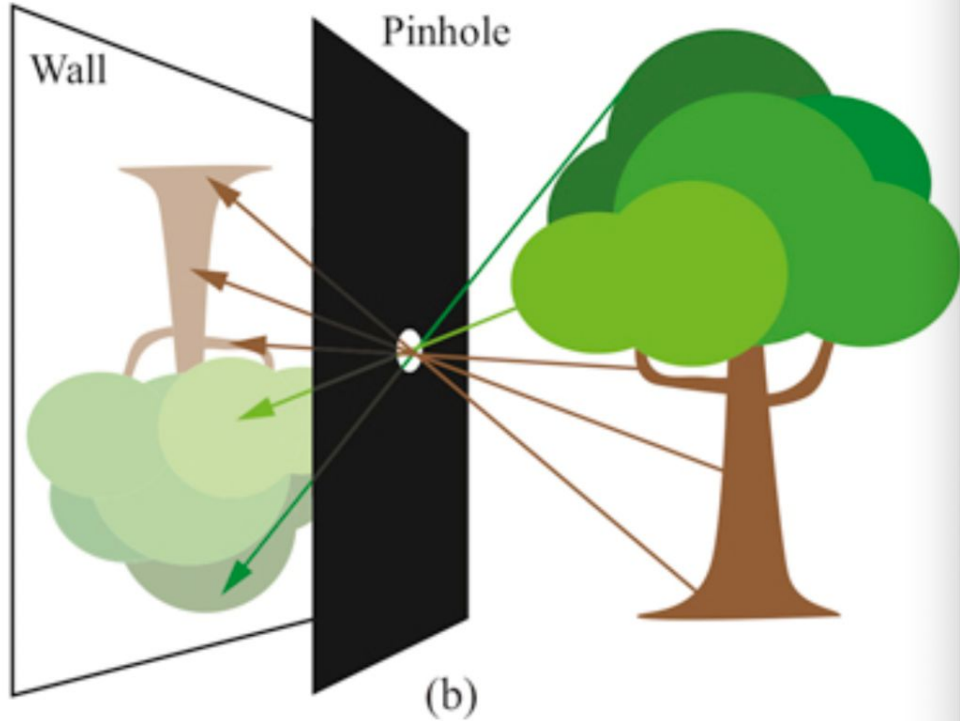
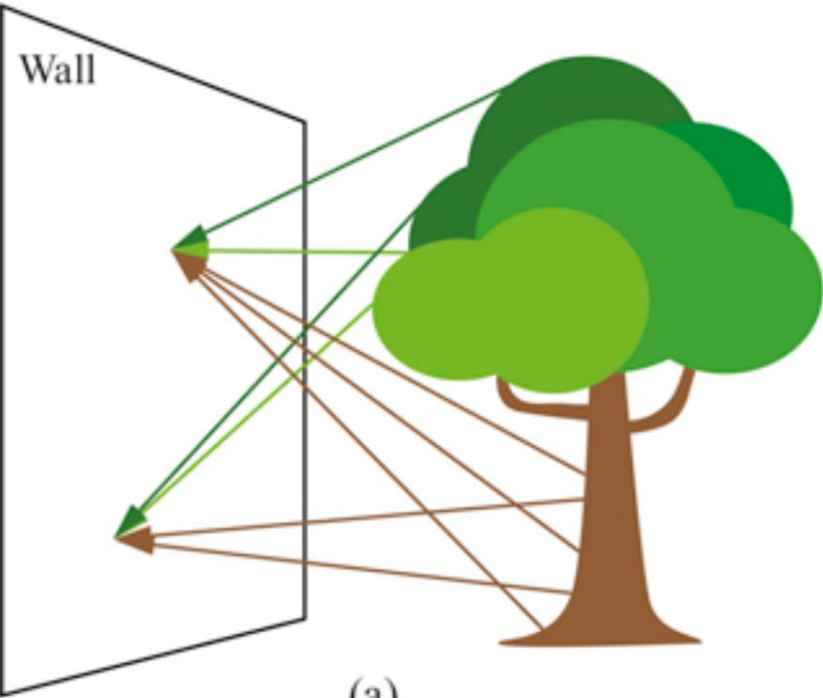


