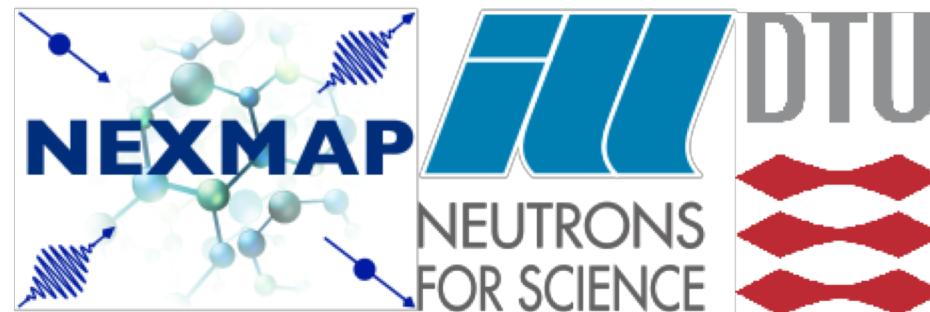
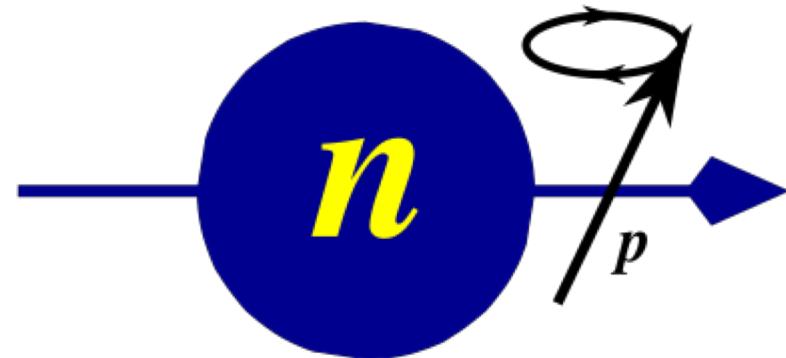
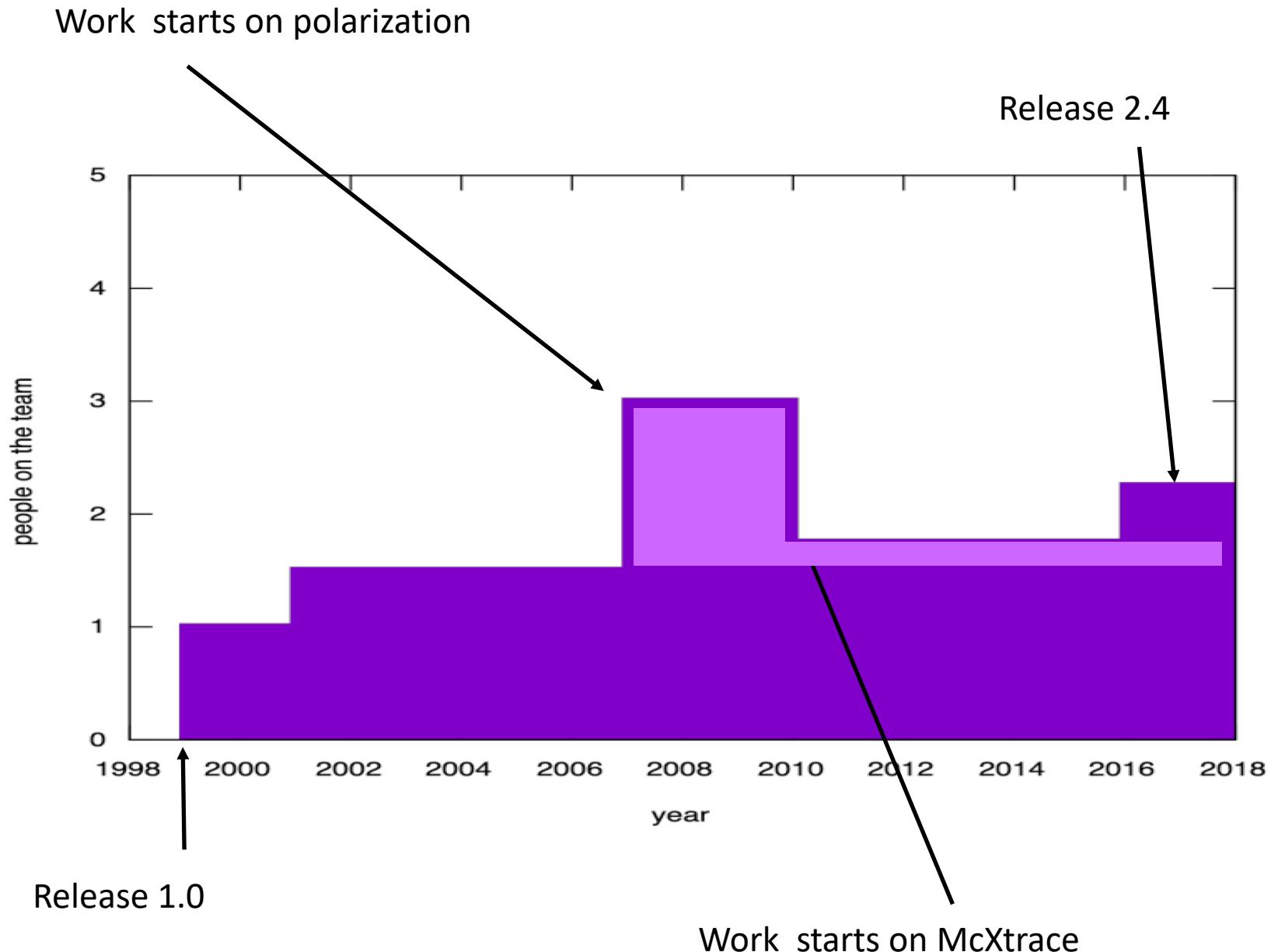


McStas



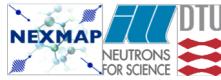
Simulating Polarized Neutron Scattering Experiments
and Equipment with McStas

Emmanuel Farhi, ILL
(Slides from Erik Bergbäck Knudsen, DTU Physics)

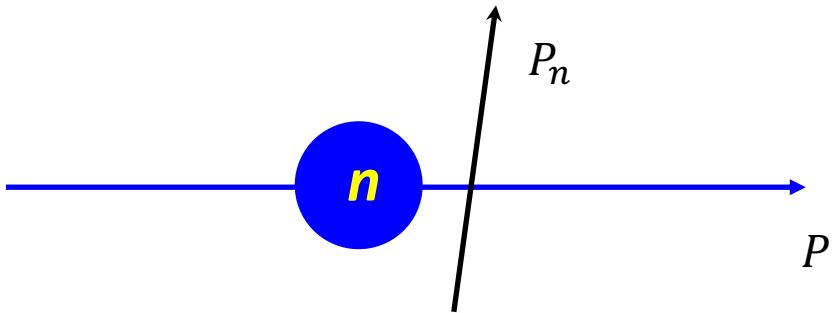


Neutron ray/package:

Weight: (p) # neutrons left in the package
 Position: (x, y, z)
 Velocity: (v_x, v_y, v_z)
 Polarization: (s_x, s_y, s_z)
 Time: (t)



$$P_n = \frac{1}{p} \sum_i^p P_i, n = \text{raynumber}$$

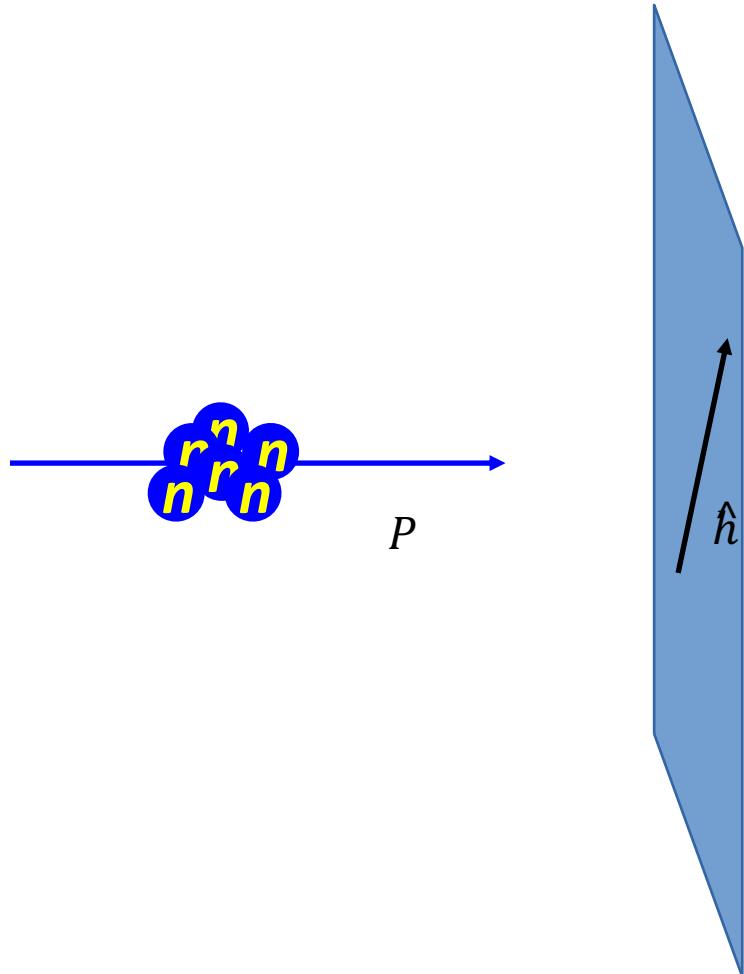


$$P_i = 2(\langle \hat{s}_{x,i} \rangle \hat{t}_{x,i} + \langle \hat{s}_{y,i} \rangle \hat{t}_{y,i} + \langle \hat{s}_{z,i} \rangle \hat{t}_{z,i})$$

$$P = \frac{1}{N} \sum_{n=0}^N P_n$$

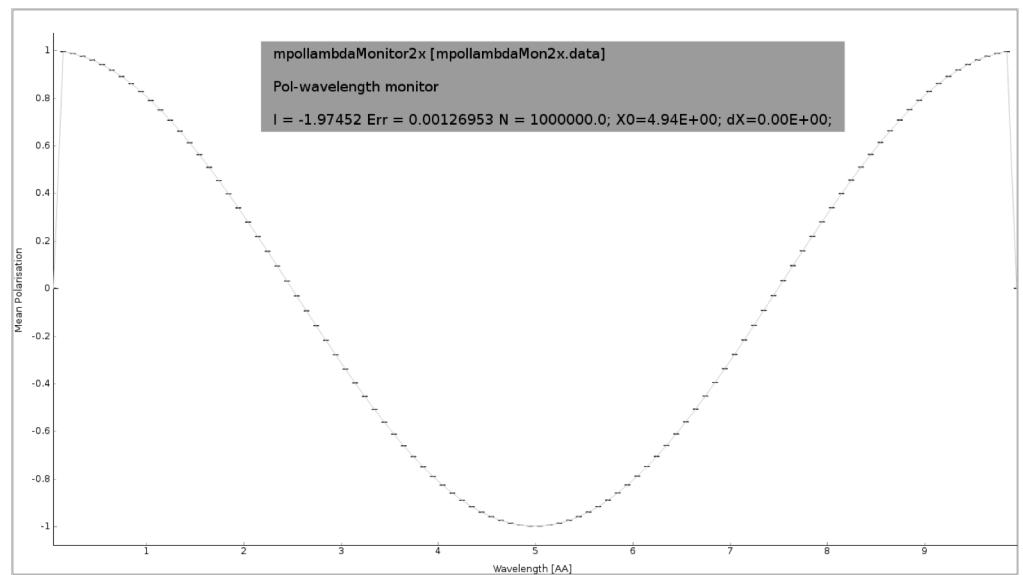
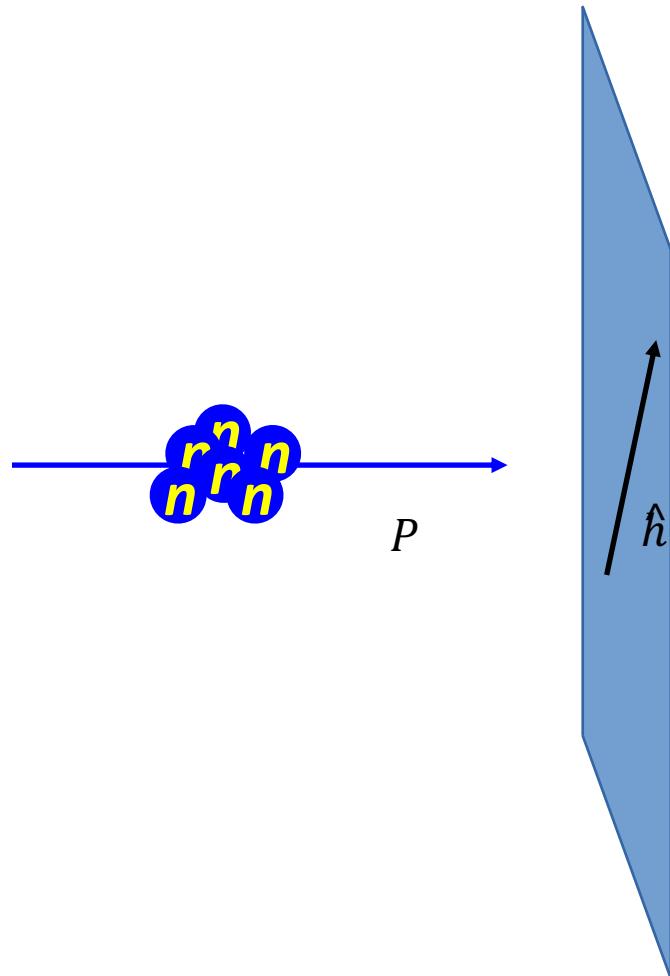
From G. Williams: “Polarized neutrons”, Oxford Science Publ., 1988

Monitoring: How and What do we monitor?

