

1.

1. Given a point in motion we can detect its velocity by evaluating its distance traveled over time via $V_w = X_w - X_w' / T$.

As point X_w is $X_{avg}(|B|^2/B*\delta t)$ then we can equate V_w to as the average of the world velocity * $(|B|^2/B*\delta t)$ – the original point * change in δt /change in time

This can be written as

$$V_{avg}(|B|^2/B*\delta t) - X_w(B*(d\delta t/dt)/B*\delta t) = V_w$$

2.

$$X_w = \text{Avg}(X_l, X_r) * b^2 / B * \delta t$$

$$\text{Avg}(X_l, X_r) = [0, 2t, 0, f]$$

$$X_w = [0, 2t, 0, f] * [\delta t * b, 0, 0] - [0, 2t, 0, f] * [\delta t * b, 0, 0]$$

$$V_w = [0, 0, 0, 0]$$

2.

1. a) $p(x, y) = 2x$ $q(x, y) = 2y$

- b) $p(x, y) = 2y$ $q(x, y) = 2x$

2. Given rotationally symmetric over reflectance such that $x = y$ at a 90° rotation.

The above equations are equivalent such that if $x' = y$ and $y' = x$

- c) $p(x', y') = 2x' = 2y$ $q(x', y') = 2y' = 2x$

- d) $p(x', y') = 2y' = 2x$ $q(x', y') = 2x' = 2y$

here the equation c is equivalent to equation b and a equal to d

3. The vector X_k has two parts that of the pose x_{vk} and set of map locations m .

$$\text{As } P_{k-1|k-1} = [[P_{vv} \ P_{vm}][P_{vm}^T \ P_{mm}]]$$

$$\text{and } P_{k|k-1} = \nabla f_x P_{k-1|k-1} \nabla f_x^T + \nabla f_u U_k \nabla f_u^T$$

where $\nabla f_{vx} = \partial f_v / \partial x_{vk-1}$ and $\nabla f_{vu} = \partial f_v / \partial u_k$,

The pose only changes relative to $P_{k|k-1}$ in terms of v , m .

P_{vv} is equivalent to $P_{k|k-1}$ in terms of $P_{k-1|k-1}$.

and P_{mm} is equivalent to P_{mm} in terms of $P_{k-1|k-1}$

As P_{vm} and P_{mv} are relative to the pose of a robot it is scaled to ∇f_{vx} (transpose for P_{mv})

Therefore the covariance prediction must simplify to

$$P_{k|k-1} = [[\nabla f_x P_{k-1|k-1} \nabla f_x^T + \nabla f_u U_k \nabla f_u^T \quad \nabla f_{vx} P_{vv, k-1|k-1}, \\ [P_{Tvv, k-1|k-1} \nabla f_{vx}^T \quad P_{mm, k-1|k-1}]]$$