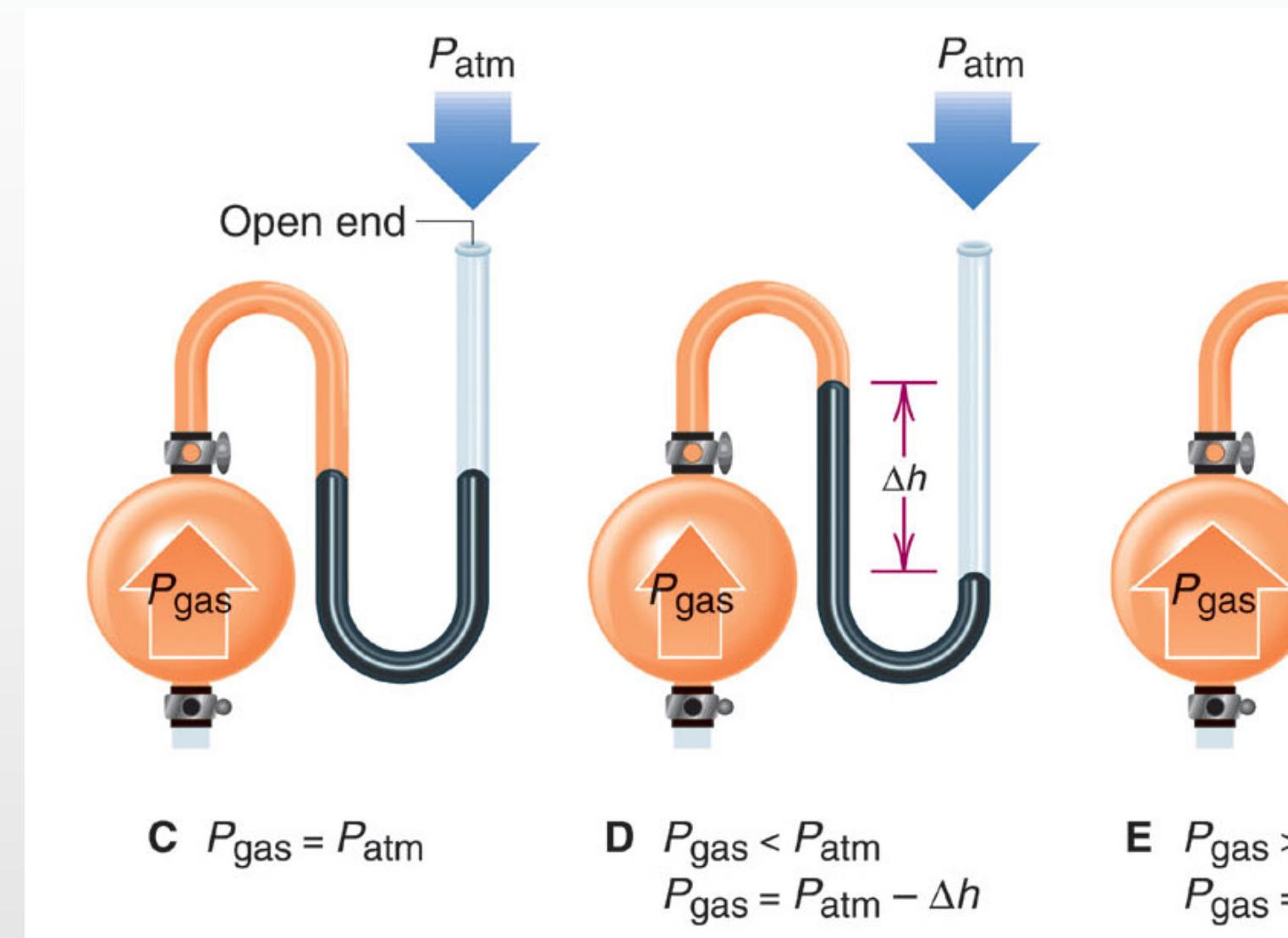