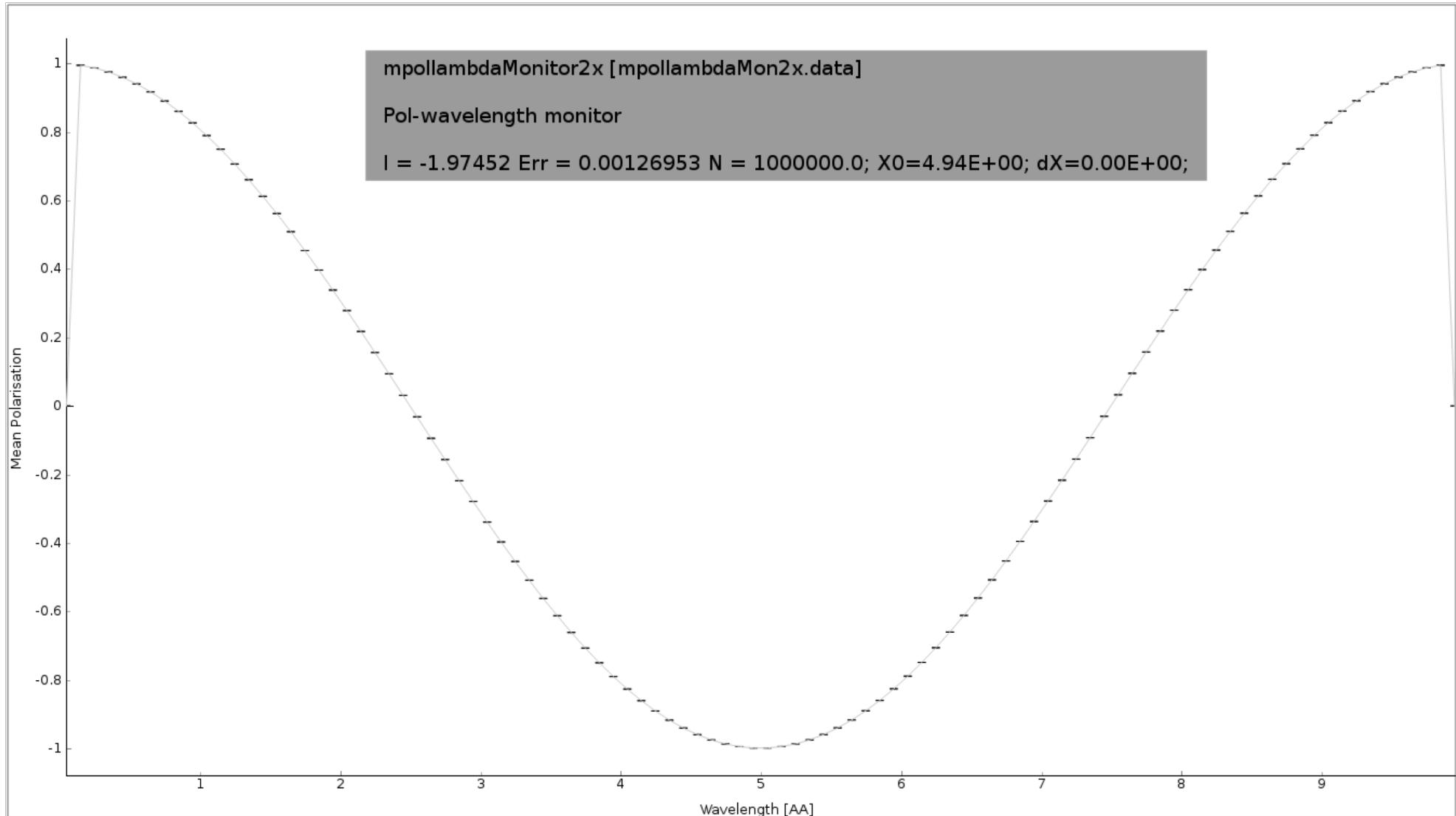


$$P_{\hat{h}} = \frac{\sum_{n=0}^N p_n P_n \cdot \hat{h}}{\sum_n p_n}$$

Monitoring: How and What do we monitor?



Monitoring: How and What do we monitor?



- Available monitors:
 - Pol_monitor.comp: 0D
 - PolLambda_monitor.comp: 2D
 - MeanPolLambda_monitor.comp: 1D

- ➊ Magnetic fields in McStas

- ➋ The challenge:

- * Fast beam/ray transport: # $\text{rays} > 10^6$
- * Unknown magnetic field and field strength
- * >1 Magnet \rightarrow nested fields.

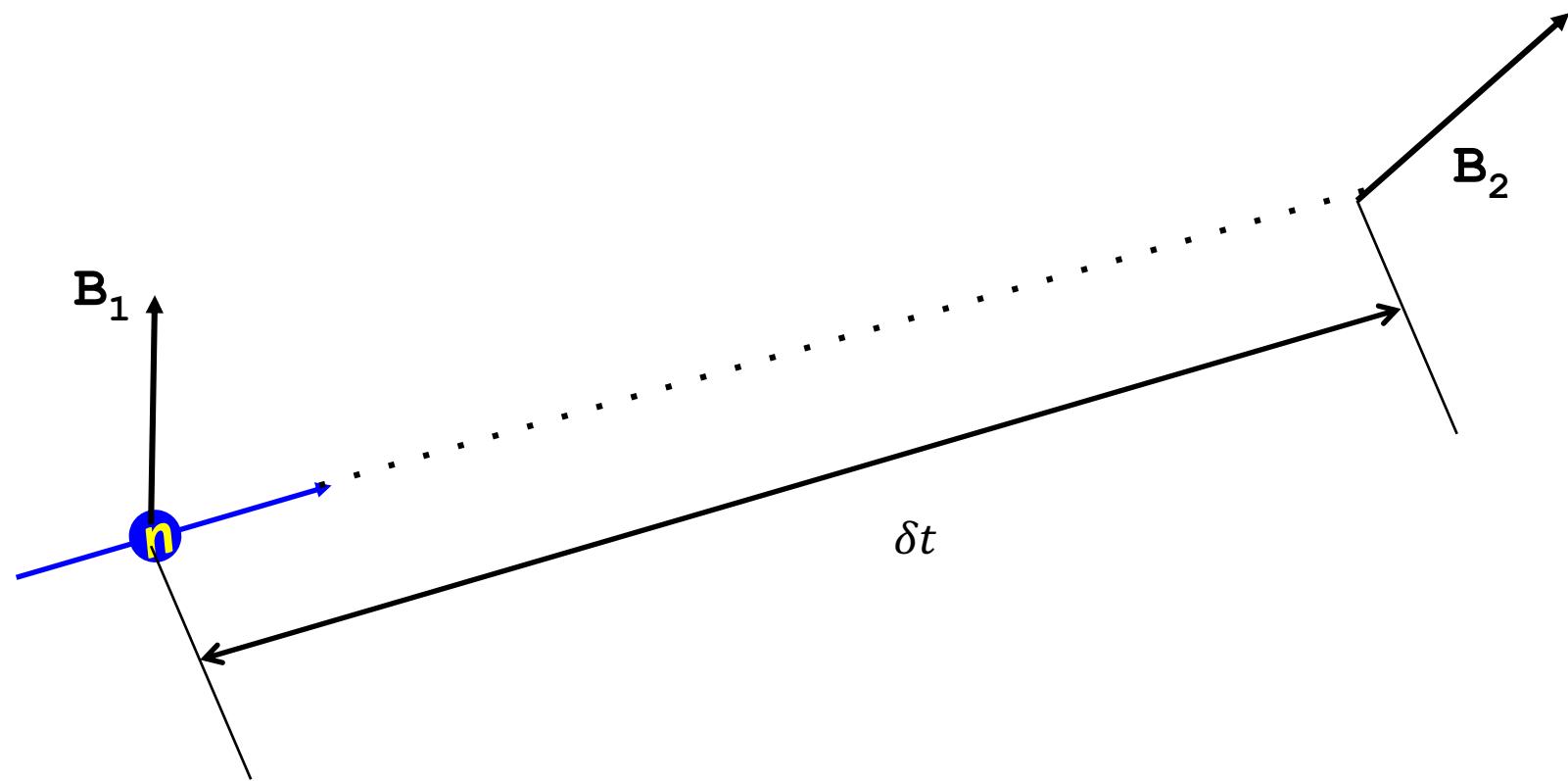
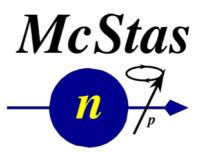
```

while  $n_t < t_{\text{target}}$  do
    store neutron;
    sample magnetic field:  $\mathbf{B}_1 = \mathbf{B}(n_x, n_y, n_z, n_t)$ ;
    propagate neutron:  $\delta t (< \Delta t)$ ;
    sample magnetic field:  $\mathbf{B}_2 = \mathbf{B}(n_x, n_y, n_z, n_t)$ ;
    while  $|\mathbf{B}_1 - \mathbf{B}_2| > \delta B_{\text{threshold}}$  do
        restore neutron;
         $\delta t := \delta t / 2$ ;
        propagate neutron:  $\delta t (< \Delta t)$ ;
        sample magnetic field:  $\mathbf{B}_1 = \mathbf{B}(n_x, n_y, n_z, n_t)$ ;
    precess polarization:  $\mathbf{P}_n$  by  $\omega$  around  $\frac{\mathbf{B}_1 + \mathbf{B}_2}{2}$ ;
  
```

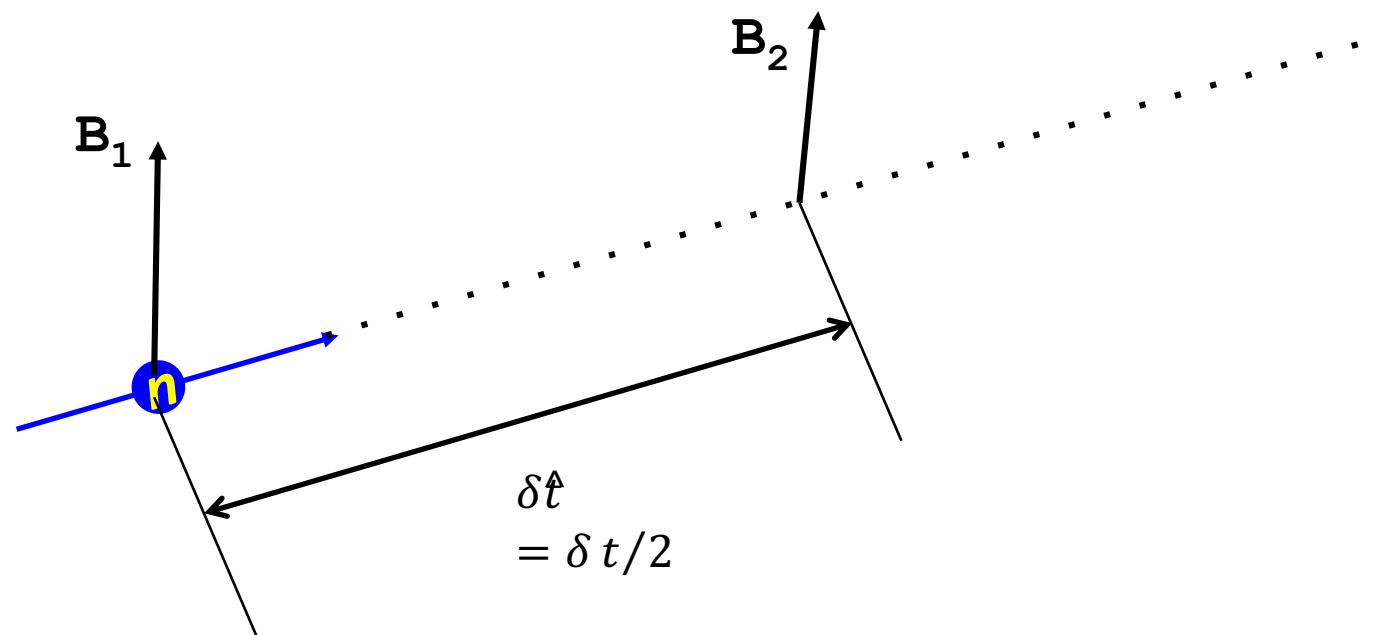
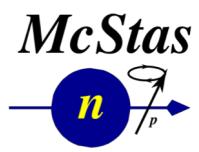
Algorithm 1: SimpleNumMagnetPrecession: Simplistic algorithm for tracking polarization of a Monte-Carlo neutron in a magnetic field. The neutron's state is stored as a position (n_x, n_y, n_z), a velocity \mathbf{v} , time n_t , and polarization vector \mathbf{P}_n .

From: Knudsen et.al., *J. Neutron Research*, 2014

McStas precession algorithm



McStas precession algorithm



```

while  $n_t < t_{\text{target}}$  do
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        sample magnetic field:  $\mathbf{B}_1 = \mathbf{B}(n_x, n_y, n_z, n_t)$ ;
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```

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From: Knudsen et.al., *J. Neutron Research*, 2014

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        sample magnetic field:  $\mathbf{B}_1 = \mathbf{B}(n_x, n_y, n_z, n_t)$ ;
        precess polarization:  $\mathbf{P}_n$  by  $\omega$  around  $\frac{\mathbf{B}_1 + \mathbf{B}_2}{2}$ ;
    
```

Algorithm 1: SimpleNumMagnetPrecession: Simplistic algorithm for tracking polarization of a Monte-Carlo neutron in a magnetic field. The neutron's state is stored as a position (n_x, n_y, n_z) , a velocity \mathbf{v} , time n_t , and polarization vector \mathbf{P}_n .

From: Knudsen et.al., *J. Neutron Research*, 2014

while $n_t < t_{\text{target}}$ **do**

 store neutron;

 sample magnetic field;

void mc_pol_set_timestep(double dt);

 propagate neutron: $\delta t (< \Delta t)$;

 sample magnet

void mc_pol_set_angular_accuracy(double domega);

while $|\mathbf{B}_1 - \mathbf{B}_2| > \delta B_{\text{threshold}}$ **do**

 restore neutron;

$\delta t := \delta t / 2$;

 propagate neutron: $\delta t (< \Delta t)$;

 sample magnetic field: $\mathbf{B}_1 = \mathbf{B}(n_x, n_y, n_z, n_t)$;

 precess polarization: \mathbf{P}_n by ω around $\frac{\mathbf{B}_1 + \mathbf{B}_2}{2}$;

Algorithm 1: SimpleNumMagnetPrecession: Simplistic algorithm for tracking polarization of a Monte-Carlo neutron in a magnetic field. The neutron's state is stored as a position (n_x, n_y, n_z) , a velocity \mathbf{v} , time n_t , and polarization vector \mathbf{P}_n .

