

Exercises

Review Questions

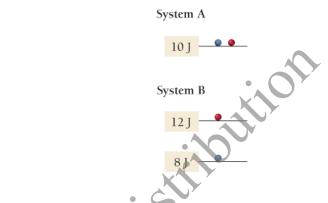
- 1. What is the first law of thermodynamics, and how does it relate to energy use?
- 2. What is nature's heat tax, and how does it relate to energy use?
- 3. What is a perpetual motion machine? Can such a machine exist given the laws of thermodynamics?
- 4. Is it more efficient to heat your home with a natural gas furnace or an electric furnace? Explain.
- 5. What is a spontaneous process? Provide an example.
- 6. Explain the difference between the spontaneity of a reaction (which depends on thermodynamics) and the speed at which the reaction occurs (which depends on kinetics). Can a catalyst make a nonspontaneous reaction spontaneous?
- 7. What is the precise definition of entropy? What is the significance of entropy being a state function?
- 8. Why does the entropy of a gas increase when it expands into a vacuum?
- 9. Explain the difference between macrostates and microstates.
- 10. Based on its fundamental definition, explain why entropy is a measure of energy dispersion.
- 11. State the second law of thermodynamics. How does the second law explain why heat travels from a substance at higher temperature to one at lower temperature?
- 12. What happens to the entropy of a sample of matter when it changes state from a solid to a liquid? From a liquid to a gas?
- 13. Explain why water spontaneously freezes to form ice below 0 °C even though the entropy of the water decreases during the state transition. Why is the freezing of water not spontaneous above 0 °C?
- 14. Why do exothermic processes tend to be spontaneous at low temperatures? Why does their tendency toward spontaneity decrease with increasing temperature?
- **15.** What is the significance of the change in Gibbs free energy (ΔG) for a reaction?
- 16. Predict the spontaneity of a reaction (and the temperature dependence of the spontaneity) for each possible combination of signs for ΔH and ΔS (for the system).
 - **a.** ΔH negative, ΔS positive
 - **b.** ΔH positive, ΔS negative
 - c. ΔH negative, ΔS negative
 - **d.** ΔH positive, ΔS positive
- 17. State the third law of thermodynamics and explain its significance.
- 18. Why is the standard entropy of a substance in the gas state greater than its standard entropy in the liquid
- 19. How does the standard entropy of a substance depend on its molar mass? On its molecular complexity?
- 20. How can you calculate the standard entropy change for a reaction from tables of standard entropies?
- **21.** Describe the three different methods to calculate ΔG^o for a reaction. Which method would you choose to calculate ΔG^o for a reaction at a temperature other than 25 °C?
- 22. Why is free energy "free"?
- **23.** Explain the difference between ΔG^o and ΔG .
- **24.** Why does water spilled on the floor evaporate even though ΔG^o for the evaporation process is positive at room temperature?
- 25. How do you calculate the change in free energy for a reaction under nonstandard conditions?
- **26.** How does the value of ΔG^o for a reaction relate to the equilibrium constant for the reaction? What does a negative ΔG^o for a reaction imply about K for the reaction? A positive ΔG^o ?

Problems by Topic

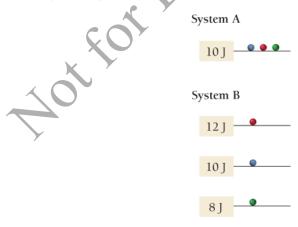
are paired, with each odd-numbered problem followed by a similar even-numbered problem. Exercises in the Cumulative Problems section are also paired but more loosely. Because of their nature, Challenge Problems and Conceptual Problems are unpaired.

Entropy, the Second Law of Thermodynamics, and the Direction of Spontaneous Change

- 27. Which of these processes is spontaneous?
- a. the combustion of natural gas
- b. the extraction of iron metal from iron ore
- c. a hot drink cooling to room temperature
- d. drawing heat energy from the ocean's surface to power a ship
- 28. Which of these processes are nonspontaneous? Are the nonspontaneous processes impossible?
- a. a bike going up a hill
- b. a meteor falling to Earth
- c. obtaining hydrogen gas from liquid water
- d. a ball rolling down a hill
- **29.** Suppose that two systems, each composed of two particles represented by circles, have 20 J of total energy. Which system, A or B, has the greater entropy? Why?



30. Suppose two systems, each composed of three particles represented by circles, have 30 J of total energy. In how many energetically equivalent ways can you distribute the particles in each system? Which system has greater entropy?



- **31.** Calculate the change in entropy that occurs in the system when 1.00 mole of isopropyl alcohol (C_3H_8O) melts at its melting point (-89.5 °C). See **Table 11.9** for heats of fusion.
- **32.** Calculate the change in entropy that occurs in the system when 1.00 mole of diethyl ether $(C_4H_{10}O)$ condenses from a gas to a liquid at its normal boiling point (34.6 °C). See **Table 11.7** for heats of vaporization.
- **33.** Calculate the change in entropy that occurs in the system when 45.0 g of acetone (C_3H_6O) freezes at its melting point (-94.8 °C). See **Table 11.9** for heats of fusion.
- 34. Calculate the change in entropy that occurs in the system when $55.0~{\rm g}$ of water vaporizes from a

liquid to a gas at its boiling point (100.0 °C). See **Table 11.7** for heats of vaporization.