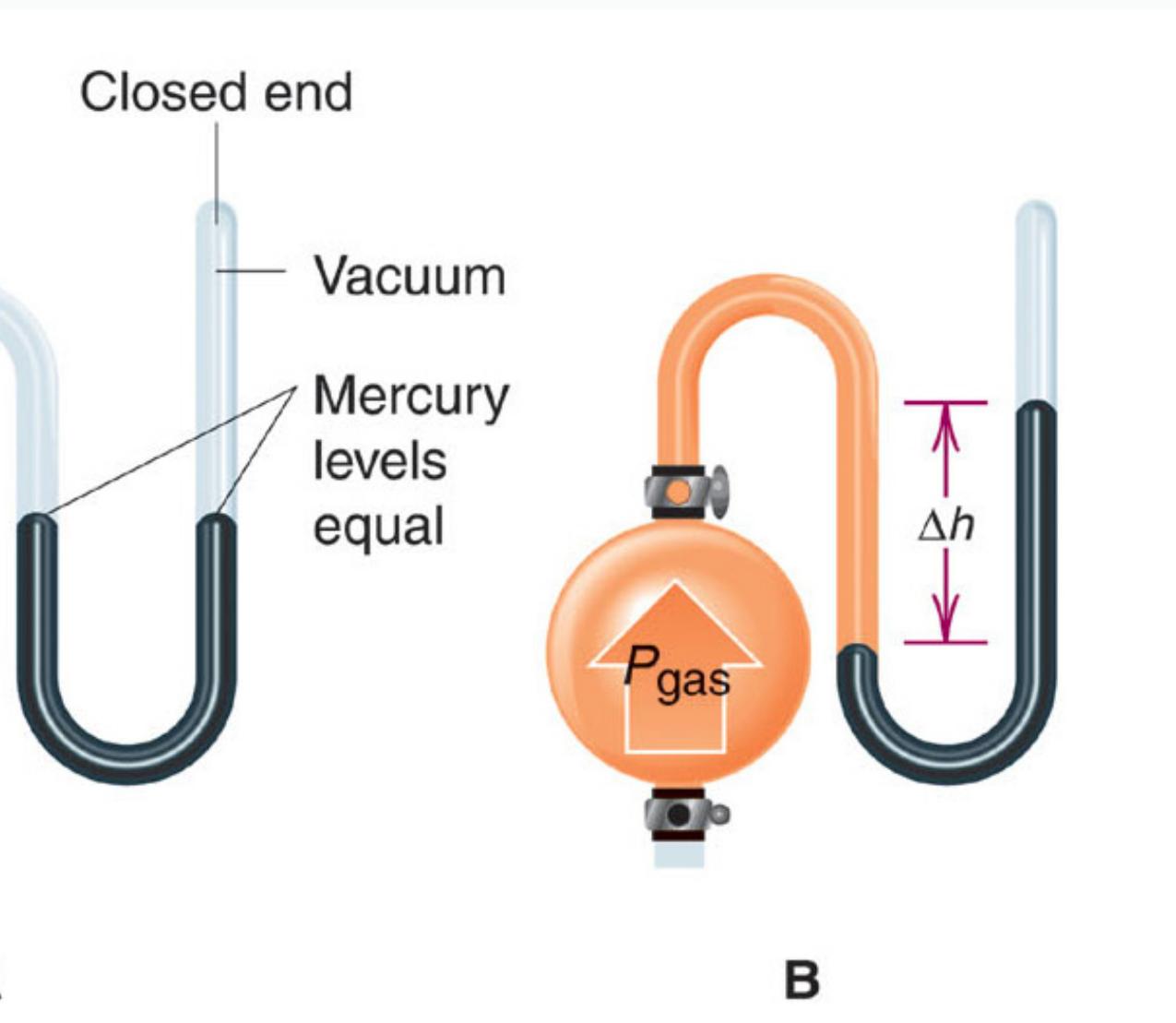