From: Knudsen et.al., *J. Neutron Research*, 2014

Magnetic fields:

- `Pol_FieldBox.comp`
- `Pol_constBfield.comp`
- `Pol_simpleBfield.comp`
- `Pol_simpleBfield_stop.comp`
- `Pol_triafield.comp`

Optics:

- `Monochromator_pol.comp`
- `Pol_bender.comp`
- `Pol_guide_vmirror.comp`
- `Pol_mirror.comp`
- `Pol_pi_2_rotator.comp`
- `Transmission_polarisatorABSnT.comp`
- `Pol_bender_tapering.comp`

Monitors:

- `Pol_monitor.comp`
- `MeanPolLambda_monitor.comp`
- `PolLambda_monitor.comp`

Idealized components:

- `PolAnalyser_ideal.comp`
- `Set_pol.comp`

Contrib:

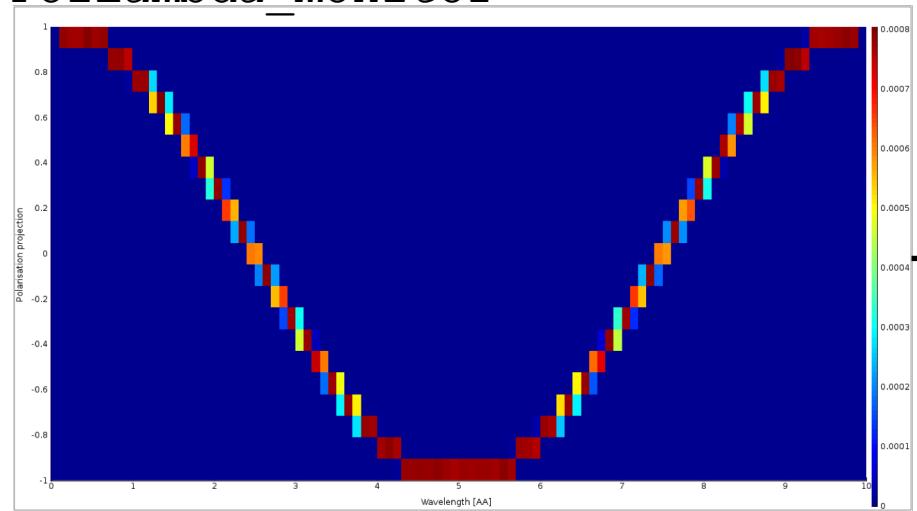
- `Foil_flipper_magnet.comp`

McStas polarization monitors

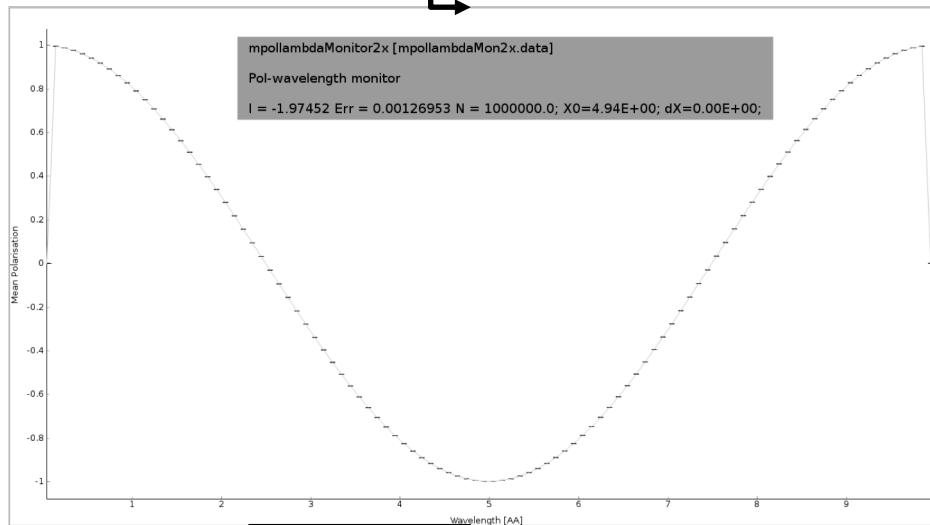


Monitors

PolLambda_monitor

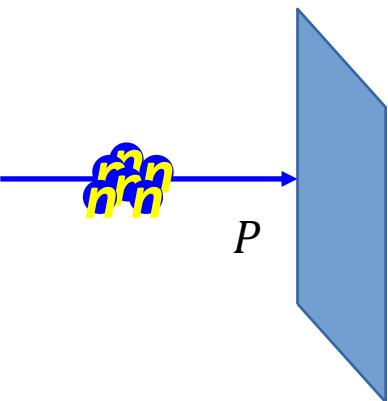


MeanPolLambda_monitor

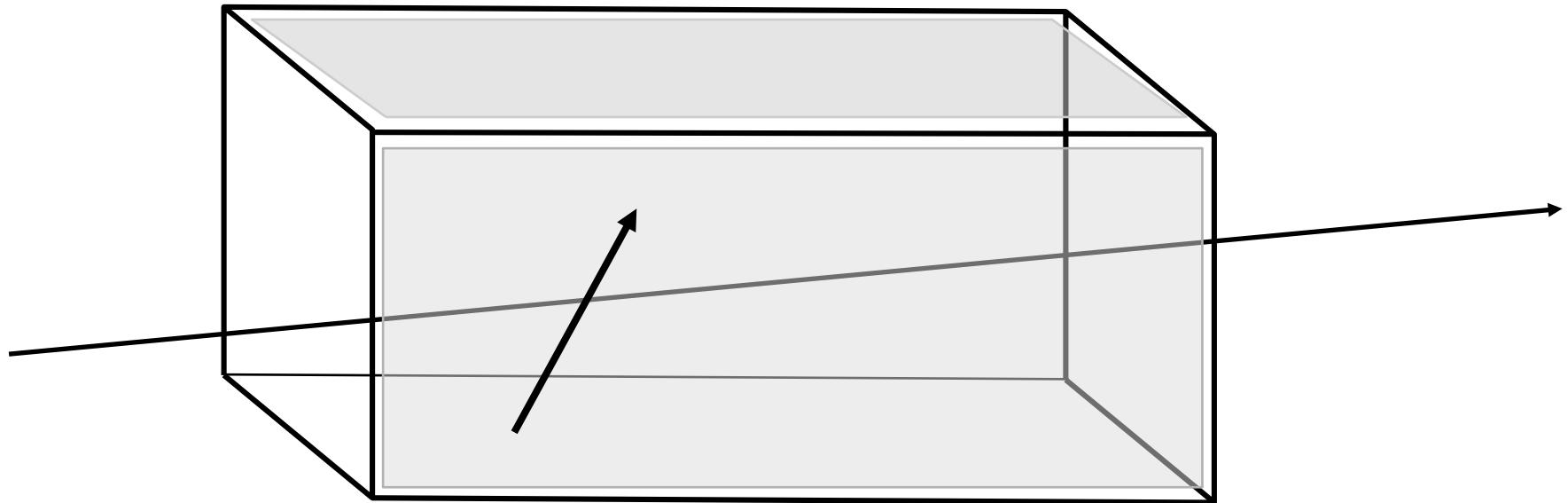


Pol_monitor

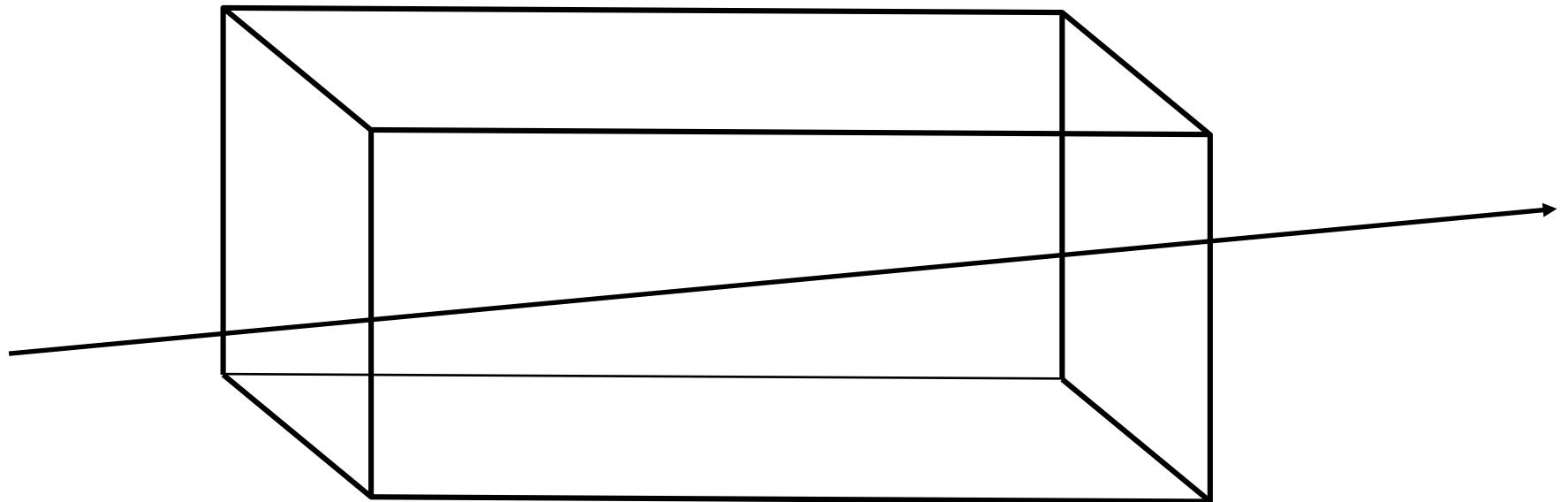
$$P \parallel (m_x, m_y, m_z) = 0.87$$



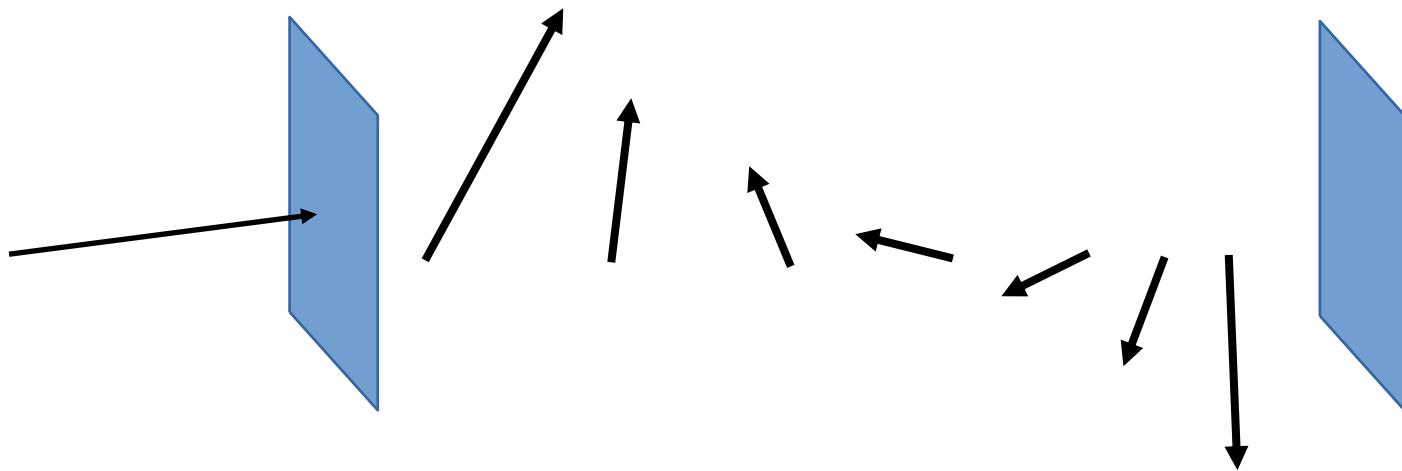
- **Pol_constBfield.comp**
- Single constant Magnetic field in a “box”.
- - user may specify a wavelength to flip.
 - blocking walls



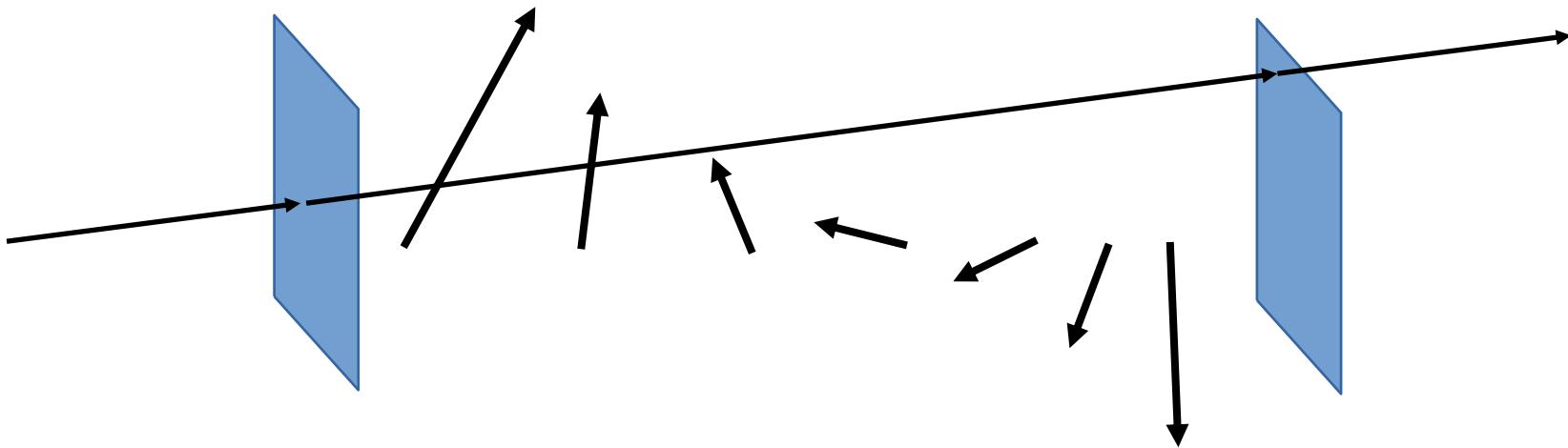
- **Pol_FieldBox.comp**
- Single Magnetic field in a “box”
- - optional user supplied field c-function