- **35.** Without doing any calculations, determine the sign of ΔS_{sys} for each chemical reaction.
- **a.** $2KClO_3(s) \rightarrow 2KCl(s) + 3O_2(g)$
- **b.** $CH_2 = CH_2(g) + H_2(g) \rightarrow CH_3CH_3(g)$
- c. Na(s) + $\frac{1}{2}$ Cl₂(g) \rightarrow NaCl(s)
- **d.** $N_2(g) + 3H_2(g) \rightarrow 2NH_3(g)$
- **36.** Without doing any calculations, determine the sign of $\Delta S_{\rm sys}$ for each chemical reaction.
- **a.** $Mg(s) + Cl_2(g) \rightarrow MgCl_2(s)$
- **b.** $2H_2S(g) + 3O_2(g) \rightarrow 2H_2O(g) + 2SO_2(g)$
- **c.** $2O_3(g) \to 3O_2(g)$
- **d.** $HCl(g) + NH_3(g) \rightarrow NH_4Cl(s)$
- 37. Without doing any calculations, determine the sign of ΔS_{sys} and ΔS_{sur} for each chemical reaction. In addition, predict under what temperatures (all temperatures, low temperatures, or high temperatures), if any, the reaction is spontaneous.
- **a.** $C_3H_8(g) + 5O_2(g) \rightarrow 3CO_2(g) + 4H_2O(g)\Delta H_{rxn}^0 = -2044 \text{ kJ}$
- **b.** $N_2(g) + O_2(g) \rightarrow 2NO(g) \Delta H_{rxn}^o = + 182.6 \text{ kJ}$
- c. $2N_2(g) + O_2(g) \rightarrow 2N_2O(g)$ $\Delta H_{\text{rxn}}^o = +163.2 \text{ kJ}$
- **d.** $4NH_3(g) + 5O_2(g) \rightarrow 4NO(g) + 6H_2O(g) \quad \Delta H_{rxn}^o = -906 \text{ kJ}$
- **38.** Without doing any calculations, determine the sign of $\Delta S_{\rm sys}$ and $\Delta S_{\rm sur}$ for each chemical reaction. In addition, predict under what temperatures (all temperatures, low temperatures, or high temperatures), if any, the reaction is spontaneous.
- **a.** $2CO(g) + O_2(g) \rightarrow 2CO_2(g)$ $\Delta H_{rxn}^o = -566.0 \text{ kJ}$
- **b.** $2NO_2(g) \rightarrow 2NO(g) + O_2 \quad \Delta H_{rxn}^o = +113.1 \text{ kJ}$
- c. $2H_2(g) + O_2(g) \rightarrow 2H_2O(g)$ $\Delta H_{rxn}^o = -483.6 \text{ kJ}$
- **d.** $CO_2(g) \rightarrow C(s) + O_2(g)$ $\Delta H_{rxn}^0 = +393.5 \text{ kJ}$
- **39.** Calculate ΔS_{surr} at the indicated temperature for each reaction.
- **a.** $\Delta H_{\text{rxn}}^o = -385 \text{ kJ}; 298 \text{ K}$
- **b.** $\Delta H_{\text{rxn}}^o = -385 \text{ kJ}; 77 \text{ K}$
- $\Delta H_{\text{ryn}}^{o} = +114 \text{ kJ}; 298 \text{ K}$
- **d.** $\Delta H_{\text{rxn}}^{o} = +114 \text{ kJ}; 77 \text{ K}$
- **40.** A reaction has $\Delta H_{\text{rxn}}^o = -112 \text{ kJ}$ and $\Delta H_{\text{rxn}}^o = 354 \text{ J/K}$ At what temperature is the change in entropy for the reaction equal to the change in entropy for the surroundings?
- **41.** Given the values of $\Delta H_{\text{rxn}}^o \Delta S_{\text{rxn}}^o$ and T, determine ΔS_{univ} and predict whether each reaction is spontaneous. (Assume that all reactants and products are in their standard states.)
- **a.** ΔH_{rxn}^o , = +115 kJ; ΔS_{rxn}^o = -263 J/K; T = 298 K
- **b.** ΔH_{rxn}^o , = -115 kJ; ΔS_{rxn}^o = +263 J/K; T = 298 K
- **c.** $\Delta H_{\text{rxn}}^{o}$, = -115 kJ; $\Delta S_{\text{rxn}}^{o}$ = -263 J/K; T = 298 K **d.** $\Delta H_{\text{rxn}}^{o}$, = -115 kJ; $\Delta S_{\text{rxn}}^{o}$ = -263 J/K; T = 615 K
- **42.** Given the values of $\Delta H_{\rm rxn}$, $\Delta S_{\rm rxn}^o$, and T, determine $\Delta S_{\rm univ}$ and predict whether each reaction is spontaneous. (Assume that all reactants and products are in their standard states.)
- **a.** $\Delta H_{\text{rxn}}^o = -95 \text{ kJ}; \quad \Delta S_{\text{rxn}}^o = -157 \text{J/K}; \quad T = 298 \text{ K}$
- **b.** $\Delta H_{\text{rxn}}^o = -95 \text{ kJ}; \quad \Delta S_{\text{rxn}}^o = -157 \text{J/K}; \quad T = 855 \text{ K}$
- **c.** $\Delta H_{\text{rxn}}^o = -95 \text{ kJ}; \quad \Delta S_{\text{rxn}}^o = -157 \text{J/K}; \quad T = 298 \text{ K}$
- **d.** $\Delta H_{\text{rxn}}^o = -95 \text{ kJ}; \quad \Delta S_{\text{rxn}}^o = +157 \text{J/K}; \quad T = 398 \text{ K}$

Standard Entropy Changes and Gibbs Free Energy

- **43.** Calculate the change in Gibbs free energy for each set of ΔH , ΔS , and T given in **Problem 41** \Box . Predict whether each reaction is spontaneous at the temperature indicated. (Assume that all reactants and products are in their standard states.)
- **44.** Calculate the change in Gibbs free energy for each set of ΔH , ΔS , and T given in **Problem 42**. Predict whether each reaction is spontaneous at the temperature indicated. (Assume that all reactants and products are in their standard states.)
- **45.** Calculate the free energy change for this reaction at 25 °C. Is the reaction spontaneous?

$$C_3H_8(g) + 5O_2(g) \rightarrow 3CO_2(g) + 4H_2O(g)$$

$$\Delta H_{\text{rxn}}^{o} = -2217 \text{ kJ}; \quad \Delta S_{\text{rxn}}^{o} = 101.1 \text{J/K};$$

46. Calculate the free energy change for this reaction at 25 °C. Is the reaction spontaneous? (Assume that all reactants and products are in their standard states.)

$$\begin{aligned} &2\mathrm{Ca}(s) + \mathrm{O}_2(g) \rightarrow 2\mathrm{CaO}(s) \\ \Delta H^o_{\mathrm{rxn}} = & -1269.8 \text{ kJ}; \Delta H^o_{\mathrm{rxn}} = & -364.6 \text{ J/K} \end{aligned}$$