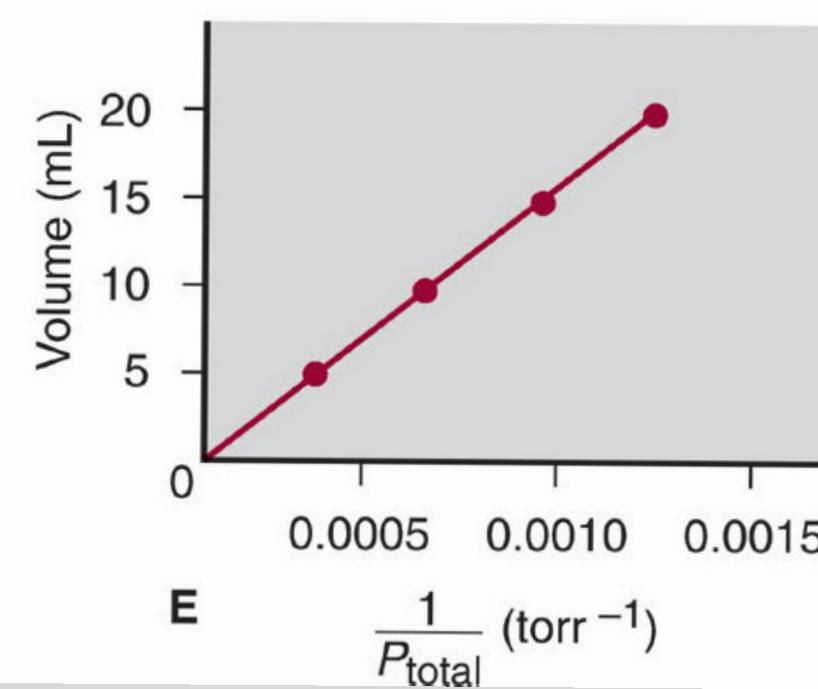
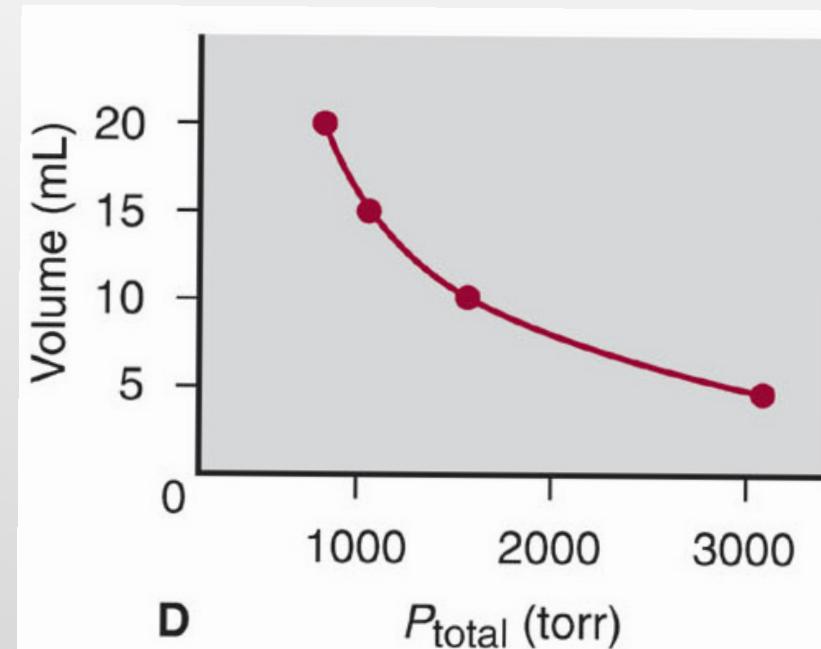
Manometer



