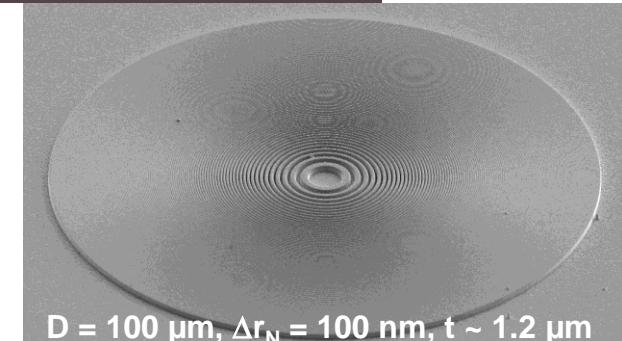


## Diffractive X-ray Lenses: Circular transmissive diffraction gratings with radially decreasing line width giving focusing effect

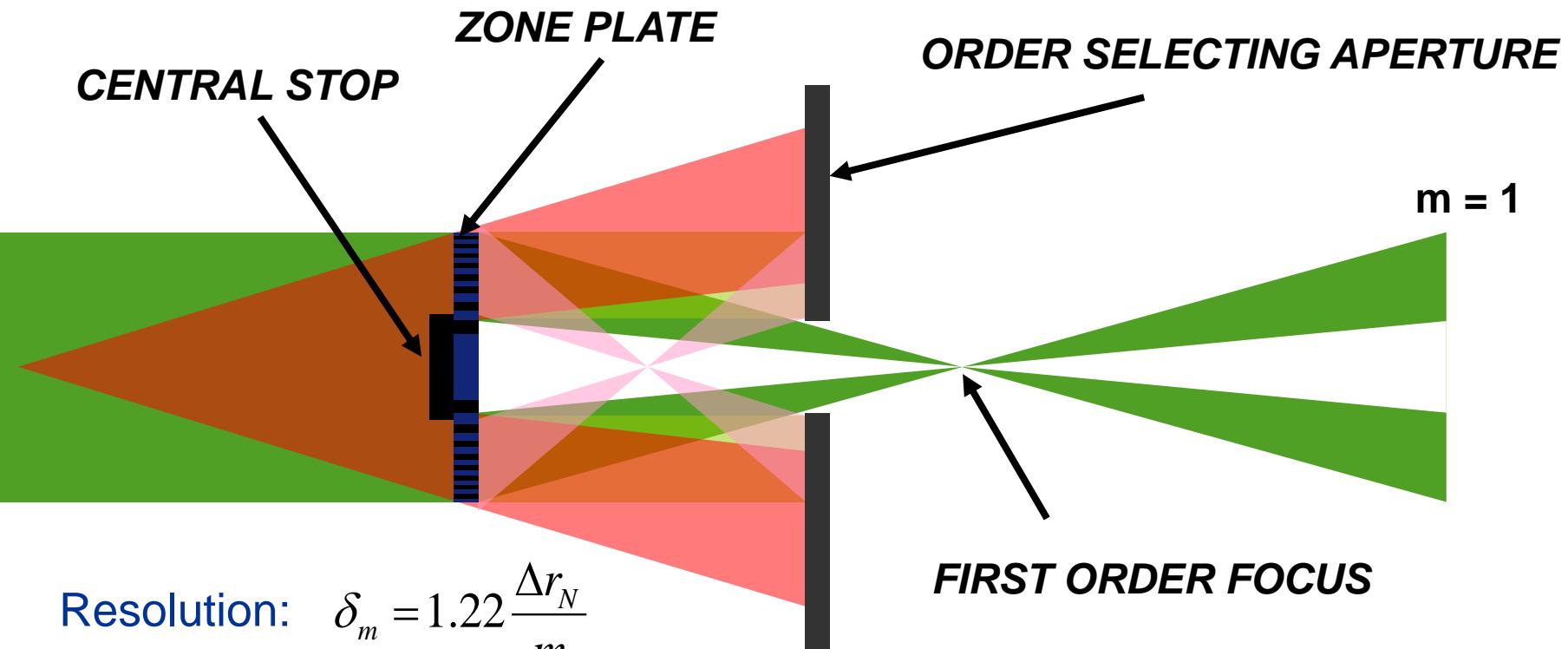


Alternate 'zones' modify phase/amplitude of incident wavefront: for material of thickness, t, wavelength,  $\lambda$ , refractive index  $1-\delta-i\beta$ , phase shift,  $\Delta\phi$ , is:

$$\Delta\phi = \frac{2\pi\delta t}{\lambda}$$



Rejection of unwanted diffraction orders requires central stop & OSA



$$\text{Resolution: } \delta_m = 1.22 \frac{\Delta r_N}{m}$$

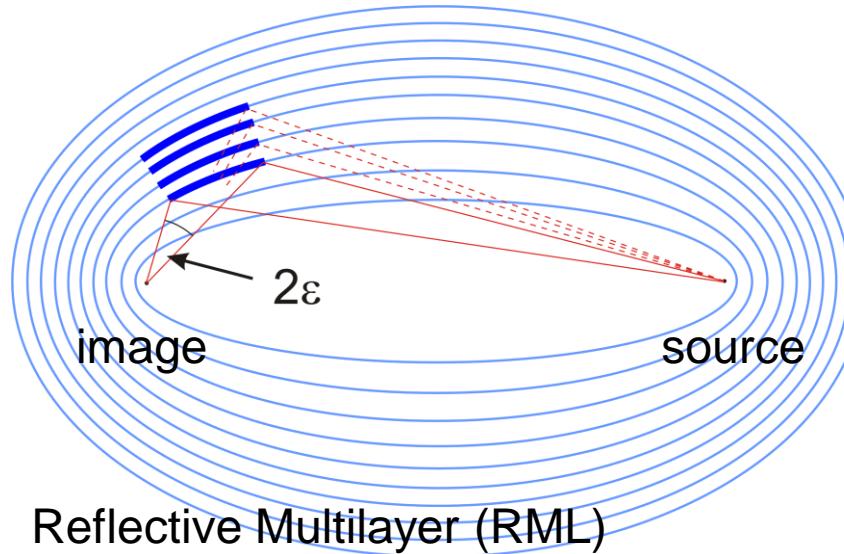
$$\text{Focal length: } f_m = \frac{D \Delta r_N}{m \lambda}$$

$$\text{Depth of focus: } DOF = \pm \frac{2 \Delta r_N^2}{m \lambda}$$

### FIRST ORDER FOCUS

- best zone plates  $\Delta r_N \sim 10\text{nm}$
- zone aspect ratio limits efficiency (often just a few %): better adapted to lower energies  $<10\text{keV}$

# FOCUSING WITH ELLIPTICAL MIRROR SURFACES



Diffraction limited focusing:

$$D_{diff} = \frac{0.44 \cdot \lambda}{NA} = \frac{0.44 \cdot \lambda}{\epsilon}$$

$$\epsilon_{max} \approx \frac{\theta_c}{4}, \quad D_{diff}(TRM) \approx \frac{1.76 \cdot \lambda}{\sqrt{2 \cdot \delta}}$$

