Spatial Data Structures

Types of Queries

- Graphic applications often require spatial queries
 - Find the k points closer to a specific point p (k-Nearest Neighbours, knn)
 - Is object X intersection with object Y? (Intersection)
 - What is the volume of the intersection between two objects?
- Brute force search is expensive. Instead, you can solve these queries with an initial preprocessing that creates a data structure which supports efficient queries
- The data structure to use is application-specific



Two Main Ideas

- 1. You can explicitly index the space itself (Spatial Index)
- 2. You can "sort" the primitives in the scene, which implicitly induces a partition of the space (Bounding Volume Hierarchies)

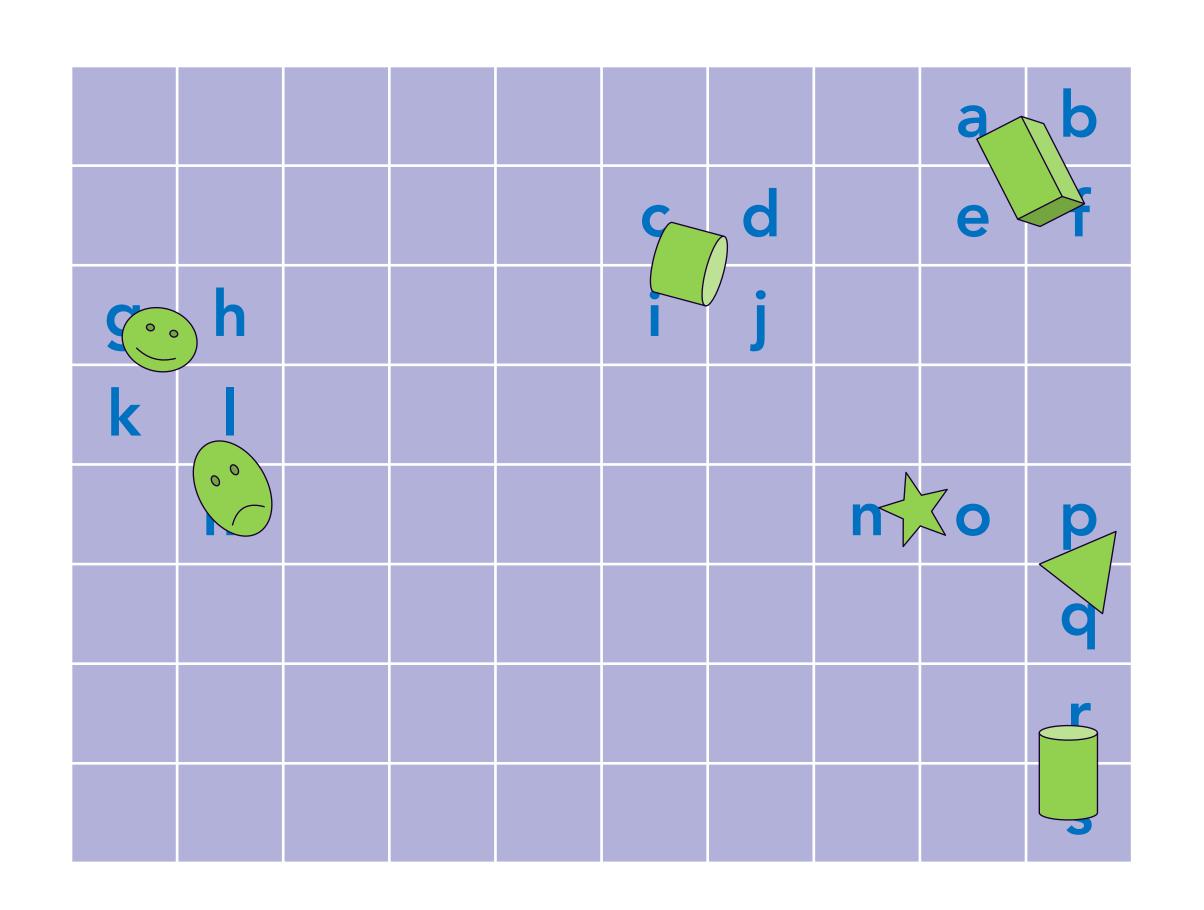
Spatial Indexing Structures

Spatial Indexing Structures

- Data structures to accelerate queries of the kind: "I'm here. Which object is around me?"
- Tasks:
 - (1) construction / update
 - for static parts of the scene, a preprocessing.
 - for moving parts of the scene, an update.
 - (2) access / usage
 - as fast as possible
- The most common structures are:
 - Regular Grid
 - kD-Tree
 - Oct-Tree/Quad-Tree
 - BSP Tree



Regular Grid (aka lattice)



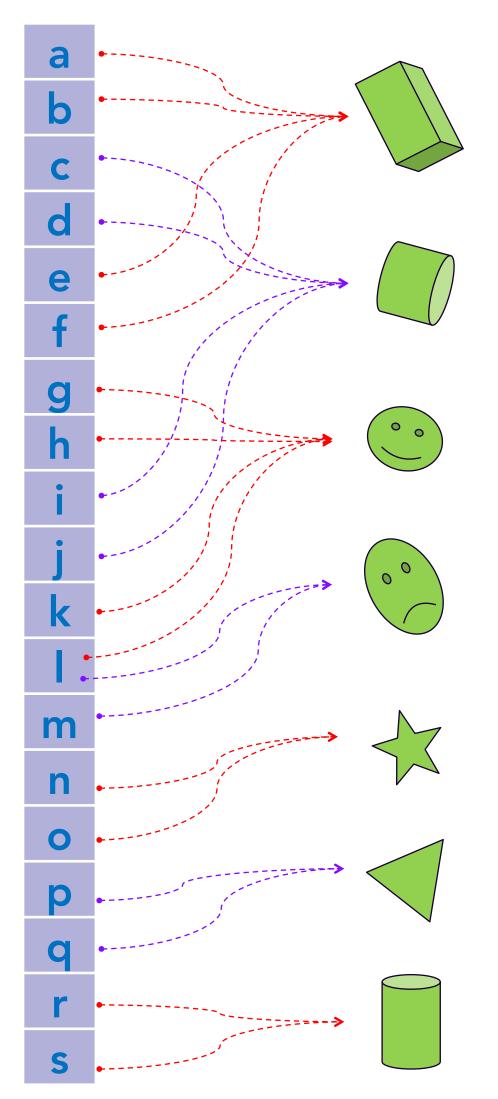


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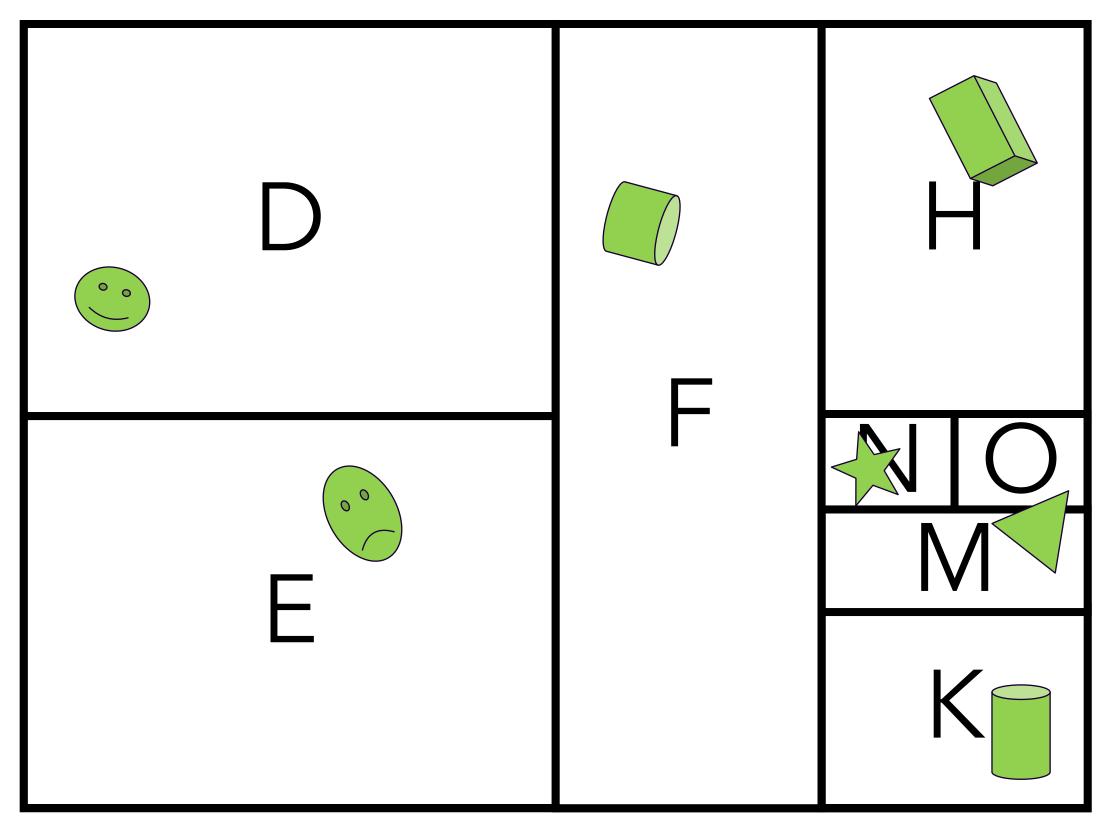
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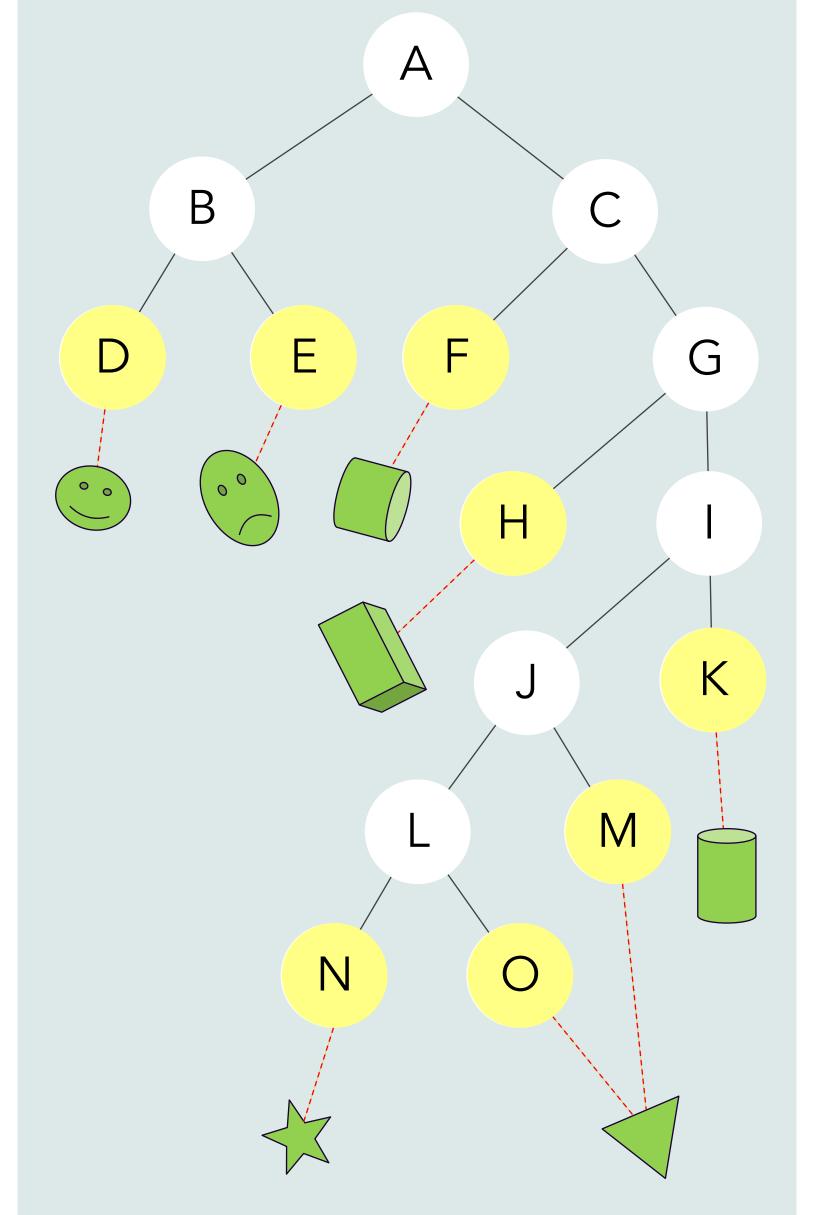
Regular Grid (or: lattice)