Image Formation

Pinhole Camera

Pinhole camera - Perspective Projection



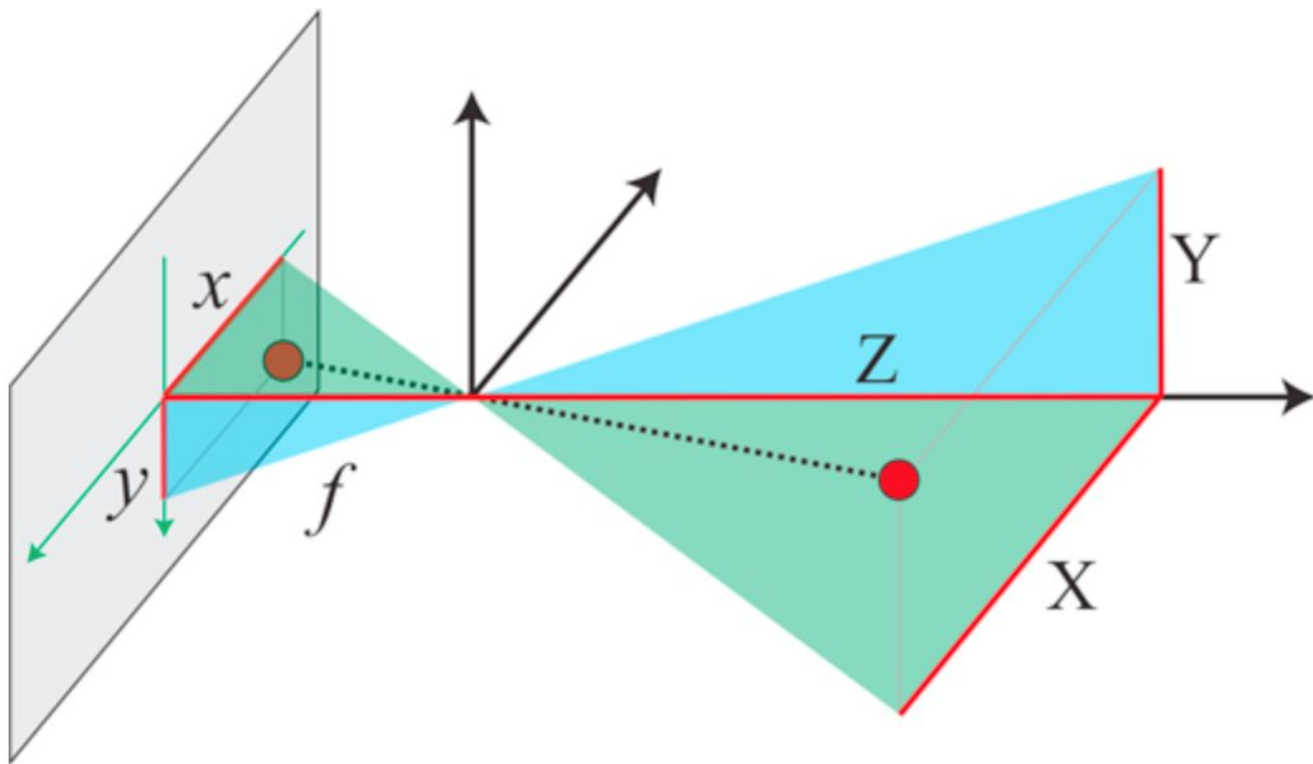


Figure 5.9: Perspective projection equations derived geometrically. From similar triangles, we have $x/f = X/Z$ and $y/f = Y/Z$. Similar triangles are indicated by the same color.