Closed End Manometer

Open End Manometer

Relationship between Volume and Pressure: Boyle's Law



Boyle's Law: $V \propto \frac{1}{P}$ (constant T and n)
 $P \cdot V = \text{constant}$

Boyle's Law

A cylinder with a movable piston has a volume of 5.75 L under an applied pressure of 3.60 atm. What is the pressure in Pa when the piston is expanded to 7.60 L?

$$P_1 = 3.60 \text{ atm} \quad P_2 = ?$$

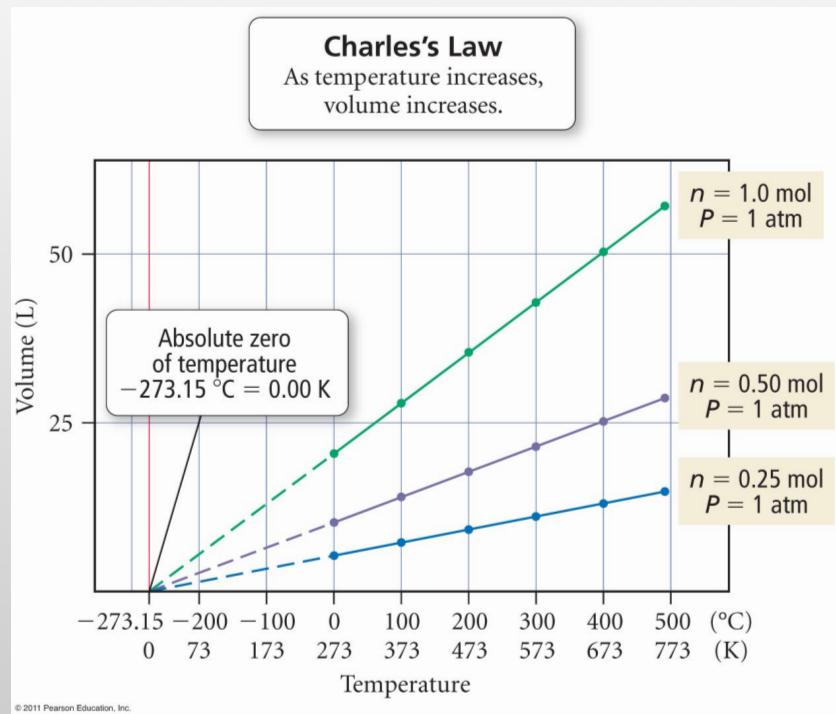
$$V_1 = 5.75 \text{ L} \quad V_2 = 7.60 \text{ L}$$

$$P_1 V_1 = P_2 V_2 \quad P_2 = \frac{P_1 V_1}{V_2}$$

$$P_2 = 3.60 \text{ atm} \cdot \frac{5.75 \text{ L}}{7.60 \text{ L}} = 2.72 \text{ atm}$$

$$P_2 = 2.72 \text{ atm} \cdot \frac{101325 \text{ Pa}}{1 \text{ atm}} = 275977 \text{ Pa} \\ = 276 \text{ kPa}$$

Relationship between Volume and Temperature: Charles's Law



Charles's Law: $V \propto T$ (constant P and n)

$$V = \text{constant} \cdot T$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

Charles Law

$$V \propto T$$

$$\frac{V}{T} = \text{const.}$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

For all gas calc., the temp. has to be expressed in Kelvin

A sample of gas has a volume of 3.10L at 20°C. What is the volume at -57°C?

$$T_1 = 20^\circ\text{C} + 273.15\text{K} = 293.15\text{K} = 293\text{K}$$

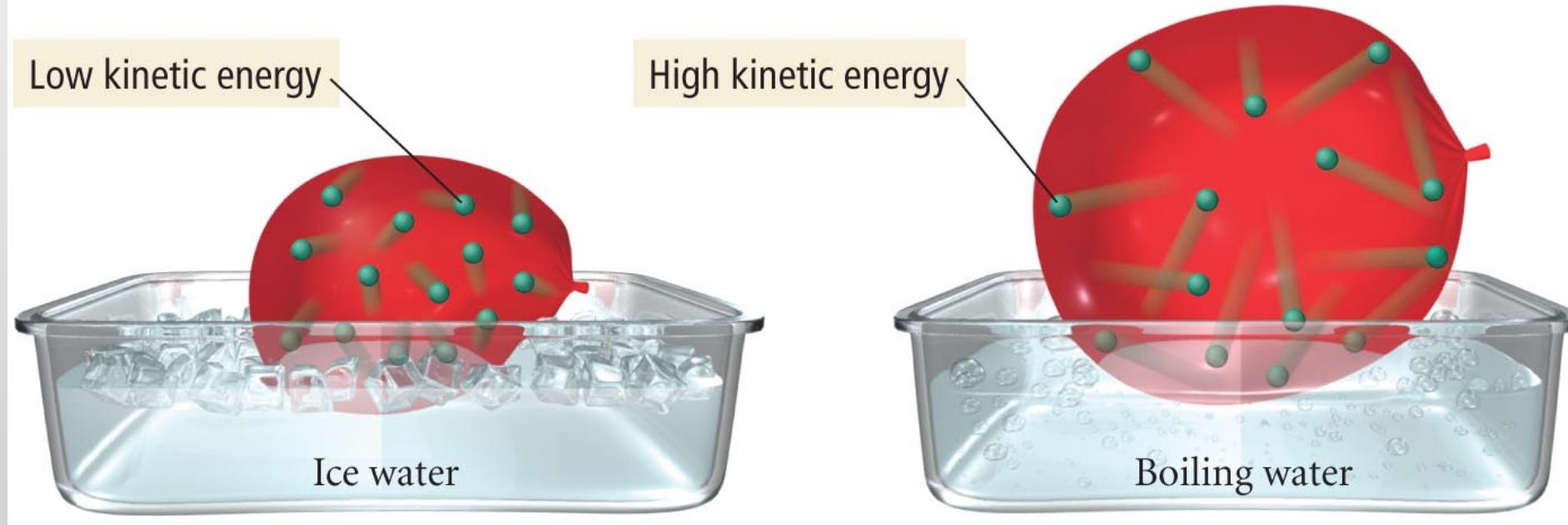
$$T_2 = -57^\circ\text{C} + 273 = 216\text{K}$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2} \Rightarrow V_2 = \frac{T_2}{T_1} V_1$$

