

Log [7-Times]

$$\log 10 = 1$$

$$\log 1 = 0$$

$$\log ab = \log a + \log b$$

$$\log a/b = \log a - \log b$$

$$\log a^m = m \log a$$

$$\frac{\log a}{\log b} = \log_b a$$

$$\frac{1}{\log_b a} = \log_a b$$

$$\log a = \log b = \log c$$

then

$$a = b = c$$

$$\log_a x = k$$

$$\text{then } \underline{a = x^k}$$

$$\log_a(\log_b(\log_c x)) = k$$

$$\text{then } \underline{\text{"x" = ?}}$$

$$\underline{x = c^{b^{a^k}}}$$

$$\underline{\log_a} (\log_b (\log_c x)) = k$$

$$\log_a (\log_b (\log_c x)) = k \cdot \log_a^k$$

$$\underline{\underline{\log_a}} (\log_b (\log_c x)) = \underline{\log_a^k}$$

$$\log_b (\log_c x) = a^k$$

$$\log_b (\log_c x) = (a^k) \log_b^k$$

$$\left| \begin{array}{l} \log_b (\log_c x) = \underline{\underline{\log_b^k}} \\ \log_c x = b^{a^k} \\ x = c^{b^{a^k}} \end{array} \right.$$

$$\log [1+x] = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$$

GATE:-

①  $\log_x^{5/7} = -1/3$  Find "x" = ?

$$x^{-1/3} = 5/7$$

$$x^{-1} = \frac{125}{343}$$

then  $x = \frac{343}{125}$



01. The value of  $\log \tan 1^\circ + \log \tan 2^\circ + \log \tan 3^\circ + \dots + \log \tan 89^\circ = ?$  (GATE-15 ME)

- (a) 1  
(c) 3

- (b) 0  
(d) None of these

$$\begin{aligned}\tan 1 &= \tan (90^\circ - 89^\circ) \\ &= \cot 89^\circ\end{aligned}$$

$$\Rightarrow \log \tan 1 + \log \tan 2 + \dots + \log \tan 45 + \dots + \log \tan 89$$

$$\Rightarrow \log \tan 1 \cdot \tan 2 \cdot \dots \cdot \tan 45 \cdot \dots \cdot \tan 89.$$

$$\Rightarrow \log \cancel{\cot 89} \cdot \cancel{\cot 88} \cdot \dots \cdot \cancel{\tan 45} \cdot \dots \cdot \cancel{\tan 89}$$

$$\Rightarrow \log \tan 45^\circ \Rightarrow \log 1 = \underline{\underline{0}}$$

03. If  $\log_2 [\log_3 (\log_2 x)] = 1$ , then  $x$  is equal to:

(a) 0

$$x = 2^{3^2}$$

(c) 128

$$x = 2^9 \Rightarrow \underline{\underline{512}}$$

(b) 125

(d) 512

04. If  $a^2 + b^2 = c^2$ , then  $\frac{1}{\log_{c+a} b} + \frac{1}{\log_{c-a} b}$
- (a) 1      (b) 2      (c) -1      (d) -2

$$\begin{aligned}
 \frac{1}{\log_{c+a} b} + \frac{1}{\log_{c-a} b} &\Rightarrow \log_b^{c+a} + \log_b^{c-a} \\
 &\Rightarrow \log_b^{c-a} \\
 &\Rightarrow \log_b^{b^2} \\
 &\Rightarrow 2 \log_b b = 2(1) = \underline{\underline{2}} \quad \checkmark
 \end{aligned}$$

10. Given that  $\frac{\log P}{(y-z)} = \frac{\log Q}{(z-x)} = \frac{\log R}{(x-y)} = 10$  for  $x \neq y \neq z$ , what is the value of the product PQR?
- (GATE)
- (a) 0  
 (b) 1  
 (c) xyz  
 (d)  $10^{xyz}$

$$\frac{\log P}{y-z} = 10$$

$$\log P = 10(y-z)$$

$$\log Q = 10(z-x)$$

$$\log R = 10(x-y)$$

$$\log P + \log Q + \log R = 10[y-z + z-x + x-y]$$

$$\log PQR = 10[0]$$

$$\log PQR = 0$$

$$\log PQR = \log 1$$

$\therefore$   
 $\boxed{PQR = 1}$

09. The value of the expression

$$\frac{1}{1 + \log_w uv} + \frac{1}{1 + \log_u vw} + \frac{1}{1 + \log_v wu} \text{ is } \underline{\quad}.$$

(GATE-18)

(a) -1

(c) 1 ✓

(b) 0

(d) 3

$$\log_w uvw + \log_u uvw + \log_v uvw$$

$$\Rightarrow \log_{uvw} uvw$$

$$\Rightarrow \underline{\underline{\frac{1}{uvw}}}$$

$$\frac{1}{\log_w uv + \log_w wu} + \frac{1}{\log_u vu + \log_u uw} + \frac{1}{\log_v vw + \log_v uw}$$

$$\Rightarrow \frac{1}{\log_{uvw} uvw} + \frac{1}{\log_{uvw} uwv} + \frac{1}{\log_{uvw} vwu}$$

07. For non-negative integers, a, b, c, what would be the value of  $a + b + c$ , if  $\log a + \log b + \log c = 0$ ?

$$\cancel{\log a + \log b + \log c = 0}$$

(GATE-18)

- (a) 3  
(c) 0

- (b) 1  
(d) -1

08. For integers, a, b and c, what would be the minimum and maximum values respectively of  $a+b+c$  if  $\log |a| + \log |b| + \log |c| = 0$ ? (GATE-18)

- (a) -3 and 3
- (b) -1 and 1
- (c) -1 and 3
- (d) 1 and 3

$$\begin{aligned}a &= \pm 1 \\b &= \pm 1 \\c &= \pm 1 \\&\text{+3, -3}\end{aligned}$$

06. If  $\log(P) = (1/2)\log(Q) = (1/3)\log(R)$ , then which of the following options is TRUE? (GATE-11)
- (a)  $P^2 = Q^3R^2$
  - (b)  $Q^2 = PR$
  - (c)  $Q^2 = R^3P$
  - (d)  $R = P^2Q^2$

$$\log P = \frac{1}{2} \log Q = \frac{1}{3} \log R$$

$$\log P = \log Q^{1/2} = \log R^{1/3}$$

$$P = Q^{1/2} = R^{1/3}$$

$$P = Q^{1/2} = R^{1/3} = k \text{ say}$$

$$P = k$$

$$Q^{1/2} = k$$

$$Q = k^2$$

$$R^{1/3} = k$$

$$R = k^3$$

$$Q^2 = P \cdot R$$

$$(k^2)^2 = k \cdot k^3$$

$$k^4 = k^4$$

995  
05.  $\log_4 2 - \log_8 2 + \log_{16} 2 - \dots$  to  $\infty$  is

- (a)  $e^2$
- (b)  $\ln 2 + 1$
- (c)  $\ln 2 - 1$
- (d)  $1 - \ln 2$

$$\log_2^2 - \log_2^2 + \log_2^2 - \dots$$

$$\frac{1}{2} \log_2^2 - \frac{1}{3} \log_2^2 + \frac{1}{4} \log_2^2 - \dots$$

$$\frac{1}{2} - \frac{1}{3} + \frac{1}{4} - \dots$$

$$\log(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$$

$$+1 - 1 + \frac{1}{2} - \frac{1}{3} + \frac{1}{4} - \dots$$

$$+1 - \left[ 1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} - \dots \right]$$

$$1 - \log(1+1)$$

$$1 - \log_2$$

$$\log_b^a \Rightarrow m \log_b^a$$

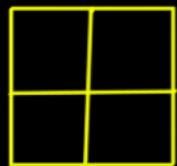
$$\log_b^a = \frac{1}{m} \log_b^a$$

## Analytical figures

- no of Squares
- no of Rectangle
- no of parallelogram
- no of Δ's.

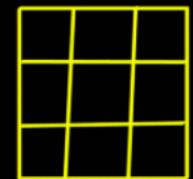
no of squares :-

$$\sum n^2$$



$$2^2 + 1^2 + 0^2$$

$$\underline{\underline{5}}$$



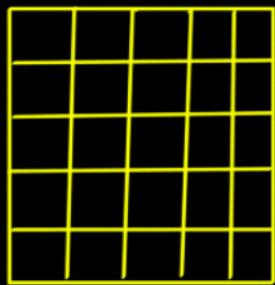
$$3^2 + 2^2 + 1^2$$

$$(14)$$

$$\sum n^2 = \frac{n(n+1)(2n+1)}{6}$$

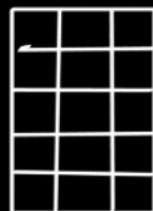
$$= \frac{5(6)(11)}{6}$$

$$= 55$$



$$\frac{5^2 + 4^2 + 3^2 + 2^2 + 1^2}{= 55}$$

$$\sum m \times n$$



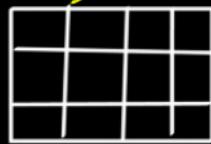
$$(3 \times 3)$$

$$+(2 \times 3)$$

$$+(1 \times 2)$$

$$+(2 \times 0)$$

$$15 + 8 + 3 \\ = 26$$



$$(6 \times 4)$$

$$+(2 \times 3)$$

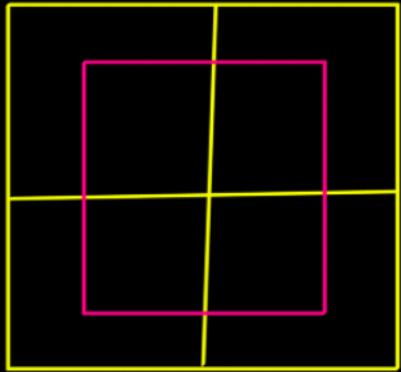
$$+(1 \times 2)$$

$$12 + 6 + 2 \\ = 20$$

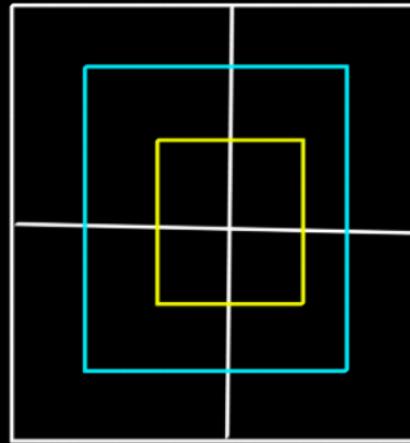


$$\sum 8^2 = 204$$

$$\frac{8(8+1)(16+1)}{6}$$



$$5 + 5 = \underline{\underline{10}}$$



$$5 + 5 + 5 = \underline{\underline{15}}$$

no of Rectangle

$$m_{c_2} \times n_{c_2}$$

[ GATE  $\Rightarrow$  2 Times ]