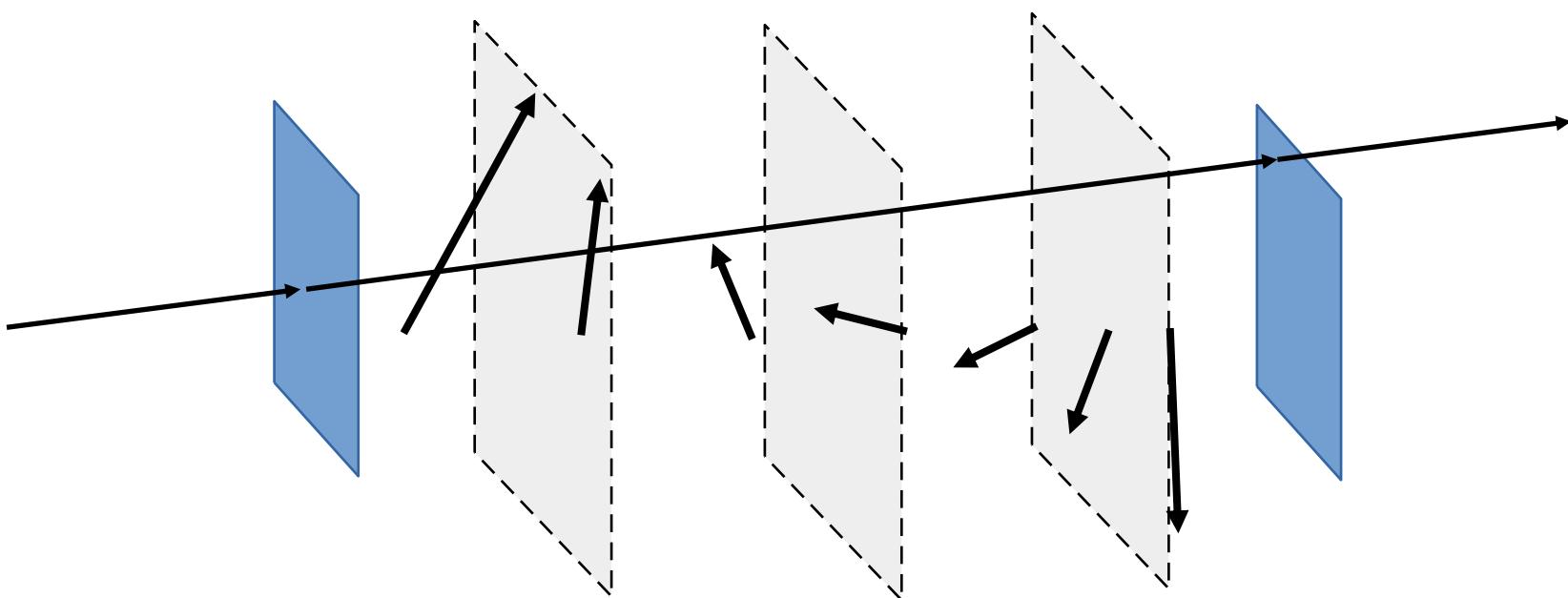
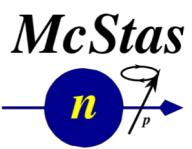
- `Pol_simpleBfield.comp`
- `Pol_simpleBfield_stop.comp`
 - - Entry/Exit construction allows for nested magnetic field descriptions.
 - - Any magnetic fields through user supplied c-function
 - - Tabled magnetic fields



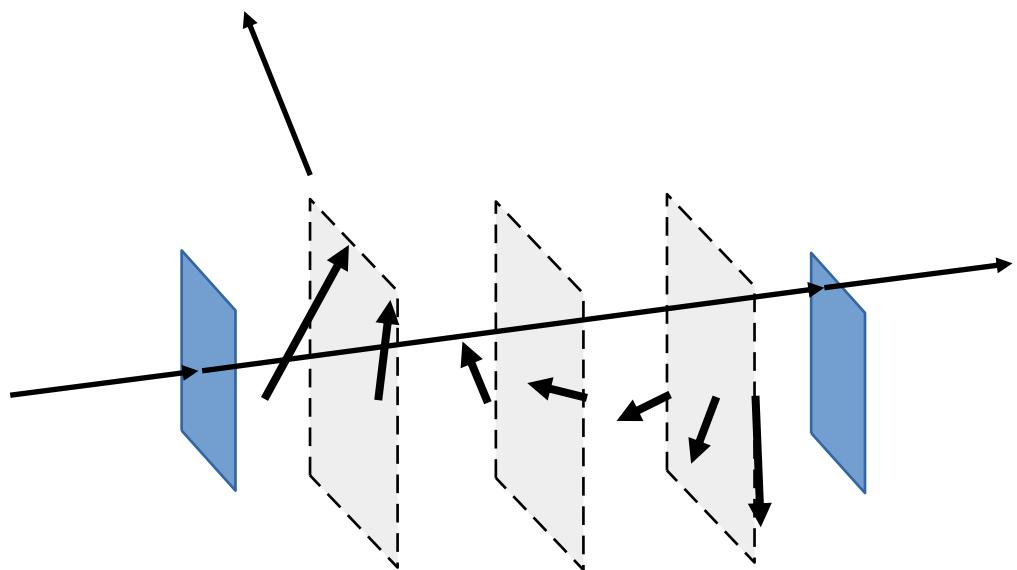
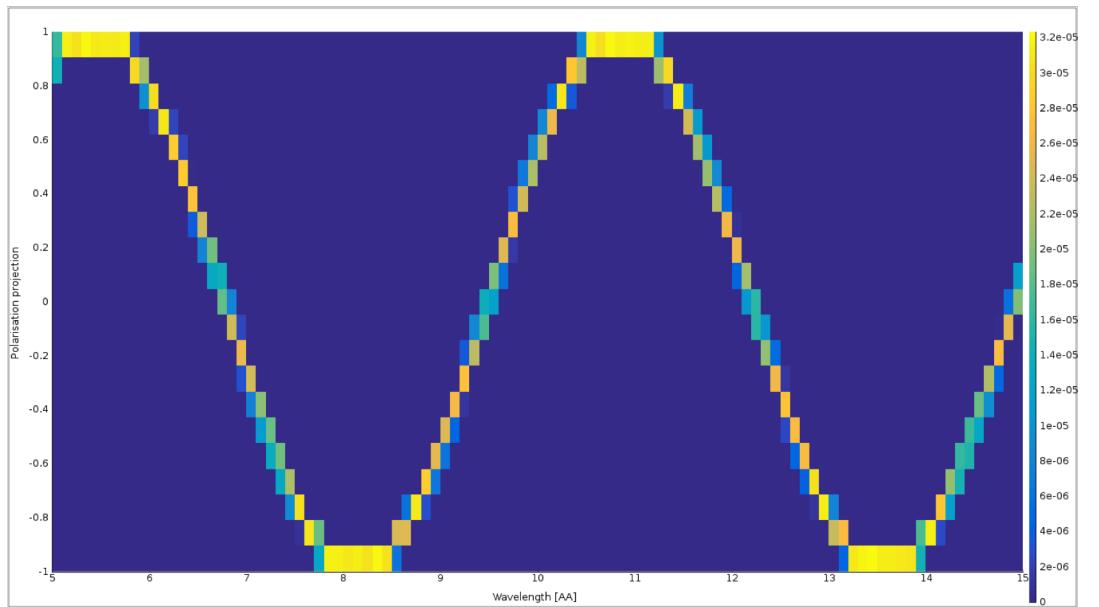
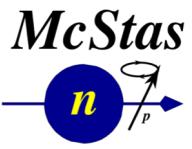
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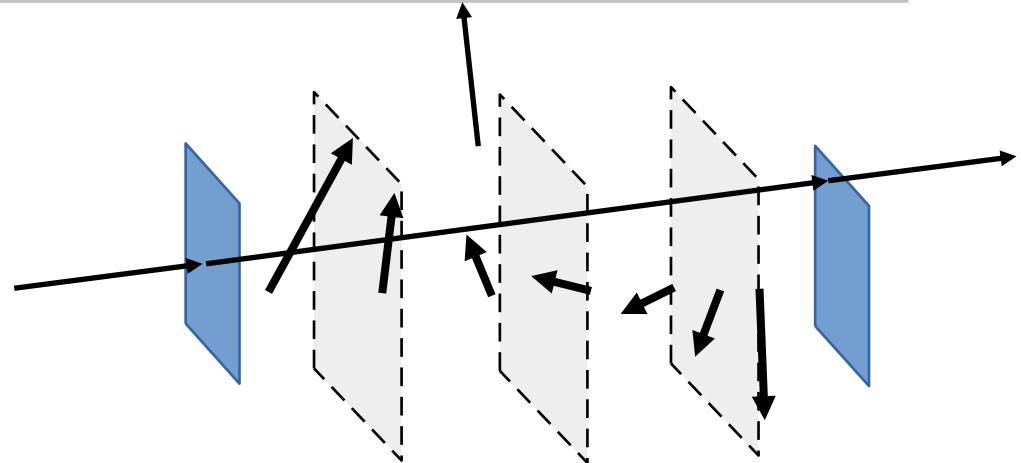
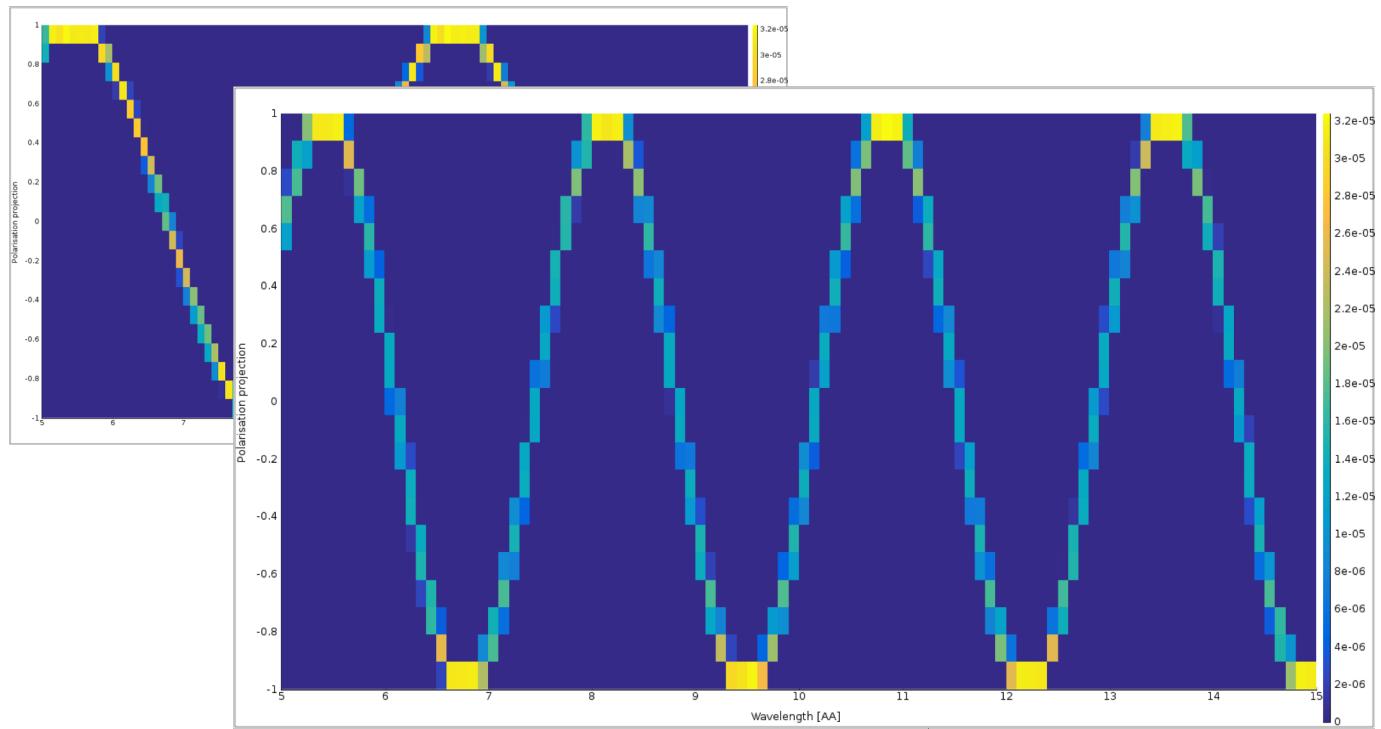
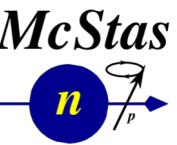
Pol_monitors along the way...