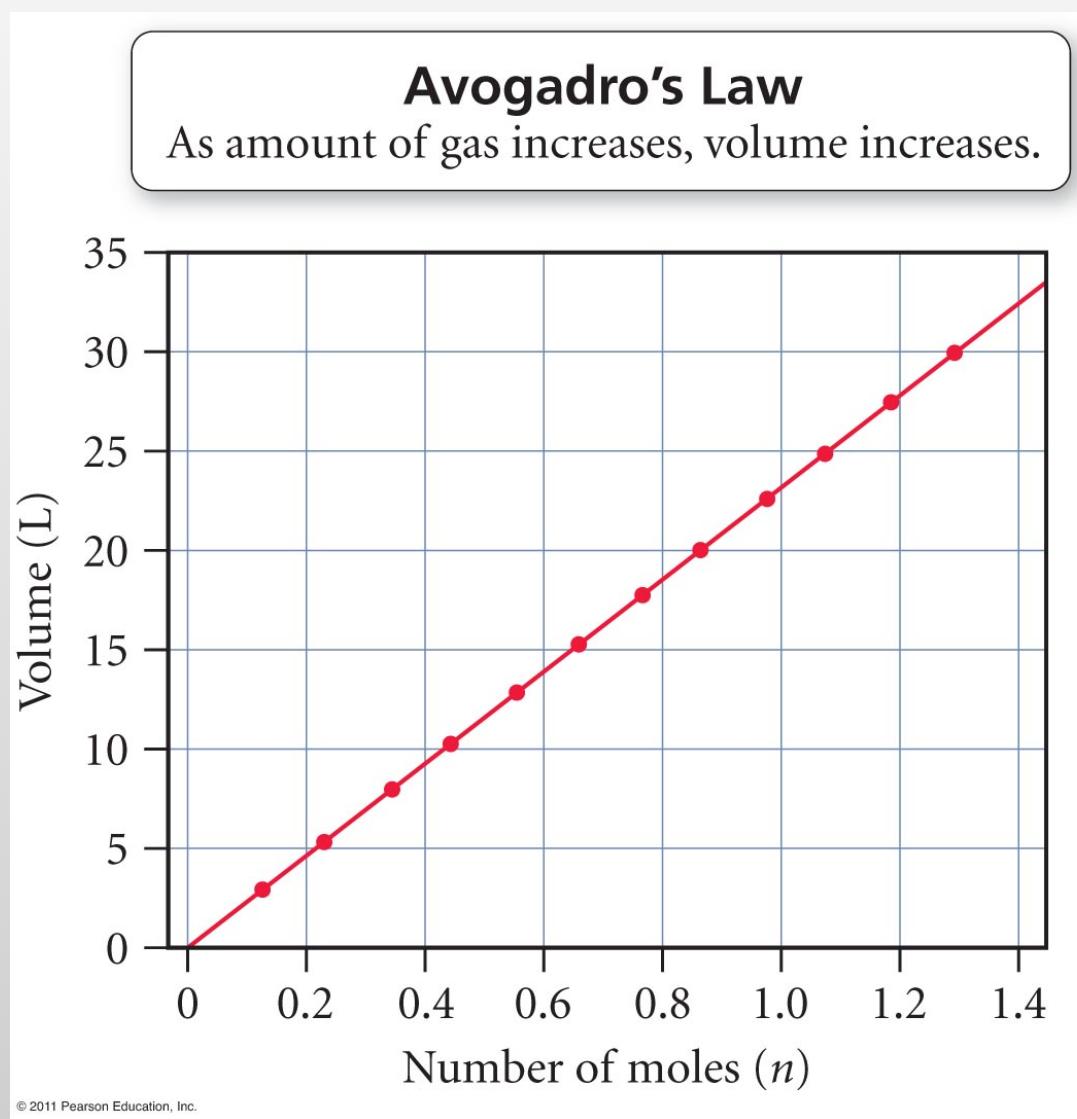
$$V_2 = \frac{216\text{K}}{293\text{K}} \cdot 3.10\text{L} = 2.29\text{L}$$