Perspective Projection

1. Perspective equations $x = f \frac{X}{Z}$ (5.6)

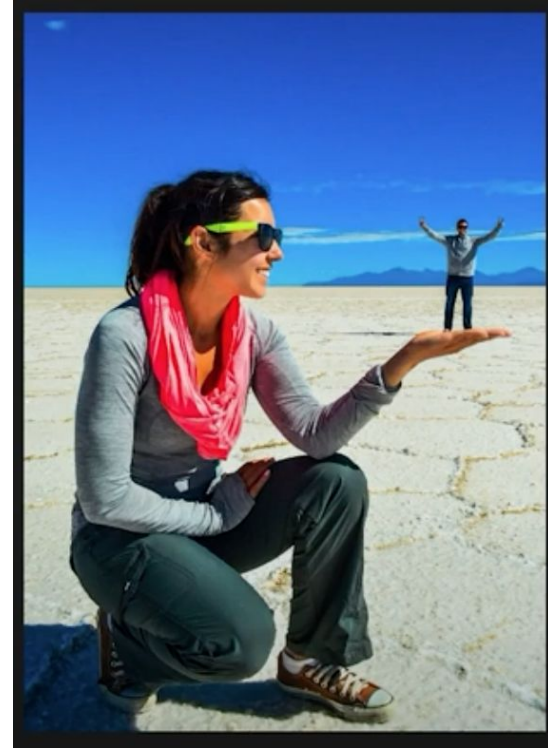
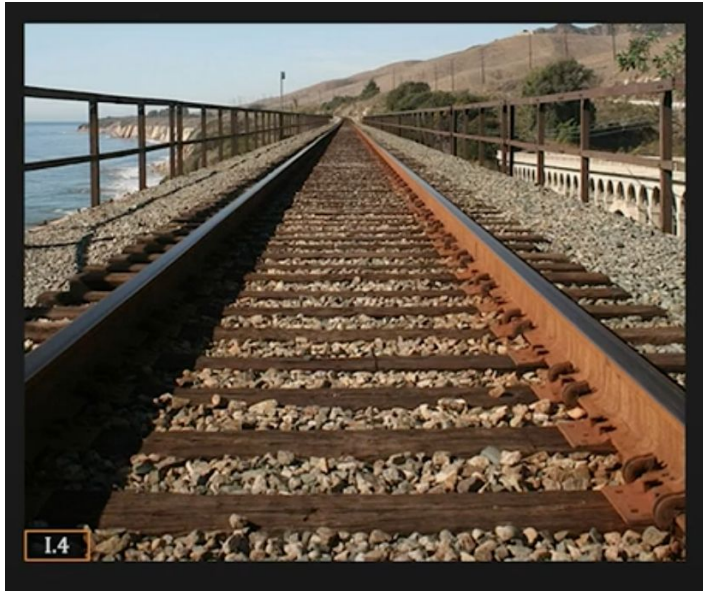
$$y = f \frac{Y}{Z} \quad (5.7)$$

2. “Under perspective projection, distant objects become smaller, through the inverse scaling by Z.”