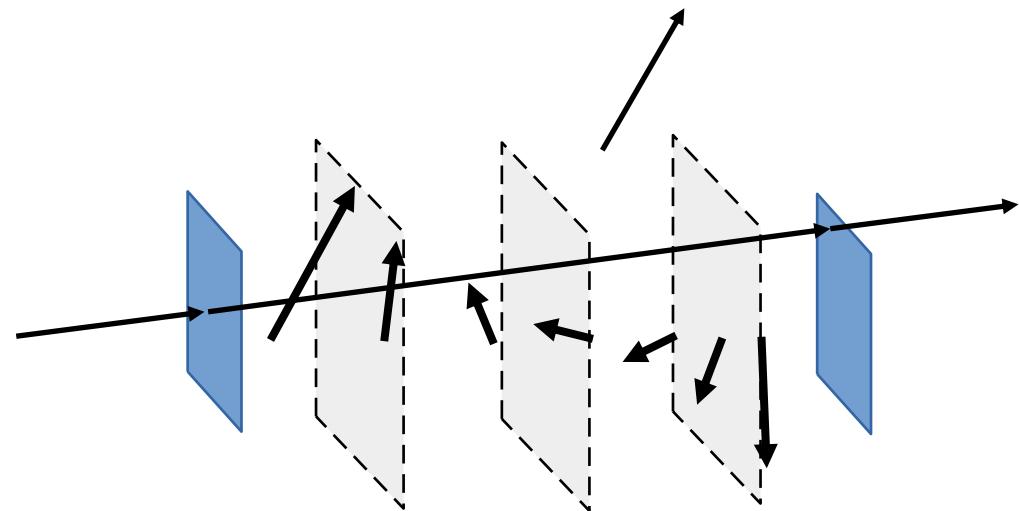
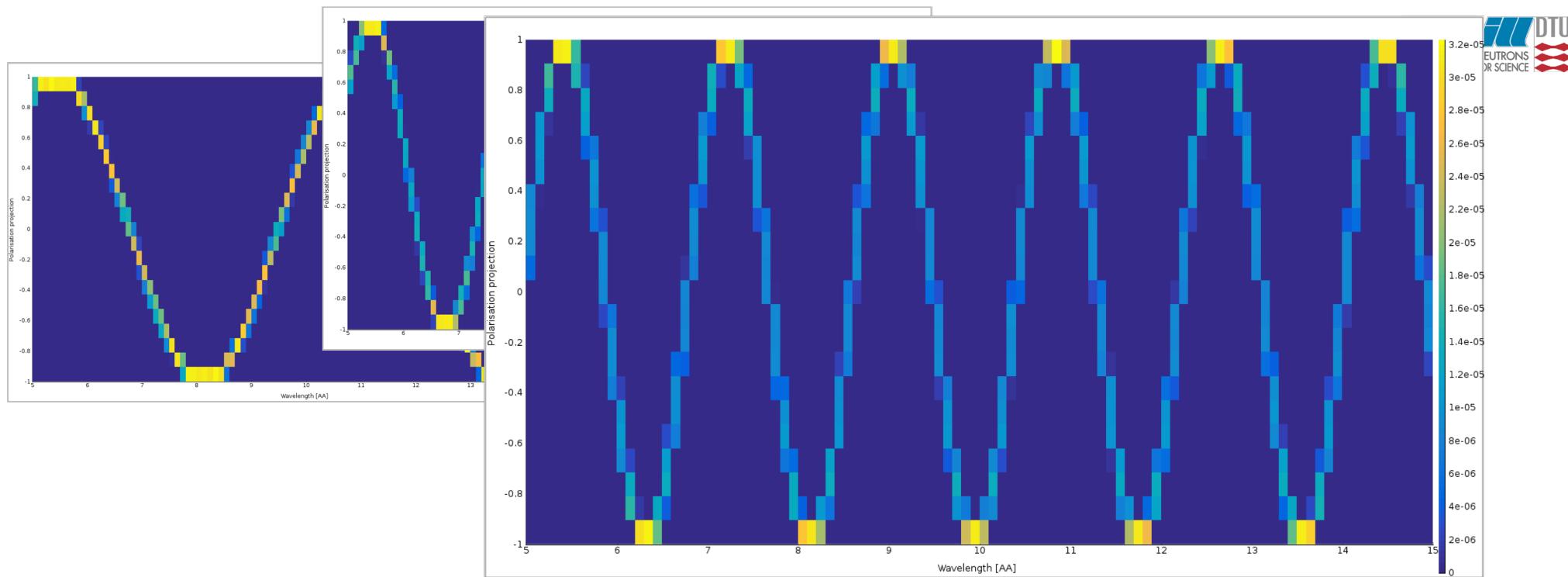
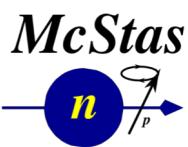
Pol_monitors along the way...



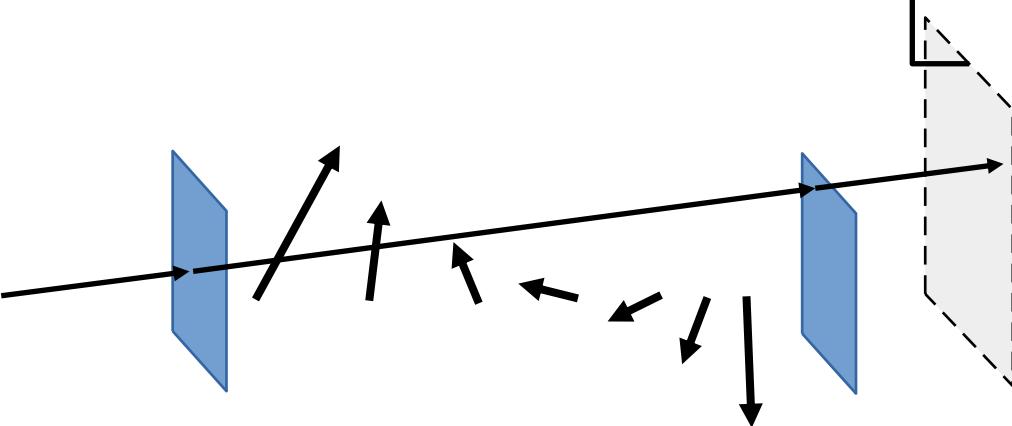
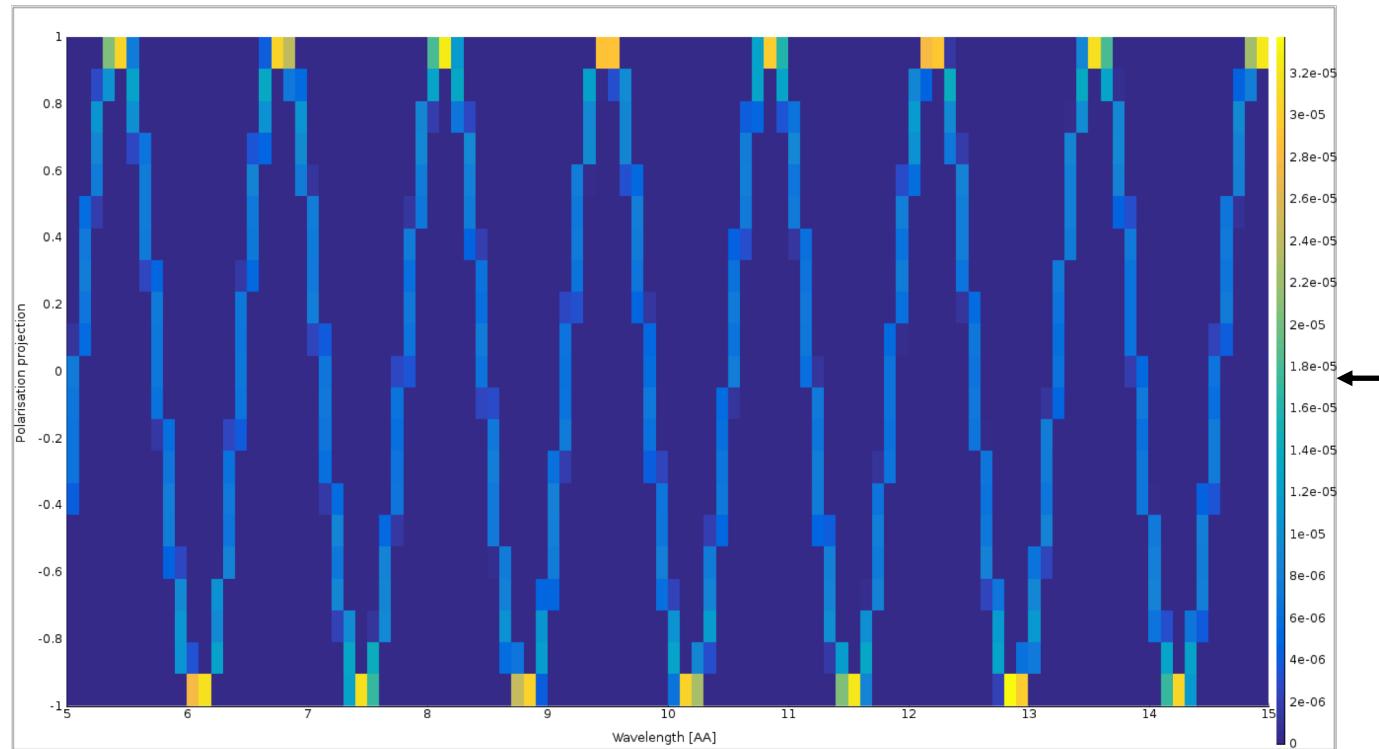
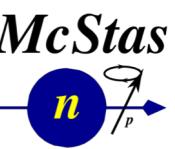
Pol_monitors along the way...



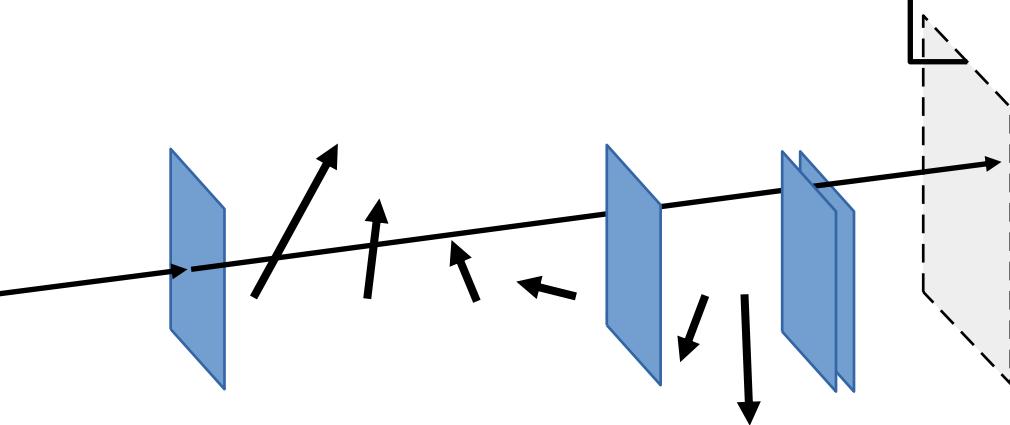
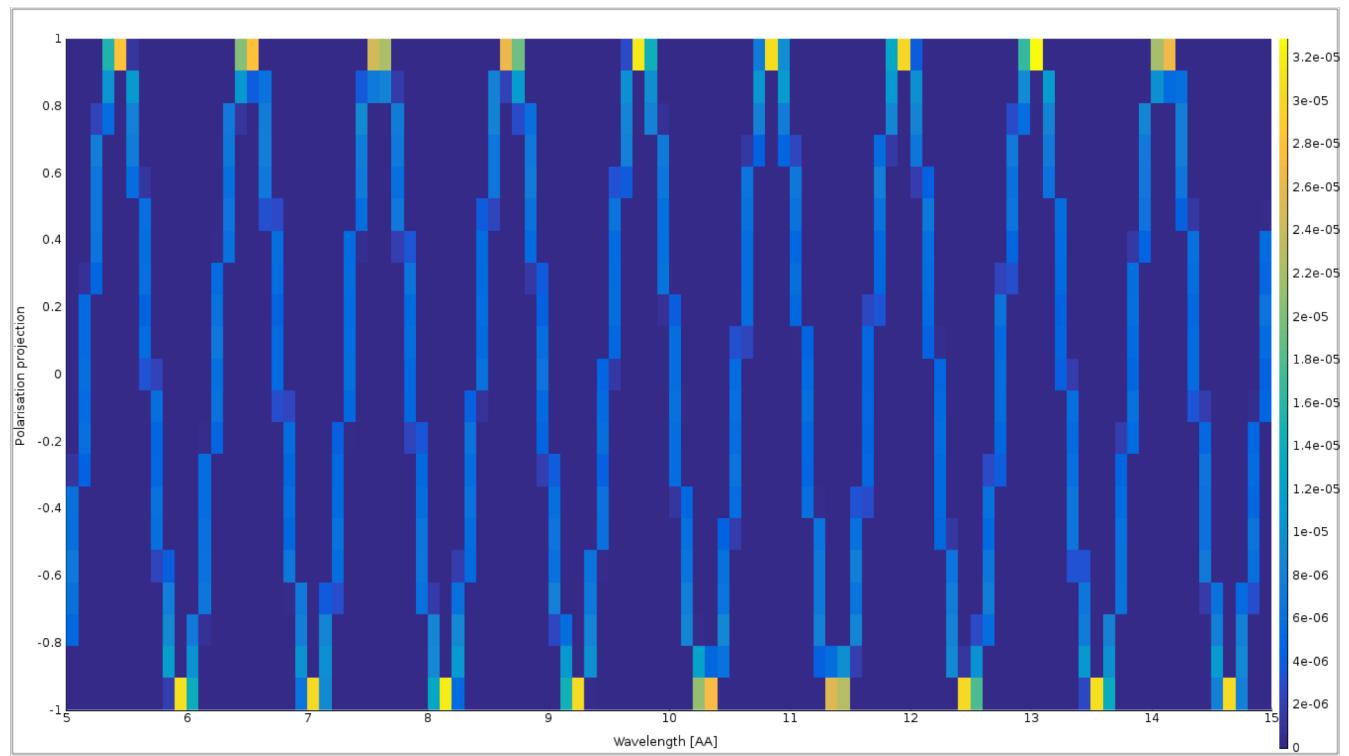
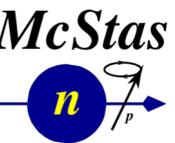
Pol_monitors along the way...



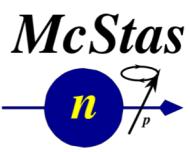
Nested fields



Nested fields



How does one go about it?