Molecular Interpretation of Charles Law

Volume versus Temperature: A Molecular View



Relationship between Volume and Amount: Avogadro's Law



Avogadro's Law: $V \propto n$ (constant T and P)

$$\frac{V_1}{n_1} = \frac{V_2}{n_2}$$

Ideal Gas Law

Boyle's Law : $V \propto \frac{1}{P}$

Charles Law : $V \propto T$

Avogadro Law : $V \propto n$

$$V \propto \frac{nT}{P} \quad \text{or} \quad PV \propto nT$$

$$PV = nRT$$

Ideal Gas Law

$$PV = nRT$$

constant
 n and T

constant
 n and P

constant
 P and T

$$V = \frac{nRT}{P}$$

$$V \propto \frac{1}{P}$$

Boyle's Law

$$V = \frac{nRT}{P}$$

$$V \propto T$$

Charles's Law

$$V = \frac{nRT}{P}$$

$$V \propto n$$

Avogadro's Law

R can be calculated based upon standard conditions:

$$R = \frac{PV}{nT}$$

$$R = \frac{1 \text{ atm} \cdot 22.4141 \text{ L}}{1 \text{ mole} \cdot 273.15 \text{ K}}$$

$$R = 0.082058 \frac{\text{atm} \cdot \text{L}}{\text{mol} \cdot \text{K}}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \quad \text{at const. } n$$

A steel tank has a volume of 438L and is filled with 0.885 kg of O₂. Calculate the pressure (in atm) of O₂ at 21°C

Given:

$$V = 438 \text{ L}$$

$$T = 21^\circ\text{C} + 273 \text{ K} = 294 \text{ K}$$

$$n(\text{O}_2) = 0.885 \text{ kg} \cdot \frac{1000 \text{ g}}{1 \text{ kg}} \cdot \frac{1 \text{ mol}}{32.00 \text{ g}} = 27.7 \text{ mol}$$

$$\rho V = n k T \Rightarrow P = \frac{n k T}{V}$$

$$P = \frac{27.7 \text{ mol} \cdot 0.0821 \frac{\text{atm}}{\text{mol K}} \cdot 294 \text{ K}}{438 \text{ L}}$$

