



Indian Institute of Technology Bhubaneswar
School of Infrastructure

Subject Name : Solid Mechanics	Subject Code: CE2L001
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1. Different simple cases of transformations are illustrated in Fig.1, where α and β are arbitrary scalar positive values. Consider the two-dimensional context and determine the deformation map, $\chi(\mathbf{x})$, deformation gradient, \mathbf{F} , the strain tensor, $\mathbf{E} = (1/2)(\mathbf{F}^T \mathbf{F} - \mathbf{I})$, displacement vector, \mathbf{u} and the linearized strain tensor, \mathbf{E}_s , for each case.

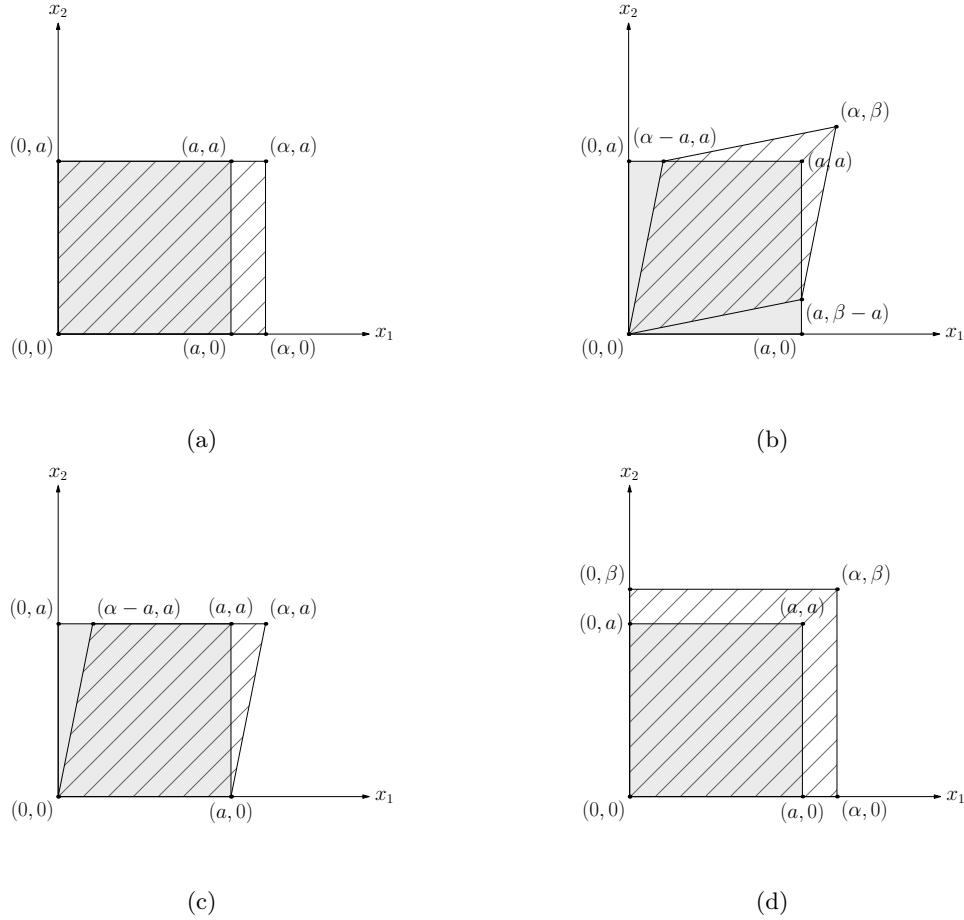


Figure 1: The undeformed and deformed configurations of a body under different cases of transformations with a, α, β denoting arbitrary scalar positive constants. The hatched area illustrates the deformed configurations.