47. Fill in the blanks in the table. Both ΔH and ΔS refer to the system.

ΔH	ΔS	ΔG	Low Temperature	High Temperature
_	+	_	Spontaneous	
-	_	Temperature dependent		
+	+			Spontaneous
	_		Nonspontaneous	Nonspontaneous

- 48. Predict the conditions (high temperature, low temperature, all temperatures, or no temperatures) under which each reaction is spontaneous.
- **a.** $H_2O(g) \rightarrow H_2O(l)$
- **b.** $CO_2(s) \rightarrow CO_2(g)$
- **c.** $H_2(g) \rightarrow 2H(g)$
- **d.** $2NO_2(g) \rightarrow 2NO(g) + O_2(g)$ (endothermic)
- 49. How does the molar entropy of a substance change with increasing temperature?
- 50. What is the molar entropy of a pure crystal at 0 K? What is the significance of the answer to this question?
- 51. For each pair of substances, choose the one that you expect to have the higher standard molar
- (S^o) at 25 °C. Explain the reasons for your choices.
- **a.** CO(g); $CO_2(g)$
- **b.** $CH_3OH(l)$; $CH_3OH(g)$
- **c.** Ar(g); CO₂(g)
- **d.** $CH_4(g)$; $SiH_4(g)$
- e. NO₂(g); CH₃CH₂CH₃(g)
- **f.** NaBr(s); NaBr(aq)
- 52. For each pair of substances, choose the one that you expect to have the higher standard molar entropy (S^o) at 25 °C. Explain the reasons for your choices.
- **a.** $NaNO_3(s)$; $NaNO_3(aq)$
- **b.** $CH_4(g)$; $CH_3CH_3(g)$
- **c.** $Br_2(l)$; $Br_2(g)$
- **d.** $Br_2(g)$; $F_2(g)$
- **e.** PCl(*g*); PCl₅(*g*)
- **f.** $CH_3CH_2CH_2CH_3(g)$; $SO_2(g)$
- 53. Rank each set of substances in order of increasing standard molar entropy (S^o). Explain your reasoning.
- a. $NH_3(g)$; Ne(g); $SO_2(g)$; $CH_3CH_2OH(g)$; He(g)
- **b.** $H_2O(s)$; $H_2O(l)$; $H_2O(g)$
- c. $CH_4(g)$; $CF_4(g)$; $CCl_4(g)$
- **54.** Rank each set of substances in order of increasing standard molar entropy (S^o) . Explain your reasoning.
- **a.** $I_2(s)$; $F_2(g)$; $Br_2(g)$; $Cl_2(g)$
- **b.** $H_2O(g)$; $H_2O_2(g)$; $H_2S(g)$

- c. C(s, graphite); C(s, diamond); C(s, amorphous)
- **55.** Use data from Appendix IIB to calculate ΔS^o_{rxn} for each of the reactions. In each case, try to rationalize the sign of ΔS^o_{rxn} .
- **a.** $C_2H_4(g) + H_2(g) \rightarrow C_2H_6(g)$
- **b.** $C(s) + H_2O(g) \rightarrow CO(g) + H_2(g)$
- c. $CO(g) + H_2O(g) \rightarrow H_2(g) + CO_2(g)$
- **d.** $2H_2S(g) + 3O_2(g) \rightarrow 2H_2O(l) + 2SO_2(g)$
- **56.** Use data from Appendix IIB to calculate $\Delta S_{\rm rxn}^o$ for each of the reactions. In each case, try to rationalize the sign of $\Delta H_{\rm rxn}$.
- a. $3NO_2(g) + H_2O(l) \rightarrow 2HNO_3(aq) + NO(g)$
- **b.** $\operatorname{Cr_2O_3}(s) + 3\operatorname{CO}(g) \rightarrow 2\operatorname{Cr}(s) + 3\operatorname{CO_2}(g)$
- c. $SO_2(g) + \frac{1}{2}O_2(g) \to SO_3(g)$
- **d.** $N_2O_4(g) + 4H_2(g) \rightarrow N_2(g) + 4H_2O(g)$
- **57.** Find ΔS^o for the formation of $\mathrm{CH_2Cl_2}(g)$ from its gaseous elements in their standard states. Rationalize the sign of ΔS^o .
- **58.** Find ΔS^o for the reaction between nitrogen gas and fluorine gas to form nitrogen trifluoride gas. Rationalize the sign of ΔS^o .
- **59.** Methanol burns in oxygen to form carbon dioxide and water. Write a balanced equation for the combustion of liquid methanol and calculate ΔH^o_{rxn} , ΔS^o_{rxn} , and ΔG^o_{rxn} at 25 °C. Is the combustion of methanol spontaneous?
- **60.** In photosynthesis, plants form glucose $(C_6H_{12}O_6)$ and oxygen from carbon dioxide and water. Write a balanced equation for photosynthesis and calculate ΔH^o_{rxn} , ΔS^o_{rxn} , and ΔG^o_{rxn} at 25 °C. Is photosynthesis spontaneous?
- **61.** For each reaction, calculate ΔH^o_{rxn} , ΔS^o_{rxn} , and ΔG^o_{rxn} and ΔG^o_{rxn} at 25 °C and state whether the reaction is spontaneous. If the reaction is not spontaneous, would a change in temperature make it spontaneous? If so, should the temperature be raised or lowered from 25 °C?
- **a.** $N_2O_4(g) \rightarrow 2NO_2(g)$
- **b.** $NH_4Cl(s) \rightarrow HCl(g) + NH_3(g)$
- c. $3H_2(g) + Fe_2O_3(s) \rightarrow 2Fe(s) + 3H_2O(g)$
- **d.** $N_2(g) + 3H_2(g) \rightarrow 2NH_3(g)$
- **62.** For each reaction, calculate ΔH_{ran}^o , ΔS_{rxn}^o and ΔG_{rxn}^o at 25 °C and state whether the reaction is spontaneous. If the reaction is not spontaneous, would a change in temperature make it spontaneous? If so, should the temperature be raised or lowered from 25 °C?
- **a.** $2CH_4(g) \rightarrow C_2H_6(g) + H_2(g)$
- **b.** $2NH_3(g) \rightarrow N_2H_4(g) + H_2(g)$
- **c.** $N_2(g) + O_2(g) \rightarrow 2NO(g)$
- **d.** $2KClO_3(s) \rightarrow 2KCl(s) + 3O_2(g)$
- **63.** Use standard free energies of formation to calculate ΔG^o at 25 °C for each reaction in **Problem**
- **61**. How do the values of ΔG^o calculated this way compare to those calculated from ΔH^o and ΔS^o ? Which of the two methods could be used to determine how ΔG^o changes with temperature?
- **64.** Use standard free energies of formation to calculate ΔG^o at 25 °C for each reaction in **Problem**
- **62** How well do the values of ΔG^o calculated this way compare to those calculated from ΔH^o and ΔS^o Which of the two methods could be used to determine how ΔG^o changes with temperature?
- 65. Consider the reaction:

$$2 \operatorname{NO}(g) + \operatorname{O}_2(g) \to 2 \operatorname{NO}_2(g)$$

Estimate ΔG^o for this reaction at each temperature and predict whether the reaction is spontaneous. (Assume that ΔH^o and ΔS^o do not change too much within the given temperature range.)

- a. 298 K
- **b.** 715 K
- **c.** 855 K
- 66. Consider the reaction:

$$CaCO_3(s) \rightarrow CaO(s) + CO_2(g)$$

(Assume that ΔH^o and ΔS^o do not change too much within the given temperature range.)

- a. 298 K
- **b.** 1055 K
- **c.** 1455 K
- **67.** Determine ΔG^o for the reaction:

$$\operatorname{Fe_2O_3}(s) + 3\operatorname{CO}(g) \to 2\operatorname{Fe}(s) + 3\operatorname{CO_2}(g)$$

Use the following reactions with known ΔG_{rxn}^o values:

$$2\text{Fe}(s) + \frac{3}{2}\text{O}_2(g) \to \text{Fe}_2\text{O}_3(s) \quad \Delta G_{\text{rxn}}^o = -742.2 \text{ kJ}$$

 $\text{CO}(g) + \frac{1}{2}\text{O}_2(g) \to \text{CO}_2(g) \quad \Delta G_{\text{rxn}}^o = -257.2 \text{ kJ}$

68. Calculate $\Delta G_{\rm rxn}^o$ for the reaction:

$$CaCO_3(s) \rightarrow CaO(s) + CO_2(g)$$

Use the following reactions and given $\Delta G_{\rm rxn}^o$ values:

$$Ca(s) + CO_2(g) + \frac{1}{2}O_2(g) \longrightarrow CaCO_3(s) \quad \Delta G_{\text{rxn}}^{\circ} = -734.4 \text{ kJ}$$

$$2 Ca(s) + O_2(g) \longrightarrow 2 CaO(s) \quad \Delta G_{\text{rxn}}^{\circ} = -1206.6 \text{ kJ}$$

Free Energy Changes, Nonstandard Conditions, and the Equilibrium Constant

69. Consider the sublimation of iodine at 25.0 °C:

$$I_2(s) \to I_2(g)$$

- **a.** Find $\Delta G_{\rm rxn}^o$ at 25.0 °C.
- **b.** Find $\Delta G_{\rm rxn}$ at 25.0 °C under the following nonstandard conditions:
 - **i.** $P_{I_2} = 1.00 \text{ mmHg}$
 - **ii.** $P_{I_2} = 0.100 \text{ mmHg}$
- c. Explain why iodine spontaneously sublimes in open air at 25 $^{\circ}$ C.
- 70. Consider the evaporation of methanol at 25.0 °C.

$$CH_3OH(l) \rightarrow CH_3OH(g)$$

- a. Find ΔG^o at 25.0 °C
- **b.** Find ΔG_{ren} at 25.0 °C under the following nonstandard conditions:
 - **i.** $P_{\text{CH}_2\text{OH}} = 150.0 \text{ mmHg}$
 - **ii.** $P_{\text{CH}_2\text{OH}} = 100.0 \text{ mmHg}$
- **iii.** $P_{\text{CH}_3\text{OH}} = 10.0 \text{ mmHg}$
- c. Explain why methanol spontaneously evaporates in open air at 25.0 $^{\circ}\text{C}.$
- 71. Consider the reaction:

$$\mathrm{CH_3OH}(g) \rightleftharpoons \mathrm{CO}(g) + 2\mathrm{H}_2(g)$$

Calculate ΔG for this reaction at 25 °C under the following conditions:

$$P_{\text{CH}_3\text{OH}} = 0.855 \text{atm}$$

$$P_{\text{CO}} = 0.125 \text{atm}$$

$$P_{\rm H_2} = 0.183$$
atm

72. Consider the reaction:

$$CO_2(g) + CCl_4(g) \rightleftharpoons 2COCl_2(g)$$

Calculate ΔG for this reaction at 25 °C under the following conditions:

$$P_{\text{CO}_2} = 0.112 \text{atm}$$

$$P_{\text{CCl4}} = 0.174$$
atm

$$P_{\text{COCl}_2} = 0.744$$
atm

73. Use data from Appendix IIB to calculate the equilibrium constant at 25 °C for each reaction.

a.
$$2CO(g) + O_2(g) \rightleftharpoons 2CO_2(g)$$

b.
$$2H_2S(g) \rightleftharpoons 2H_2(g) + S_2(g)$$

74. Use data from Appendix IIB to calculate the equilibrium constant at 25 °C for each reaction. $\Delta G_{\rm f}^{\rm o}$ for BrCl(g) is -1.0 kJ/mol.

a.
$$2NO_2(g) \rightleftharpoons N_2O_4(g)$$

b.
$$Br_2(g) + Cl_2(g) \rightleftharpoons 2BrCl(g)$$

75. Consider the reaction:

$$CO(g) + 2 H_2(g) \rightleftharpoons CH_3OH(g) K_p = 2.26 \times 10^4 \text{ at } 25 \degree C$$