- Array 3D of cells (same size)
 - each cell: a list of pointers to colliding objects
- Indexing function:
 - Point3D ∩ cell index, (constant time!)
- Construction: ("scatter" approach)
 - for each object B[i]
 - find the cells C[j] which it touches
 - add a pointer in C[j] to B[i]
- Queries: ("gather" approach)
 - given a point to test *p*, find cell C[j], test all objects linked to it
- Problem: cell size
 - too small: memory occupancy too large quadratic with inverse of cell size!
 - too big: too many objects in one cell
 - sometimes, no cell size is good enough



kD-tree







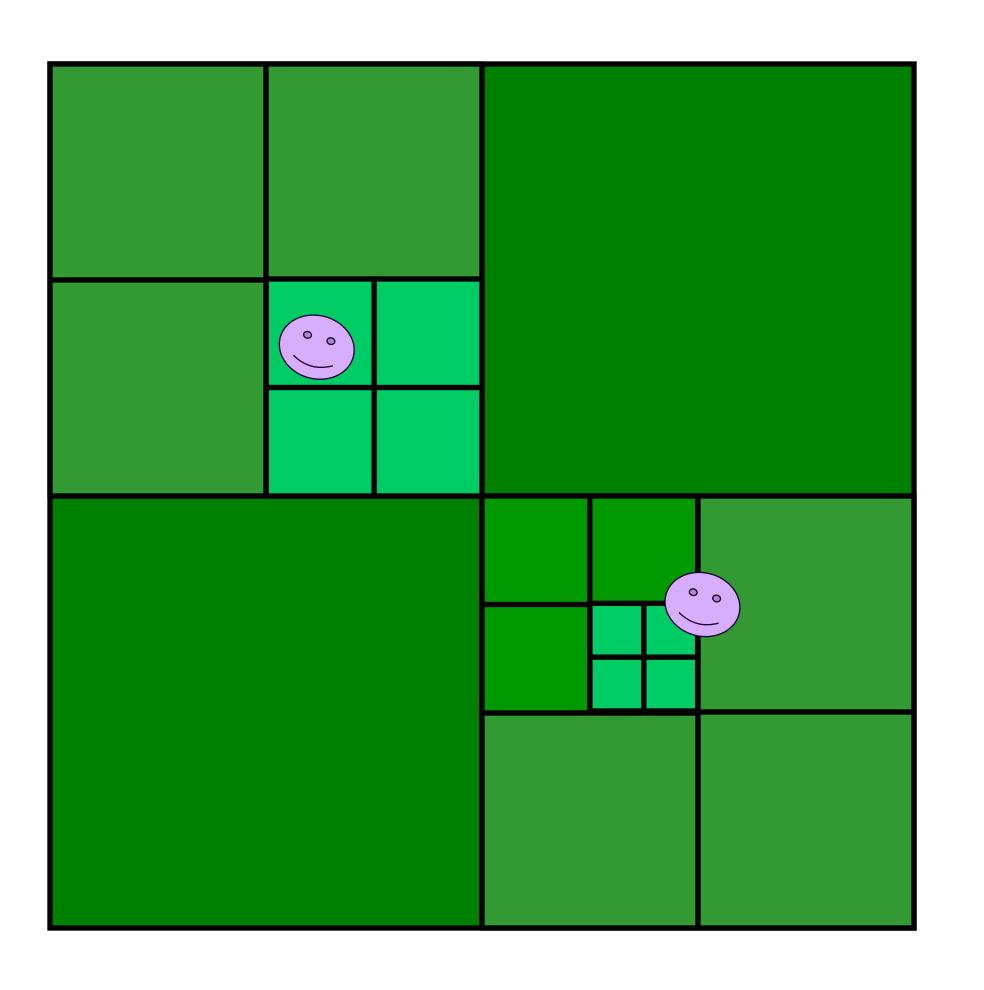
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kD-trees

- Hierarchical structure: a tree
 - each node: a subpart of the 3D space
 - root: all the world
 - child nodes: partitions of the father
 - objects linked to leaves
- kD-tree:
 - binary tree
 - each node: split over one dimension (in 3D: X,Y,Z)
 - variant:
 - each node optimizes (and stores) which dimension, or
 - always same order: e.g. X then Y then Z
 - variant:
 - each node optimizes the split point, or
 - always in the middle

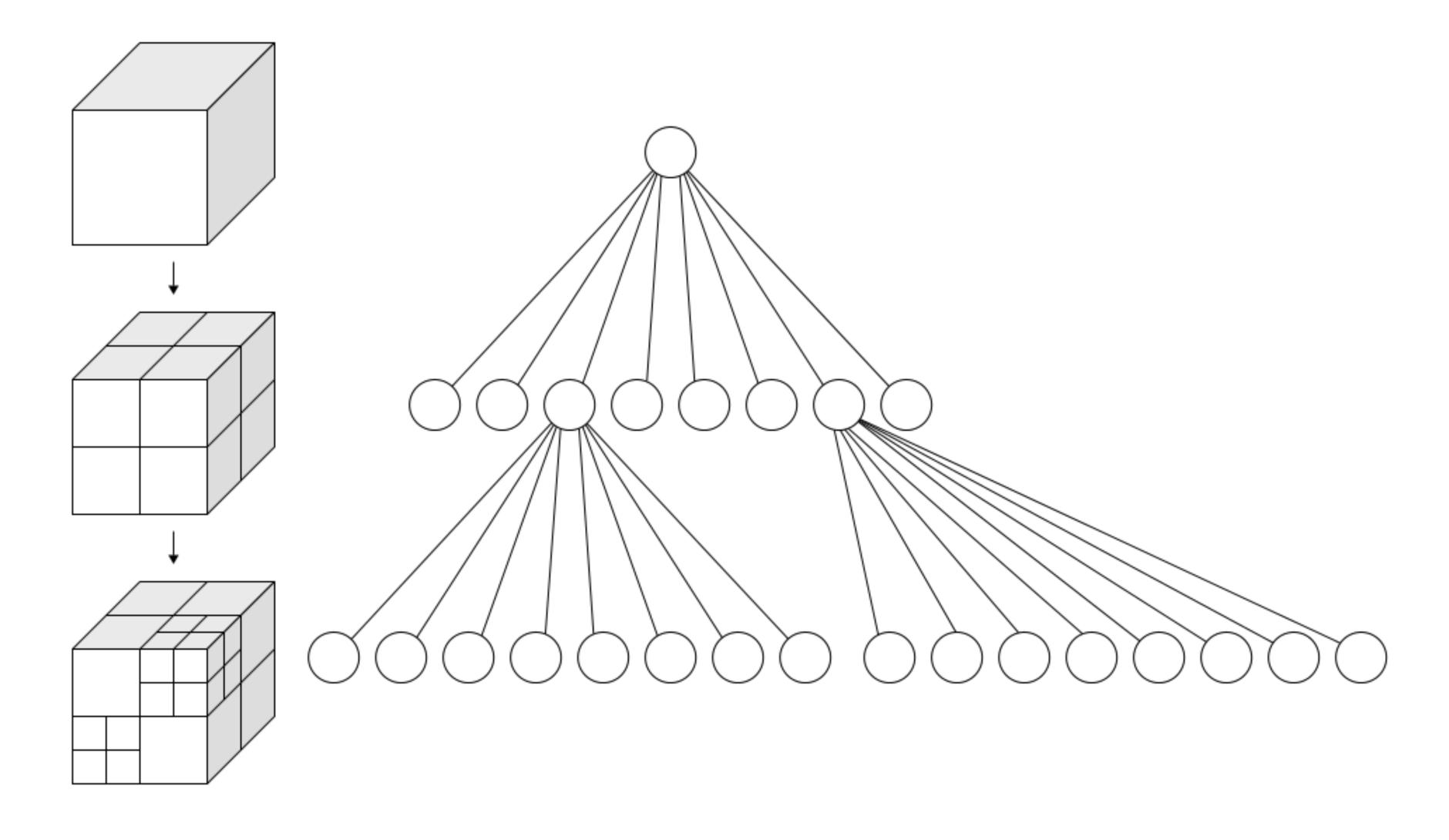


Quad-Tree (2D)