[ Each & Every grid also Rectangle ]

$m =$  no of horizontal lines

$n =$  no of vertical lines

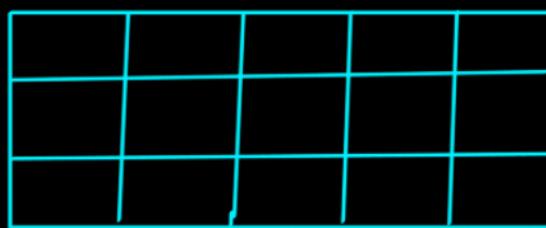


$$m = 3$$

$$n = 3 \quad 3_{c_2} \times 3_{c_2}$$

$$= 3 \times 3$$

$$= 9 \checkmark$$



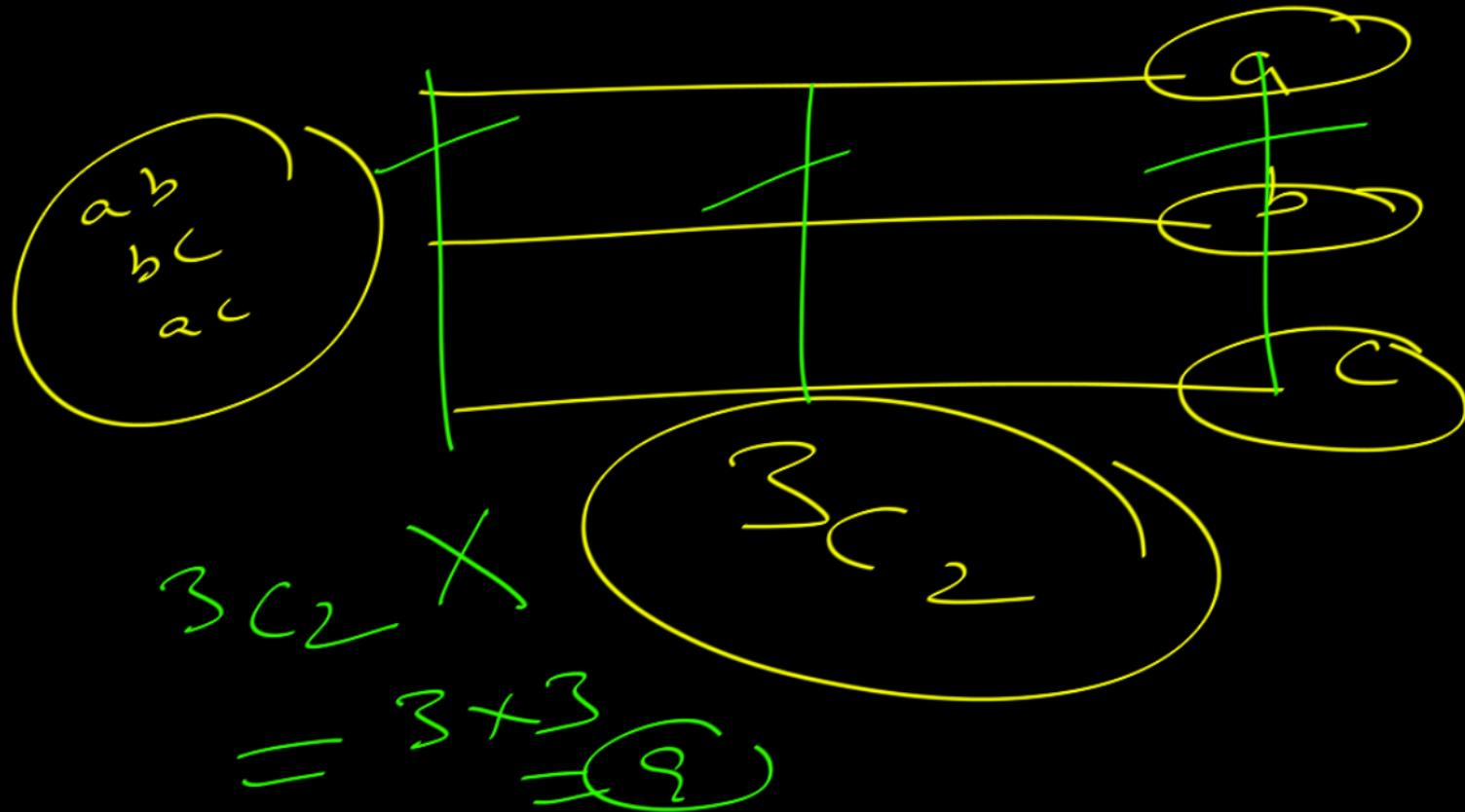
$$\begin{aligned} & 6_{c_2} \times 4_{c_2} \\ & = \frac{6 \times 5}{2 \times 1} \times \frac{4 \times 3}{2 \times 1} \\ & \Rightarrow 90 \end{aligned}$$



$$3_{c_2} \times 5_{c_2}$$

$$= 3 \times \frac{5 \times 4}{2 \times 1}$$

$$\Rightarrow \underline{\underline{30}}$$



$$n_{C_0} = \frac{n!}{(n-0)!0!}$$

$$n_{C_\gamma} = n_{C_{n-\gamma}}$$

$$n_{C_1} = n$$

$$n_{C_n} = 1$$

$$n_{C_0} = 1$$

$$10_{C_2} = \frac{10!}{[10-2]! 2!}$$

(1)

$$\frac{10 \times 9}{2 \times 1}$$

$$\frac{10 \times 9 \times 8!}{8! \times 2!}$$
$$\frac{10 \times 9}{2 \times 1}$$

$$7_{C_3} = \frac{7 \times 6 \times 5}{3 \times 2 \times 1}$$

no of parallelograms :-

$$m_{C_2} \times n_{C_2}$$

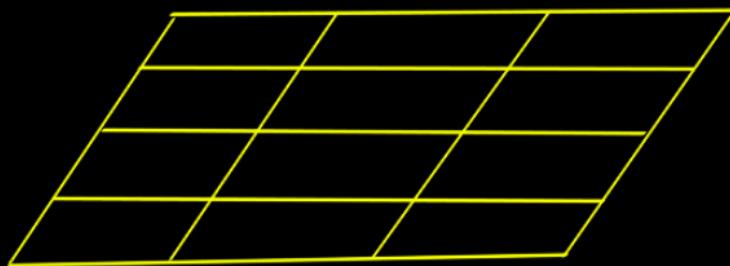


$$3_{C_2} \times 3_{C_2}$$

$$= 3 \times 3$$

$$= \underline{9}$$

GATE 2019



$$m = 5, n = 4$$

$$5_{C_2} \times 4_{C_2}$$

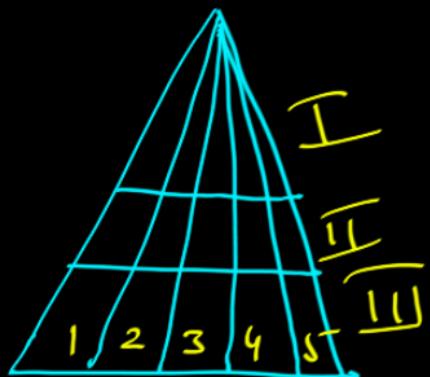
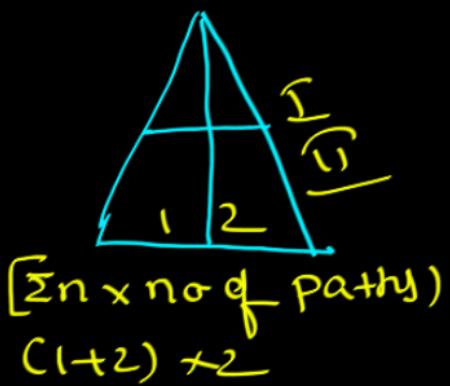
$$= \frac{5 \times 4}{2 \times 1} \times \frac{4 \times 3}{2 \times 1} \Rightarrow \underline{(60)}$$

no of  $\Delta$ 's :-  
 $\Sigma n$

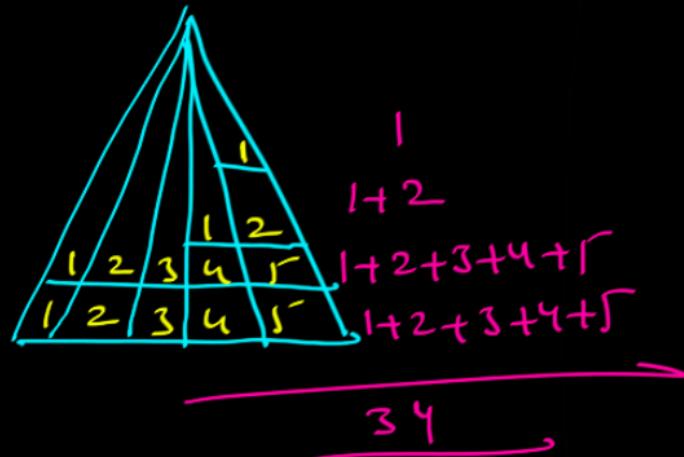
$$\begin{array}{c} \Delta \\ | \\ 1 \end{array} = 1$$

$$\begin{array}{c} \Delta \\ | \\ 1 \quad 2 \end{array} 1+2 = \underline{\underline{3}}$$