Pt mirror:  
25 nm

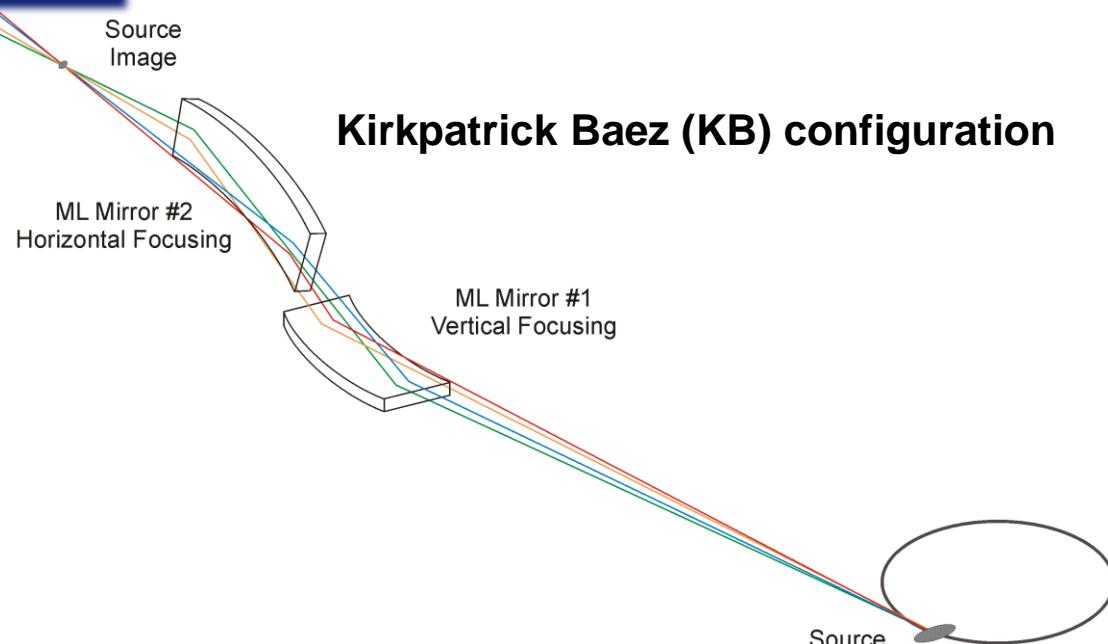
$$D_{diff}(RML) \approx \frac{0.88}{1/\Lambda_2 - 1/\Lambda_1}$$

7 nm focus  
Mimura et al,(2010)

Use of MLs => increased aperture → flux!

## Elliptical Mirrors for micro- & nano-focusing

- Dynamic figure
  - Adapt figure to focusing requirements ( $f$ ,  $\lambda$ , multilayers)
  - Increased figure errors
- Static figure
  - Fixed focusing configuration
  - Better figure – less flexible operation

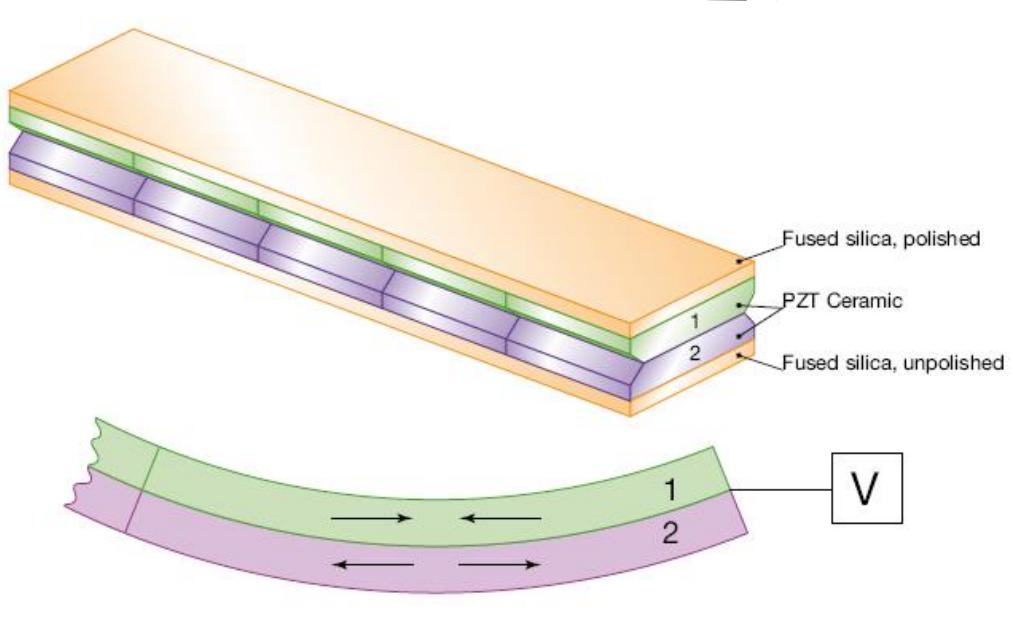


## 2 major classes:

- Piezoelectric bimorph systems
- Mechanically actuated systems

Extension of these technologies – increase number of actuators to correct local figure errors – active optics (several projects)

2 independent bending moments: Elliptical Figure



Principle of Bimorph Mirror (from FMB-Oxford)

2 independent actuators

ESRF mirror bender based on monolithic flexure hinge technology

# ESRF NANOFOCUSING KB SYSTEM: ID16B

## Smallest ESRF dynamic bending system

HF Mirror focal distance ~83 mm

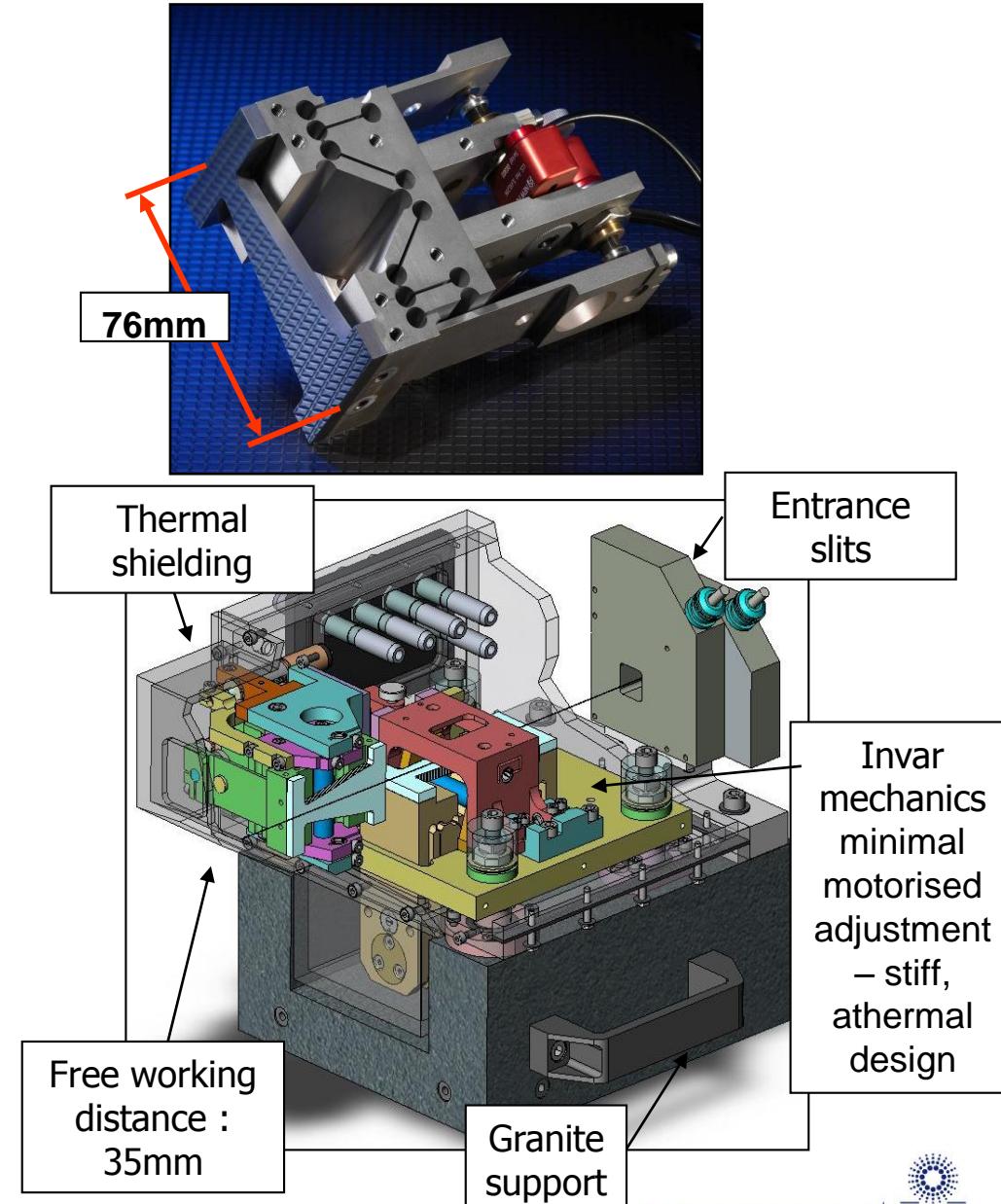
Close to the current limits of bending technology:

Local bending radius down to 10 m

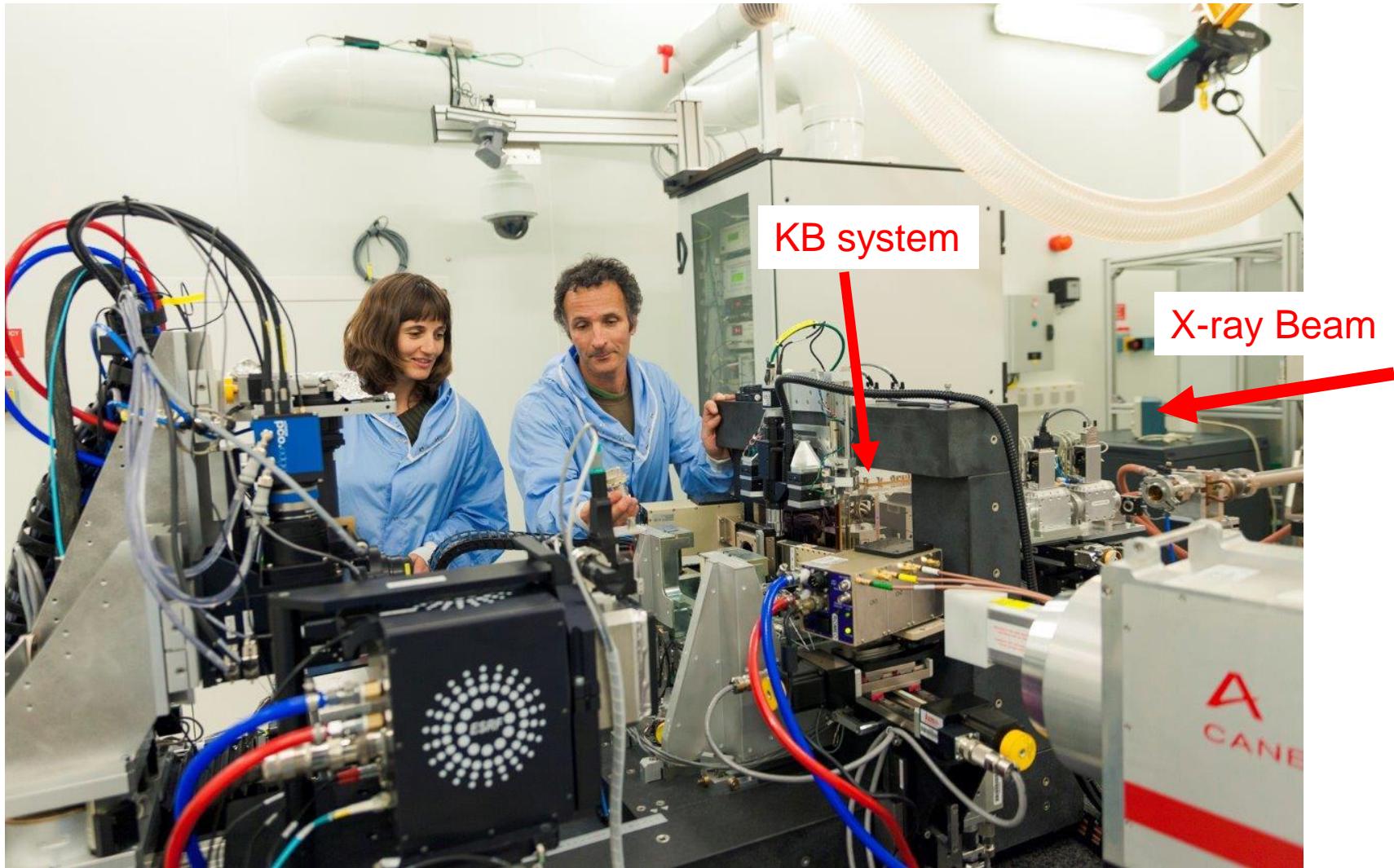
Mirror stress up to 30 MPa

Optimised figure at 17keV: 8 mrad  
(25keV 5.5 mrad)

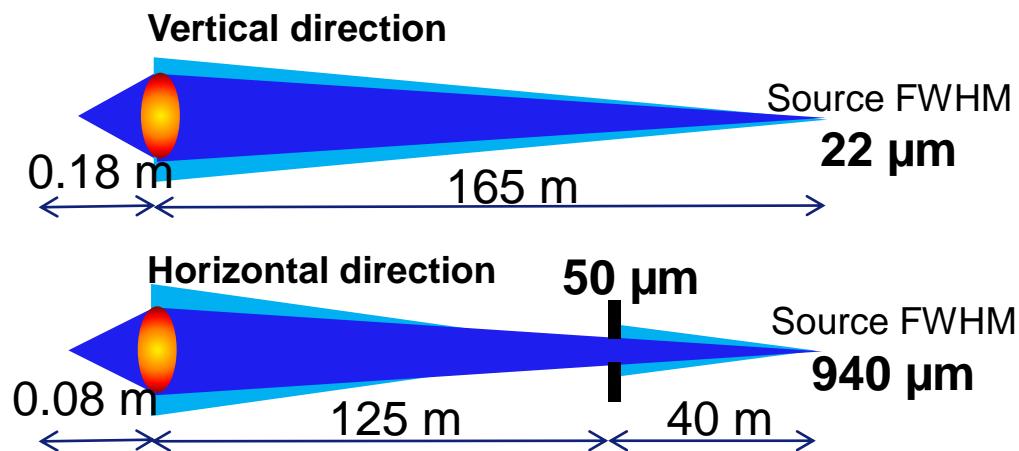
	slope error [μrad rms]	figure error [nm rms]
HF (40 mm)	0.15 (0.11)	0.38 (0.16)
VF (70 mm)	0.09 (0.06)	0.32 (0.16)