Calculate $\Delta \textit{G}_{rxn}$ for the reaction at 25 °C under the following conditions:

- a. standard conditions
- b. at equilibrium

c.
$$P_{\text{CH}_3\text{OH}}$$
 = 1.0 atm; P_{CO} = P_{H_2} = 0.010 atm

76. Consider the reaction:

$$_{2}(g) + \text{Cl}_{2}(g) \rightleftharpoons 2 \text{ ICl}(g) \text{ K}_{p} = 81.9 \text{ at } 25^{\circ}\text{C}$$

Calculate $\Delta G_{\rm rxn}$ for the reaction at 25 °C under the following conditions:

- a. standard conditions
- **b.** at equilibrium

c.
$$P_{\text{ICI}} = 2.55 \text{atm}; P_{\text{I}_2} = 0.325 \text{atm}; P_{\text{cl}_2} = 0.221 \text{ atm}$$

- 77. Estimate the value of the equilibrium constant at 525 K for each reaction in Problem 73.
- **78.** Estimate the value of the equilibrium constant at 655 K for each reaction in **Problem 74** \Box . (ΔH_f^o for Brcl is 14.6 KJ/mol.)
- 79. Consider the reaction:

$$H_2(g) + I_2(g) \rightleftharpoons 2HI(g)$$

The following data show the equilibrium constant for this reaction measured at several different temperatures. Use the data to find ΔH^o_{rxn} and ΔS^o_{rxn} for the reaction.

Temperature	$K_{ m p}$
150 K	1.4×10^{-6}
175 K	4.6×10^{-4}
200 K	3.6×10^{-2}
225 K	1.1
250 K	15.5

80. Consider the reaction:

$$2NO(g) + O_2(g) \rightleftharpoons 2NO_2(g)$$

The following data show the equilibrium constant for this reaction measured at several different temperatures. Use the data to find $\Delta \textit{H}^\textit{o}_{rxn}$ and $\Delta \textit{S}^\textit{o}_{rxn}$ for the reaction.

remperature	p
170 K	3.8×10^{-3}
180 K	0.34
190 K	18.4
200 K	681

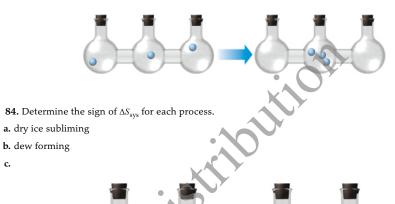
- **81.** The change in enthalpy $\left(\Delta H_{\text{rxn}}^{o}\right)$ for a reaction is -25.8 kJ/mol. The equilibrium constant for the reaction is 1.4×10^3 at 298 K. What is the equilibrium constant for the reaction at 655 K?
- **82.** A reaction has an equilibrium constant of 8.5×10^3 at 298 K. At 755 K, the equilibrium constant is 0.65. Find $\Delta H_{\rm rxn}^o$ for the reaction.

Cumulative Problems

- 83. Determine the sign of ΔS_{sys} for each process.
- a. water boiling
- b. water freezing

c.

c.



85. Our atmosphere is composed primarily of nitrogen and oxygen, which coexist at 25 °C without reacting to any significant extent. However, the two gases can react to form nitrogen monoxide according to the reaction:

$$N_2(g) + O_2(g) \rightleftharpoons 2NO(g)$$

- **a.** Calculate ΔG^o and K_p for this reaction at 298 K. Is the reaction spontaneous?
- **b.** Estimate ΔG^o at 2000 K. Does the reaction become more spontaneous as temperature increases?
- 86. Nitrogen dioxide, a pollutant in the atmosphere, can combine with water to form nitric acid. One of the possible reactions is shown here. Calculate ΔG^o and $K_{\rm p}$ for this reaction at 25 °C and comment on the spontaneity of the reaction.

$$3NO_2(g) + H_2O(l) \rightarrow 2HNO_3(aq) + NO(g)$$

87. Ethene (C_2H_4) can be halogenated by the reaction:

$$C_2H_4(g) + X_2(g) \rightleftharpoons C_2H_4X_2(g)$$

where X_2 can be Cl_2 , Br_2 , or I_2 . Use the thermodynamic data given to calculate ΔH^o , ΔS^o , ΔG^o and K_p for the halogenation reaction by each of the three halogens at 25 $^{\circ}$ C. Which reaction is most spontaneous? Least spontaneous? What is the main factor responsible for the difference in the spontaneity of the three reactions? Does higher temperature make the reactions more spontaneous or less spontaneous?

Compound	$\Delta H_{ m f}^{\circ}$ (kJ/mol)	S°(J/mol·K)
$C_2H_4CI_2(g)$	-129.7	308.0
$C_2H_4Br_2(g)$	+38.3	330.6
C ₂ H ₄ I ₂ (<i>g</i>)	+66.5	347.8

88. H_2 reacts with the halogens (X_2) according to the reaction:

$$H_2(g) + X_2(g) \rightleftharpoons 2HX(g)$$

where X_2 can be Cl_2 , Br_2 or I_2 . Use the thermodynamic data in Appendix IIB to calculate ΔH^o , ΔS^o , ΔG^o , and K_p for the reaction between hydrogen and each of the three halogens. Which reaction is most spontaneous? Least spontaneous? What is the main factor responsible for the difference in the spontaneity of the three reactions? Does higher temperature make the reactions more spontaneous or less spontaneous?