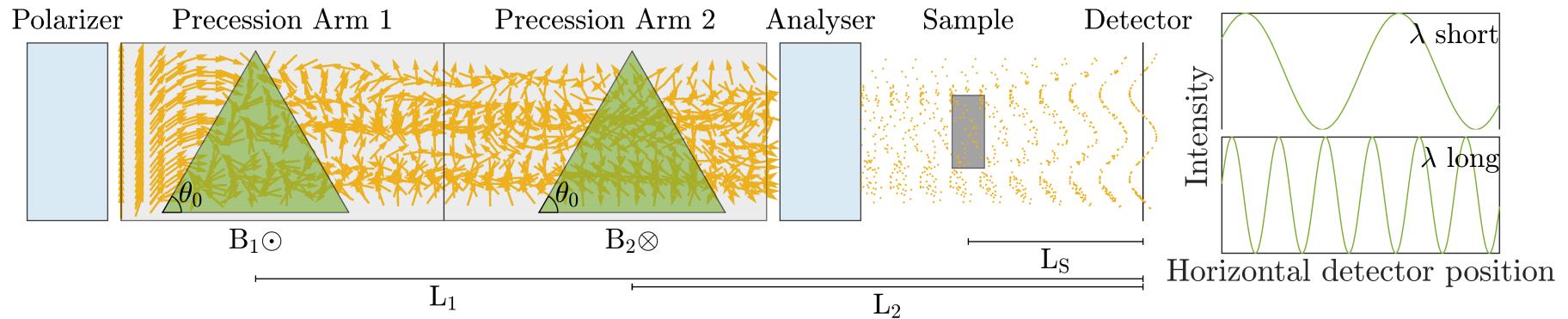
Example walk-through: SE-template

Example walk-through: SE-template

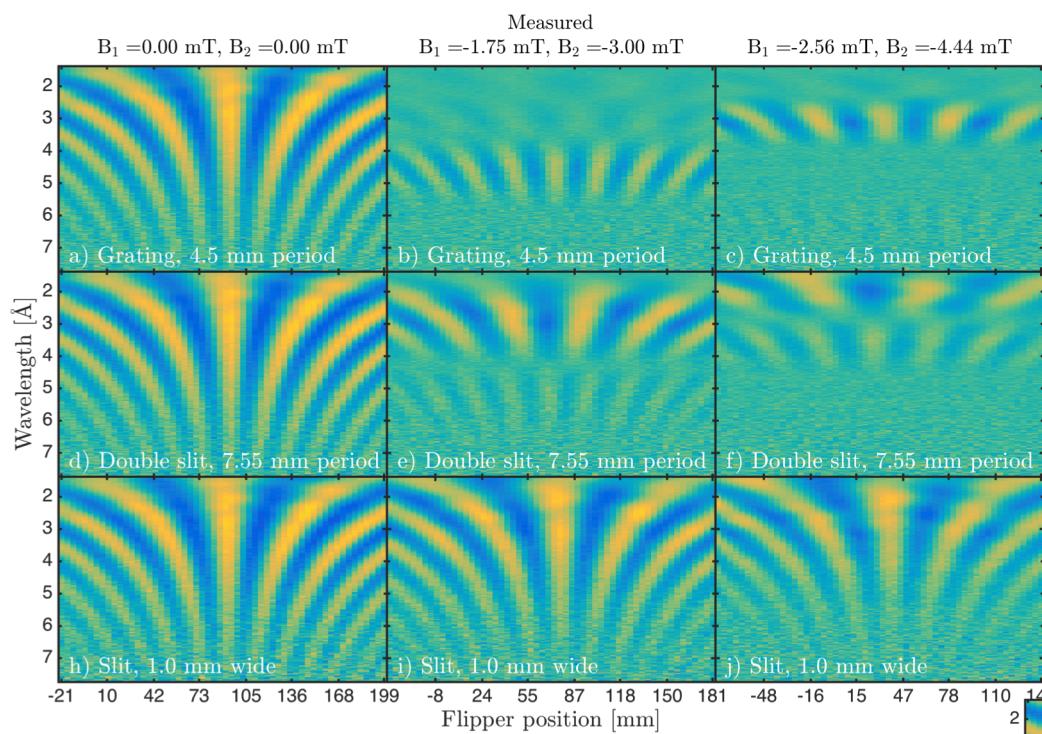


- ➊ Check example header.
- ➋ Use mcdoch
- ➌ Read/check the manual
- ➍ User mailing list: mcstas-users@mcstas.org
- ➎ Give us a call/write us an email!

Courtesy: M. Sales et.al.

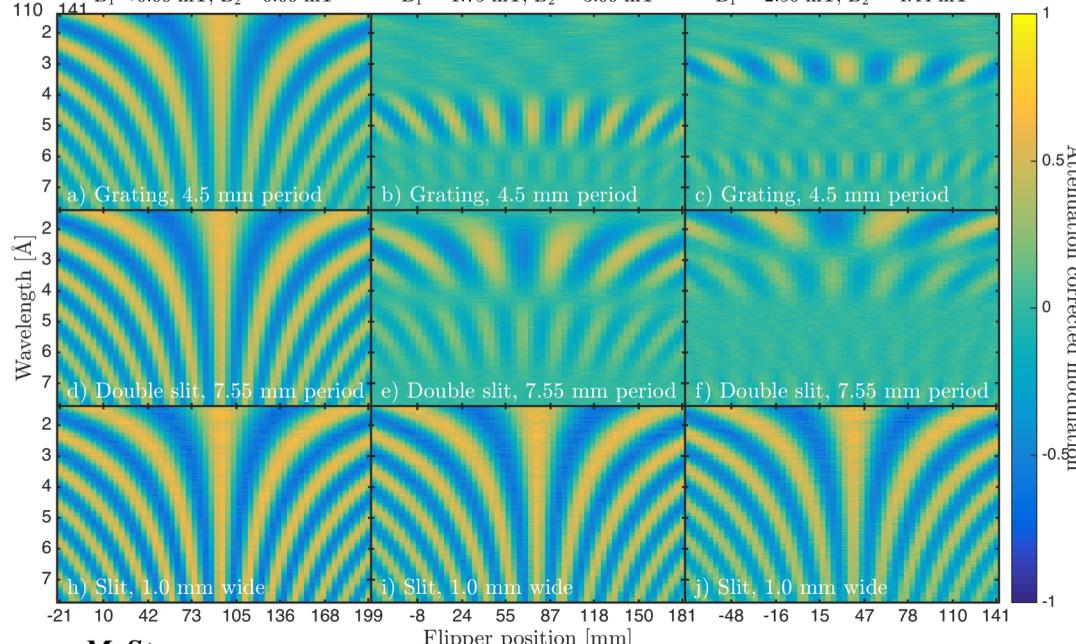
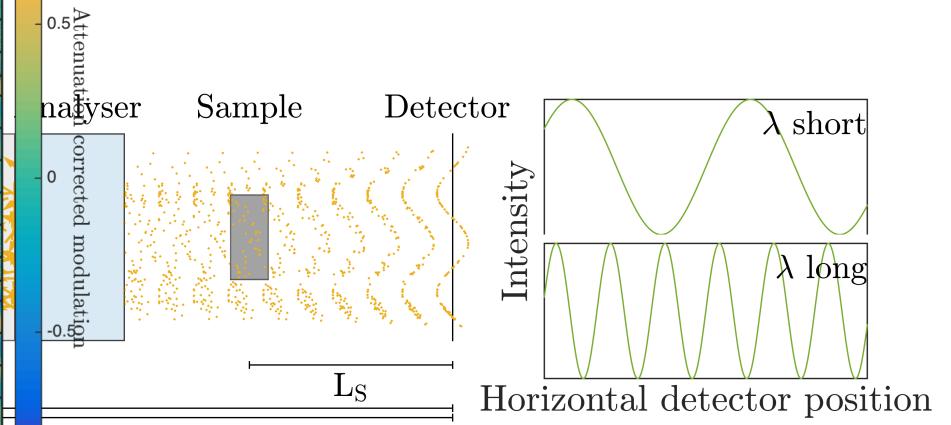