## ID16B END STATION

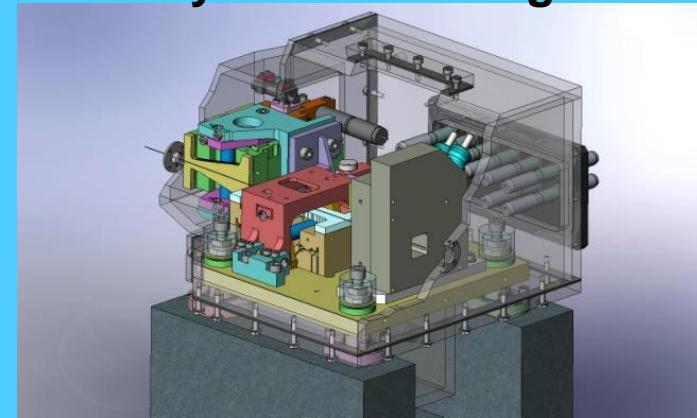


# FOCUSING OPTICS PERFORMANCE ON ID16B

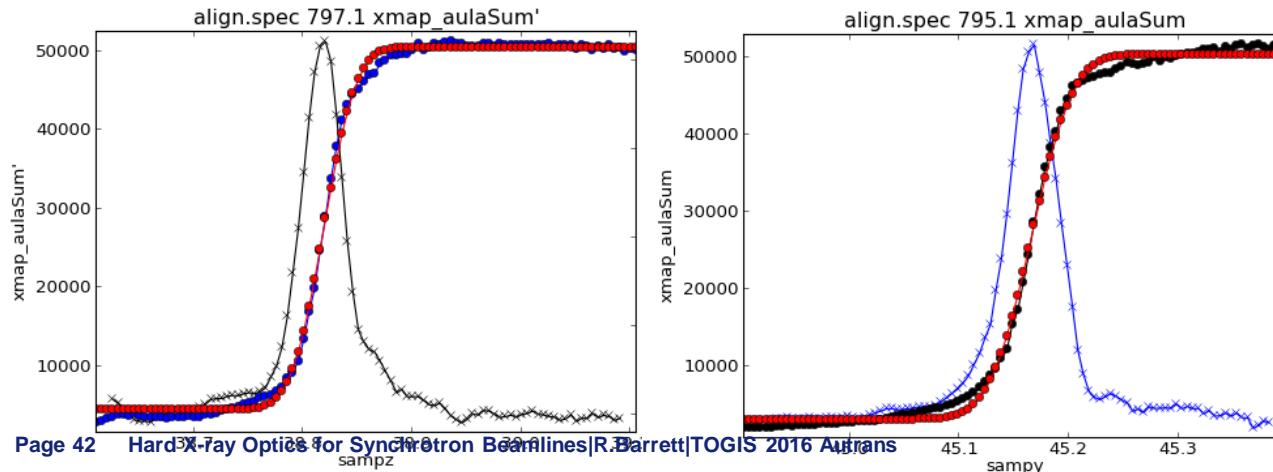


**Knife-edge scans:**  
FWHM horiz. = 50 nm  
FWHM vert. = 48 nm

**KB mirrors + Multilayers +dynamic bending**

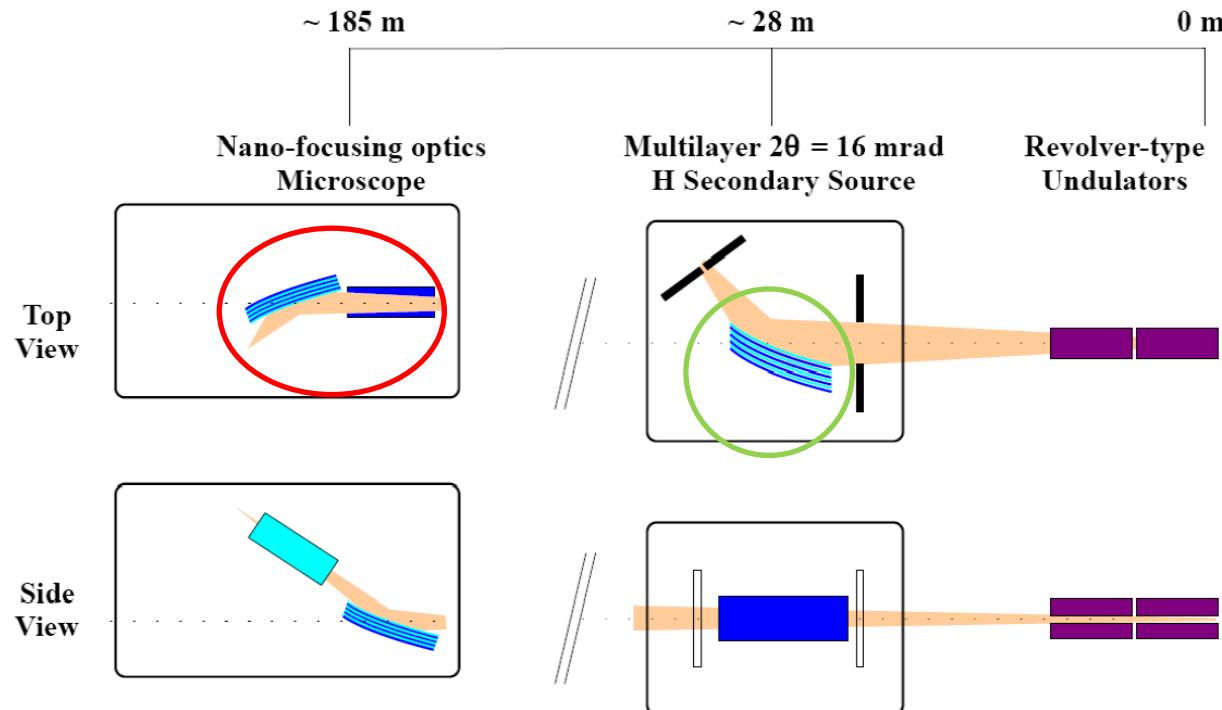


- High Flux
- High numerical aperture
- Achromaticity



**E = 17.5 keV**  
**Pink beam mode**  
**Flux =  $5 \cdot 10^{11} \text{ ph/s}$**   
**Energy range: 17-29 keV**  
**Tunable bandwidth:**  
 $\Delta E/E \sim 1.5 - 7 \%$

# ID16A “NI” OPTICAL SCHEME



## Nano-imaging applications:

- 17 and 34 keV
- High throughput
- Pink beam (full undulator peak)
- Target fwhm spot size ~20-25 nm

- Horizontal: Secondary source by **focusing ML**
- Three ML stripes for  $E = 11.2 / 17.0 / 33.6$  keV
- **2 sets of static figured KBs** with graded ML coatings
- KB1: 17.0 keV, KB2: 33.6 keV

## STATICALLY FIGURED NANOFOCUSING KB MIRROR SYSTEM

Radius of curvature and figure specifications too severe for bending ⇒  
Fixed curvature KB mirrors (JTEC, Japan)  
ML coating at ESRF and integrated into in-house designed mechanics

2 mirror pairs KB1:17 keV, KB2: 33.6 keV

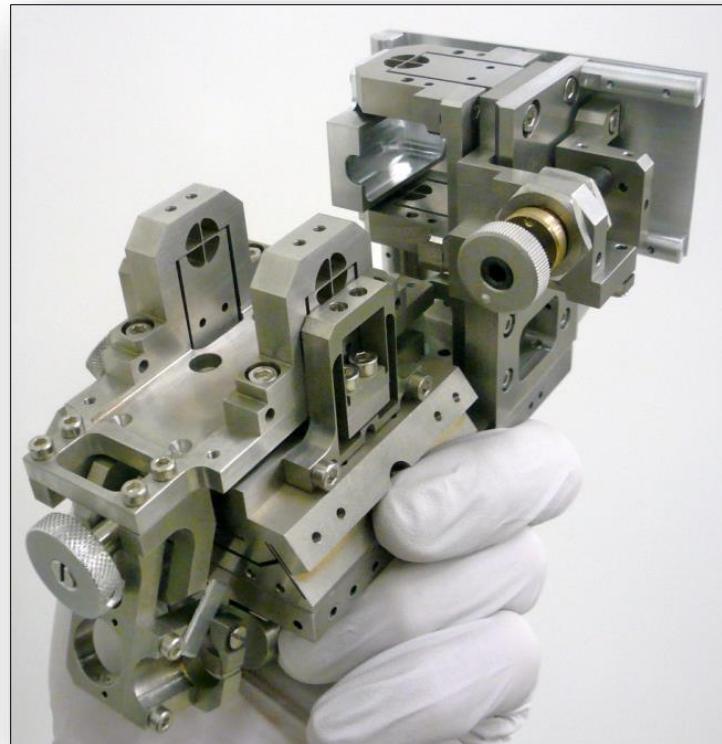
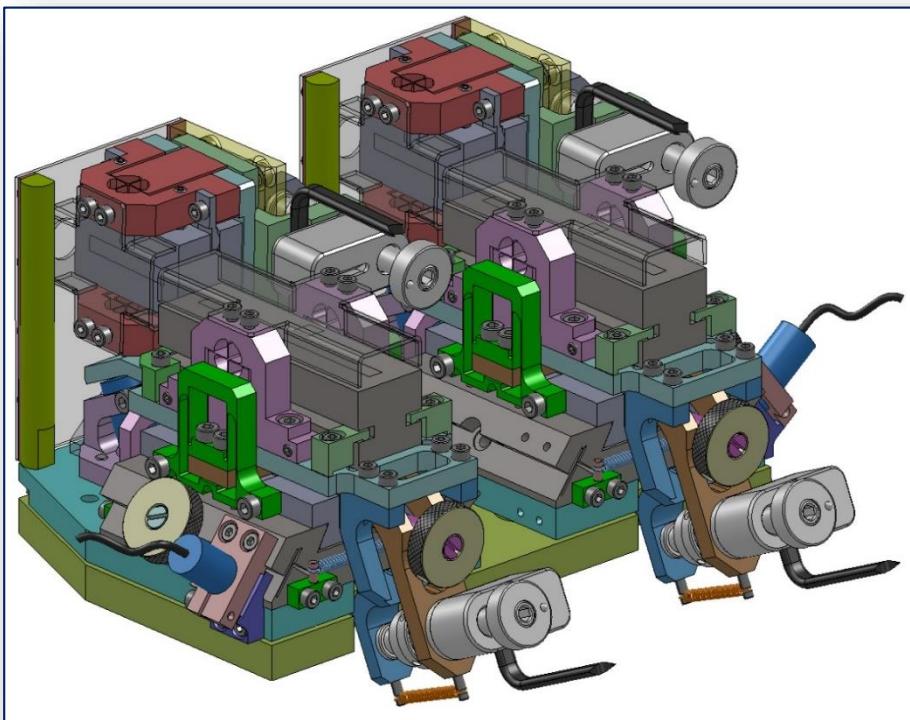
**Extreme asphericity:**

VFM: 22 to 7 m over 70 mm

HFM: 10 to 2.7 m over 36 mm (for KB1)

Target figure errors < 1 nm p.v.