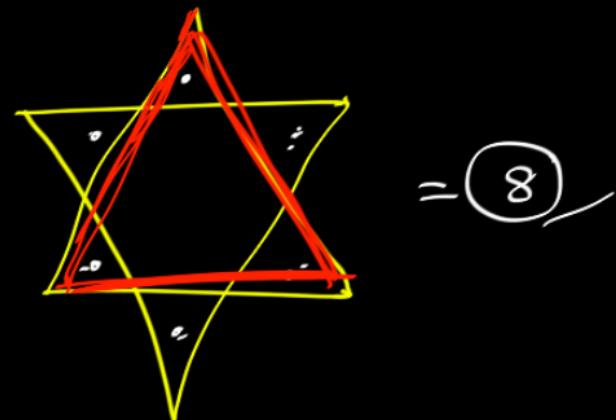
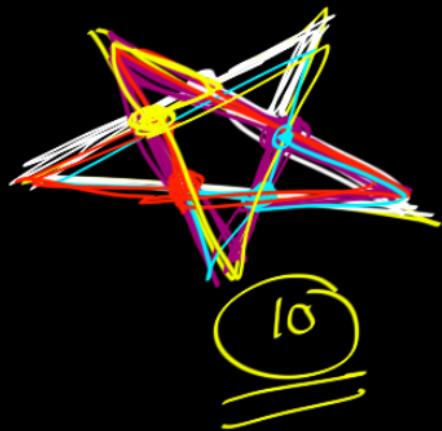
$$\begin{array}{c} \Delta \\ | \\ 1 \quad 2 \quad 3 \quad 4 \quad 5 \end{array} 1+2+3+4+5 = \underline{\underline{15}}$$



$$(1+2+3+4+5) \times 3 = \underline{\underline{45}}$$

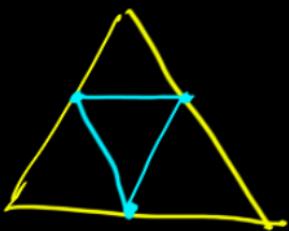


Bases on Stars:



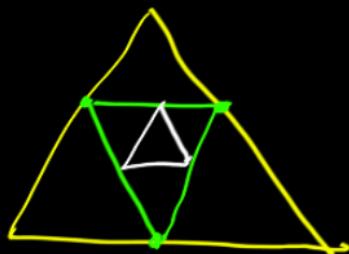
IV

Join the mid points of sides



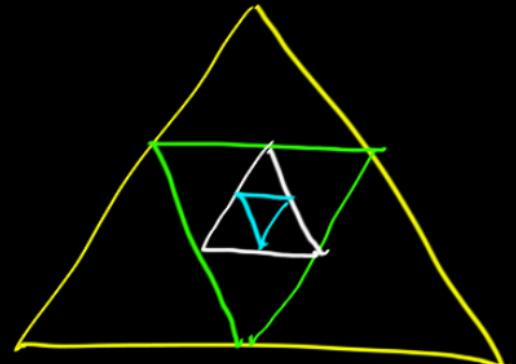
$$1 + 4 = S^-$$

|



$$1 + 4 + 4$$

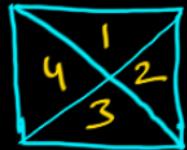
⑨



$$1 + 4 + 4 + 4$$

⑯

v



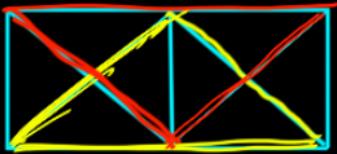
8



10

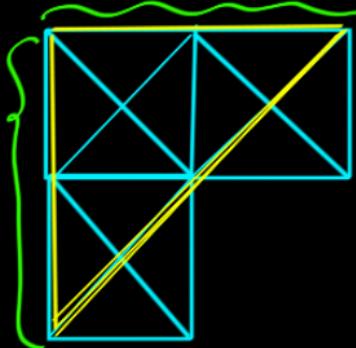


16



$$8 + 8 + 2$$

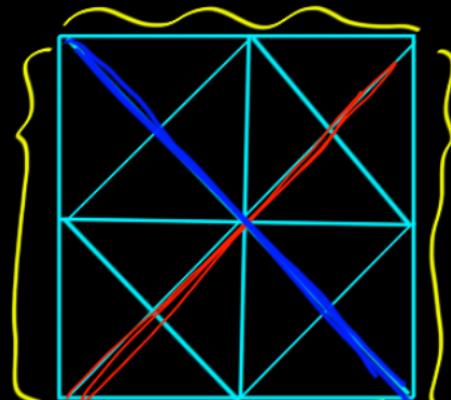
$$= \underline{\underline{18}} \checkmark$$



$$8 + 8 + 8$$

$$2 + 2$$

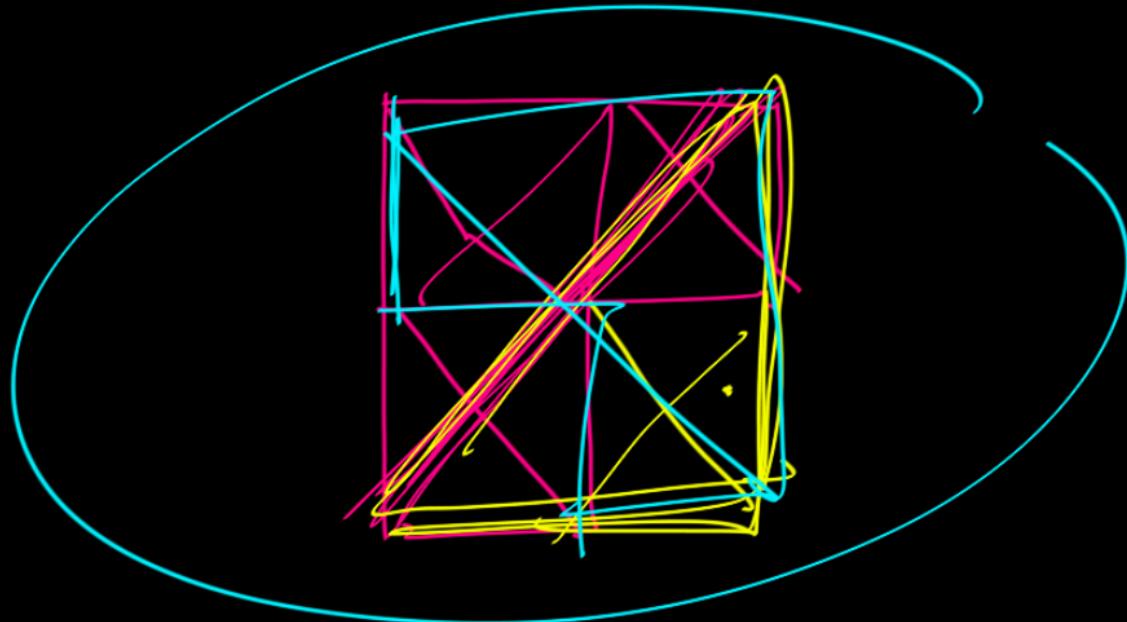
$$\begin{array}{r} + 1 \\ \hline 29 \end{array}$$