Oc-Tree (3D)

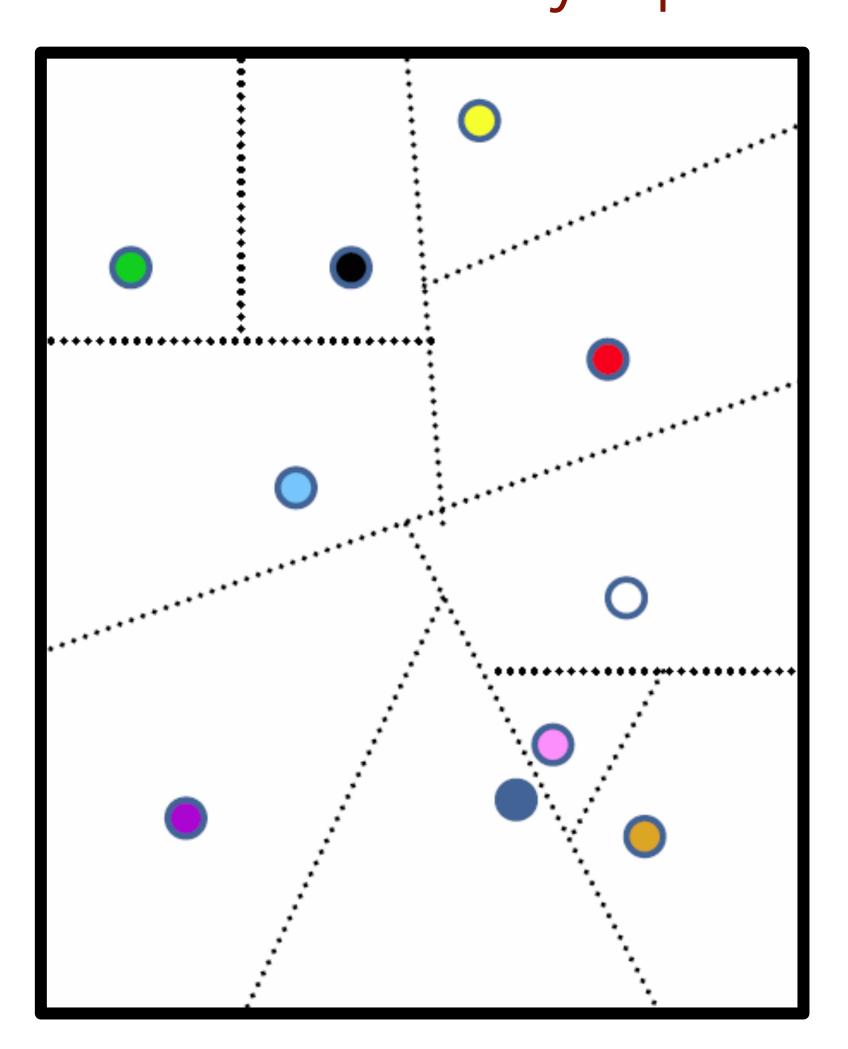




Quad trees (in 2D) Oct trees (in 3D)

- Similar to kD-trees, but:
 - tree: branching factor: 4 (2D) or 8 (3D)
 - each node: splits into all dimensions at once, (in the middle)
- Construction (just as kD-trees):
 - continue splitting until a end nodes has few enough objects (or limit level reached)

BSP-tree Binary Spatial Partitioning tree



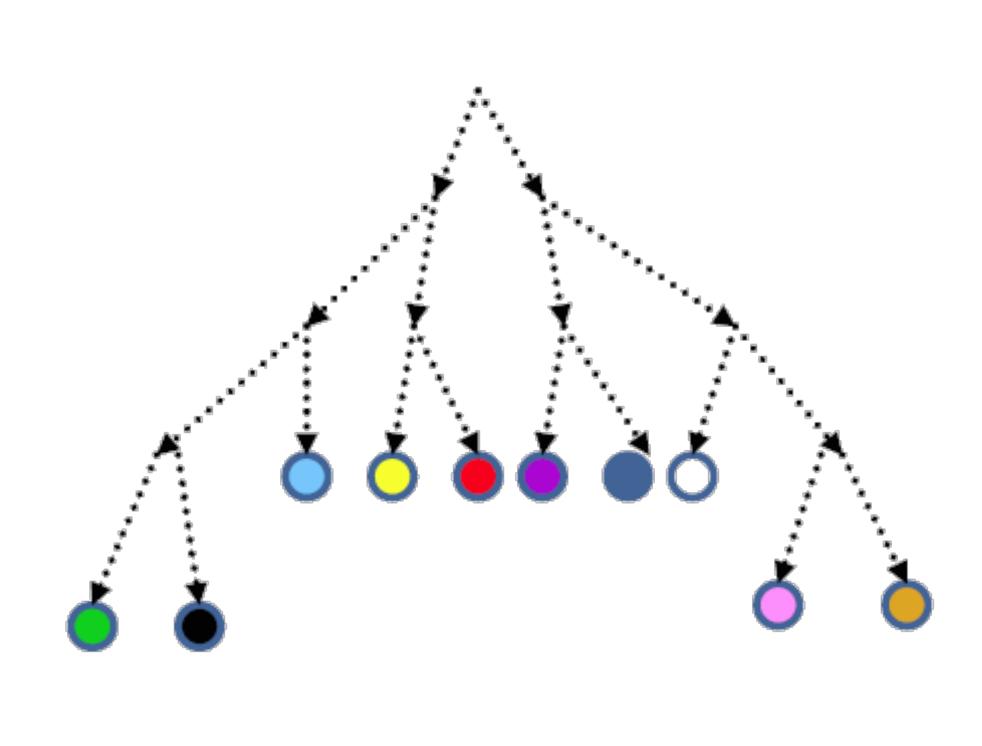
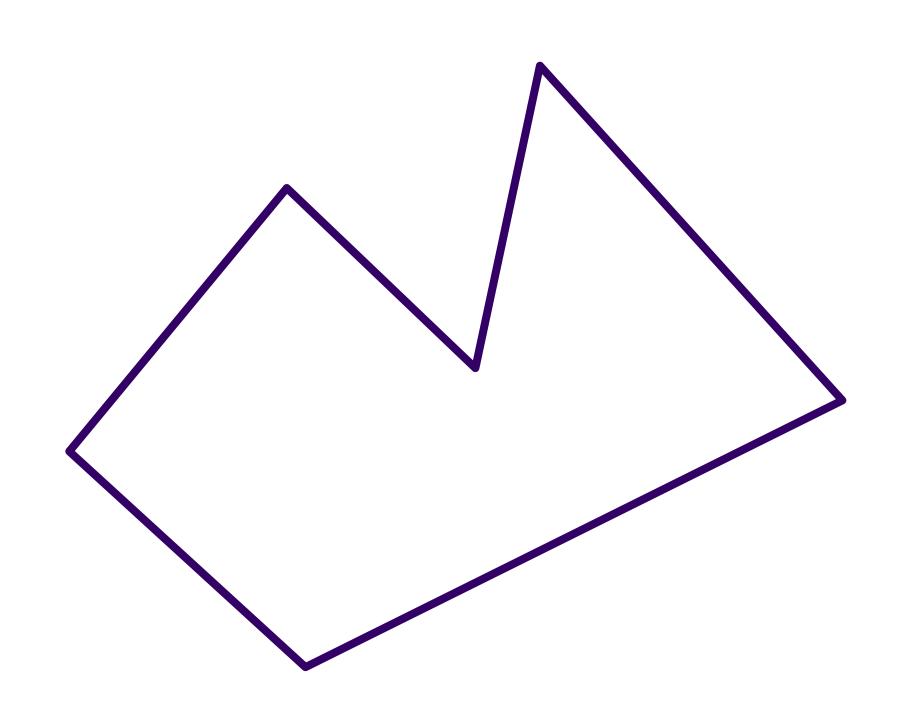


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BSP-trees for the Concave Polyhedron proxy