89. Consider this reaction occurring at 298 K:

$$N_2O(g) + NO_2(g) \rightleftharpoons 3 NO(g)$$

- a. Show that the reaction is not spontaneous under standard conditions by calculating $\Delta G_{\rm rxn}^{\circ}$.
- b. If a reaction mixture contains only N_2O and NO_2 at partial pressures of 1.0 atm each, the reaction will be spontaneous until some NO forms in the mixture. What maximum partial pressure of NO builds up before the reaction ceases to be spontaneous?
- c. Can the reaction be made more spontaneous by an increase or decrease in temperature? If so, what temperature is required to make the reaction spontaneous under standard conditions?
- 90. Consider this reaction occurring at 298 K:

$$BaCO_3(s) \rightleftharpoons BaO(s) + CO_2(g)$$

- a. Show that the reaction is not spontaneous under standard conditions by calculating $\Delta G_{\rm rxn}^{\circ}$.
- **b.** If $BaCO_3$ is placed in an evacuated flask, what is the partial pressure of CO_2 when the reaction reaches equilibrium?
- c. Can the reaction be made more spontaneous by an increase or decrease in temperature? If so, at what temperature is the partial pressure of carbon dioxide 1.0 atm?
- **91.** Living organisms use energy from the metabolism of food to create an energy-rich molecule called adenosine triphosphate (ATP). The ATP then acts as an energy source for a variety of reactions that the living organism must carry out to survive. ATP provides energy through its hydrolysis, which can be symbolized as follows:

$$ATP(aq) + H_2O(l) \rightarrow ADP(aq) + P_1(aq) \quad \Delta G_{rxn}^{\circ} = -30.5 \text{ kJ}$$

where ADP represents adenosine diphosphate and P_i represents an inorganic phosphate group (such as $HPO_4^{\ 2^-}$).

- a. Calculate the equilibrium constant, K, for the given reaction at 298 K.
- b. The free energy obtained from the oxidation (reaction with oxygen) of glucose $\left(C_6H_{12}O_6\right)$ to form carbon dioxide and water can be used to re-form ATP by driving the given reaction in reverse. Calculate the standard free energy change for the oxidation of glucose and estimate the maximum number of moles of ATP that can be formed by the oxidation of one mole of glucose.
- 92. The standard free energy change for the hydrolysis of ATP was given in Problem 91 $^{\square}$. In a particular cell, the concentrations of ATP, ADP, and P_i are 0.0031 M, 0.0014 M, and 0.0048 M, respectively. Calculate the free energy change for the hydrolysis of ATP under these conditions. (Assume a temperature of 298 K.)
- 93. These reactions are important in catalytic converters in automobiles. Calculate ΔG^o for each at 298

K. Predict the effect of increasing temperature on the magnitude of ΔG^o .

- **a.** $2 \text{ CO}(g) + 2 \text{ NO}(g) \rightarrow \text{N}_2(g) + 2 \text{ CO}_2(g)$
- **b.** $5 \text{ H}_2(g) + 2 \text{ NO}(g) \rightarrow 2 \text{ NH}_3(g) + 2 \text{ H}_2\text{O}(g)$
- c. $2 H_2(g) + 2 NO(g) \rightarrow N_2(g) + 2 H_2O(g)$
- **d.** $2 \text{ NH}_3(g) + 2 \text{ O}_2(g) \rightarrow \text{N}_2\text{O}(g) + 3 \text{ H}_2\text{O}(g)$
- **94.** Calculate ΔG^o at 298 K for these reactions and predict the effect on ΔG^o of lowering the temperature.
- **a.** $NH_3(g) + HBr(g) \rightarrow NH_4Br(s)$
- **b.** $CaCO_3(s) \rightarrow CaO(s) + CO_2(g)$

 $CH_4(g) + 3 Cl_2(g) \rightarrow CHCl_3(g) + 3 HCl(g)$

- c. $\left(\Delta G_{\rm f}^{\circ} \text{ for CHCl}_{3}(g) \text{ is } -70.4 \text{ kJ/mol.}\right)$
- **95.** All the oxides of nitrogen have positive values of $\Delta G_{\rm f}^{\rm o}$ at 298 K, but only one common oxide of nitrogen has a positive ΔS_{r}^{0} . Identify that oxide of nitrogen without reference to thermodynamic data
- **96.** The values of $\Delta G_{\rm f}^{\rm o}$ for the hydrogen halides become less negative with increasing atomic number. The $\Delta G_{\varepsilon}^{0}$ of HI is slightly positive. On the other hand, the trend in $\Delta S_{\varepsilon}^{0}$ is to become more positive with increasing atomic number. Explain.
- **97.** Consider the reaction $X_2(g) \rightarrow 2 X(g)$. When a vessel initially containing 755 torr of X_2 comes to equilibrium at 298 K, the equilibrium partial pressure of X is 103 torr. The same reaction is repeated with an initial partial pressure of 748 torr of X₂ at 755 K; the equilibrium partial pressure of X is 532 torr. Find ΔH° for the reaction.
- 98. Dinitrogen tetroxide decomposes to nitrogen dioxide:

$$N_2O_4(g) \to 2 NO_2(g) \ \Delta H_{rxn}^{\circ} = 55.3 \text{ kJ}$$

At 298 K, a reaction vessel initially contains 0.100 atm of N₂O₄. When equilibrium is reached, 58% of the N₂O₄ has decomposed to NO₂. What percentage of N₂O₄ decomposes at 388 K? Assume that the initial pressure of N_2O_4 is the same (0.100 atm).

- **99.** Indicate and explain the sign of ΔS_{univ} for each process
- **a.** $2 H_2(g) + O_2(g) \rightarrow 2 H_2O(l)$ at 298 K
- **b.** the electrolysis of $H_2O(l)$ to $H_2(g)$ and $O_2(g)$ at 298 K
- c. the growth of an oak tree from an acorn
- 100. The Haber process is very important for agriculture because it converts $N_2(g)$ from the atmosphere into bound nitrogen, which can be taken up and used by plants. The Haber process reaction is $N_2(g) + 3 H_2(g) \Rightarrow 2 NH_3(g)$. The reaction is exothermic but is carried out at relatively high temperatures. Why?
- 101. A metal salt with the formula MCl_2 crystallizes from water to form a solid with the composition $MCl_2 \cdot 6 H_2O$. The equilibrium vapor pressure of water above this solid at 298 K is 18.3 mmHg. What is the value of ΔG for the reaction $MCl_2 \cdot 6 H_2O(s) \rightleftharpoons MCl_2(s) + 6 H_2O(g)$ when the pressure of water vapor is 18.3 mmHg? When the pressure of water vapor is 760.0 mmHg?
- **102.** The solubility of AgCl(s) in water at 25 °C is 1.33×10^{-5} mol/L, and its ΔH° of solution is 65.7 k/mol. What is its solubility at 50.0 °C?