McStas example SEMSANS

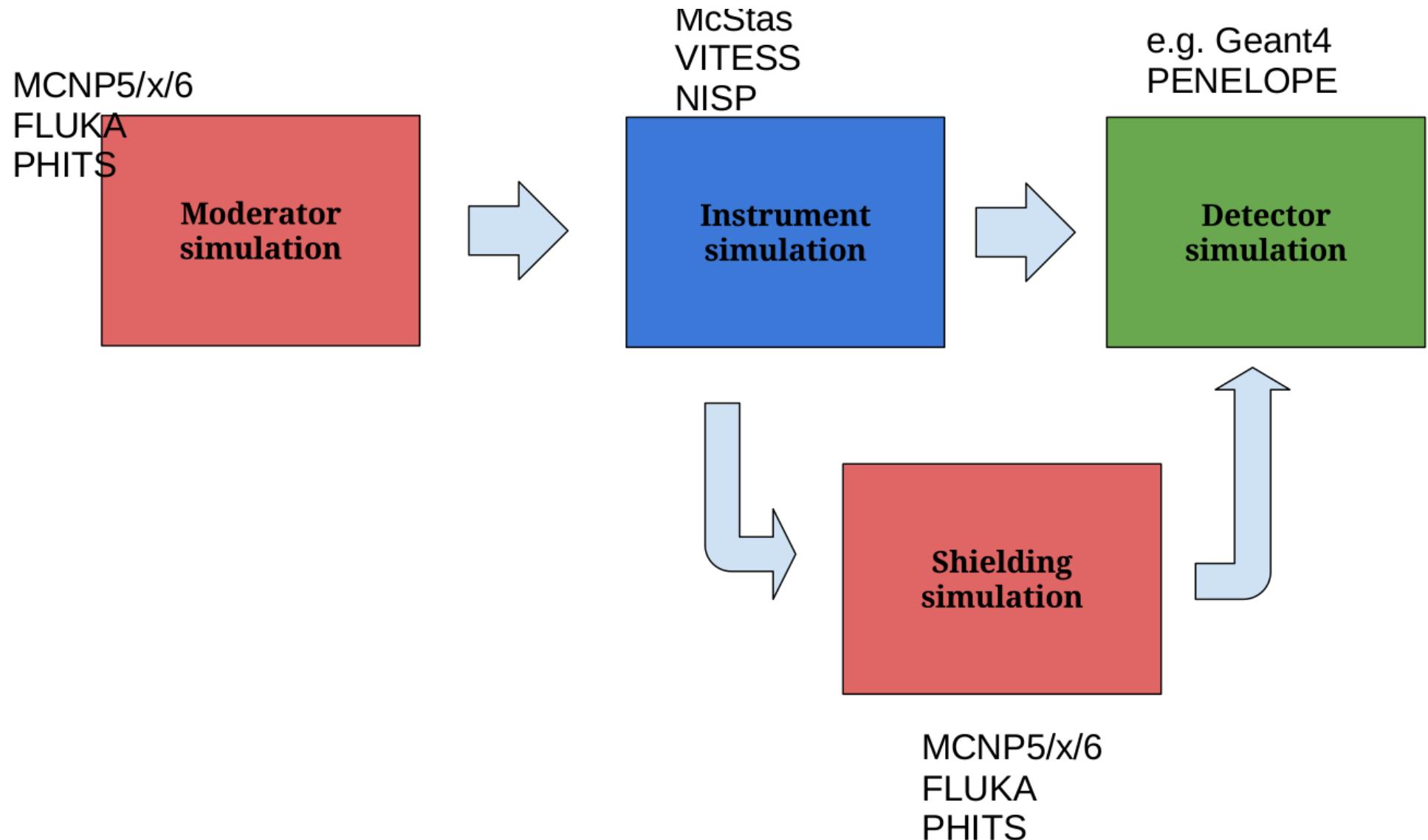


1
0.5
0
-0.5
-1

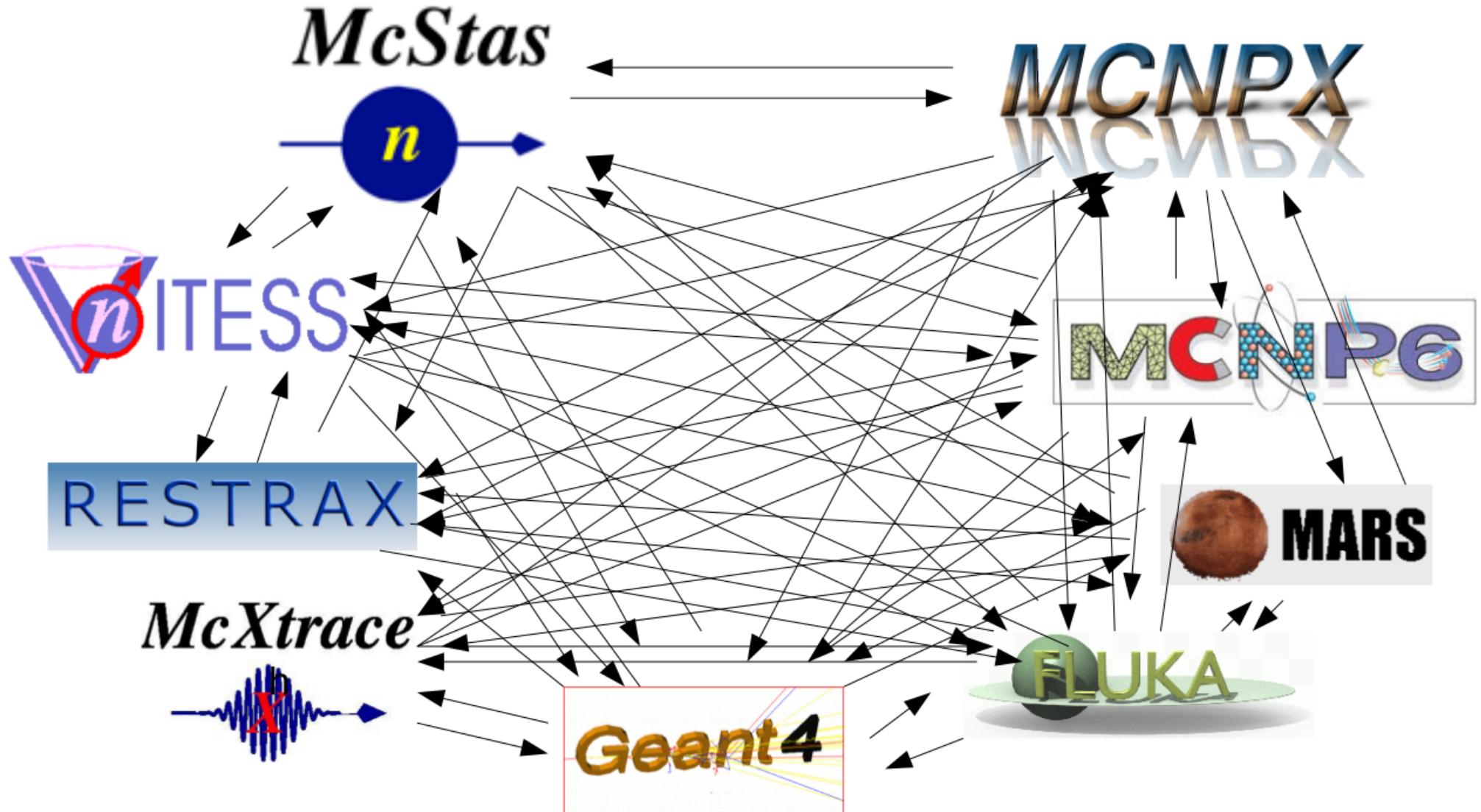
Attenuation corrected modulation



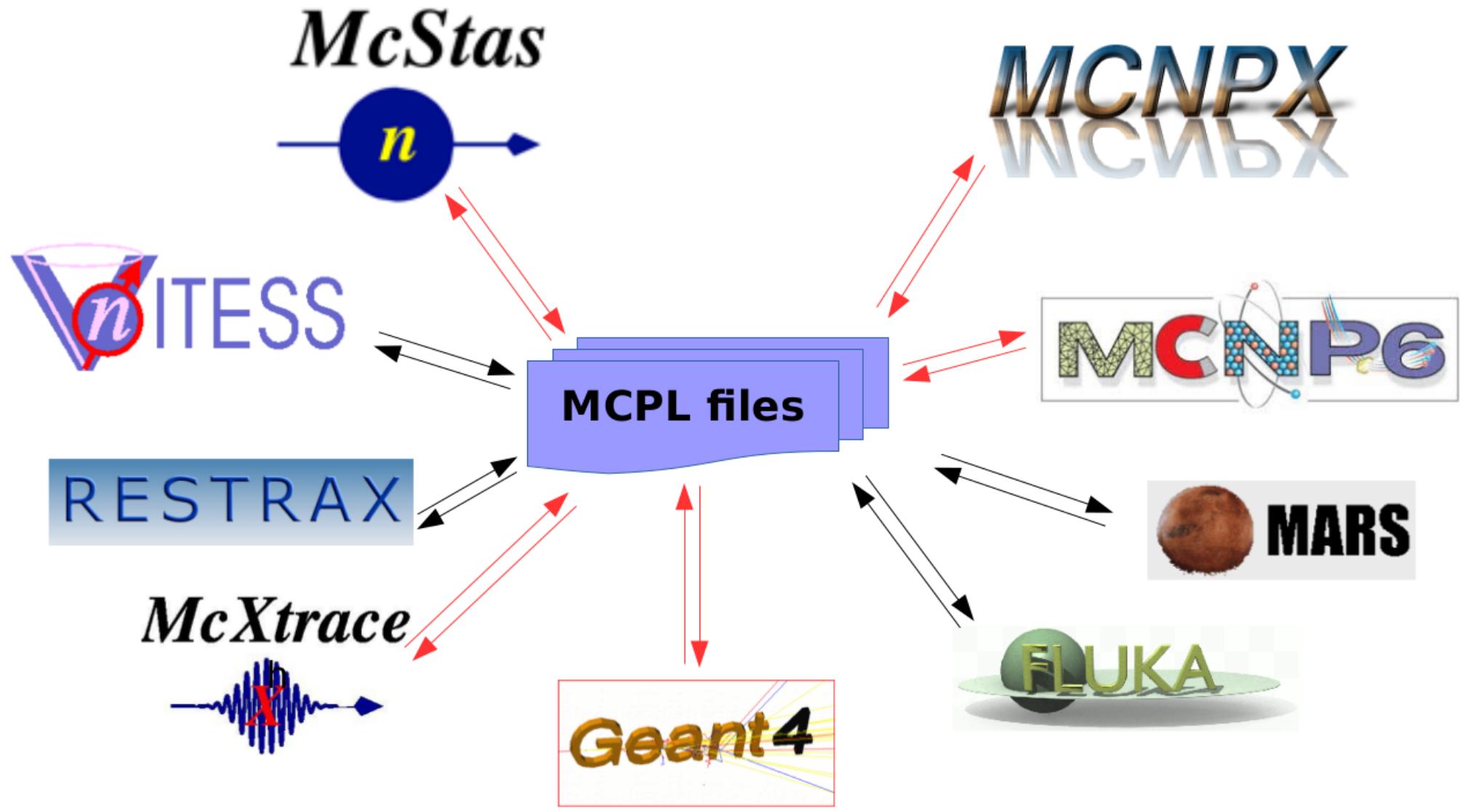
A goal: real sims with background



The problem



The solution



Things on the way

Magnetic fields:

- `Pol_FieldBox.comp`
 - Tabled fields
- `Pol_constBfield.comp`
- `Pol_simpleBfield.comp`
 - 3D entry/exit windows
- `Pol_simpleBfield_stop.comp`
- `Pol_triafield.comp`

Optics:

- `Monochromator_pol.comp`
- `Pol_bender.comp`
- `Pol_guide_vmirror.comp`
- `Pol_mirror.comp`
- `Pol_pi_2_rotator.comp`
- `Transmission_polarisatorABSnT.comp`
- `Pol_bender_tapering.comp`
- `Pol_McRadia.comp`
 - Dynamic coupling to RADIA

Monitors:

- `Pol_monitor.comp`
- `MeanPolLambda_monitor.comp`
- `PolLambda_monitor.comp`
- `Pol_PSD_monitor.comp`

Idealized components:

- `PolAnalyser_ideal.comp`
- `Set_pol.comp`
- `Pol_SF_ideal.comp`

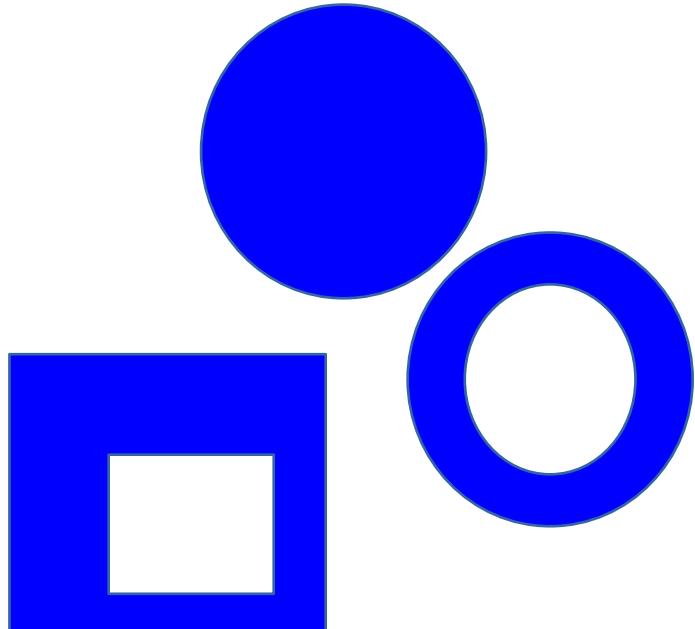
Contrib:

- `Foil_flipper_magnet.comp`

Sample component

- `Magnetic_single_crystal.comp`

Generalized Simple B-Fields: constant, functional, tabled, ... but in more general shapes