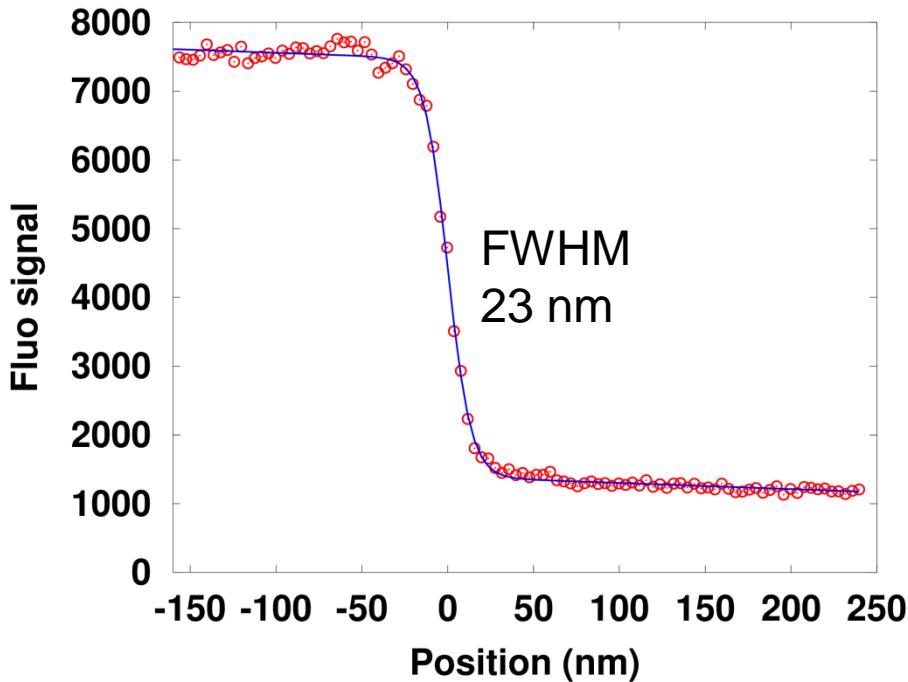
Surface roughness < 1 Å rms



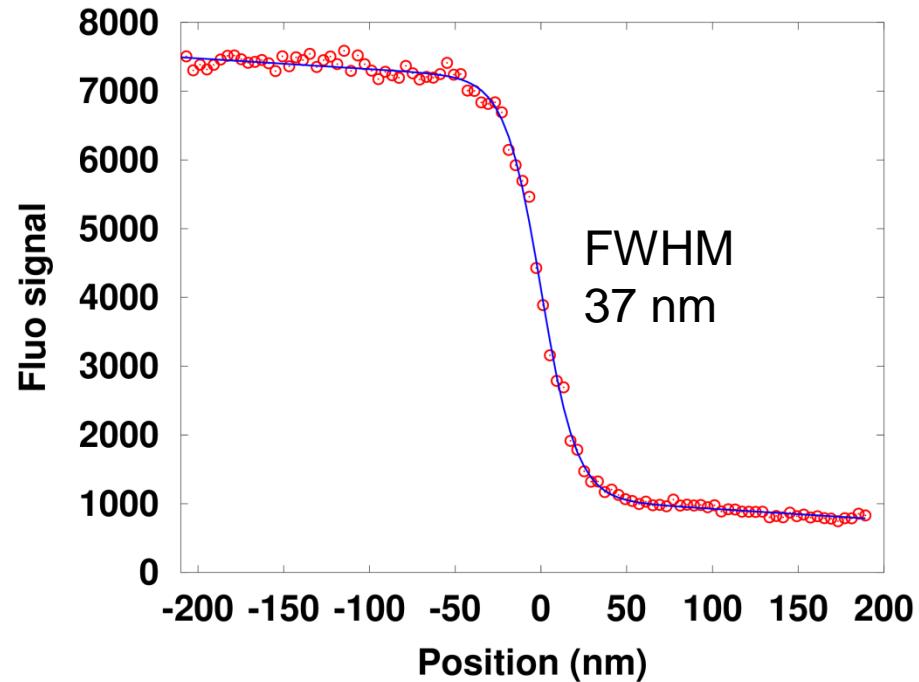
**Focus size: 75 nm (July 2014) → 50 nm (August)  
→ 30 x 40 nm (September) → 23 x 37 nm (October)**