BSP-trees for Inside-Outside Test

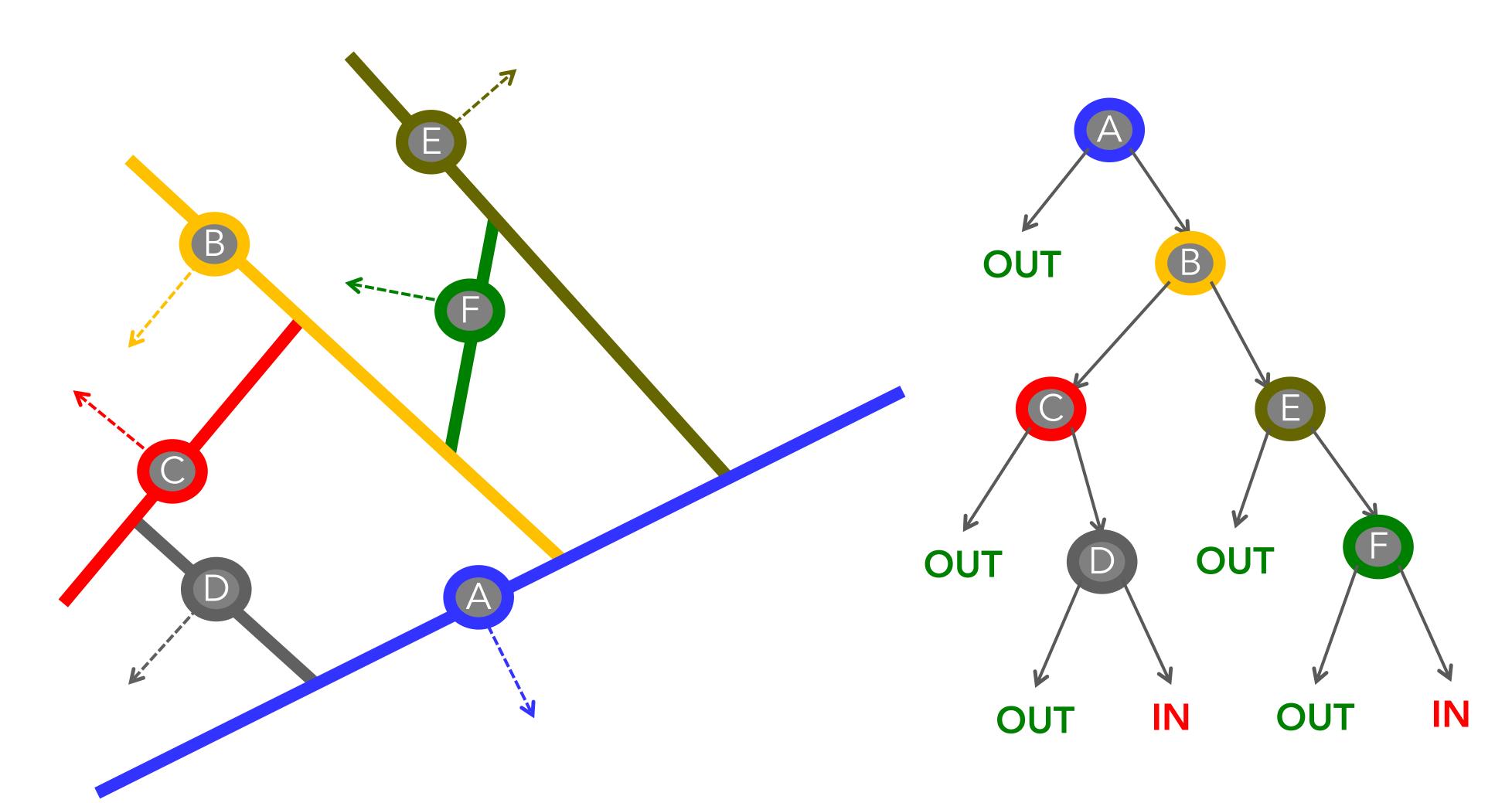


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BSP-tree

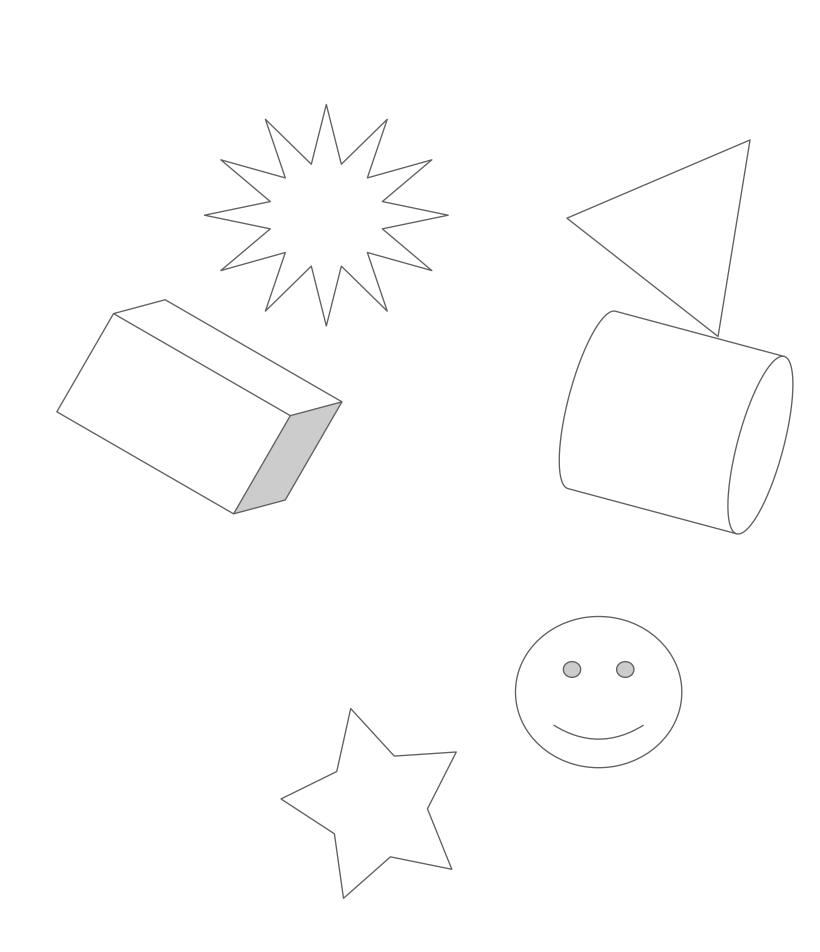
Binary Spatial Partitioning tree

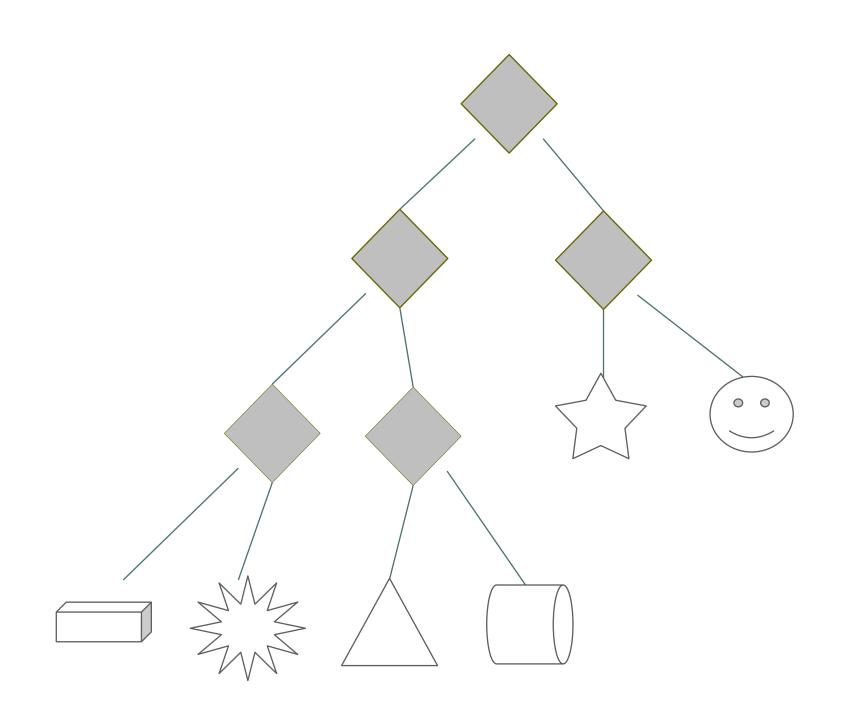
- Another variant
 - a binary tree (like the kD-tree)
 - root = all scene (like kD-tree)
 - but, each node is split by an arbitrary plane
 - (or a line, in 2D)
 - plane is stored at node, as (nx, ny, nz, k)
 - planes can be optimized for a given scene
 - e.g. to go for a 50%-50% object split at each node
- Another use: to test (Generic) Polyhedron proxy:
 - note: with planes defined in its object space
 - each leaf: inside or outside
 - (no need to store them: left-child = in, right-child = out)
 - tree precomputed for a given object



Primitive Sorting Structures

Bounding Volume Hierarchies (BVH)

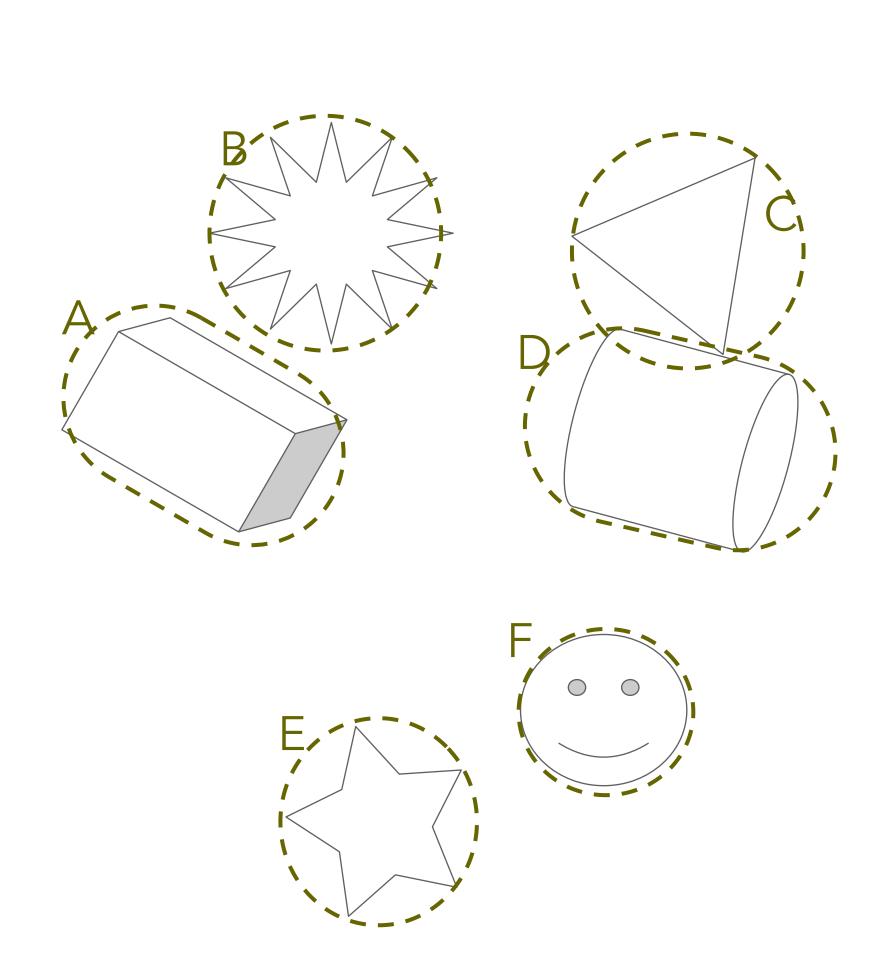








Bounding Volume Hierarchies (BVH)