$$P = 1.53 \text{ atm}$$

Molar Volume of Gases at STP

STP: Standard Temperature and Pressure

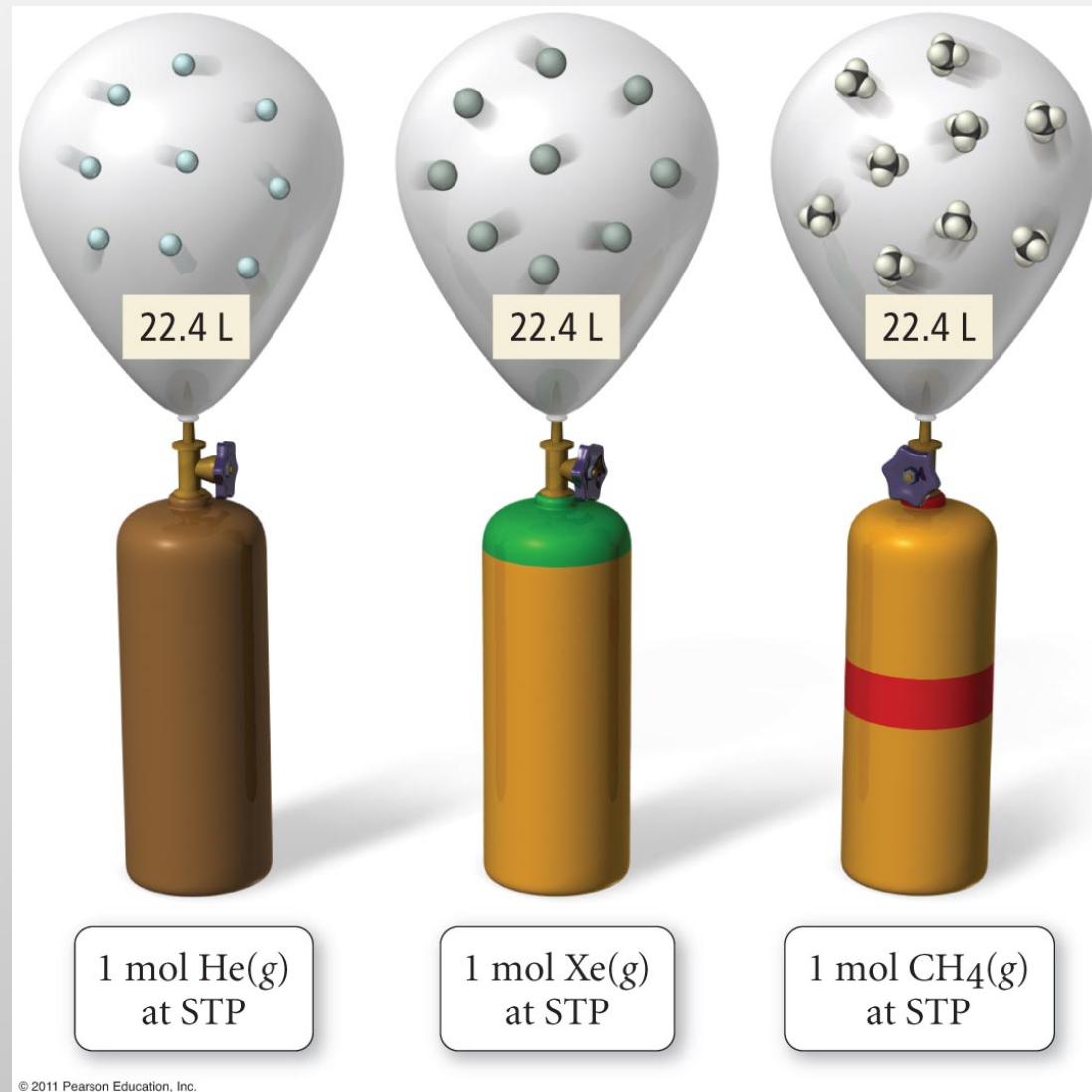
Standard Temperature: 0°C or 273 K

Standard Pressure: 1 atm

$$V = \frac{nRT}{P}$$

$$V = \frac{1.00 \text{ mol} \cdot 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}} \cdot 273 \text{ K}}{1 \text{ atm}}$$

$$V = 22.4 \text{ L}$$



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The molar volume of gases at standard temperature and pressure is
22.4 L

Density of gases

$$\text{Density} = \frac{\text{molar mass}}{\text{molar volume}}$$

$$d_{N_2} = \frac{28.02 \text{ g mol}^{-1}}{22.4 \text{ L mol}^{-1}} = 1.25 \text{ g/L}$$

For non-standard conditions:

$$PV = nRT \Rightarrow \frac{n}{V} = \frac{P}{RT} \quad \text{molar density}$$

Multiply with molar mass

$$M \frac{n}{V} = M \frac{P}{RT} \Rightarrow \frac{\text{mass}}{V} = d = \frac{P \cdot M}{R \cdot T}$$

Find the density in g/L of CO_2 at STP and at room conditions (20°C , 1 atm)

a). $T = 273 \text{ K}$ $p = 1 \text{ atm}$

$$M = 44.01 \text{ g/mol}$$

$$d = \frac{M \cdot P}{R \cdot T} = \frac{44.01 \text{ g/mol} \cdot 1 \text{ atm}}{0.0821 \frac{\text{L atm}}{\text{mol K}} \cdot 273 \text{ K}} = 1.96 \text{ g/L}$$

b). $T = 20^\circ\text{C} + 273 \text{ K} = 293 \text{ K}$

$$d = \frac{44.01 \text{ g/mol} \cdot 1 \text{ atm}}{0.0821 \frac{\text{L atm}}{\text{mol K}} \cdot 293 \text{ K}} = 1.83 \text{ g/L}$$