Acceptance: 550μm x 300μm

**Horizontal**



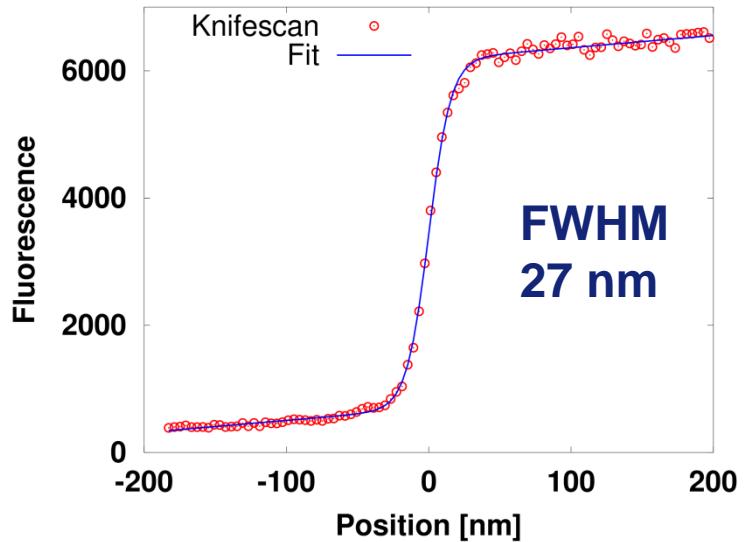
**Vertical**



**Flux (in smallest beam):  $7 \cdot 10^{11}$  ph/s with single undulator!**

**Focus size: 27 x 21 nm (July 2015)**

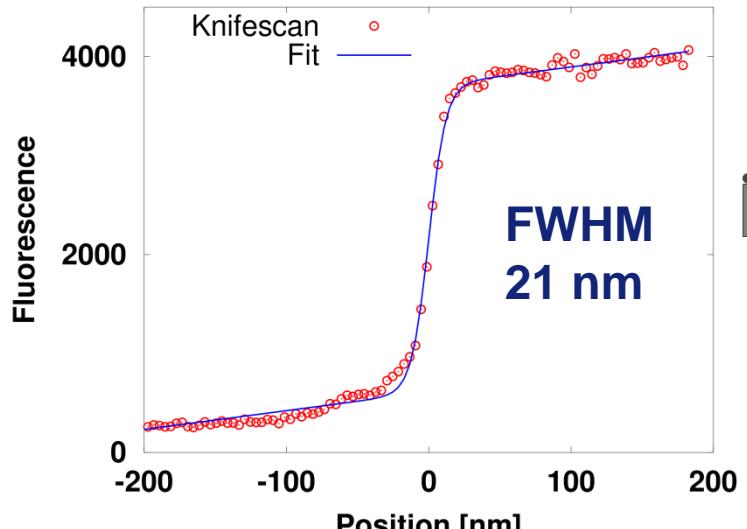
**Horizontal**



Flux  $6 \cdot 10^{10}$  ph/s



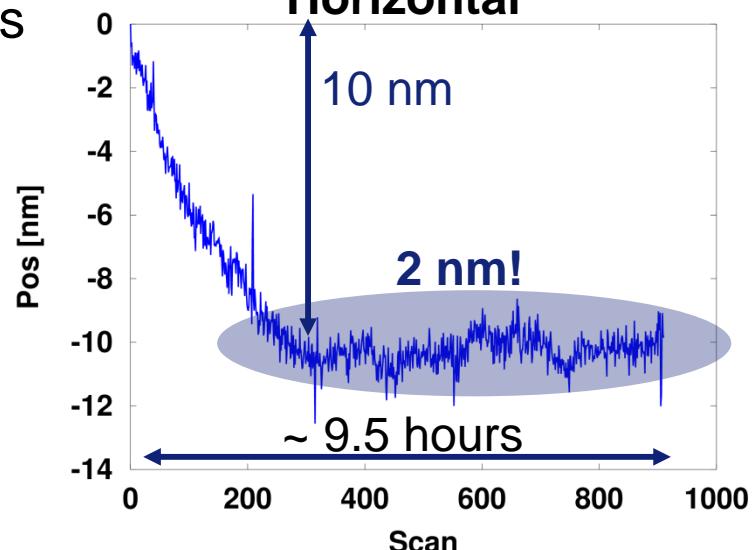
**Vertical**



4-bunch mode,  
KB or sample stage drift?

**Stability (Sept 2015, 4-bunch)**

**Horizontal**

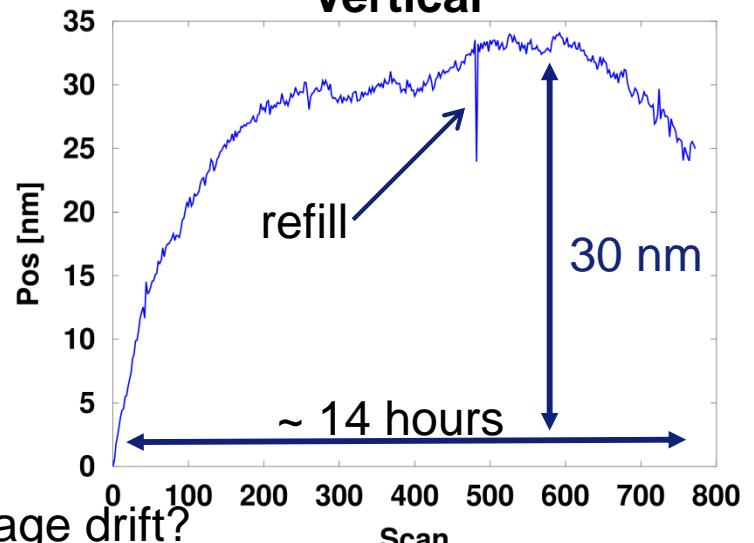


2 nm!

~ 9.5 hours

Scan

**Vertical**



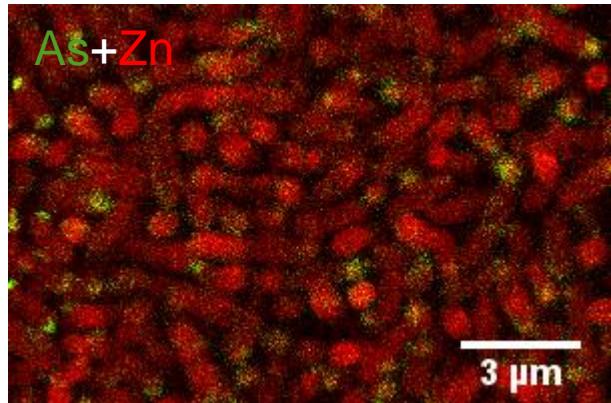
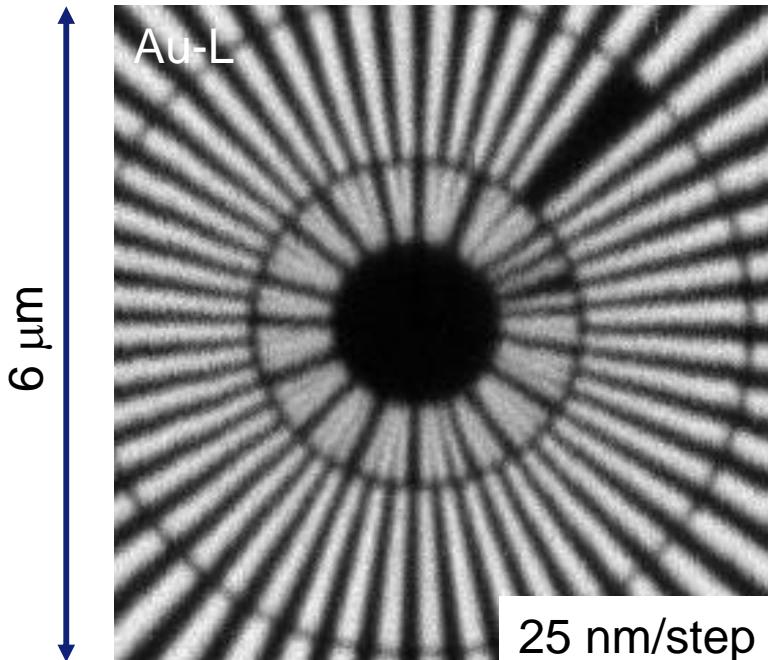
refill

~ 14 hours

30 nm

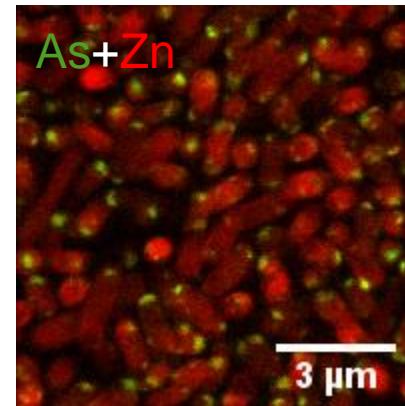
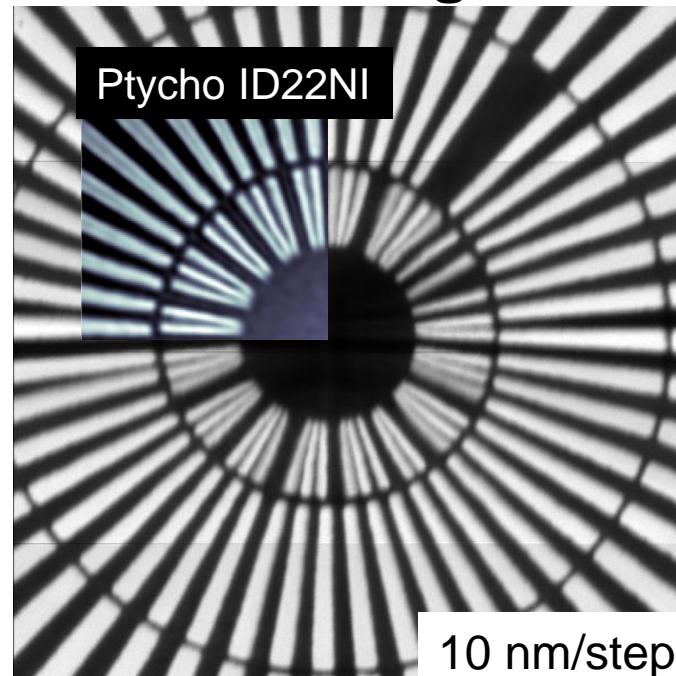
Scan

### XRF: Dynamic bending



50 nm/step  
100ms  
exposure

### XRF: Static figure



Study of As metal uptake within bacteria populations.