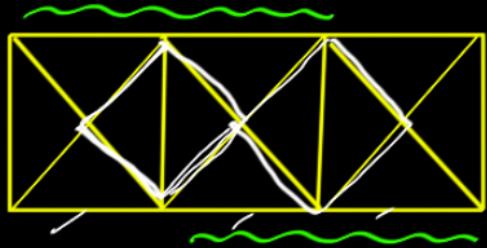
$$8 + 8 + 8 + 8$$

$$2 + 2 + 2 + 2$$

$$\begin{array}{r} + 4 \\ \hline 44 \end{array}$$

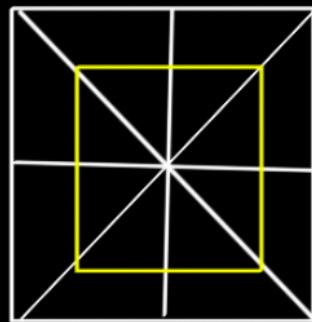


Ex:-

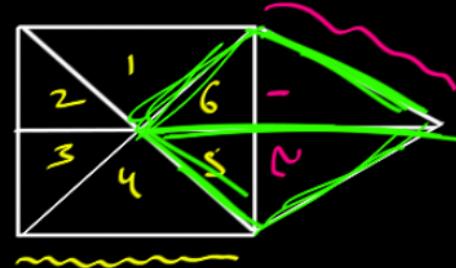


$$\begin{array}{r} 8+8+8 \\ 2+2 \\ \hline 28 \Delta^{\text{es}} \end{array}$$

How many  $\square \Rightarrow 5$  ✓

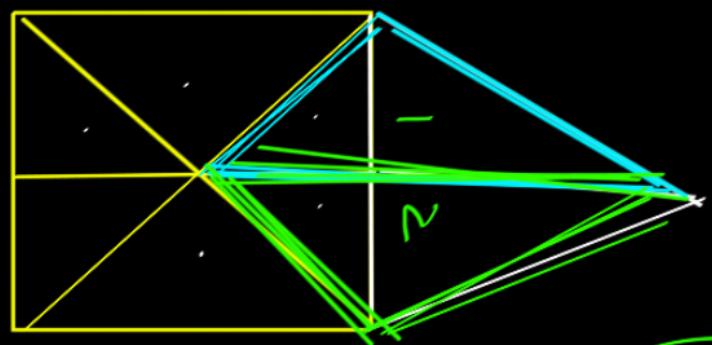


$$\begin{array}{r} 16+16 \\ 32 \Delta^{\text{es}} \end{array}$$



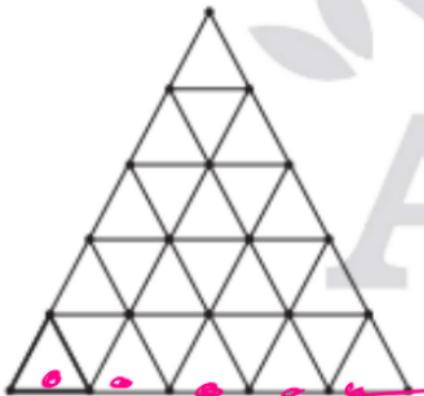
$$\begin{array}{r} 12+3+2 \\ 17 \Delta^{\text{es}} \end{array}$$

\_\_\_\_\_ X \_\_\_\_\_



$$12 + 3 + 2 = \textcircled{17}$$

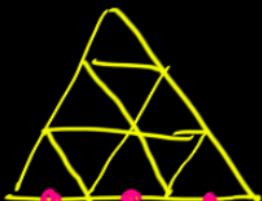
10. How many triangles are there in the given figure?



NOTE:-    Symmetric     $\Delta^{(e)}$

base	no of $\Delta^{(e)}$
1	1
2	5
3	13
4	27
5	<u>48</u>

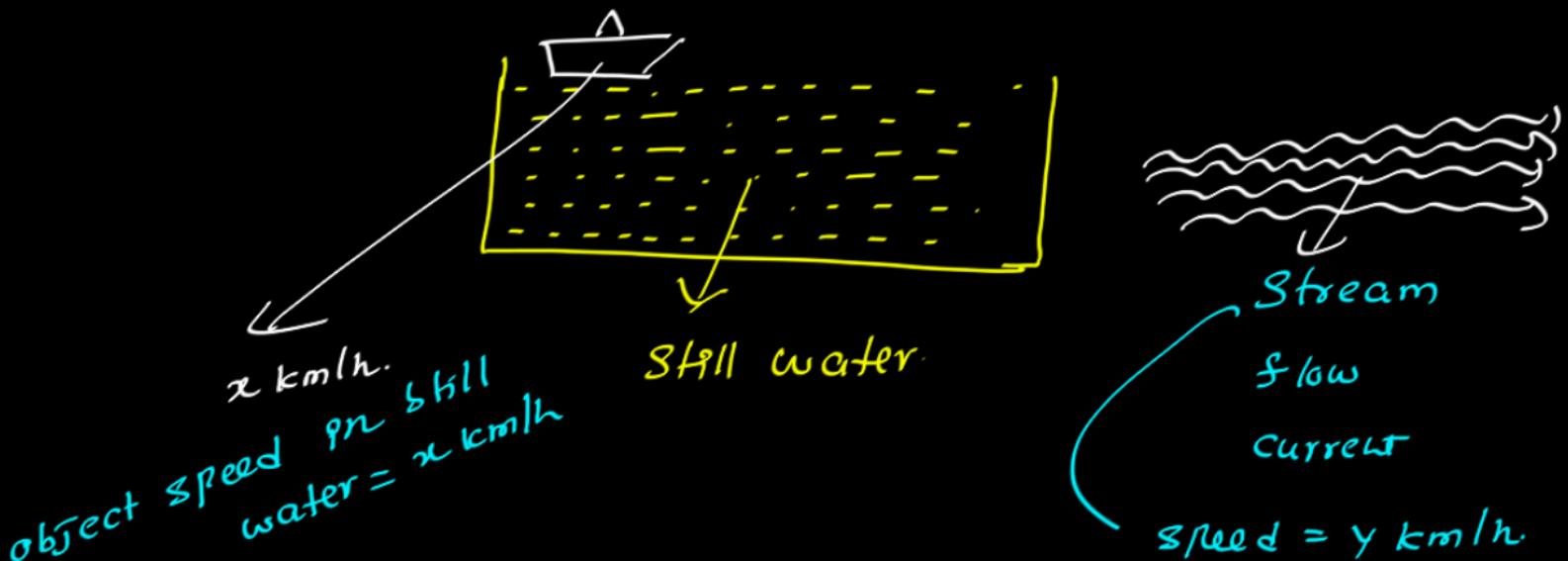
↑



## Boats & streams

1 - Time

PSU + static - 1 Quest



DSS, USS :-



Down stream speed =  $x+y$



upstream speed =  $x-y$  km/h

$$\begin{aligned} DSS &= x+y \\ USS &= x-y \end{aligned}$$

DSS, USS given then  
 $x$  &  $y$  values.

$$\begin{aligned} DSS &= a \\ USS &= b \end{aligned} \quad \text{say}$$

$$x+y = a$$

$$x-y = b$$

$$\begin{aligned} 2x &= a+b \\ x &= \frac{1}{2}(a+b) \end{aligned}$$

object speed in

$$\text{still water } (u) = \frac{1}{2} (DSS + USS)$$

$$\text{stream speed } (y) = \frac{1}{2} (DSS - USS)$$

U.S.T, UST time

$$T = \frac{D}{S}$$



$$T = \frac{D}{DSS}$$



$$U.S.T = \frac{D}{USS}$$

vvv Imp: [Distance, Total Travelling dist] ✓

speed of man in still water ( $x$ ) km/h, and stream speed  $y$  km/h.  
he travelled from  $A \rightarrow B$  &  $B \rightarrow A$  in  $T$  hrs,

$$\text{Distance b/w Two places } [D] = \frac{T(x-y)}{2x}$$

$$\text{Total Travelling Dist } [TT-D] = \underline{\underline{2D}}$$



$$T = t_1 + t_2$$

$$= \frac{D}{x+y} + \frac{D}{x-y}$$

$$T = D \left[ \frac{x-y+x+y}{(x+y)(x-y)} \right]$$

$$T = D \left[ \frac{2x}{x^2 - y^2} \right]$$

$$D = \frac{T(DS) (VS)}{DS + VS}$$

$$D = \frac{T(u^2 - v^2)}{2u}$$

speed of Man in still water 10 km/h  
 stream speed 4 km/h. he travelled  
 from A → B and B → A in 20 hrs.

Find distance b/w two places?

$$\begin{aligned}x &= 10 \\y &= 4 \\T &= 20\end{aligned}$$

$$D = \frac{20(10^2 - 4^2)}{2(10)} \\= 84$$

$$\cancel{T.T - D = 168}$$

Down stream speed of man is  
 20 km/h and up stream speed  
 of man is 16 km/h. he taken  
 36 hours for Total Journey.  
 Find distance b/w Two places?

$$\begin{aligned}D &= 20 \\U.S &= 16 \\T &= 36\end{aligned}$$

$$D = \frac{36(20)(16)}{20 + 16} \\= \underline{\underline{320}}$$

25. A man rows downstream 32 km and 14 km upstream. If he takes 6 hours to cover each distance, then the velocity (in kmph) of the current is:
- (a)  $\frac{1}{2}$       (b) 1      (c)  ~~$1\frac{1}{2}$~~       (d) 2

Q) ~~(2)~~

DSS = 20  
USS = 16

$x = ?$

$$\frac{1}{2} (20+16) \\ = \underline{\underline{18}}$$

$$DSS = \frac{32}{6} \quad \text{--- (1)} \quad \checkmark$$

$$USS = \frac{14}{6} \quad \text{--- (2)} \quad \checkmark$$

$$V = \frac{1}{2} \left[ \frac{32}{6} - \frac{14}{6} \right] = \frac{1}{2} \left[ \frac{\cancel{18}}{\cancel{6}} \right] = \frac{3}{2} \Rightarrow \underline{\underline{1\frac{1}{2}}}$$

26. Speed of a boat in still water is 16 km/h. If it can travel 20 km downstream in the same time as it can travel 12 km upstream, the rate of stream is  $x = 16$   $y = ?$

- (a) 1 km/h      (b) 2 km/h  
~~(c) 4 km/h~~      (d) 5 km/h

$$\frac{20}{16+y} = \frac{12}{16-y}$$

27. If boats rate in still water is 20 km/hr and stream rate is 10 km/hr, and it takes him 10 hrs to row to a place and back, then how far is the place?
- (a) 75 kms       $x = 20$   
 (c) 70 kms       $y = 10$   
~~(a)~~  $T = 10 \text{ hr}$
- (b) 60 kms  
 (d) 40 kms
- $$\frac{10(20^2 - 10^2)}{2(20)} = 75$$

28. If boat's rate in still water is 10 km/hr and river is flowing with a certain speed, it takes him 20 hrs to row to a place and back and the length of the river is 75 kms. Then find the velocity of water?