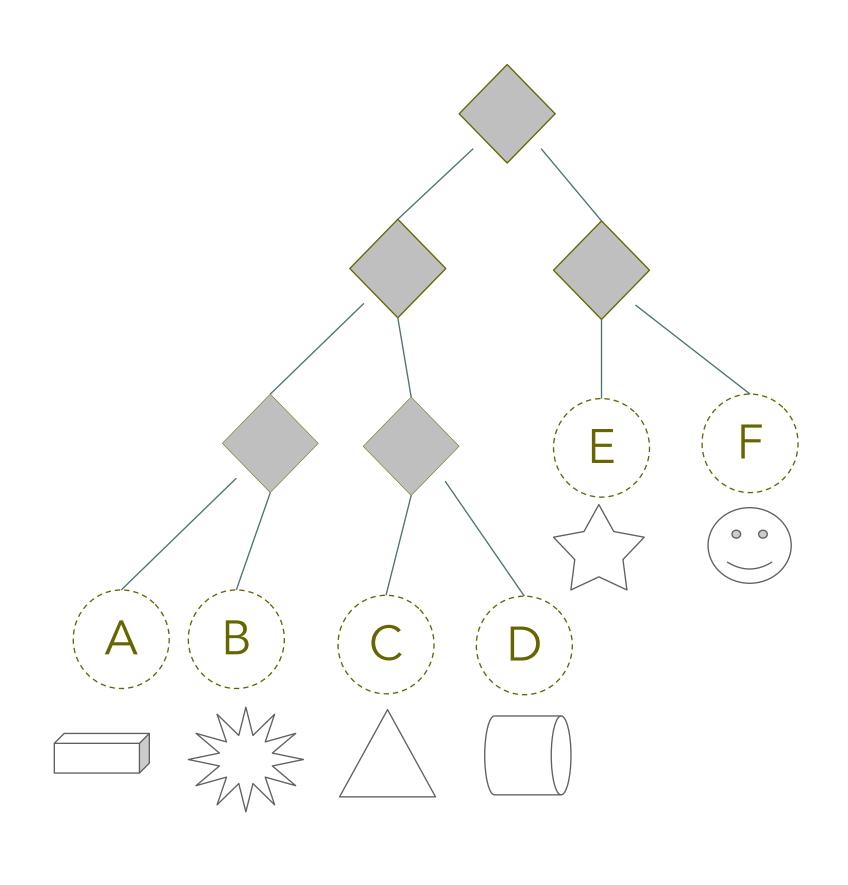


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Bounding Volume Hierarchies (BVH)

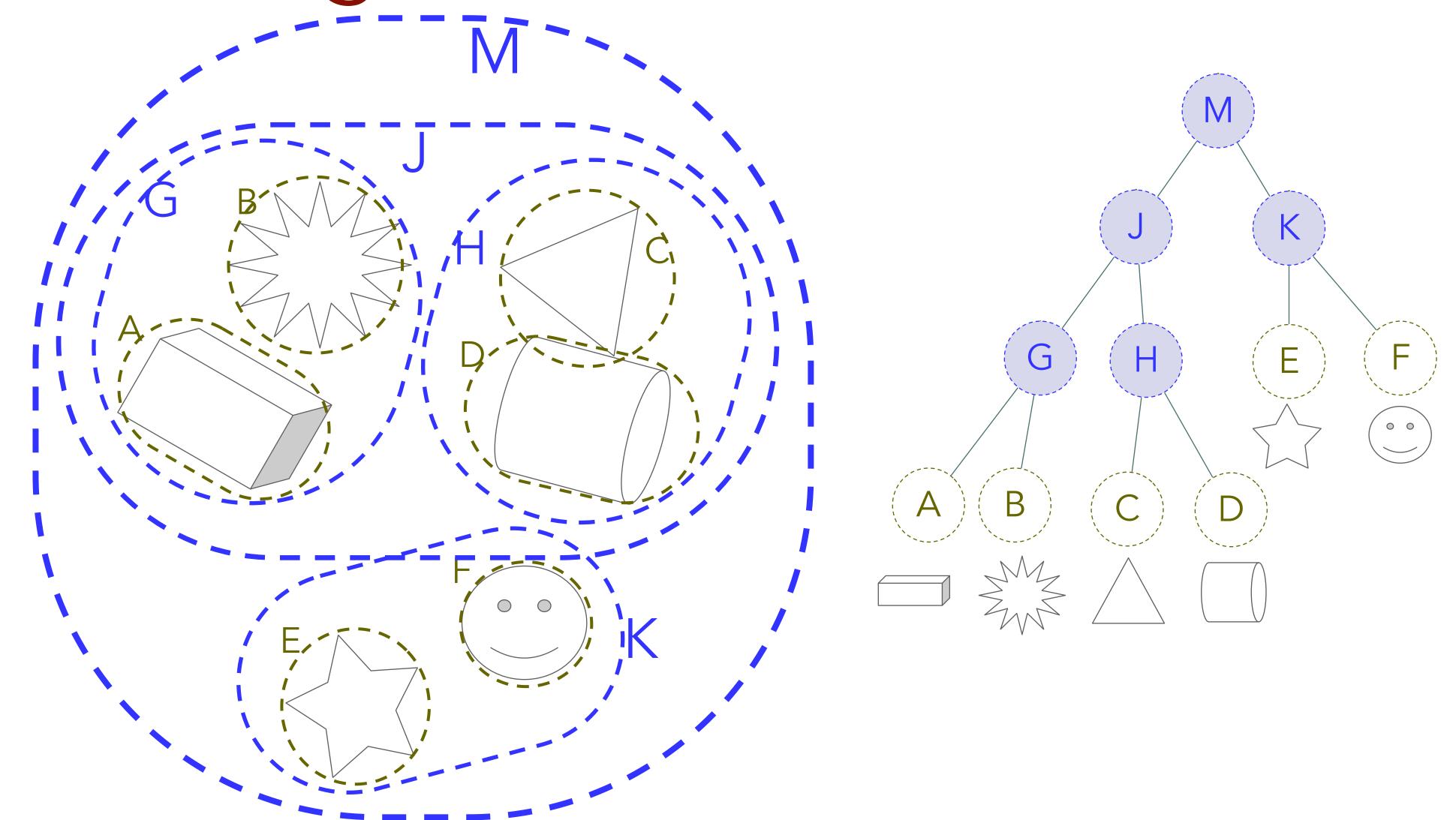


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BVH

Bounding Volume Hierarchy

- Idea: use the scene hierarchy given by the scene graph
 - (instead of a spatial derived one)
- associate a Bounding Volume to each node
 - rule: a BV of a node bounds all objects in the subtree
- construction / update is fast
 - bottom-up: recursive
- using it:
 - top-down: visit
 - note: **not** a single root to leaf path
 - may need to follow multiple children of a node (in a BSP-tree: only one)



Spatial Indexing Structures

- Regular Grid
 - the most parallelizable (to update / construct / use)
 - constant time access (best!)
 - quadratic / cubic space (2D, 3D)
- kD-tree, Oct-tree, Quad-tree
 - compact
 - simple
 - non constant accessing time (still logarithmic on average)
- BSP-tree
 - optimized splits! best performance when accessed
 - optimized splits! more complex construction / update
 - ideal for static parts of the scene
 - (also, used for generic polyhedron inside/outside test)
- BVH
 - simplest construction
 - non necessarily very efficient to access
 - may need to traverse multiple children
 - if you do not have a scene-graph you need to create one
 - ideal for dynamic parts of the scene



Intersection Acceleration Data Structures



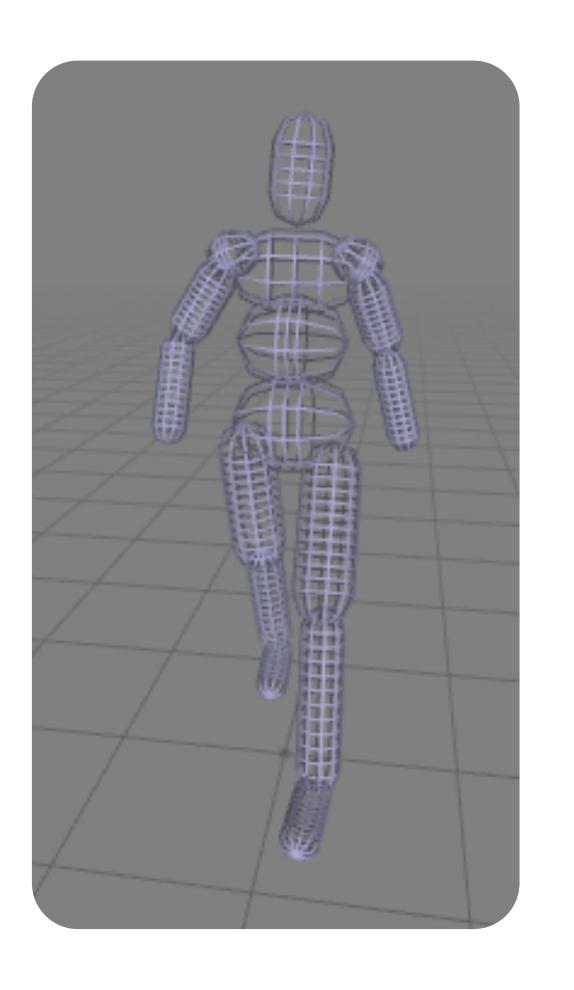
Collision Detection

- It is easy to do, the challenge is to do it efficiently
- An observation:
 - most pair of objects do not intersect each other in a scene,
 collisions are rare
 - optimizing the intersections directly is important but not sufficient, we need to optimize the detection of non intersecting pairs ("early rejects")