S.Kirchen, IFG,  
Karlsruhe Institute of Technology

## REQUIRED QUALITY OF X-RAY OPTICS (DIFFRACTION LIMITED FOCUSING)

**Strehl ratio:** > 80% (i.e. <20% of intensity outside spot)

**Maréchal Criterion:** rms wavefront error  $\lambda/13$  (but  $\lambda \sim 1 \text{ \AA}$ !)

**Reflective Optics:** Any deviation  $h$  from the ideal surface introduces a phase distortion  $\varphi$ . At grazing angle  $\theta$ ,  $\varphi = (4\pi/\lambda) \cdot h \cdot \sin\theta$

X-ray energy (keV)	Coating material	Incidence angle $\theta$ (mrad)	Figure specification $\sigma$ (nm, rms)
8	Rhodium	6.0	1.0
20	Platinum	3.0	0.8
50	Multilayer (W/B <sub>4</sub> C)	5.9	0.15

e.g. O. Hignette *et al.*, Proc. SPIE 4501:43–53. San Diego 2001

**Refractive Optics:** Cumulated thickness errors,  $t$ , of lenses introduce phase distortion  $\varphi$ . For material with  $n=1-\delta-i\beta$ ,  $\varphi = 2\pi\delta t/\lambda$

X-ray energy (keV)	Lens material	delta	Figure specification $\sigma$ (nm, rms) (full stack)	Figure specification $\sigma$ (nm, rms) (per lens *)
8	Be	5.3E-06	2200	980
20	Be	8.5E-07	5600	1000
50	Al	2.2E-07	8700	810

\* Assumes focal length of 1m with lenses R=50μm

**Fresnel Zone Plates:** Zone placement accuracy ~ 1/3 zone width (3-4 nm!)

e.g. A.G. Michette, *Optical Systems for Soft X Rays*. Plenum Press, 1986

# DEFECTS ON COHERENTLY ILLUMINATED MIRRORS

Ideal Focus (15keV)

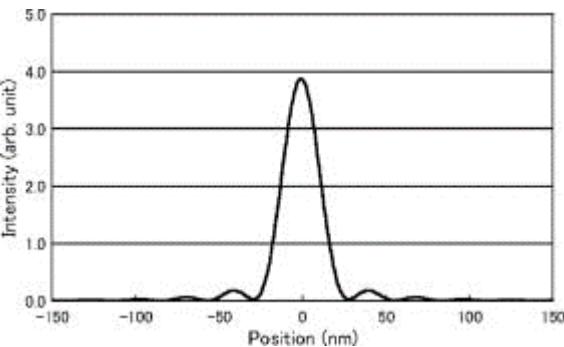
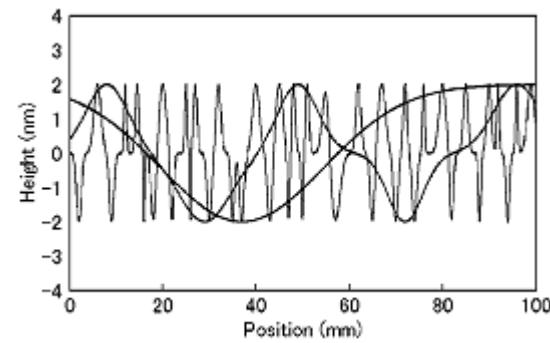
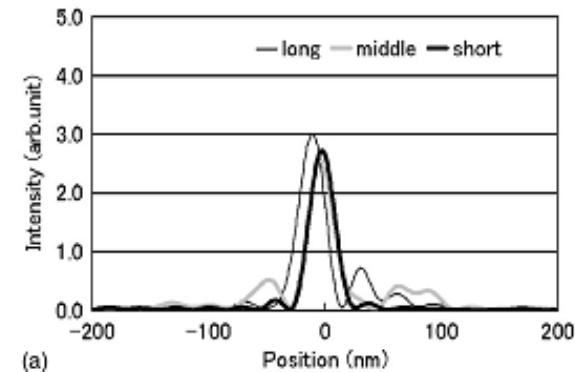


Figure Errors



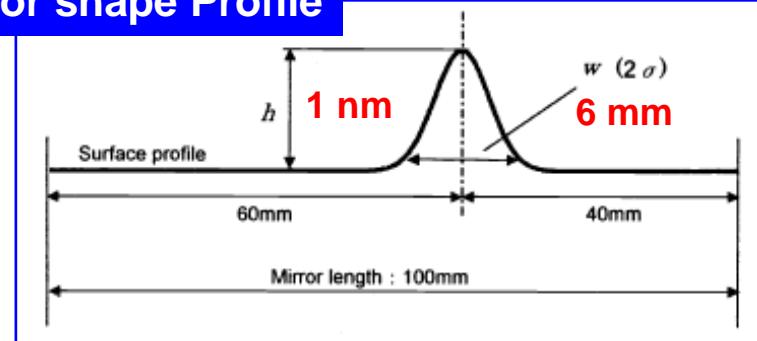
Aberrated focus



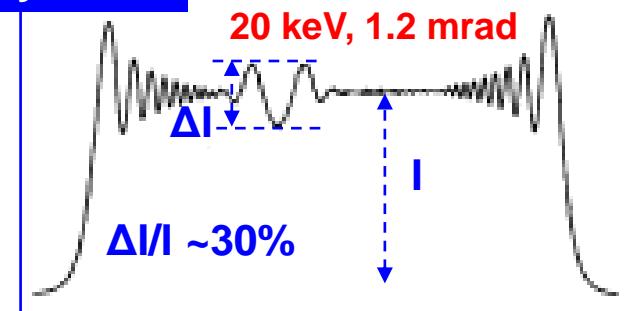
(a)

H. Mimura et al, *Rev. Sci Inst* 76, [4] (2005) 045102–6 doi:10.1063/1.1868472.

Mirror shape Profile



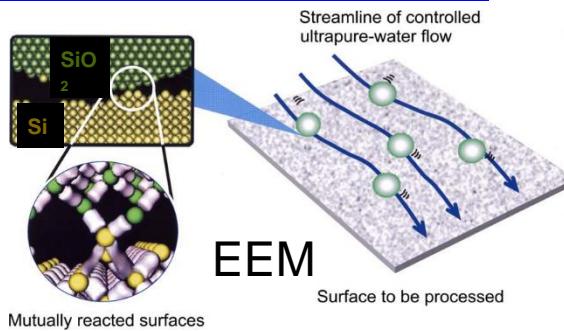
Intensity @ 1m



Current state of the art of X-ray mirror quality is for slope errors  $\sim 0.1 \text{ urad rms}$ , figure errors  $\sim 1 \text{ nm p.v.}$  - both still limit optimal source exploitation