- (a) 10 km/hr  
 (c) 7 km/hr

- (b) 15 km/hr  
 (d) 5 km/hr

$$x = 10 \quad D = 75 \quad T = 20$$

$$y = ?$$

$$75 = \frac{20(10^2 - y^2)}{2(10)}$$

$$75 = 100 - y^2$$

$$y^2 = 25$$

+ len  $y = 5$

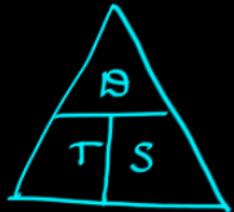


24-8-2022  
GATE-EE

{ → Time & Distance  
→ Shift cuts  
→ DICE

X

M Code  
1:- D, T, S Law :-



$$D = T \times \text{speed}$$

$$T = D / \text{speed}$$

$$\text{Speed} = D / \text{Time}$$

Time & Distance  
[5 - Times]

M Code  $\frac{x+y}{2}$

2:- Avg speed :-

A Man travelled from A  $\rightarrow$  B @  $x$  km/h.

and B  $\rightarrow$  A @  $y$  km/h then Avg speed

of Man is  $\Rightarrow \boxed{\frac{2xy}{x+y} \text{ km/h}}$

Avg speed:-

$$\text{Speed} = \frac{D}{T}$$

$$\text{Avg Speed} = \frac{\text{Total Distance}}{\text{Total Time}}$$

(iii)

$$\frac{\text{Sum of Individual dist}}{\text{Sum of Individual Times}}$$



$$A \xrightarrow{x, D, T_1} B \\ (2, 10 - y) \in$$

$$\text{Avg Speed} = \frac{D+D}{t_1+t_2}$$

$$= \frac{2D}{\frac{D}{x} + \frac{D}{y}}$$

$$= \frac{2D}{D(\frac{1}{x} + \frac{1}{y})}$$

$$= \frac{2xy}{x+y} \text{ km/h}$$



A Man Travelled From A → B @ 60 km/h  
and B → A @ 90 km/h. Find Avg speed

of Man ?

$$\frac{2xy}{x+y} = \frac{2(60)90}{150}$$

$$= \underline{\underline{72 \text{ km/h}}}$$

② A Man covered 200 kms. he travelled  
First 100 kms @ 25 km/h, next 50 kms  
@ 10 km/h. Remaining distance @ 50 km/h.

Find Avg speed of Man ?



$$\frac{200}{\frac{100}{25} + \frac{50}{10} + \frac{50}{50}} = \frac{200}{4+5+1} = \underline{\underline{20 \text{ km/h}}}$$

A Man Travelled First  
200 kms @ 40 km/h,  
next 150 kms @ 30 km/h.  
next 100 kms @ 20 km/h.  
Find Avg speed of Man ?

$$\frac{200 + 150 + 100}{\frac{200}{40} + \frac{150}{30} + \frac{100}{20}}$$

$$= \frac{450}{5+5+5} = \frac{450}{15}$$

$$= \underline{\underline{30 \text{ km/h}}}$$

## Average Speed

11. A person travels 200 kms in 3 hrs, next 300 kms in 4 hrs, last 500 kms in 3 hrs. What is his average speed?

- (a) 120 kmph
- (c) 80 kmph

$$\frac{200 + 300 + 500}{3 + 4 + 3}$$

- (b) 100 kmph
- (b) 130 kmph

$$\frac{1000}{10}$$

12. A car covers half of the journey at 36 kmph and the rest at 24 kmph? What is its average speed?

(a) 28.8 kmph

(c) 14 kmph

$$\frac{2(36 \times 24)}{60} = 28.8$$

(b) 30 kmph

(d) 15 kmph

13. A person divides his total route of journey into three equal parts and decides to travel the three parts at the speeds of 80 kmph, 60 kmph and 30 kmph respectively. What is the average speed during the journey?

$$\frac{D}{80} + \frac{D}{60} + \frac{D}{30}$$

$$\text{Avg Speed} = \frac{T-D}{T-1}$$

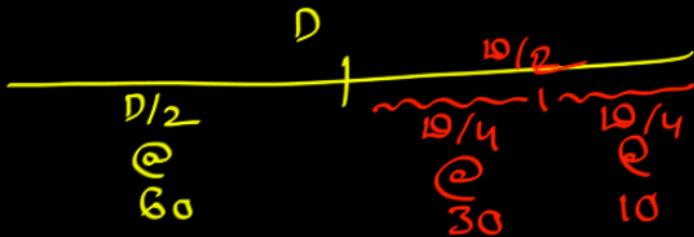
- (a) 40 kmph
- (c) 48 kmph

- (b) 45 kmph
- (d) 49 kmph

$$\begin{aligned}
 &= \frac{3D}{\frac{D}{80} + \frac{D}{60} + \frac{D}{30}} \\
 &= \frac{3D}{D \left[ \frac{3+4+8}{240} \right]} = \frac{3(240)}{15} \\
 &\Rightarrow 48
 \end{aligned}$$

14. A tourist covers half of his journey by train at 60 km/h, half of the remainder by bus at 30 km/h and the rest by cycle at 10 km/h. Average speed of the tourist during the journey is (ESE-19)

- (a) 36 km/h
- (b) 33 km/h
- (c) 24 km/h
- (d) 18 km/h



$$\frac{D}{\frac{D/2}{60} + \frac{D/4}{30} + \frac{D/4}{10}}$$

$$= \frac{D}{\frac{D}{120} + \frac{D}{120} + \frac{D}{40}}$$

$$= \frac{D}{D \left[ \frac{1+1+3}{120} \right]} = \frac{120}{5} = \underline{\underline{24 \text{ km/h}}}$$

15. A, B and C are on a trip by a car. A drives during the first hour at an average speed of 50 km/hr. B drives during the next 2 hours at an average speed of 48 km/hr. C drives for the next 3 hours at an average speed of 52 km/hr. They reached their destination after exactly 6 hours. Their mean speed was:

- (a) 50 km/hr
- (b)  $50\frac{1}{3}$  km/hr
- (c) 52 km/hr
- (d) 52 km/hr

$$\frac{1(50) + 2(48) + 3(52)}{6}$$

$$\frac{50 + 96 + 156}{6}$$

$$\Rightarrow \frac{302}{6} = \frac{151}{3}$$

$$\underline{\underline{50\frac{1}{3}}}$$

Ques.: A man using  $\frac{4}{5}$ th of his original speed and he is 12 min late to reach the destination. Find correct time to reach the destination?

*Correct*

$$D = S \cdot t$$

$$100 = \frac{4}{5}(S) [t + 12]$$

$$\cancel{S}t = \frac{4}{5}(S)(t + 12)$$

$$5t = 4t + 48$$

$$\boxed{t = 48 \text{ min}}$$



before = —
Late = +

s. cut -

$\frac{a}{b}$ , time ✓

$$\frac{\text{Numerator}}{\text{diff b/w (N & D)}}$$

x given Time

$$\frac{4}{5}, 12$$

$$\frac{4}{11} \times 12$$

48

04. If I travel at  $\frac{5}{4}$  of my speed, I reach my office 6 minutes early. What is the original duration of time I take to reach office?

- (a) 30 min
- (c) 35 min

$$\frac{5}{4} \times 6 = 30$$

- (b) 24 min
- (d) None

Q:- without stoppages & including stoppages :-

without stoppages speed of Bus is 48 km/h. and including stoppages speed of Bus is 36 km/h. Find Time Taken for stoppages in 1-hour. & also find in 2-hours?

$$\begin{array}{rcl} 48 \text{ km} & \rightarrow & 60 \text{ min} \\ 36 \text{ km} & \rightarrow & 60 \text{ min} \\ \hline 12 \text{ km} & \rightarrow & ? \end{array}$$

$$\begin{array}{rcl} 48 \text{ km} & \rightarrow & 60 \\ 12 \text{ km} & \xrightarrow{x} & ? \\ \hline \frac{60 \times 12}{48} & & 15 \end{array}$$



$$\begin{aligned} \text{for } 2 \text{ hrs} &= 2 \times 15 \\ &= 30 \text{ min} \checkmark \end{aligned}$$

S-cut

$$\boxed{\frac{\text{Dist}}{\text{Max Speed}} \times 60} \rightarrow \text{for } 1\text{hr only}$$

$$\frac{15}{48} \times 60 = 15 \text{ min.}$$

$$2 \times 15 = \underline{\underline{30}}$$

06. The average speed for an entire journey is 60 kmph without considering the stoppages. When the stoppages are considered the average speed becomes 48 kmph. How many minutes per hour on an average were the stoppages?