3. Magnification = f / Z

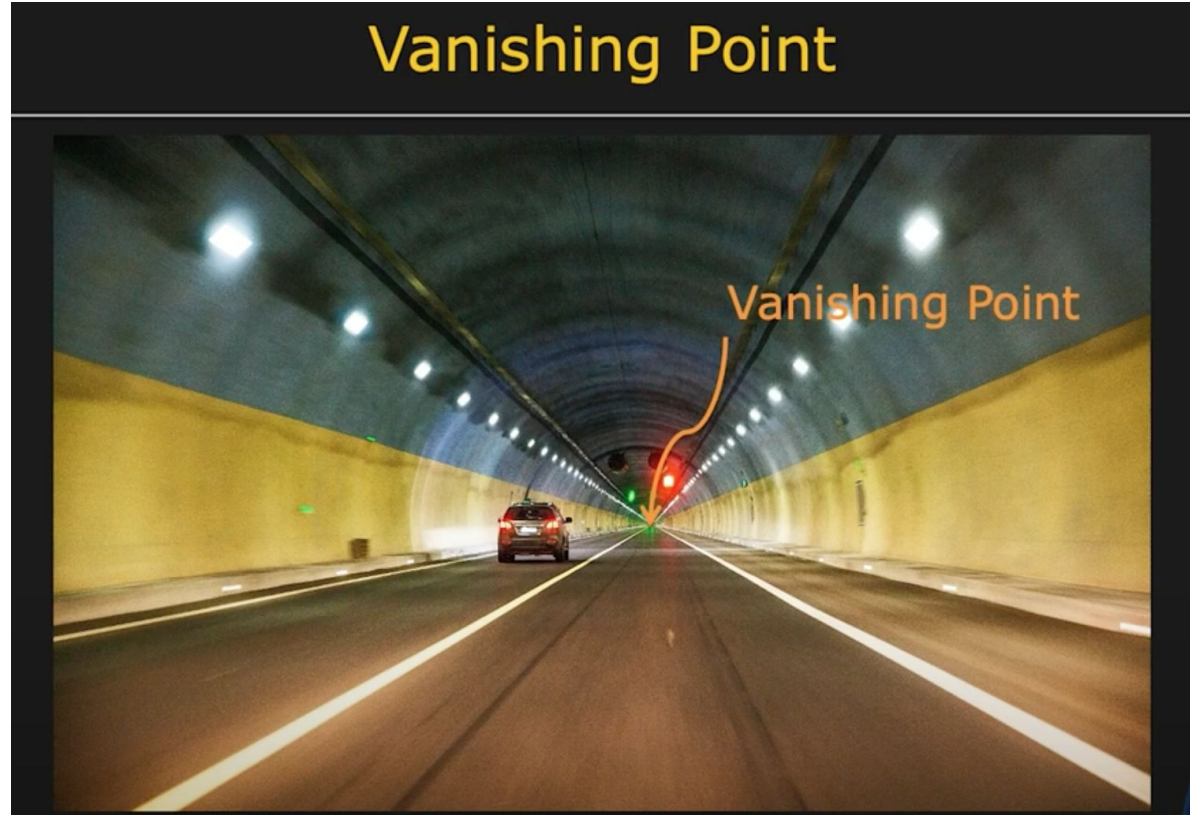
Perspective Projection - Magnification

1. Magnification $m = f / Z$
2. $\text{Area}_{\text{image}} = \text{Area}_{\text{object}} * m^2$



Vanishing Point

All parallel lines
share the same
vanishing point



Vanishing Point in Art

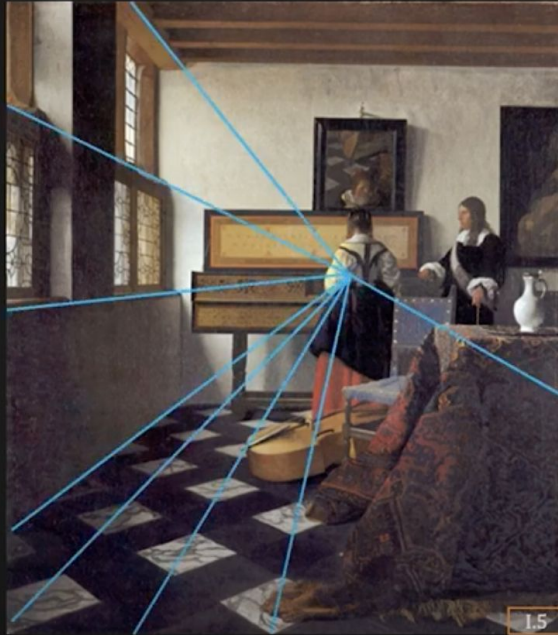
Use of Vanishing Point in Art



The Music Lesson, Johannes Vermeer, c. 1662-1664

Vanishing Point in Art

Use of Vanishing Point in Art



The Music Lesson, Johannes Vermeer, c. 1662-1664

False Perspective



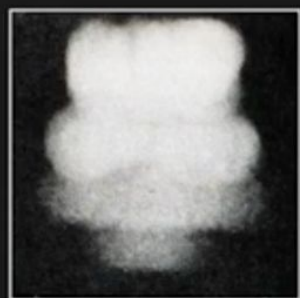
Depth appears to be ~155 feet



Depth is actually ~30 feet

Galleria Spada, Francesco Borromini, 1652

What is the Ideal Pinhole Size?



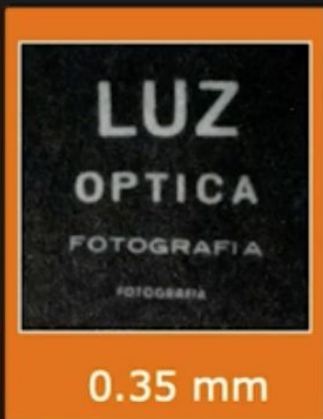
2 mm



1 mm



0.6 mm



0.35 mm



0.15 mm



0.07 mm

The pinhole must be **tiny**,
but if it's too tiny it will cause **diffraction**.