Geometric Proxies

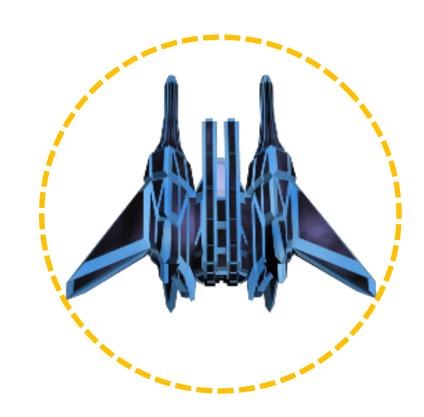
• Idea: use a geometric proxy to approximate the objects in the scene





Geometric Proxy

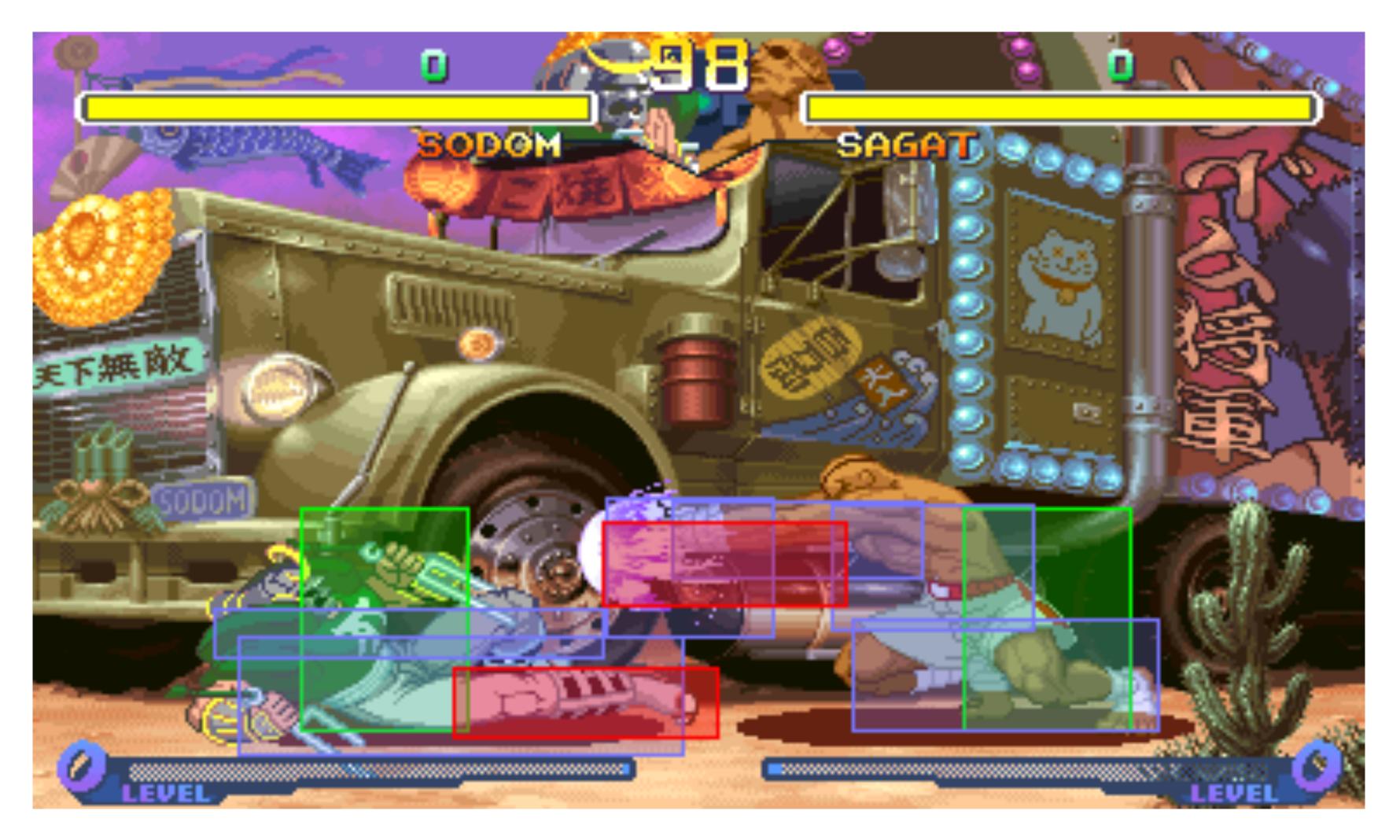
- Extremely coarse approximation
- Used as a:
 - Bounding Volume
 - the entire object must be contained inside
 - exact result, you need to do more work if you detect a collision
 - Collision Object (or "hit-box")
 - approximation of the object
 - no need to do anything else if an approximation is ok for your use case







Example: Fighting Games

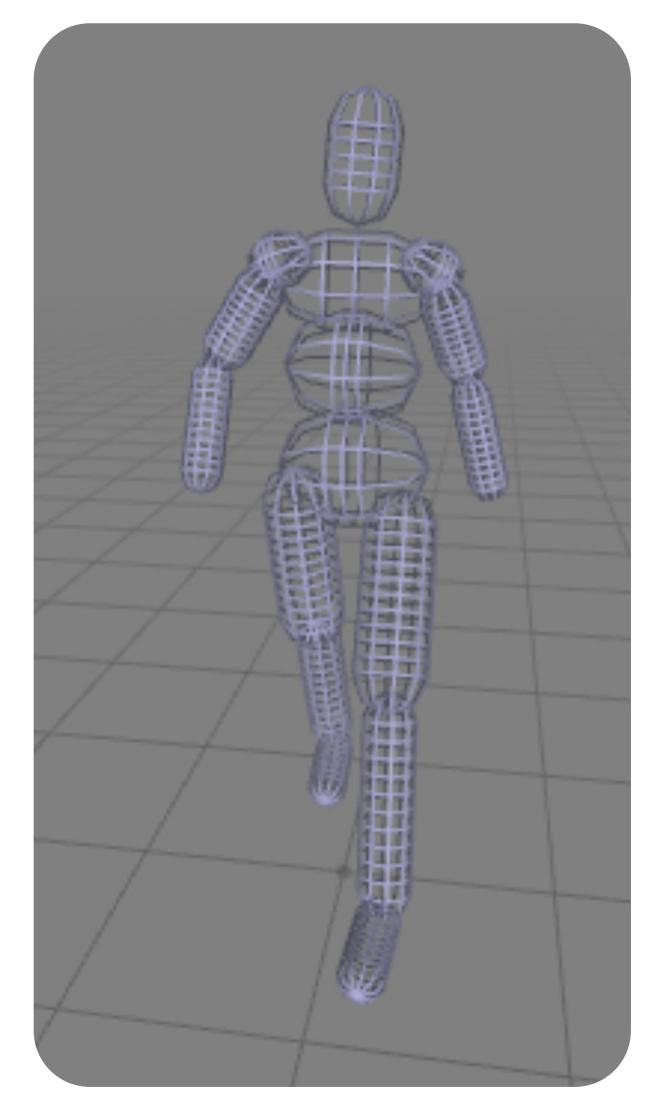


Street Fighter Alpha, CAPCOM 1995



Extremely Common

- Physic engine
 - collision detection
 - collision response
- Rendering
 - view frustum culling
 - occlusion culling
- A
 - visibility test
- GUI
 - picking



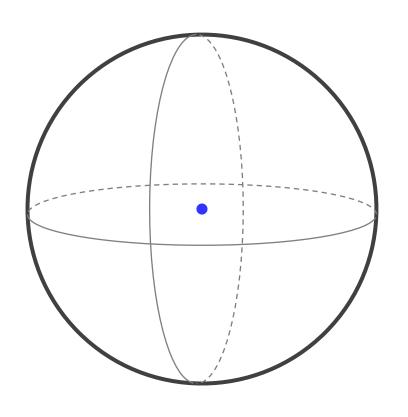
Properties of Geometric Proxies

- 1. How expensive are they to compute/update?
- 2. How much space do you need?
- 3. Are they invariant to the transformations applied on the object?
- 4. How good is the approximation?
- 5. How expensive are the collision queries with the other objects in the scene?