Challenge Problems

103. Review the subsection in this chapter entitled Making a Nonspontaneous Process Spontaneous in Section 18.8 □. The hydrolysis of ATP, shown in Problem 91 □, is often used to drive nonspontaneous processes—such as muscle contraction and protein synthesis—in living organisms. The nonspontaneous process to be driven must be coupled to the ATP hydrolysis reaction. For example, suppose the nonspontaneous process is $A+B \to AB$ (ΔG° positive). The coupling of a nonspontaneous reaction such as this one to the hydrolysis of ATP is often accomplished by the mechanism:

$$\begin{array}{c} A + ATP + H_2O \longrightarrow A - P_i + ADP \\ \\ A - P_i + B \longrightarrow AB + P_i \\ \hline \\ A + B + ATP + H_2O \longrightarrow AB + ADP + P_i \end{array}$$

As long as $\Delta G_{\rm rxn}$ for the nonspontaneous reaction is less than 30.5 kJ, the reaction can be made spontaneous by coupling in this way to the hydrolysis of ATP. Suppose that ATP is to drive the reaction between glutamate and ammonia to form glutamine:

- a. Calculate K for the reaction between glutamate and ammonia. (The standard free energy change for the reaction is +14.2 kJ/mol. Assume a temperature of 298 K.)
- b. Write a set of reactions such as those given showing how the glutamate and ammonia reaction can couple with the hydrolysis of ATP. What is $\Delta G_{\rm rxn}^{^{\circ}}$ and K for the coupled reaction?
- 104. Calculate the entropy of each state and rank the states in order of increasing entropy.



105. Suppose we redefine the standard state as P = 2 atm. Find the new standard ΔG_0^c values of each substance.

a. HCl(g)

b. $N_2O(g)$

c. H(g)

Explain the results in terms of the relative entropies of reactants and products of each reaction.

106. The ΔG for the freezing of $H_2O(l)$ at -10 °C is -210 J/mol, and the heat of fusion of ice at this temperature is 5610 J/mol. Find the entropy change of the universe when 1 mol of water freezes at -10 °C.

107. Consider the reaction that occurs during the Haber process:

$$N_2(g) + 3 H_2(g) \rightarrow 2 NH_3(g)$$

The equilibrium constant is 3.9×10^5 at 300 K and 1.2×10^{-1} at 500 K. Calculate $\Delta H_{\rm rxn}^o$ and $\Delta S_{\rm rxn}^o$ for this reaction.

108. The salt ammonium nitrate can follow three modes of decomposition: (a) to $HNO_3(g)$ and $NH_3(g)$, (b) to $N_2O(g)$ and $H_2O(g)$, and (c) to $N_2(g)$, $O_2(g)$, and $H_2O(g)$. Calculate ΔG^o_{rxn} for each mode of decomposition at 298 K. Explain in light of these results how it is still possible to use ammonium nitrate as a fertilizer and the precautions that should be taken when it is used.

109. Given the tabulated data, calculate ΔS_{vap} for each of the first four liquids.

$$\left(\Delta S_{\text{vap}} = \Delta H_{\text{vap}} / T, \text{ where } T \text{ is in K}\right)$$

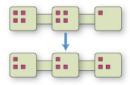
Compound	Name	bp (°C)	$\Delta H_{ m vap}$ (k $ m J/mol$) at bp
C ₄ H ₁₀ O	Diethyl ether	34.6	26.5
C ₃ H ₆	Acetone	56.1	29.1
C ₆ H ₆	Benzene	79.8	30.8
CHCI ₃	Chloroform	60.8	29.4
C ₂ H ₅ OH	Ethanol	77.8	38.6
H ₂ O	Water	100.0	40.7

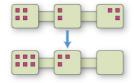
All four values should be close to each other. Predict whether the last two liquids in the table have ΔS_{van} in this same range. If not, predict whether it is larger or smaller and explain. Verify your prediction.

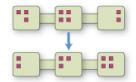
Conceptual Problems

- 110. Which statement is true?
- a. A spontaneous reaction is always a fast reaction.
- **b.** A spontaneous reaction is always a slow reaction.
- $\boldsymbol{c.}$ The spontaneity of a reaction is not necessarily related to the speed of a reaction.
- 111. Which process is necessarily driven by an increase in the entropy of the surroundings?
- a. the condensation of water
- b. the sublimation of dry ice
- c. the freezing of water
- 112. Consider the changes in the distribution of nine particles into three interconnected boxes shown here. Which has the most negative ΔS ?









- 113. Which statement is true?
- a. A reaction in which the entropy of the system increases can be spontaneous only if it is exothermic.
- b. A reaction in which the entropy of the system increases can be spontaneous only if it is endothermic.
- c. A reaction in which the entropy of the system decreases can be spontaneous only if it is exothermic.
- 114. Which process is spontaneous at 298 K?
- **a.** $H_2O(l) \rightarrow H_2O(g, 1 \text{ atm})$
- **b.** $H_2O(l) \rightarrow H_2O(g, 0.10 \text{ atm})$
- c. $H_2O(l) \rightarrow H_2O(g, 0.010 \text{ atm})$
- **115.** The free energy change of the reaction $A(g) \rightarrow B(g)$ is zero under certain conditions. The *standard* free energy change of the reaction is -42.5 kJ. Which statement must be true about the reaction?
- a. The concentration of the product is greater than the concentration of the reactant.
- b. The reaction is at equilibrium.
- c. The concentration of the reactant is greater than the concentration of the product.
- **116.** The reaction $A(g) \rightleftharpoons B(g)$ has an equilibrium constant of 5.8 and under certain conditions has
- Q = 336. What can you conclude about the sign of $\Delta G_{\rm rxn}^o$ and $\Delta G_{\rm rxn}$ for this reaction under these conditions?

Questions for Group Work

Active Classroom Learning

Discuss these questions with the group and record your consensus answer.