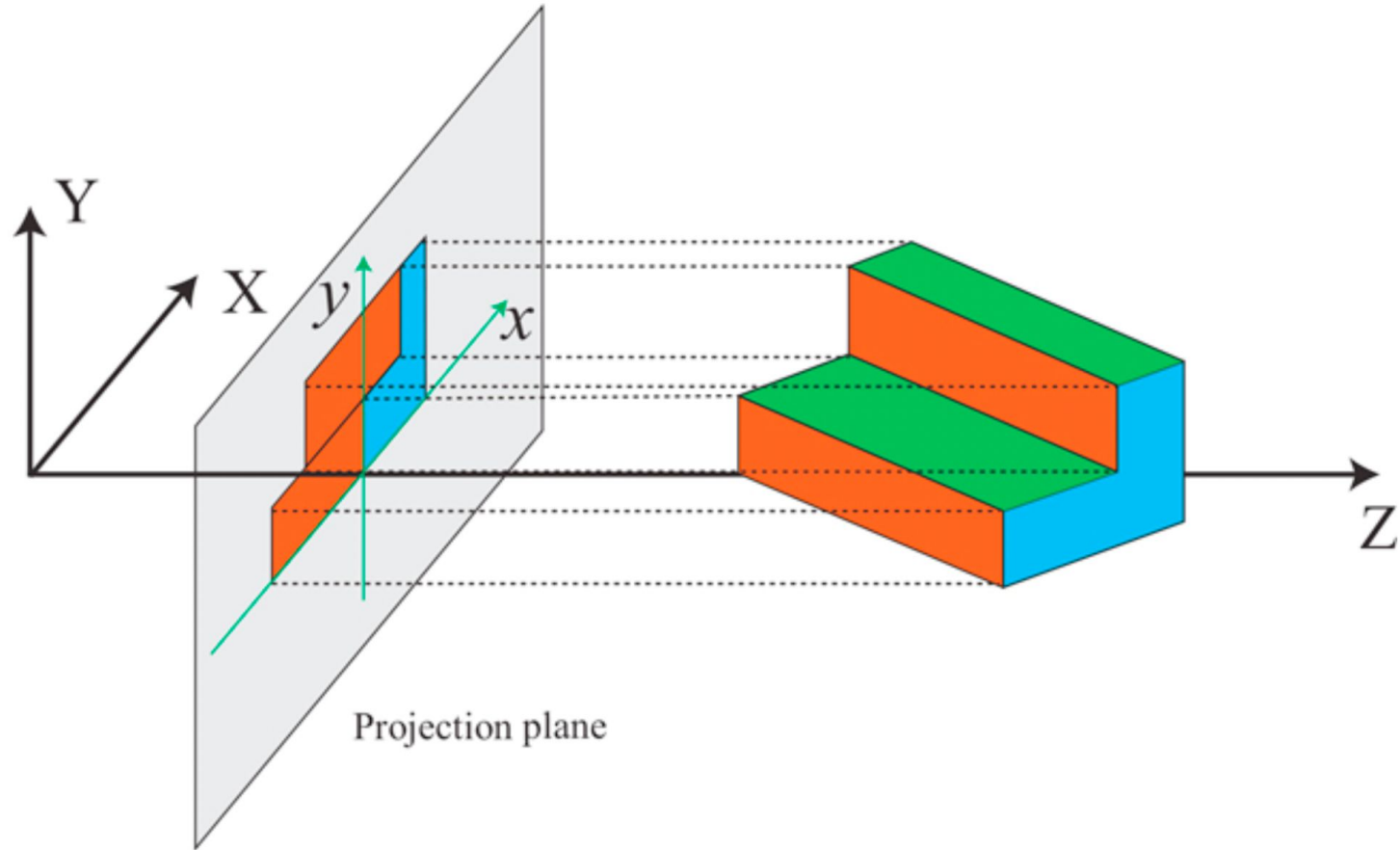
What about Exposure Time?

Pinholes pass less light and hence require **long exposures** to capture bright images.



$f = 73 \text{ mm}$, $d = 0.2 \text{ mm}$,
Exposure, $T = 12 \text{ s}$

Orthographic Projection



References

1. Foundations of Computer Vision - Chapter 5
2. Columbia University <https://fpcv.cs.columbia.edu>