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1.

Similar:

- Can compute images with multiple lenses (or two eyes)
- Both taken images are inverted
- Both have the functionality of controlling aperture via a hole in the lens or pupil
- Both (typically) have curved lenses
- Both have a limited field of vision (the range may vary but still limited)

Different:

- Cameras' record images for later viewing, eyes don't (or at least not in reliable high quality)
- Cameras don't have a "blind spot," while eyes do
- Camera's have an easily adjustable wide range shutter speed, while eyes do not
- Eyes can dry out while cameras typically cannot
- Eyes have cones and rods while Cameras have film or a photon sensor

2.

world point, $X_w = [x_w, y_w, z_w]$, camera point $X_c = [x_c, y_c, z_c]$, focal vector $F = [0, 0, f]$.

A ray leaving X_w with a slope of 0 (or parallel to the z axis), such that the slope of the bend from X_w to $X_c = 0 + -r/f$, as $-r = y_w$. If the image is in focus then, there is no blur circle, such that X_c can be linearly transformed to point X_w by the magnification M .

As $z_c = f$, and X_w and X_c are relative to each other by $M = f/z_w$ such that $X_c = M * X_w$.
Then $X_w = X_c / M = X_c * M^{-1}$

Therefore the image must be in focus when $X_w = X_c / M = X_c * M^{-1}$ and $X_c = M * X_w$

if $y_w/z_w = y_c/z_c$ (ratios are the same)
then $y_w/y_c = -z_w/z_c = -z_w/f = M^{-1}$

if $-y_c/f = y_c + y_w / z_w$

then $-y_c * x_w / (y_c + y_w) = f$

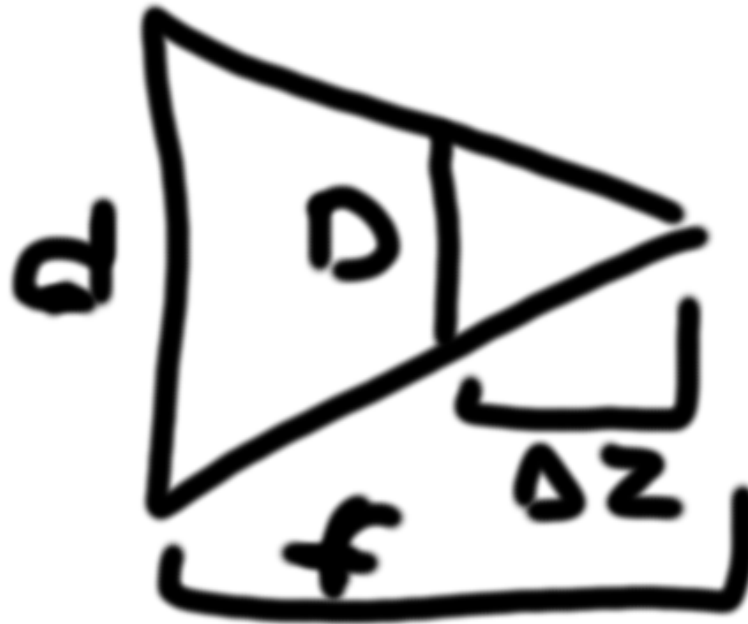
then $1/f = (y_c + y_w) / -y_c * z_w$
 $1/f = y_c / -y_c * z_w + y_w / -y_c * z_w$
 $1/f = 1 / -z_w + y_w / y_c * z_w$
 $1/f = 1 / -z_w + y_c / y_c * z_c$
 $1/f = 1 / -z_w + 1 / z_c$

Then $1 / -z_w + 1 / z_c = 1 / f$

Therefore the image must be in focus when $1 / -z_w + 1 / z_c = 1 / f$

3.

A ray leaving X_w with a slope of 0 (or parallel to the z axis), such that the slope of the bend from X_w to $X_c = 0 + -r/f$, as $-r = y_w$. As the equation is reversible it also applies to X_c to X_w therefore the lens of the diameter, d , is a scalar to determine the base size of the blur circle.



As the camera point shifts by Δz , either positively or negatively as the rays from X_w continue to form a circle in a radius determined by the ratio of the magnification and the point shift.

Assume the rays from X_w produce an equalateral triangle through a lens with diameter d . then the height of the triangle at perfect focus is z_c and the point $|\Delta z|$ determines the height of the cross section to be taken.

Therefore the ratio $D/d = \Delta z / f$

As such $D = d(\Delta z / f)$

4.

a)

a) $2\pi r^2 = \text{surface area} = 9\text{cm}^2 = 90\text{ mm}^2$

b) $150000000/90 \approx 1666666 \text{ receptors per mm}^2$

b) $y_w/z_w = y_c/z_c$

a) $z_w = 225000000\text{km}$

b) $f = z_c = 2.4\text{cm} = 0.00024\text{km}$

c) $y_w = 8000\text{km}$

d) $y_c = y_w/z_w * z_c = 8.5 \times 10^{-10}\text{km}$

e) $8.5 \times 10^{-10} * 1000000 = 0.00085$

f) $0.00085 * 1666666 \approx 1416 \text{ receptors}$

5.

R_w projects onto L_c iff every element in R_w projects onto L_c .

if s_c is a projection of s_w and t_c is a projection of t_w then by definition all elements of s_w is mapped to s_c and t_w to t_c .

$$R_w = [1, A]$$

$$L_c = [1 - B, B]$$

IFF, B is not negative or greater than 1 and related to A by the magnification of the lens, is L_c a projection of R_w