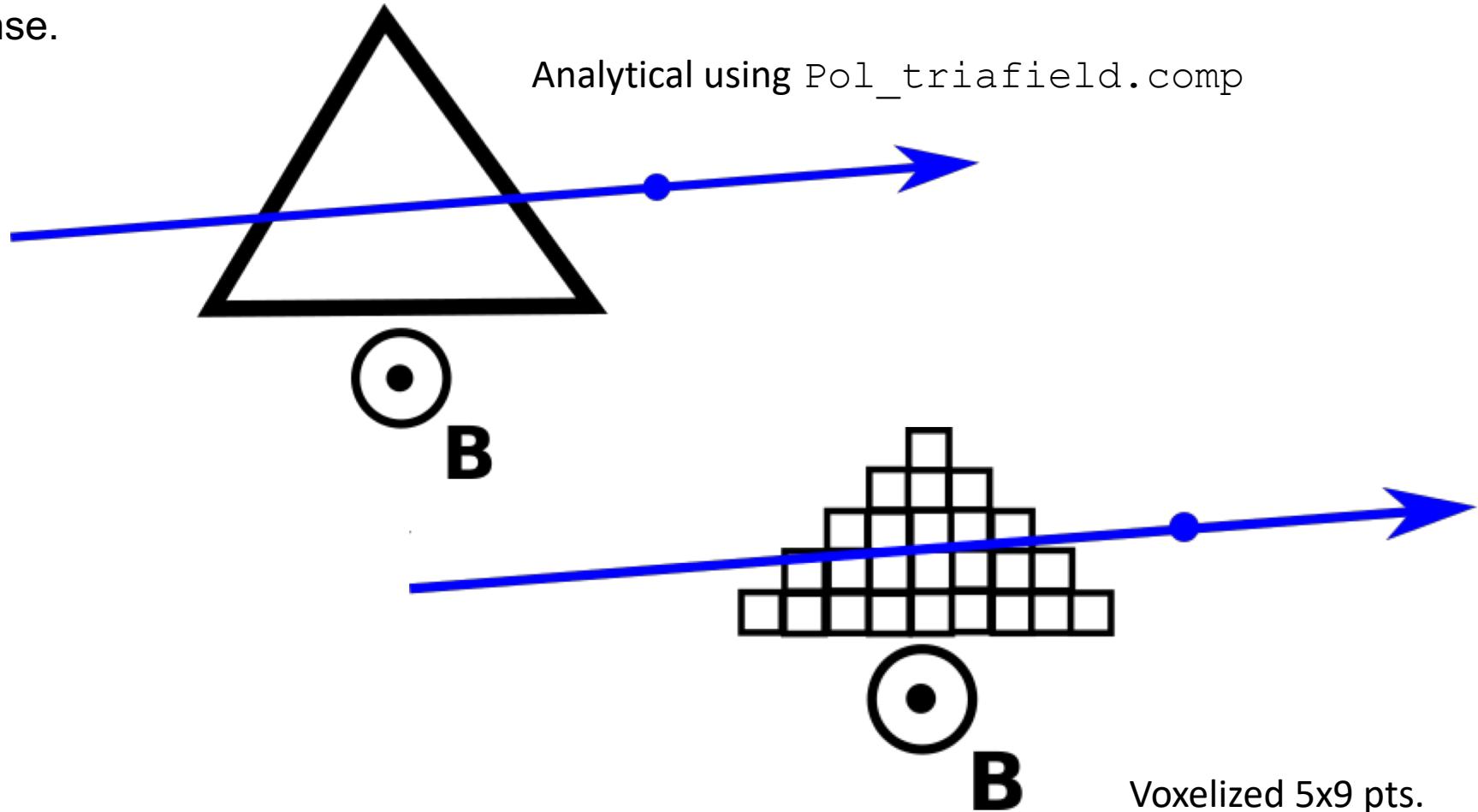


RF-flipper

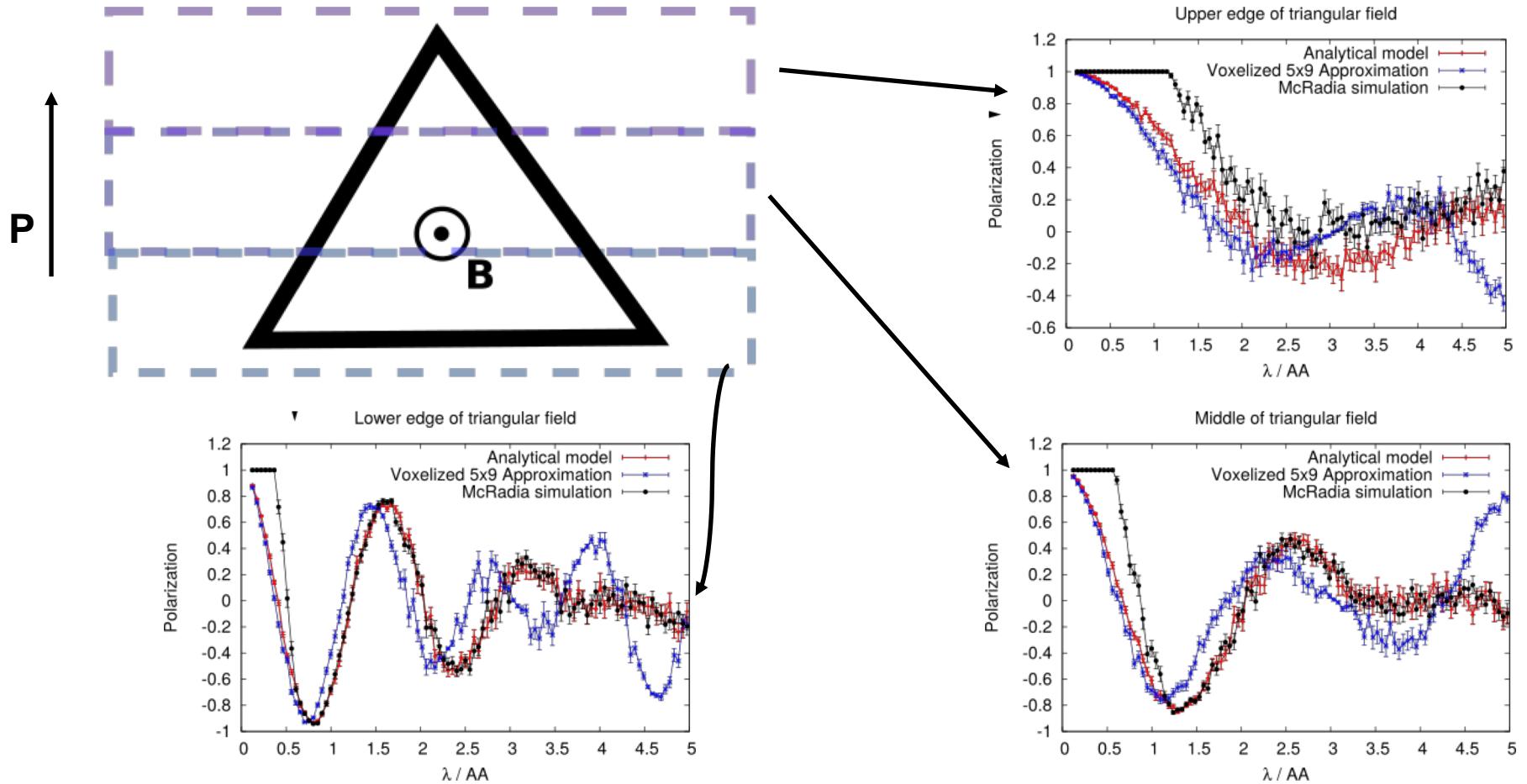
He3-objects

McRadia compared with analytical field description

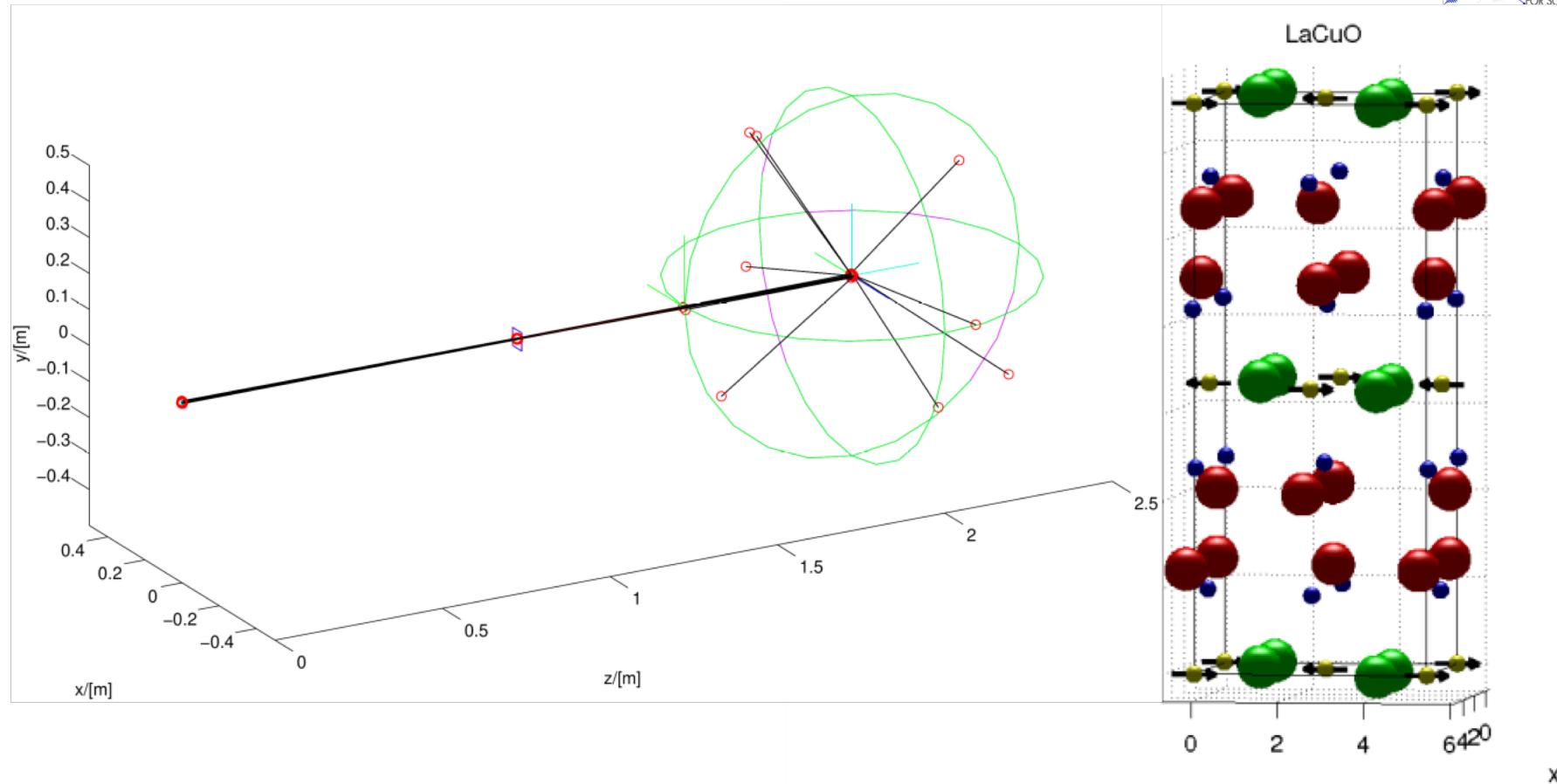
Requires a mathematica license.



McRadia compared with other field descriptions



Magnetic single crystal

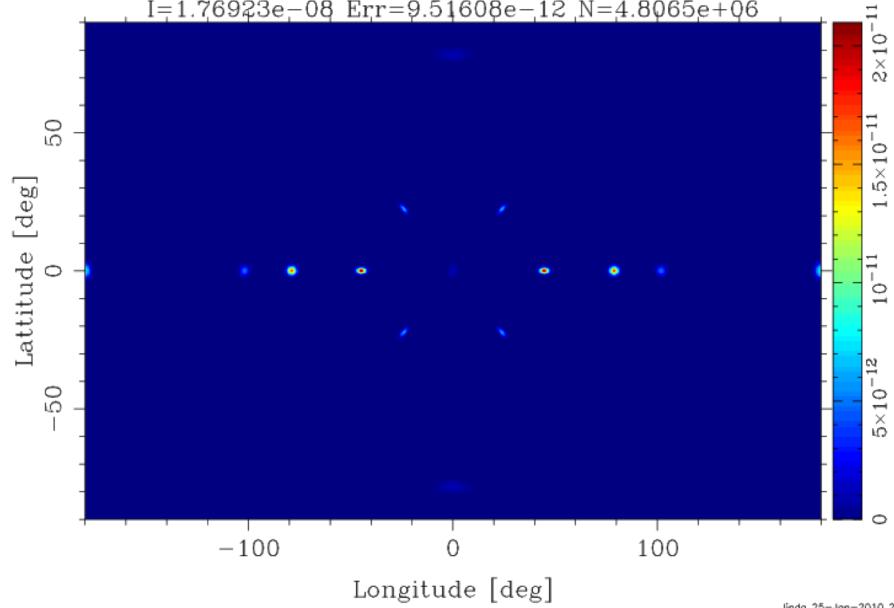


index	iontype	x	y	z	$b_{coh}[\text{fm}]$	g_s	S_x	S_y	S_z	g_L	L_x	L_y	L_z
1	Cu2+	0.5	0.5	0	7.718	2	0	-0.5	0	0	0	0	0
:	:	:	:	:	:	:	:	:	:	:	:	:	:

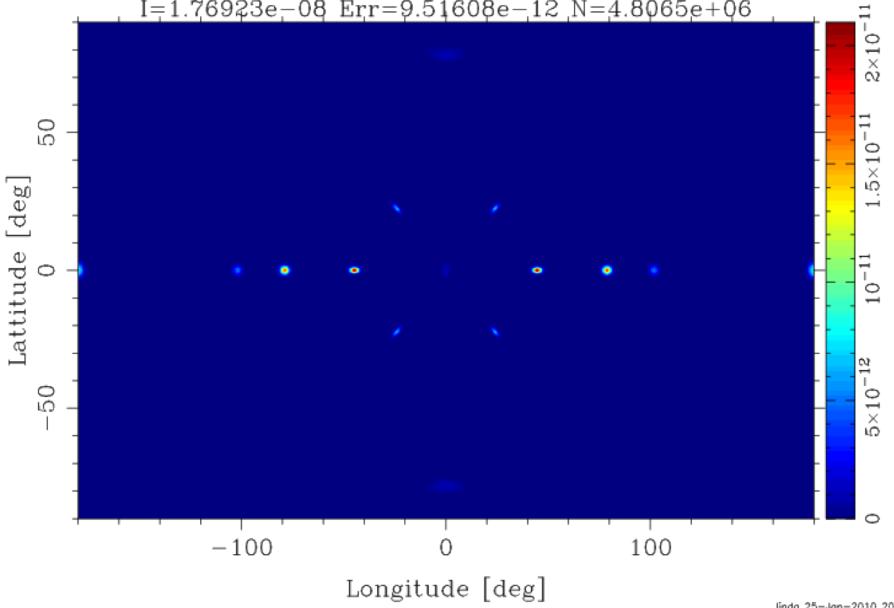
Magnetic single crystal – Unpolarized beam



4PImon_spinup [250110_SF_NSF_PX0_PY0_PZ0_1e10/PSD4PImon_spinup.
 X0=-0.104202; dX=88.4169; Y0=0.105552; dY=25.2284;
 I=1.76923e-08 Err=9.51608e-12 N=4.8065e+06]



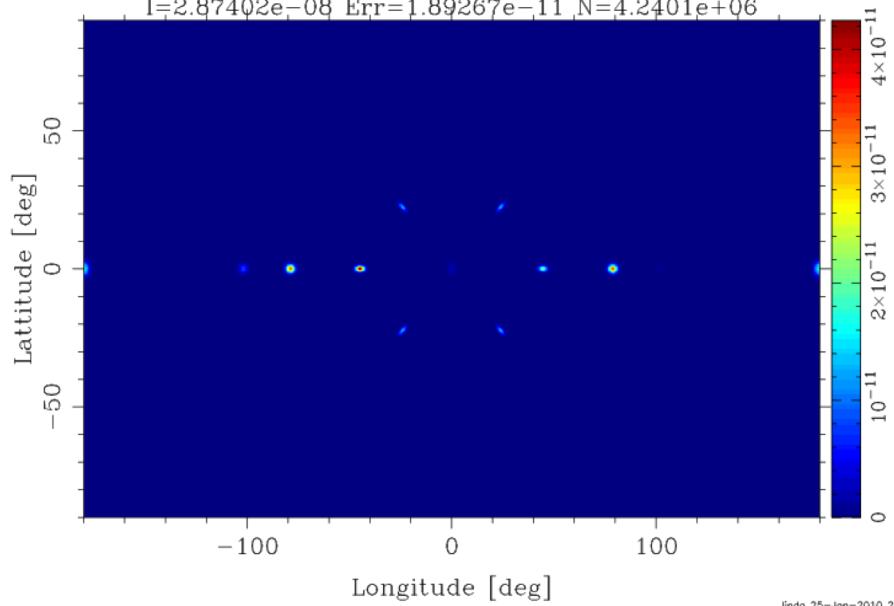
[mon_spindown [250110_SF_NSF_PX0_PY0_PZ0_1e10/PSD4PImon_spindow
 X0=-0.104202; dX=88.4169; Y0=0.105552; dY=25.2284;
 I=1.76923e-08 Err=9.51608e-12 N=4.8065e+06]



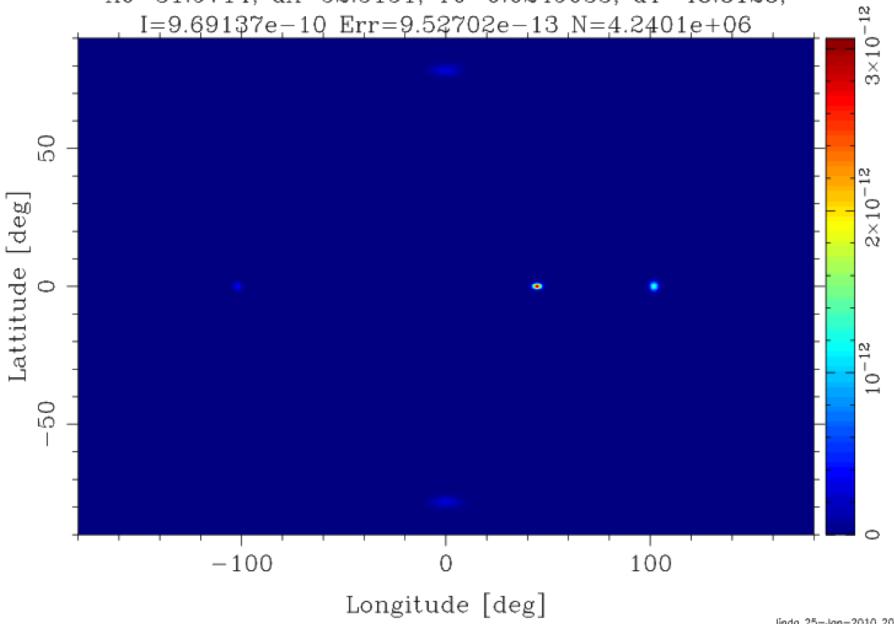
Magnetic single crystal – Polarized beam



n_spinup [250110_SF_NSF_PX-0.3800_PY0_PZ0.9249_1e10/PSD4Plmon_s]
 X0=-7.4526; dX=93.2595; Y0=0.0952368; dY=15.1242;
 I=2.87402e-08 Err=1.89267e-11 N=4.2401e+06



spindown [250110_SF_NSF_PX-0.3800_PY0_PZ0.9249_1e10/PSD4Plmon_s]
 X0=31.9714; dX=52.5151; Y0=0.0249033; dY=48.8128;
 I=9.69137e-10 Err=9.52702e-13 N=4.2401e+06



Magnetic single crystal



The magnetic scattering cross-section for a sample with localised spin+orbital angular moment $g\mathbf{J} = (g_S + g_L)\mathbf{J} = 2\mathbf{S} + \mathbf{L}$ is:

$$\frac{d^2\sigma}{d\Omega_f dE_f} = \frac{k_f}{k_i} \sum_{i,f} P(\lambda_i) \left| \langle \lambda_f | \sum_j e^{i\mathbf{Q}\cdot\mathbf{d}_j} U_j^{\sigma_i \sigma_f} | \lambda_i \rangle \right|^2 \delta(\hbar\omega + E_i - E_f)$$

where $|\lambda_i\rangle$ and $\langle\lambda_f|$ are the initial and final states of the sample with energies E_i and E_f respectively, $P(\lambda_i)$ is the distribution of initial states and

$$U_j^{\sigma_i \sigma_f} = \langle \sigma_f | b_j - m_j \mathbf{J}_{\perp j} \cdot \boldsymbol{\sigma} | \sigma_i \rangle$$

where $|\sigma_i\rangle$ and $\langle\sigma_f|$ are the initial and final spin states of the neutron, and $\boldsymbol{\sigma}$ are the Pauli spin matrices working on the neutron state.

From: G. Shirane et.al., "Neutron Scattering with Triple-Axis Spectrometer", Cambridge Univ. Press, 2002

Magnetic single crystal



If $\mathbf{P} = P(\xi, \eta, \zeta) = P\hat{\zeta}$. Thus, the matrix elements of $U^{\sigma_i \sigma_f}$ can now be written

$$\begin{aligned} U^{++} &= b - mJ_{\perp\zeta} \\ U^{--} &= b + mJ_{\perp\zeta} \\ U^{+-} &= -m(J_{\perp\xi} + iJ_{\perp\eta}) \\ U^{+-} &= -m(J_{\perp\xi} - iJ_{\perp\eta}) \end{aligned}$$

where $m = \frac{r_0\gamma}{2}gf(\mathbf{Q})$ with r_0 the classical electron radius, $\gamma = 1.913$, g the Landé splitting factor and $f(\mathbf{Q})$ the magnetic form factor of a particular ion in the sample.

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➊ How can we interact better?

- * Better support for the community?
- * Code-sharing?