- (a) 10 mins
- (b) 12 mins
- (c) 16 mins
- (d) none of these

Model  
5:-  Diff of Times :- ( $T = T_1 \sim T_2$ )

$t_1$	$t_2$	$T$
L	L	Diff
B	B	Diff
L	B	Sum
B	L	Sum

A boy going to school from his home @ 3 km/hr  
 and he is 10 min late to reach the school.  
 next day he increase the speed by 1 km /hr then  
 he is 20 early to reach the school.  
 find distance between two places?

$$D = s(t)$$

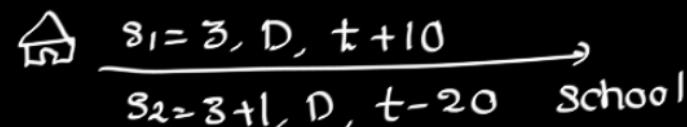
$$D = \frac{3(t+10)}{60} \text{ 1st day } A \rightarrow B$$

$$D = \frac{4(t-20)}{60} \text{ 2nd day } A \rightarrow B$$

$$\frac{3(t+10)}{60} = \frac{4(t-20)}{60}$$

$$3t + 30 = 4t - 80$$

$$t = 110$$



$$\frac{S_1 = 3, D, t + 10}{S_2 = 4, D, t - 20} \xrightarrow{\text{School}}$$

$$D = \frac{3(110 + 10)}{60}$$

$$= \underline{\underline{6 \text{ km}}}$$

$$\tau_1 \sim \tau_2 = \tau$$

$$\frac{D}{3} - \frac{D}{4} = \frac{(0+20)}{60}$$

$$D \left[ \frac{4-3}{12-6} \right] = \frac{30}{60} \quad | \\$$

$$D = 6 \text{ km/h}$$

A student travels from house to college. If he walks with 3 km/hr, he reaches to the college 5 min late. If he walks with 4 km/hr, he reaches to the college 10 min early. What is the distance from house to college?

- (a) 2 kms
- (c) 3 kms

$$\begin{aligned}T_1 &\sim T_2 = T \\ \frac{D}{3} - \frac{D}{4} &= \frac{5+10}{60} \\ D\left[\frac{4-3}{3 \times 4}\right] &= \frac{15}{60} \\ D &= \underline{\underline{3 \text{ kms}}} \end{aligned}$$

- (b) 4 kms
- (d) 5 kms

08. A car starts from A and B travelling 20 km an hour.  $1\frac{1}{2}$  hours later another car starts from A and travelling at the rate of 30 km an hour reaches B  $2\frac{1}{2}$  hours before the first car. Find the distance from A to B.

(a) 280 km

(c) 240 km

$$T_1 = T_2 = T$$

$$\frac{D}{20} - \frac{D}{30} = 1\frac{1}{2} + 2\frac{1}{2}$$

$$D \left[ \frac{30 - 20}{20 \times 30} \right] = 4 \text{ hrs}$$

$$D \left[ \frac{10}{600} \right] = 4$$

$$D = 240 \text{ km!!}$$

(b) 260 km

(d) none of these

16. A Train requires 7 seconds to pass a pole while it requires 25 seconds to cross a stationary train which is 378 m long. Find the speed of the train.

- (a) 75.6 kmph                          (b) 75.4 kmph  
(c) 76.2 kmph                           (d) 21 kmph

$$7 = \frac{L(C\tau)}{S(C\tau)} \quad \text{--- (1)}$$

$$25 = \frac{L(C\tau) + 378}{S(C\tau)} \quad \text{--- (2)}$$

$$\frac{(2)}{(1)}$$

$$\frac{25}{7} = \frac{L(C\tau) + 378}{L(C\tau)}$$

$$25x = 7x + 378(7)$$

$$18x = 378(7)$$

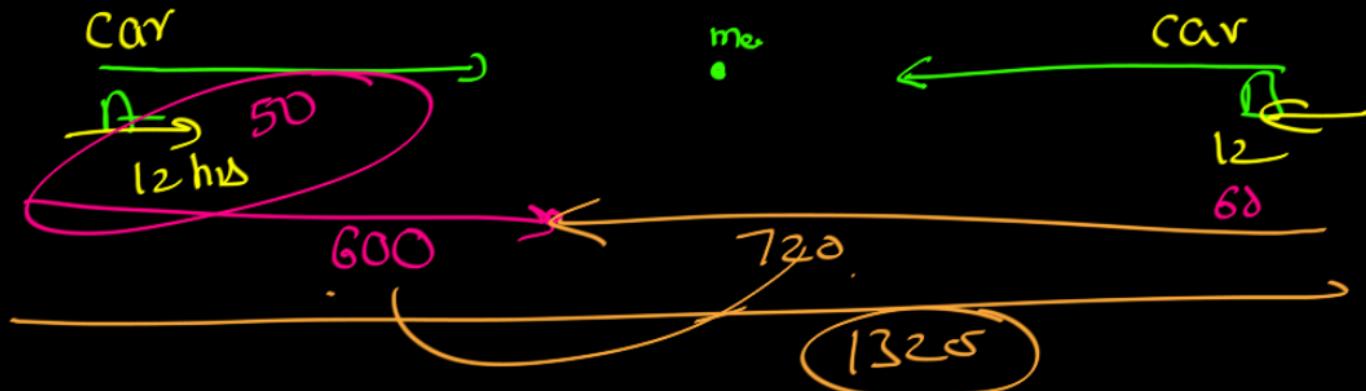
$$x = 147$$

21. Two cars starts from A and B and travel towards each other at the speed of 50 kmph and 60 kmph respectively. At the time of their meeting the second car has travelled 120 km more than the first, the distance between A and B is:?

- (a) 600 kms
- (b) 1320 kms
- (c) 720 kms
- (d) 3120 kms

For 1 hr =  
50,      60  
10

1 hr = 10 km more  
~~? = 120 km~~  
 $\frac{120}{10} = 12 \text{ hr}$



Davya

50 km/h



50

10 km/h

Mahalaxmi?

40 km/h



40

Square roots for surds [4-Times]

$$\sqrt{5+2\sqrt{6}} = \sqrt{x+y} + \sqrt{xy}$$

$$5+2\sqrt{6} = x+y + 2\sqrt{xy}$$

$$x+y = 5 \quad \text{--- (1)}$$

$$xy = 6 \quad \text{--- (2)}$$

$$\begin{aligned}(x-y)^2 &= (x+y)^2 - 4xy \\&= 5^2 - 4(6) \\&= 25 - 24 \\&= 1\end{aligned}$$

$$x-y = 1$$

$$\begin{aligned}x+y &= 5 \\x-y &= 1\end{aligned}$$

$$2x = 6$$

$$x = 3$$

$$y = 2$$

s.curv

$$\sqrt{5 + 3\sqrt{6}}$$
$$\sqrt{3} + \sqrt{2}$$

$$\sqrt{8 - 2\sqrt{15}}$$

$$(\sqrt{5} - \sqrt{3})$$

$$\sqrt{14 + 6\sqrt{5}}$$

2,3

$$\sqrt{14 + 2\sqrt{45}}$$

$$(\sqrt{9} + \sqrt{5})$$

$$\sqrt{7 + \sqrt{40}}$$

$$\sqrt{7 + \sqrt{4 \cdot 10}}$$

$$(\sqrt{5} + \sqrt{2})$$

$$\sqrt{11 + 2\sqrt{30}}$$

$$(\sqrt{6} + \sqrt{5})$$

$$\sqrt{5 + \sqrt{21}}$$

$$\sqrt{\frac{2}{2}(5 + \sqrt{21})}$$

$$\frac{1}{\sqrt{2}} (\sqrt{10} + \sqrt{2})$$

$$(\sqrt{7} + \sqrt{3})$$

$$\therefore \frac{\sqrt{7} + \sqrt{3}}{\sqrt{2}}$$

$$(a+b)^2 = a^2 + b^2 + 2ab$$

$$(a-b)^2 = a^2 + b^2 - 2ab$$

$$a^2 - b^2 = [a+b][a-b]$$

$$(a+b)^3 = a^3 + b^3 + 3ab(a+b)$$

$$(a-b)^3 = a^3 - b^3 - 3ab(a-b)$$

$$a^3 + b^3 \Rightarrow [a+b][a^2 - ab + b^2]$$

$$a^3 - b^3 \Rightarrow [a-b][a^2 + ab + b^2]$$

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ac$$

$$\underline{z + \frac{1}{z} = 10}, \quad \text{Find } \underline{\underline{z^2 + \frac{1}{z^2}}} =$$

$$(z + \frac{1}{z})^2 - 2$$

$$= 10^2 - 2$$

$$= \underline{\underline{98}} \checkmark$$

$$x - \frac{1}{x} = 5, \quad x^2 + \frac{1}{x^2} = ?$$

↓

$$(x - \frac{1}{x})^2 + 2$$

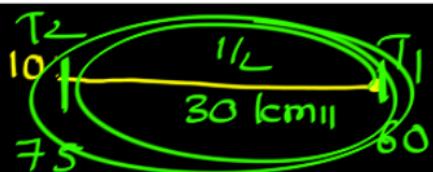
$$= \underline{\underline{27}}$$

23. Two trains for Mumbai leave Delhi at 10 am and 10.30 am and travel at the speeds of 60 kmph and 75 kmph respectively. How many kilometers from Delhi will the two trains be together.

- (a) 250 km
- (b) 200 km
- (c) 150 km
- (d) 100 km

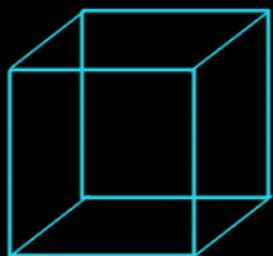
$$\frac{30}{75 - 60} = \frac{30}{15}$$

= 2 h<sup>y</sup>



## DICE

→ DICE Representation with cube.

