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 HW11
 11/22/19
 CS549

1.

1. as $f \cdot b = 0$, $R = I$, and $T = \pm B/2$

$$E = (|XL' - XL|)^2 + (|XR' - XR|)^2$$

$$XL = f \cdot XCL / F \cdot XCL = f^2(Xw + b/2) / f(Xw + b/2)$$

as X is a vector it can be separated into its core components of x, y, z such that:

$$X = f/z(x + b/2), fy/z$$

Here we will consider X_L is positive and X_R we will consider negative. as such we can substitute XL and XR from the original equation

$$E = (f/zw(xw + b/2) - xL)^2 + (f/zw(yw) - yL)^2 + (f/zw(xw - b/2) - xR)^2 + (f/zw(yw) - yR)^2$$

$$2. E \, d/xw = 2(f/zw(xw + b/2) - xL)(f/zw) + 2(f/zw(xw - b/2) - xR)(f/zw)$$

$$E \, d/xw = (zw/f) \cdot (xw - xL - xw - xR) / 2$$

$$E \, d/xw = (zw/f) \cdot ((xL + xR) / 2)$$

$$E \, d/yw = 2(f/zw(yw + b/2) - yL)(f/zw) + 2(f/zw(yw - b/2) - yR)(f/zw)$$

$$E \, d/yw = (zw/f) \cdot (yw - xL - yw - yR) / 2$$

$$E \, d/yw = (zw/f) \cdot ((yL + yR) / 2)$$

3.

$$E \, d/zw = 2(f/zw)(-2fzw) + 2(f/zw)(-2fzw)(xL - xR)$$

$$E \, d/zw = 2(f^2B/F/zw)(-4Fzw)\delta$$

$$E \, d/zw = 2(f^2B/F/zw)(-4Fzw)\delta$$

$$= (B \cdot \delta / F \cdot zw)(Fzw) = X_{avg}(B^2 / \delta \cdot b)$$

2. As X world is the average of the reference images and the change in X . then as X_r is the reference for X_w then X_l is the translation of the reference image by the average of B . as there are two images then it is translated by $B/2$.

3.

$$\min(X_{wl} - X_{wr})^2$$

$$= \min(-b/2 + lX_l - b/2 + rX_r)^2$$

$$= \min(-B + lX_l - rX_r)^2$$

$$= \text{avg}(X_l(X_r) + X_r(X_l) / X_l X_r)$$

$$= 1/2(X_l(X_r) + X_r(X_l) / X_l X_r)$$

$$= 1/2(X_l(X_r) + X_r(X_l)) / (X_l^2 X_r^2 - (X_l \cdot X_r)^2)$$

as $X_l(X_r)$ is the similarity between the two images, we take the inverse of the difference and add them to each image

$$X_l(X_r) = (X_r^2(X_l \cdot B) - X_l \cdot X_r(X_r \cdot B))X_l$$

$$X_r(X_l) = (X_l^2(X_r \cdot B) - X_r \cdot X_l(X_l \cdot B))X_r$$

$$\text{Therefore } \min(X_{wl} - X_{wr})^2 =$$

$$1/2((X_r^2(X_l \cdot B) - X_l \cdot X_r(X_r \cdot B))X_l + (X_l^2(X_r \cdot B) - X_r \cdot X_l(X_l \cdot B))X_r) / (X_l^2 X_r^2 - (X_l \cdot X_r)^2)$$