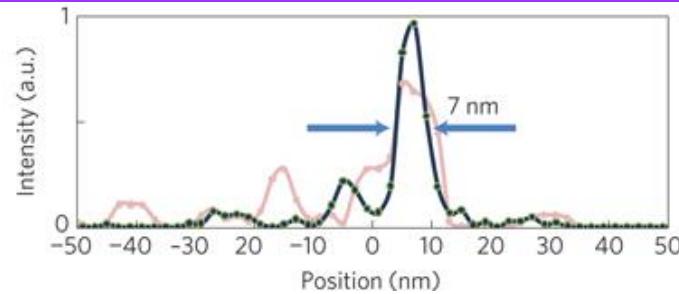
## CURRENT BEST FOCUSING PERFORMANCE

### Deterministic Polishing

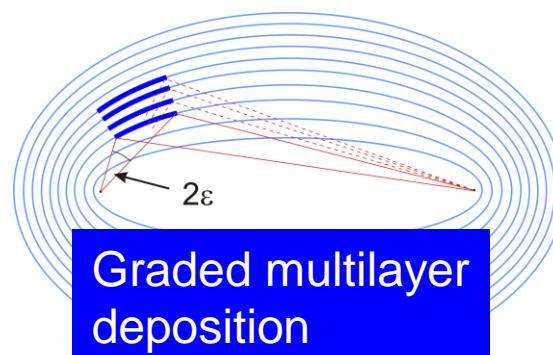


### Advanced Metrology Techniques

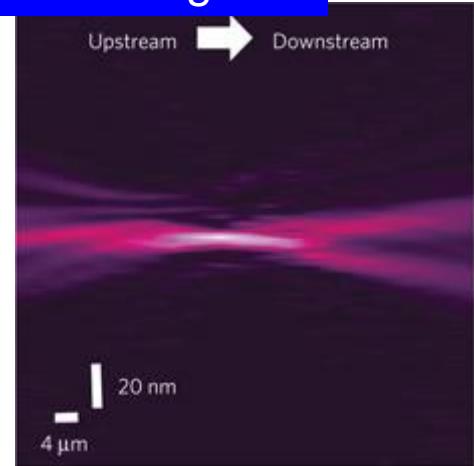
20keV: 7 nm measured focal spot



### Coherent illumination



### Wave-optical Modeling



H. Mimura et al., "Breaking the 10 nm barrier in hard-X-ray focusing," *Nat Phys* 6, (2010): 122-125

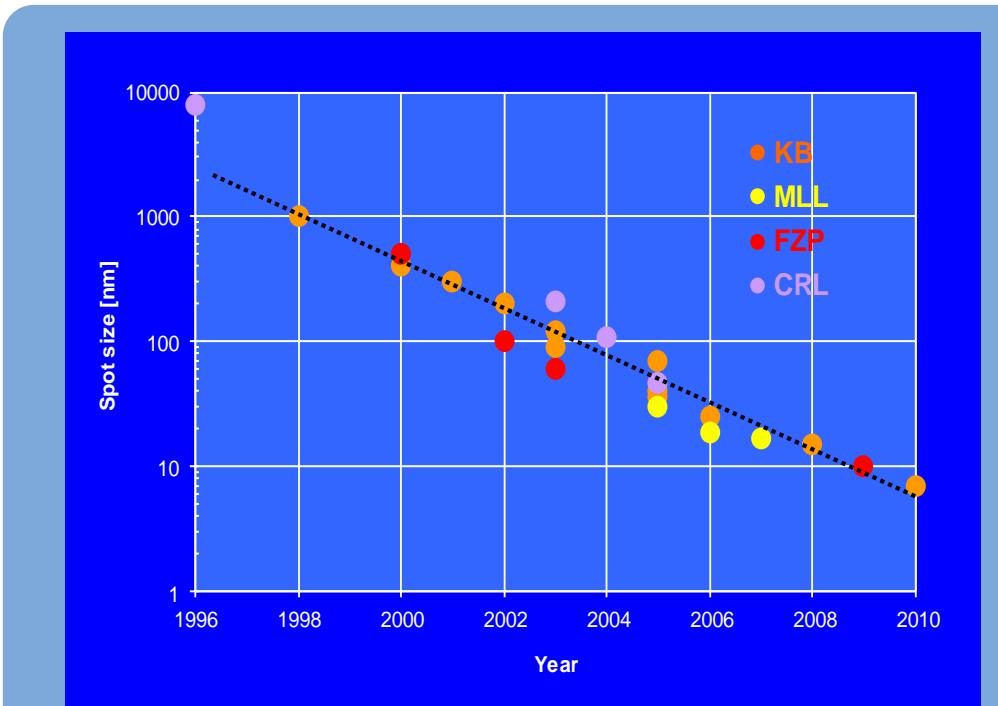
Moore's law adapted to the X-ray world:

**ESRF Red Book (1987):  
very few beamline projects  
aiming even for 10 micron  
sized beams**

**Now optics exist for 10nm  
beams**

**Routine application of sub-  
micron beams still  
complicated**

**Also many engineering  
issues in implementing  
stable, reliable X-ray  
nanofocusing systems**

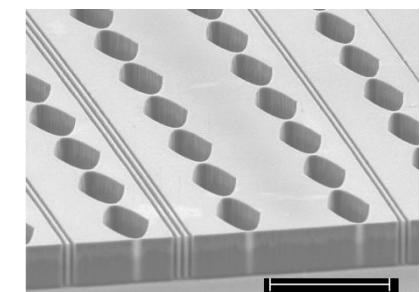
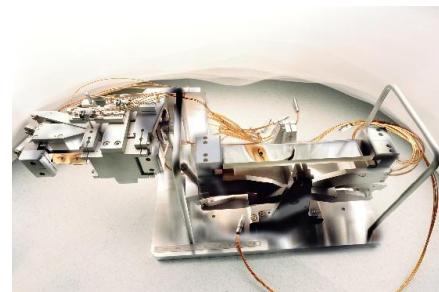
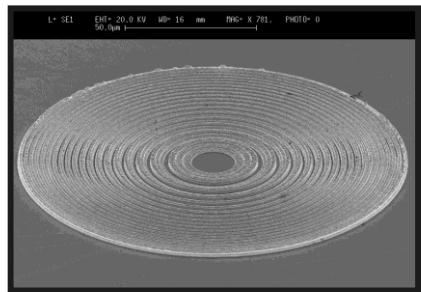
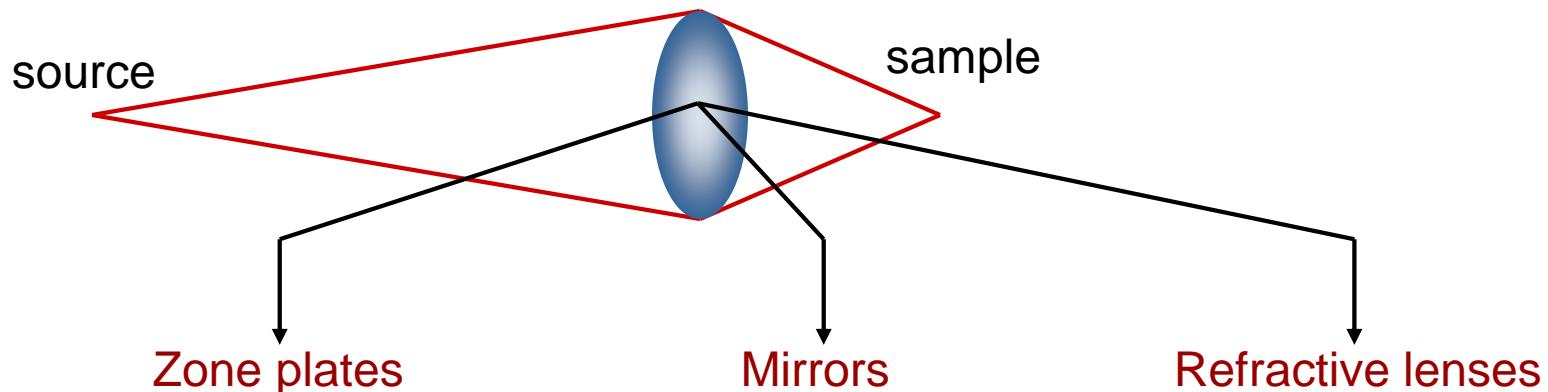


Historical evolution of the measured spot size for different hard x-ray focusing elements (courtesy C. Morawe)

- H. Mimura *et al.* *Nature Physics*, **6**, 122-125 (2010).
- J. Vila-Comamala *et al.*, *Ultramicroscopy*, **109**, 1360–1364 (2009)
- H. Kang *et al.*, *Physical Review Letters*, **96**:127401 (2006)
- C. Schroer *et al.*, *Physical Review Letters*, **94**:054802 (2005)

{ Best focus  
Experiments  
  
Ultimate resolution  
Theory

# COMPARISON OF DIFFERENT MICRO/NANOFOCUSING OPTICS



Energy →

• <b>Resolution</b>	++++	++	++
• <b>Achromaticity</b>	-(-)	+++	--(-)
• <b>Efficiency</b>	+	+++	++
• <b>Imaging (MTF)</b>	++++	+	++

*The advent of 3<sup>rd</sup> generation synchrotron X-ray sources has encouraged the development of new hard X-ray optics*

- Modern beamline design can draw on a toolbox of optical components based on diffraction, reflection and refraction of X-rays
- dramatic improvement in manufacturing and preparation techniques
  - low roughness, high-accuracy figuring, perfect crystals (Ge, Si), diamond, ...
  - improved power management strategies
  - focusing optics (spot size ~ 50- 0.01μm)
    - zone-plate and refractive lenses, elliptically figured mirrors
  - wide range of experimental requirements – no one ideal optic
- ***R&D programs continuously in progress: current hot-topics***
  - preservation of the wave-front quality – especially important for anticipated use of fully coherent XFEL sources
  - routine sub-10nm focusing