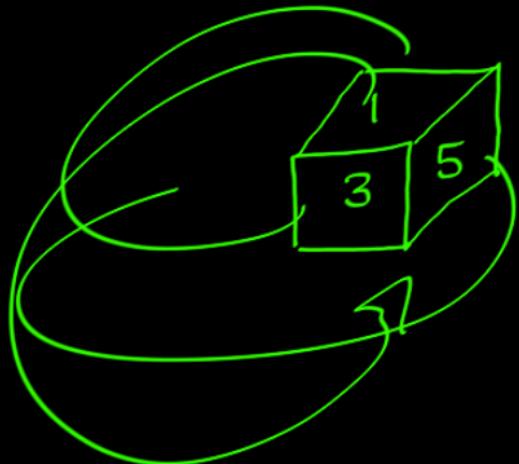


→ cube having - 6 surfaces. (1,2,3,4,5,6)

→ If A dice is rolled, then visibility = 3 faces only



We had only 1-DICE, but Every Time we are discussing  
about views only

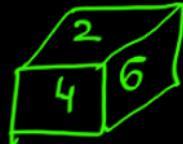


what is opposite  
surface?

## Standard dice

- Adjacent surfaces sum, does not equal to  $\textcircled{7}$ . then opposite surfaces sum should be "7"
- Such Type of dice is called standard dice.

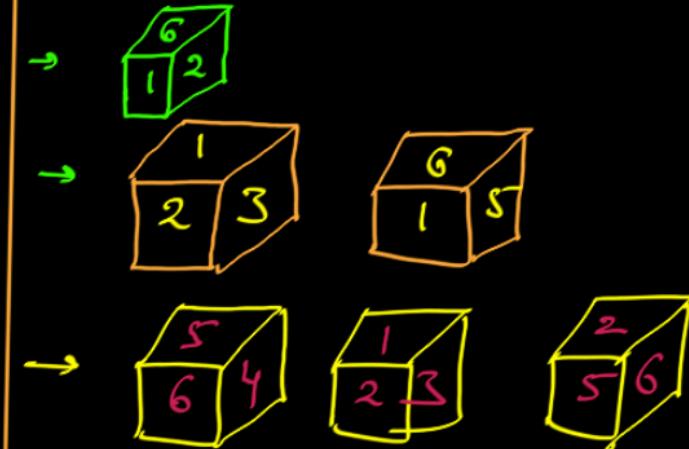
Ex:



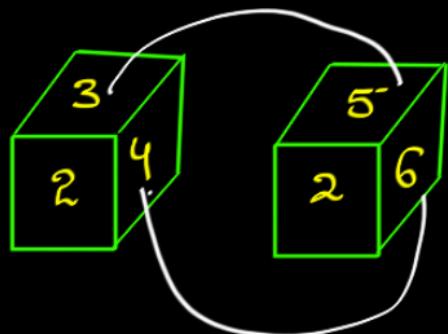
$$\begin{array}{l} 2-5 \\ 4-3 \\ 6-1 \end{array}$$

## General DICE

- One of the adjacent surfaces sum view is 7 such Type of dice is called General dice.



FQ1 Identify the opposite surface of General DICE



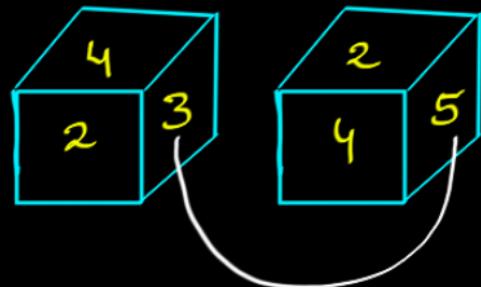
we have 1-common number and also same surface, then corresponding numbers are called opposite surfaces. and also remaining number is called opposite of common number.

3 - 5

4 - 6

2 - )

II



we have Two common numbers then  
remaining corresponding numbers  
are called opposite surfaces.

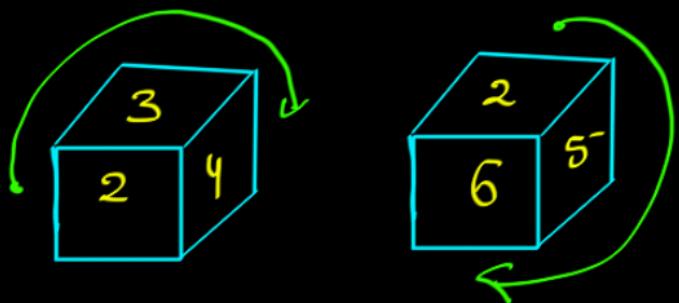
3-5 ✓

III) we had one- common number  
but different surfaces.

then  
From the common number  
we have to write the numbers  
as clock wise direction.

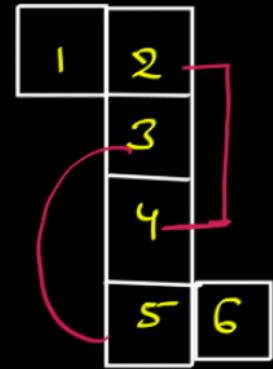
then

corresponding numbers are  
called oppsl- surfaces.

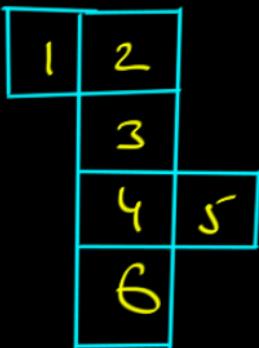


$$\begin{aligned} 2 \rightarrow & \begin{array}{|c|} \hline 3 \\ \hline \end{array} \quad \begin{array}{|c|} \hline 4 \\ \hline \end{array} \\ 2 \rightarrow & \begin{array}{|c|} \hline 5 \\ \hline \end{array} \quad \begin{array}{|c|} \hline 6 \\ \hline \end{array} \end{aligned}$$

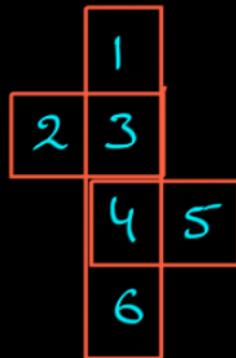
unfolded DICE given, we want To fold the DICE .



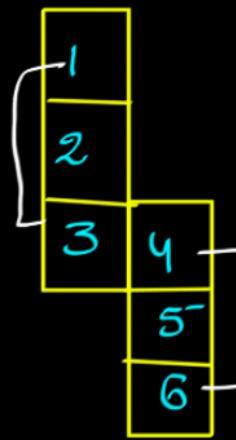
2-4  
3-5  
1-6



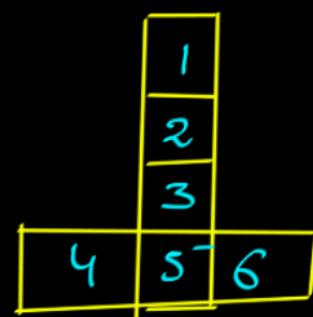
2-4  
3-6  
1-5



1-4  
3-6  
2-5



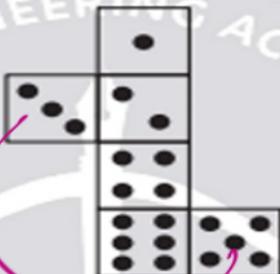
1-3  
4-6  
2-5



1-3  
4-6  
2-5

∴

09. When the following figure is folded to form a cube, how many dots would lie opposite the face bearing five dots?



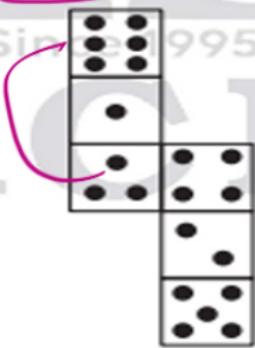
(a) 1

(b) 2

(c) 3

(d) 6

10. How many dots lie opposite the face having three dots, when the given figure is folded to form a cube?



(a) 2

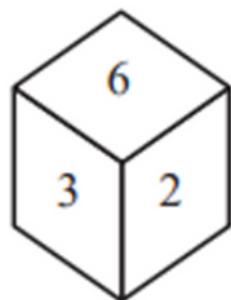
(b) 4

(c) 5

(d) 6

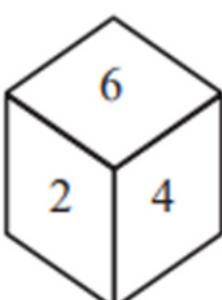
01. Which number is on the face opposite 6 ?