Geometry Proxies: Sphere

- Easy to compute and update
- Compact (center, radius)
- Very efficient collision tests
- Can only be transformed rigidly
- The quality of the approximation is low



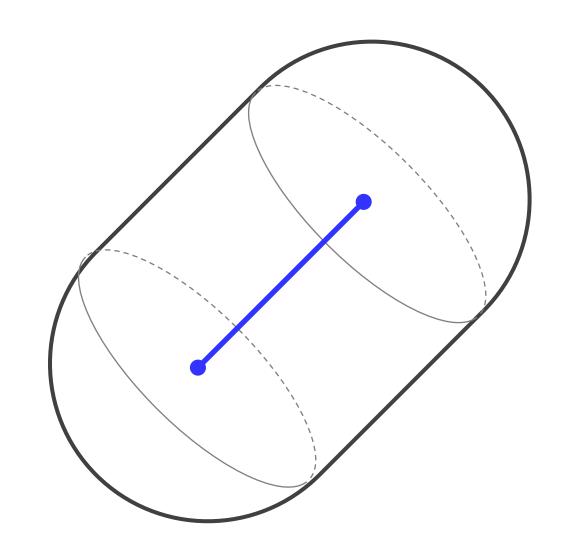
Geometry Proxies: Capsule

• Def:

- Sphere ==
 set of all points with dist from a point < radius
- Capsule ==
 set of all points with dist from a segment < radius
 - i.e. a cylinder ended with two half-spheres (all same radius)

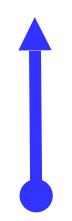


- a segment (two end-points)
- a radius (a scalar)
- Popular option, compact to store, easy to construct, easy to detect intersections, good approximation



Geometry Proxies: Half Space

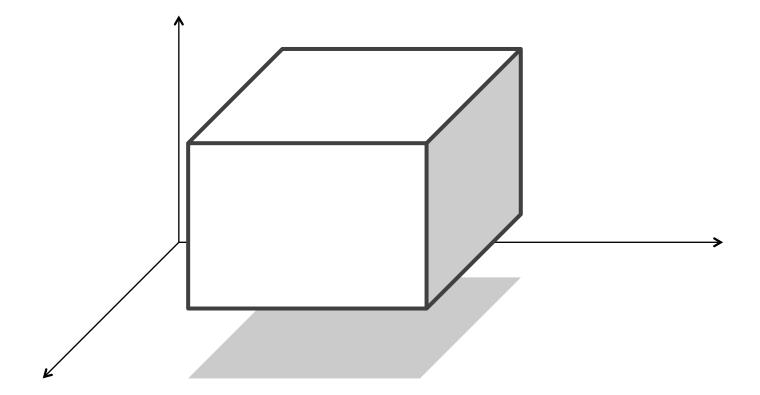
- Trivial, but useful
 - e.g. for a flat terrain, or a wall
- Storage:
 - (nx, ny, nz, k)
 - a normal, a distance from the origin
- Tests are trivial





Geometry Proxies: Axis-Aligned Bounding Box (AABB)

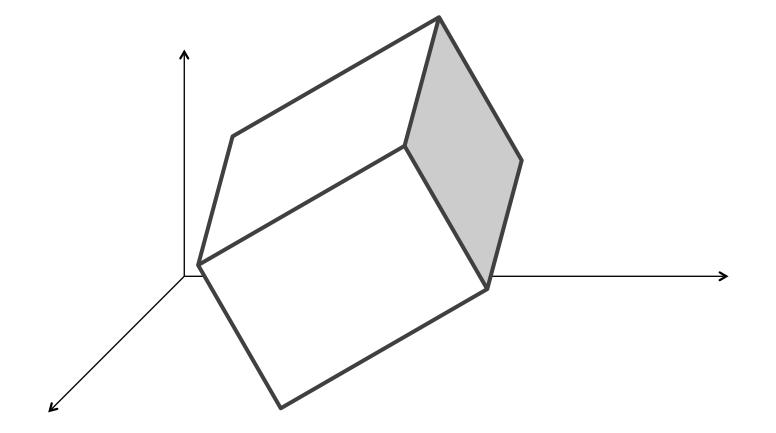
- Easy to update
- Compact (three intervals)
- Trivial to test



• It can only be translated or scaled, rotations are not supported

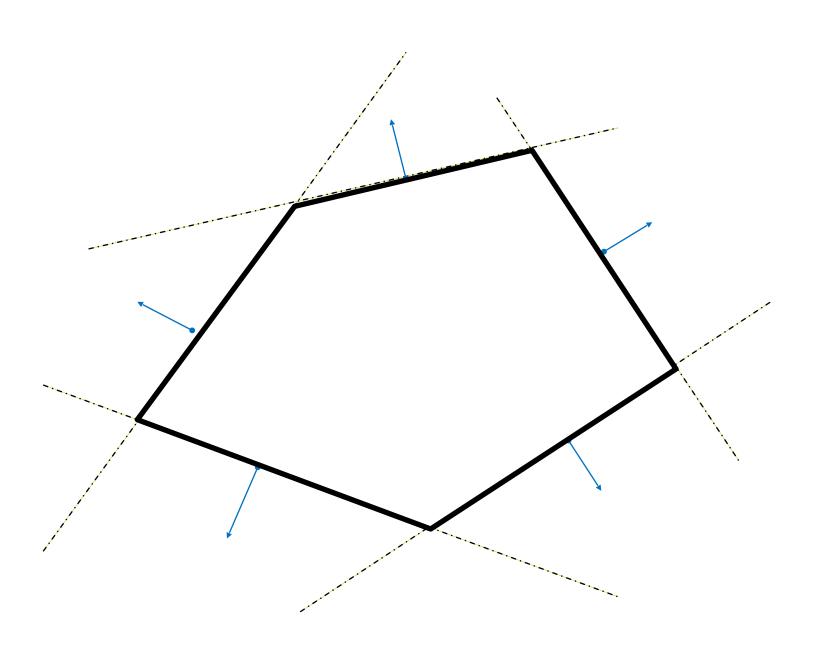
Geometry Proxies: Box

- Similar to AABB, but not axisaligned
- More expensive to compute and store
 - You need intervals and a rotation
- Still not a great approximation, but it is invariant to rotations and it is fast to compute and use



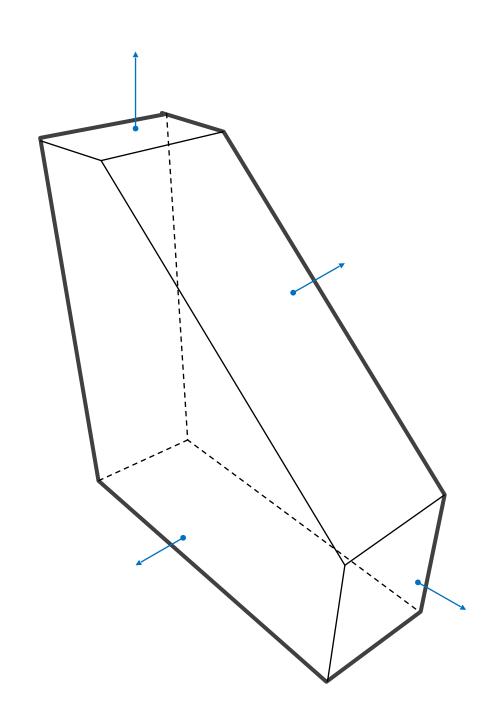
Geometry Proxies (in 2D): Convex Polygon

- Intersection of half-planes
 - each delimited by a line
- Stored as:
 - a collection of (oriented) lines
- Test:
 - a point is inside iff
 it is in each half-plane
- Good approximation
- Moderate complexity



Geometry Proxies (in 3D): Convex Polyhedron

- Intersection of half-spaces
- Similar as previous, but in 3D
 - Stored as a collection of planes
 - Each plane is a normal + distance from origin
 - Test: inside proxy iff inside each half-space





Geometry Proxies (in 3D): (General) Polyhedron

- Luxury Hit-Boxes:)
 - The most accurate approximations
 - The most expensive tests / storage
- Specific algorithms to test for collisions
 - requiring some preprocessing
 - and data structures (BSP-trees)
- Creation (as meshes):
 - sometimes, with automatic simplification
 - often, hand made (low poly modelling)

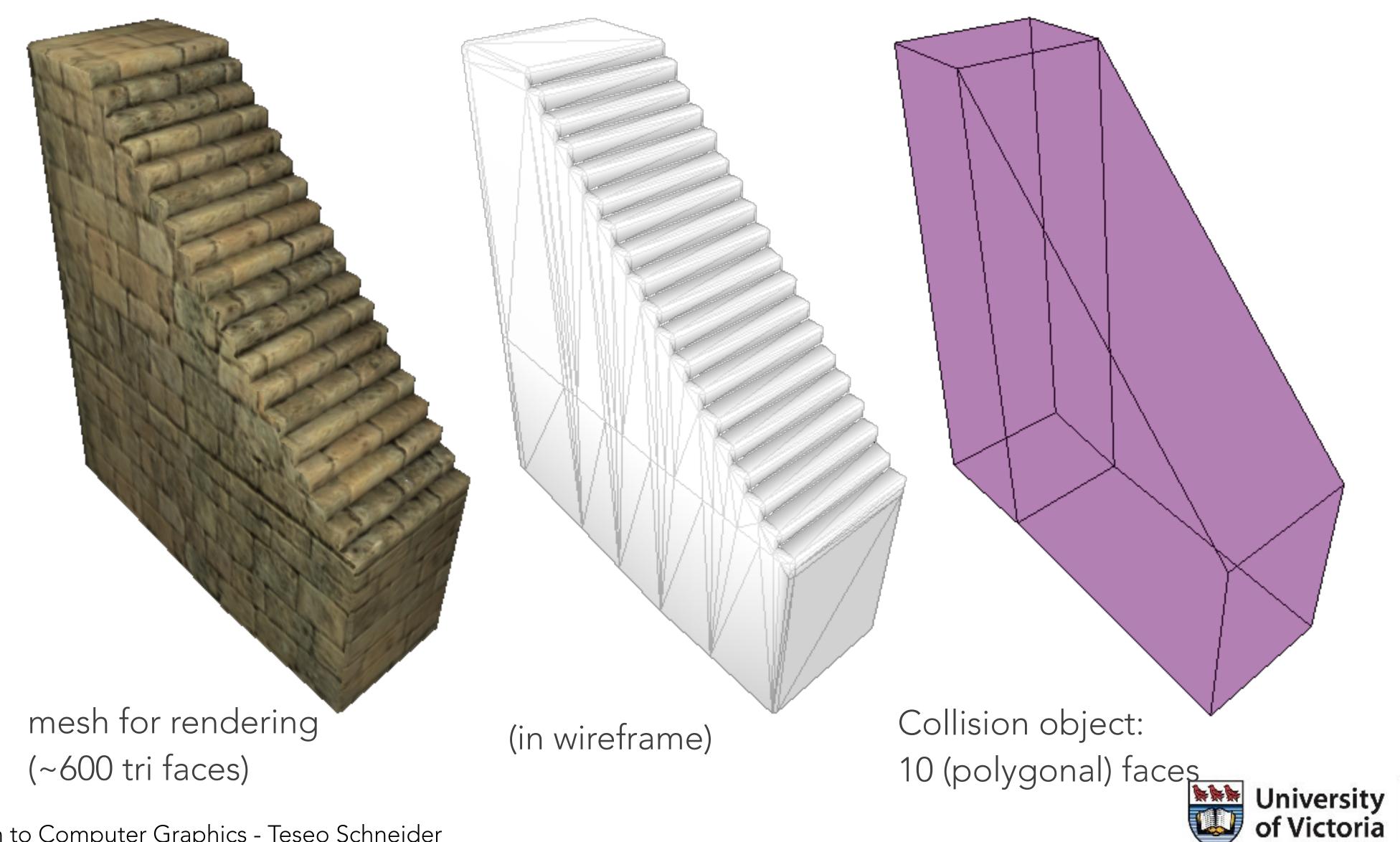


3D Meshes as Hit-Boxes

- These are often NOT the meshes that you use for rendering
 - much lower resolution (~ O(10²))
 - no attributes (no uv-mapping, no col, etc)
 - closed, water-tight (inside!= outside)
 - often convex only
 - can be polygonal (as long as the faces are flat)