2. Consider a homogeneous deformation corresponds to a strain field where the strain is the same at all points in a material body. Consider a prismatic, uniform thickness bar of initial length l_0 undergoing a homogeneous deformation as shown in Fig. 2. Determine (a) deformation gradient, \mathbf{F} , (b) finite strain, \mathbf{E} and (c) linearized strain, \mathbf{E}_s (d) Demonstrate how the finite strain component reduces to linearized strain component through a numerical example.

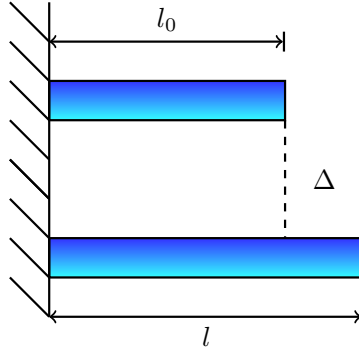


Figure 2: Undeformed and deformed element in the homogenous strain field in the bar.

3. Consider a two-dimensional (2D) square infinitesimal element in the $x_1 - x_2$ plane. The displacement field within the element is defined as,

$$[\mathbf{u}] = \begin{bmatrix} 0.1x_1 + 0.2x_2 \\ 0.2x_2 \end{bmatrix}.$$

- (a) Plot the displacement field. (b) Compute the divergence of the displacement field \mathbf{u} . (c) Determine the strain \mathbf{E} and linearized strain \mathbf{E}_s .

4. Consider the motion given by $[\mathbf{F}] = \begin{bmatrix} \lambda(t) & 0 & 0 \\ 0 & \lambda(t) & 0 \\ 0 & 0 & \lambda(t) \end{bmatrix}$, where $\lambda(t)$ is a time-dependent function.

Determine the values of $\lambda(t)$ for which the motion is a rigid body motion.

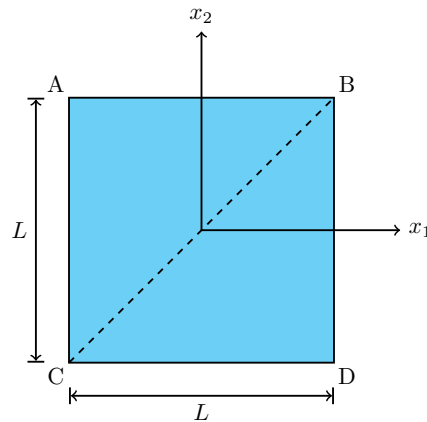


Figure 3: Inhomogeneous strain field

5. Consider the motion given by $\mathbf{x}' = \mathbf{x} + t^2 \mathbf{e}_1 + \sin(t) \mathbf{e}_2$. Determine if the motion is a rigid body motion by computing the strain tensor.
6. Consider the motion given by $\mathbf{x}' = \mathbf{Q}(t) \mathbf{x} + \mathbf{c}(t)$, where $\mathbf{Q}(t)$ is a time-dependent rotation matrix and $\mathbf{c}(t)$ is a time-dependent translation vector. Determine if the motion is a rigid body motion.
7. Consider the motion given by $\mathbf{u} = a x_1 \mathbf{e}_1 + b x_2 \mathbf{e}_2 + c x_3 \mathbf{e}_3$. Determine the values of a , b , and c for which the motion is a rigid body motion by computing the strain tensor.
8. Consider the motion given by $\mathbf{x}' = \mathbf{x} + a \sin(\omega t) \mathbf{e}_1 + b \cos(\omega t) \mathbf{e}_2$. Determine if the motion is a rigid body motion by computing the strain tensor.
9. Consider the motion given by $\mathbf{F} = \mathbf{I} + \gamma(t) \mathbf{e}_1 \otimes \mathbf{e}_2$. Determine the values of $\gamma(t)$ for which the motion is a rigid body motion by computing the strain tensor.
10. Consider the motion given by $\mathbf{u} = \beta(t) (x_2 \mathbf{e}_1 - x_1 \mathbf{e}_2)$, where $\beta(t)$ is a time-dependent function. Determine the values of $\beta(t)$ for which the motion is a rigid body motion.