1



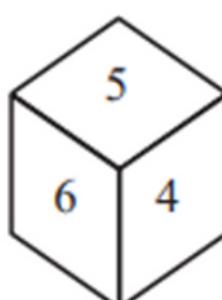
(i)

(a) 1



(ii)

(b) 2



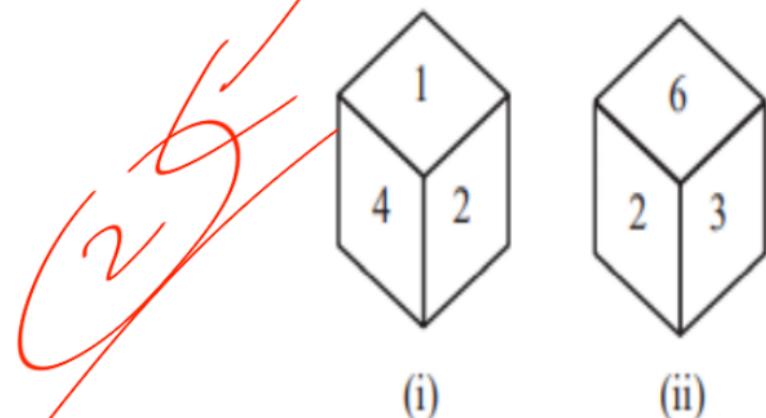
(iii)

(iv)

(c) 3

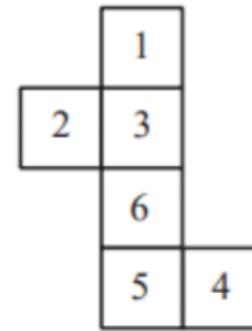
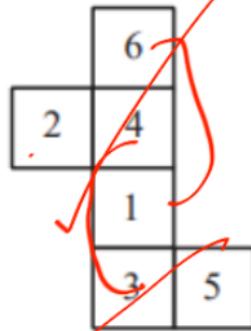
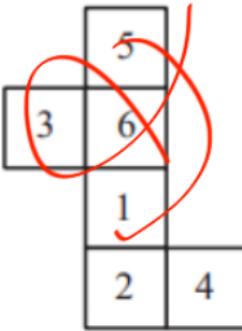
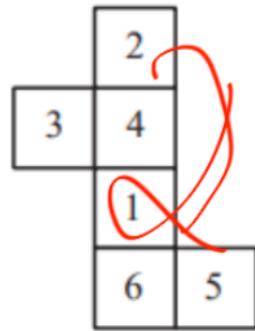
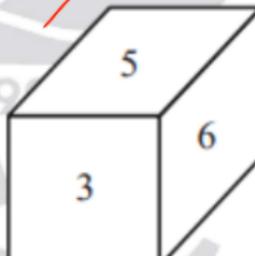
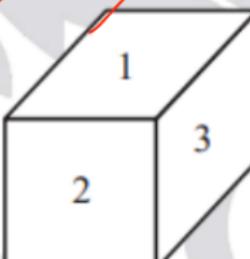
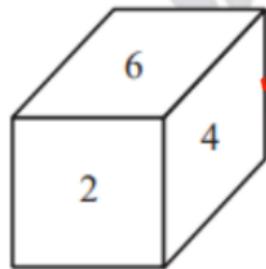
(d) 4

05. What will be the number at the bottom if 5 is at the top; the two positions of the dice being as given below:



- (a) 1
- (b) 2
- (c) 3
- (d) 6

07. The six faces of a cube have been marked with numbers 1, 2, 3, 4, 5 and 6 respectively. This cube is rolled down three times. The three positions are given. Choose the figure that will be formed when the cube is unfolded.



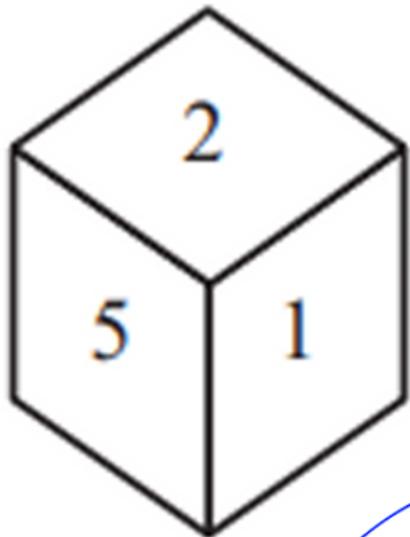
(a)

(b)

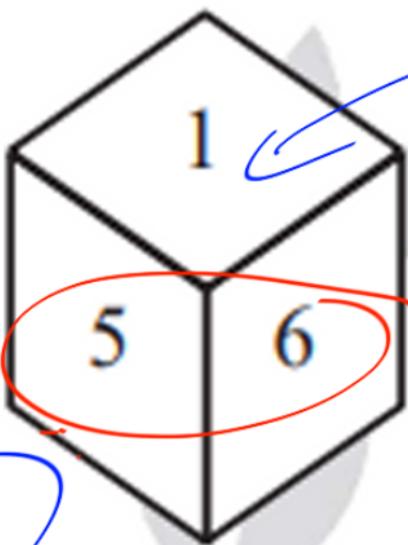
(c)

(d)

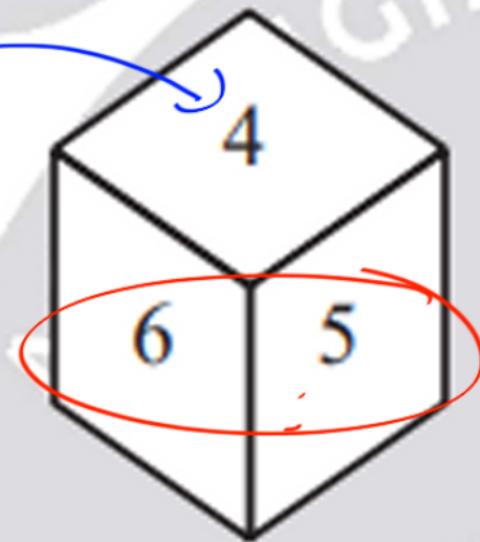
02. Which number is on the face opposite 4?



(i)

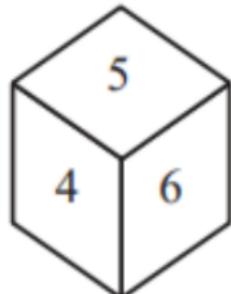


(ii)

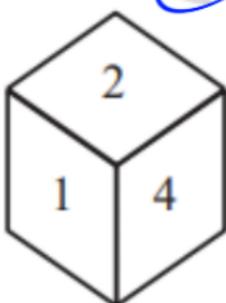


(iii)

03. Which number is opposite 3?



(i)



(ii)



(iii)



(iv)

(a) 1

(b) 2

(c) 4

(d) 6

3  
5

06. The six faces of cube as marked 1, 2, 3, 4, 5 & 6. Given below are two different view of same cube

Which face is opposite the face marked 6?

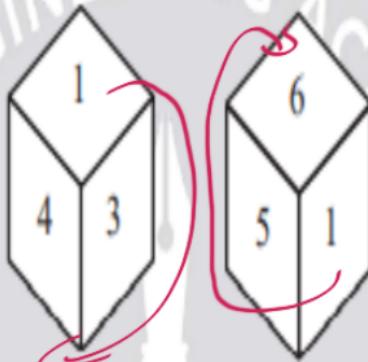
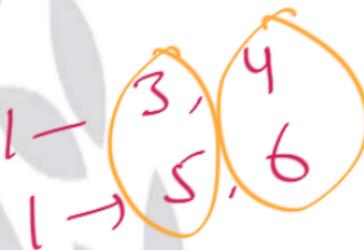


Fig (a)

Fig (b)



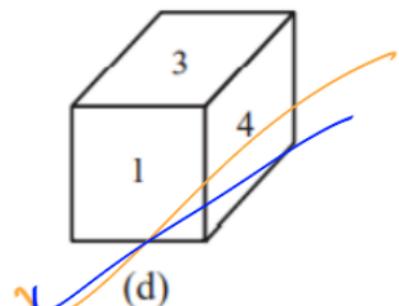
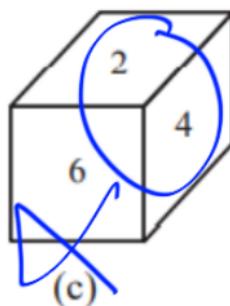
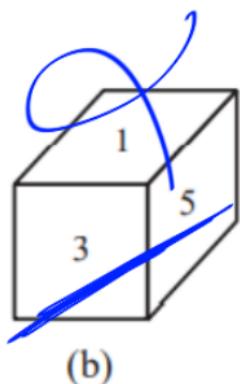
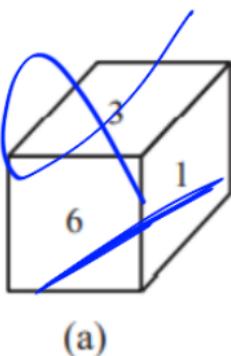
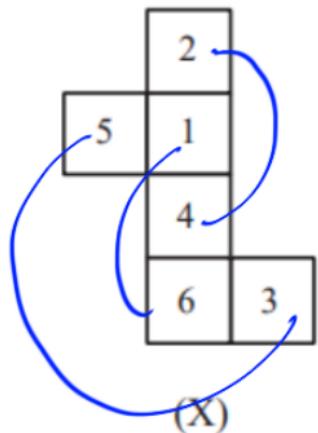
(a) 3

(b) 4

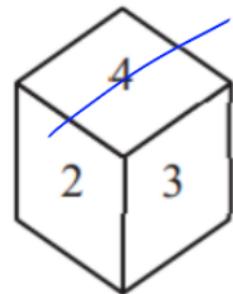
(c) 2

(d) None of these

08. If X figure is folded then which of the following cube is formed?

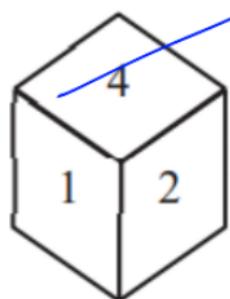


What numbers occur at the bottom face in the three positions of the same die?



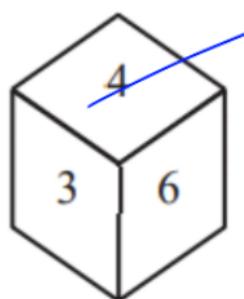
(i)

(a) 6, 6, 2



(ii)

(b) 5, 6, 1



(iii)

(c) 5, 5, 5

(d) 6, 5, 2