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JEE Advanced 2019 - Paper 1 - Physics 11

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Problem [Multiple Choice Multiple Correct]

Let us consider a system of units in which mass and angular momentum are dimensionless. If length has dimension of L, which of the following statement(s) is/are correct?

- (A) The dimension of linear momentum is L⁻¹
- (B) The dimension of energy is L^{-2}
- (C) The dimension of force is L^{-3}
- (D) The dimension of power is L^{-5}

What to Observe:

- · Mass is dimensionless.
- · Angular momentum is dimensionless.
- · Length has dimension of L.
- · The system of units is such that some physical quantities may have different dimensional representations.

My Approach:

Converting SI System to New System

Thought

To convert any physical quantity from one system to another, we need to establish a dimensional equivalence between the two systems.

In the new system, mass is dimensionless. Therefore,

$$m \Rightarrow [M^0 L^0 T^0]$$

Next, consider the expression for angular momentum:

Angular Momentum = mvr

As **angular momentum is dimensionless** in the new system:

$$mvr \Rightarrow [M^0L^0T^0]$$

Since mass is dimensionless, it follows that:

$$vr \Rightarrow [M^0L^0T^0]$$

Thus, the velocity has dimensions:

$$v \Rightarrow \frac{1}{r} \Rightarrow [M^0 L^{-1} T^0]$$

In the SI system, the dimension of velocity is:

$$v_{\rm SI} \Rightarrow [L^1 T^{-1}]$$

Equating the two expressions for velocity:

$$[L^1T^{-1}]_{SI} = [M^0L^{-1}T^0]_{new}$$

From this, we can isolate the time dimension:

$$[T^{-1}]_{SI} = [M^0 L^{-2} T^0]_{new} \Rightarrow [T]_{SI} = [M^0 L^2 T^0]_{new}$$

This gives the equivalence for time in the SI system in terms of the new system.

Checking The Options

Thought

We have established the following equivalences:

- Mass: $[M^1L^0T^0]_{SI} = [M^0L^0T^0]_{new}$
- Length: $[M^0L^1T^0]_{SI} = [M^0L^1T^0]_{new}$
- Time: $[M^0L^0T^1]_{SI} = [M^0L^2T^0]_{new}$

Now, let us determine the dimensions of various physical quantities in the SI system and convert them to the new system.

Linear Momentum (p = mv):

$$[p]_{SI} = [M^1 L^1 T^{-1}]$$

Substituting each base unit:

$$\Rightarrow [M^0L^0T^0] \cdot [M^0L^1T^0] \cdot [M^0L^2T^0]^{-1} = [M^0L^{-1}T^0]_{\text{new}}$$

Therefore, Option A is incorrect.

Energy
$$(E = \frac{1}{2}mv^2 \text{ or } Fd)$$
:

$$[E]_{SI} = [M^1 L^2 T^{-2}]$$

Substituting:

$$\Rightarrow [M^0L^0T^0] \cdot [M^0L^1T^0]^2 \cdot [M^0L^2T^0]^{-2} = [M^0L^{-2}T^0]_{\text{new}}$$

Therefore, Option B is correct.

Force (F = ma):

$$[F]_{SI} = [M^1 L^1 T^{-2}]$$

Substituting:

$$\Rightarrow [M^0L^0T^0] \cdot [M^0L^1T^0] \cdot [M^0L^2T^0]^{-2} = [M^0L^{-3}T^0]_{\text{new}}$$

Therefore, **Option C** is correct.

Power $(P = \frac{E}{-})$:

$$[P]_{SI} = [M^1 L^2 T^{-3}]$$

Substituting:

$$\Rightarrow [M^0L^0T^0] \cdot [M^0L^1T^0]^2 \cdot [M^0L^2T^0]^{-3} = [M^0L^{-4}T^0]_{\text{new}}$$

Therefore, Option D is incorrect.

Conclusion

Based on the detailed analysis and the computed expression for the physical quantity under consideration:

Option A and Option D is incorrect because the calculated value does not agree with the value stated in that option.

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