- 117. Imagine that you roll two dice. Write down all the possible rolls that sum to 2. Write all the possible rolls that sum to 12. Write all the possible rolls that sum to 7. Which configuration has the greatest entropy: 2, 12, or 7?
- 118. If you roll one million dice, what will be the average of all the dice? If there is a room with one million dice and they all have a 1 on the top face, and there is an earthquake strong enough to roll dice around, what is the likelihood that after the earthquake all the top faces will sum to one million? To six million? How does this thought experiment illustrate the second law of thermodynamics?
- 119. Not all processes in which the system increases in entropy are spontaneous. How can this observation be consistent with the second law? Provide an example and explain your answer in complete sentences.
- **120.** Have each group member look up $\Delta H_{\rm f}^{\circ}$ and S° for one substance in the reaction:
- $3 O_2(g) + 6 H_2(g) + 6 C(s, graphite) \rightarrow C_6 H_{12} O_6(s, glucose)$. What is ΔH° for this reaction? What is ΔS° ? When is ΔH_f° for a substance equal to zero? When is S° for a substance equal to zero?
- **121.** Calculate ΔG° at 25 °C for the reaction in the previous question. Is this reaction spontaneous under standard conditions? How do you know? What is the determining factor: the change in energy or the change in entropy or both? Explain.

Data Interpretation and Analysis

122. Borax, sodium tetraborate decahydrate, is an important mineral found in dry lakebeds in California. It is used to make soap and glass, and used as a preservative. You can use the values of $K_{\rm sp}$ of borax at different temperatures to determine ΔH^o , ΔS^o , and ΔG^o for the dissolution of borax:

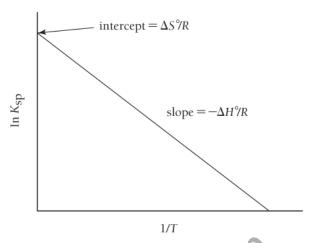
$$Na_2B_4O_5(OH)_4 \cdot 8 H_2O(s) \longrightarrow 2 Na^+(aq) + B_4O_5(OH)_4^{2-}(aq) + 8 H_2O(l)$$

(Borax) (Borate)

The relationship:

$$\ln\left(K_{\rm sp}\right) = \frac{-\Delta H^{\circ}}{RT} + \frac{\Delta S^{\circ}}{R}$$

has the form of a linear equation y = mx + b, where y is the $\ln K_{\rm sp}$ and x is 1/T. The slope is equal to $(\Delta H^\circ/R)$, and the y intercept is $\Delta S^\circ/R$, where R is the gas constant, 8.314 J/K mol. If you measure $K_{\rm sp}$ at several different temperatures, you can plot the lnK versus 1/T (T in kelvin) as shown here.



A Plot of $K_{\rm sp}$ versus 1/T where the Units of Temperature Are in Kelvin.

Knowing the values of ΔH° and ΔS° at a specific temperature allows the calculation of the change in Gibbs free energy for the reaction: $\Delta G^\circ = \Delta H^\circ - T \Delta S^\circ$.

The following table lists $K_{\rm sp}$ values for the dissolution of borax at several temperatures (°C).

 $K_{\rm sp}$ Values for the Dissolution of Borax at Several Temperatures (°C).

Temperature (°C)	$ extit{K}_{ ext{sp}}$		
40.0	0.041		
45.0	0.083		
50.0	0.264		
55.0	0.486		
60.0	0.552		

- **a.** Plot a graph of $\ln K_{\rm sp}$ versus 1/T (T in kelvin) and find the best-fitting line.
- **b.** Determine ΔH° . Is this process endothermic or exothermic?
- c. Determine ΔS°.
- **d.** Determine ΔH° at 298 K.
- e. Sketch a graph of ln K versus 1/T for an exothermic process.

Answers to Conceptual Connections

Cc 18.1 (a) The more spread out the particles are between the three boxes, the greater the entropy. Therefore, the entropy change is positive only in scheme (a).

Cc 18.2 \square Biological systems do not violate the second law of thermodynamics. The key to understanding this concept is realizing that entropy changes in the system can be negative as long as the entropy change of the universe is positive. Biological systems can decrease their own entropy, but only at the expense of creating more entropy in the surroundings (which they do primarily by emitting the heat they generate by their metabolic processes). Thus, for any biological process, ΔS_{univ} is positive.

Cc 18.3 ☐ (a) Sublimation is endothermic (it requires energy to overcome the intermolecular forces that hold solid carbon dioxide together), so ΔH is positive. The number of moles of gas increases when the solid turns into a gas, so the entropy of the carbon dioxide increases and ΔS is positive. Since $\Delta G = \Delta H - T \Delta S$, ΔG is positive

at low temperature and negative at high temperature.

Cc 18.4 ☐ Kr < Cl₂ < SO₃. Because krypton is a monoatomic gas, it has the least entropy. Because SO₃ is the most

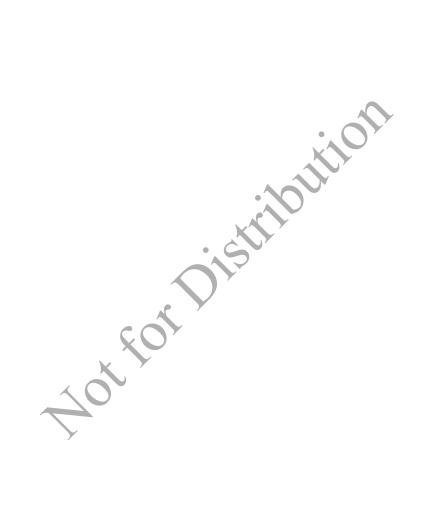
complex molecule, it has the most entropy. The molar masses of the three gases vary slightly, but not enough to overcome the differences in molecular complexity.

Cc 18.5 □ (a) A high concentration of reactants relative to products will lead to Q < 1, making the term RT ln Qin

Equation 18.14 \square negative. ΔG_{rxn} is more negative than $\Delta G_{\text{rxn}'}^o$ and the reaction is more spontaneous.

Cc 18.6 \Box (c) Since the equilibrium constant is less than 1, the reaction proceeds toward reactants under standard conditions (when Q = 1). Therefore, ΔG_{rxn}^{o} is positive.

Cc 18.7 $\triangle G_{\text{rxn}} < 0, Q < K$



Aot for Distribution

Aot for Distribution

Processing math: 100%