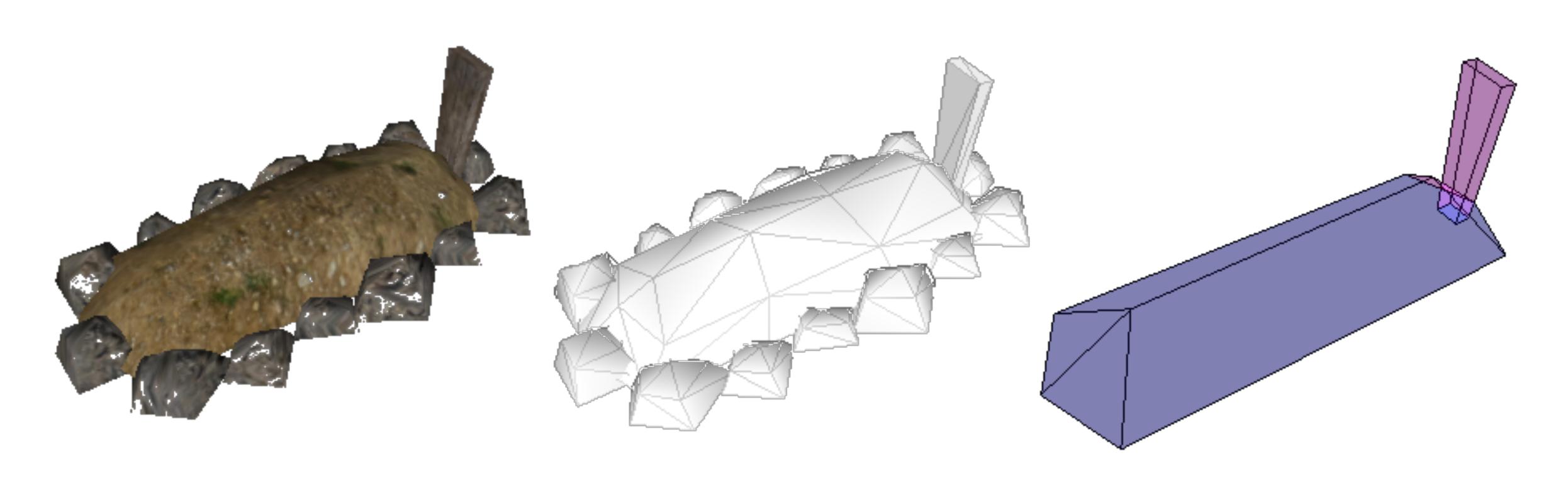


3D Meshes as Hit-Boxes



Computer Science

3D Meshes as Hit-Boxes



mesh for rendering (~300 tri faces)

(in wireframe)

Collision object: 12 (polygonal) faces



Geometry Proxies: Composite Hit-Boxes

- Union of Hit-Boxes
 - inside iff inside of any sub Hit-Box
- Flexible
 - union of convex Hit-Boxes ==> concave Hit-Box
 - shape partially defined by a sphere, partially by a box ==> better approximation
- Creation: typically by hand
 - (remember: hit-boxes are usually assets)



How To Choose The Proxy?

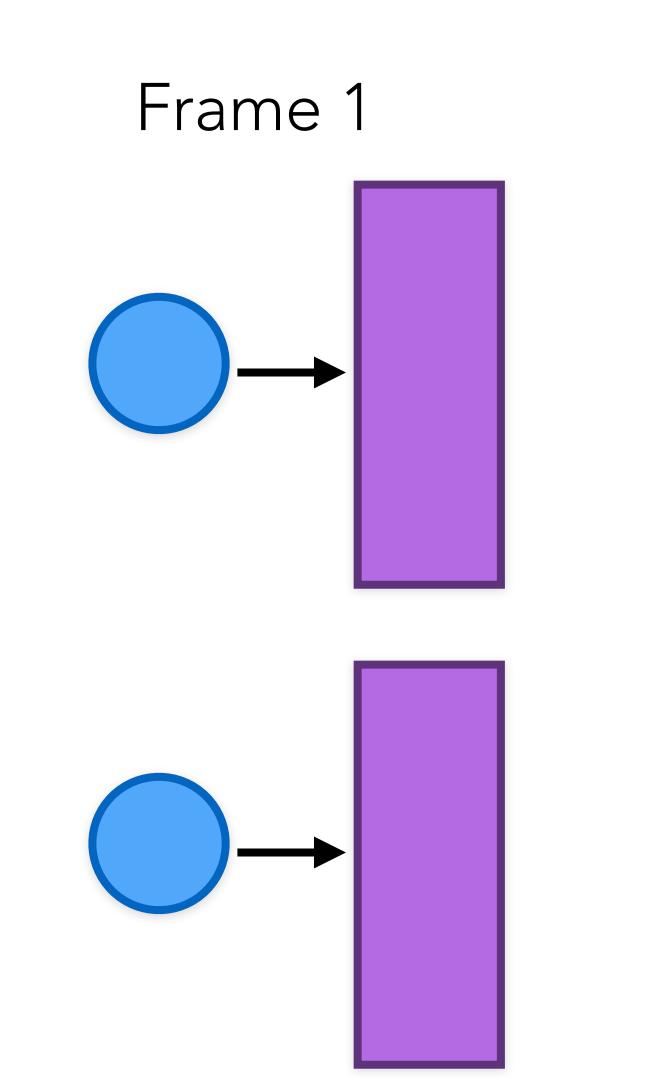
- Application dependent
- Note: # of intersection tests to be implemented quadratic wrt # of types supported

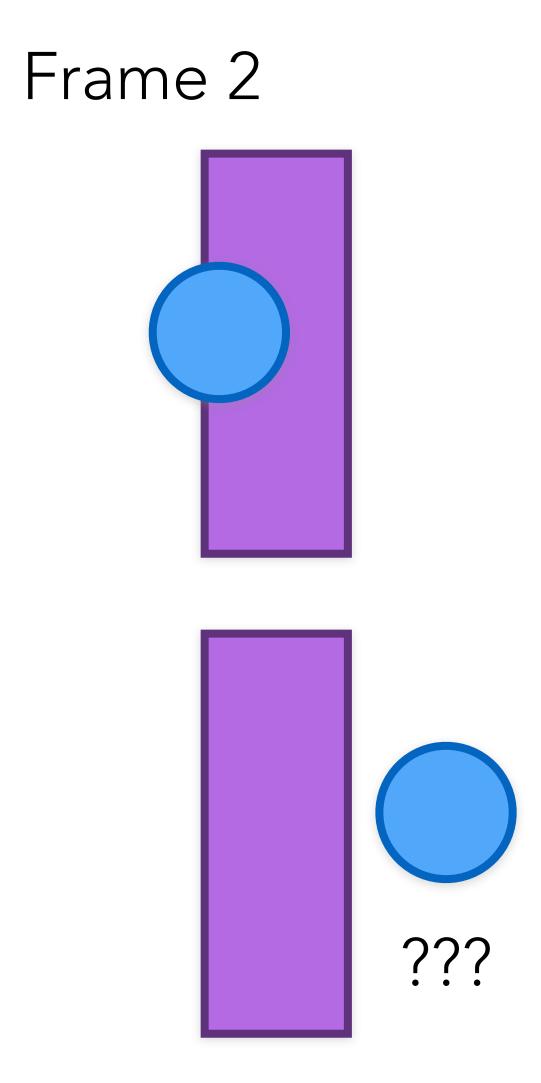
VS	Type A	Type B	Type C	Point	Ray	
Type A	algorithm	algorithm	algorithm	algorithm	algorithm	
Type B		algorithm	algorithm	algorithm	algorithm	useful,
Type C			algorithm	algorithm	algorithm	e.g. for visibility

Collision Detection Strategies

- Static Collision detection
 - ("a posteriori", "discrete")
 - approximated
 - simple + quick

- Dynamic Collision detection
 - ("a priori", "continuous")
 - accurate
 - demanding





Existing Implementations

- Intel Embree BVH Tree https://embree.github.io
- Nori BVH https://github.com/wjakob/nori
- Approximate knn https://www.cs.umd.edu/~mount/ANN/
- Intersections http://www.realtimerendering.com/intersections.html

References

Foundations of Multidimensional and Metric Data Structures
Hanan Samet

http://www.realtimerendering.com/books.html

http://www.realtimerendering.com/intersections.html

Polygon Mesh Processing

Mario Botsch, Leif Kobbelt, Mark Pauly, Pierre Alliez, Bruno Levy

Fundamentals of Computer Graphics, Fourth Edition 4th Edition by Steve Marschner, Peter Shirley Chapter 12

