

Introduction to Digital Electronics

Objectives

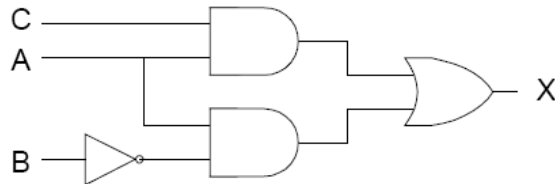
1. To draw the logic gate circuits of Boolean expressions
2. To write down the Boolean expressions of given circuit diagrams
3. To find Boolean expressions

Tasks

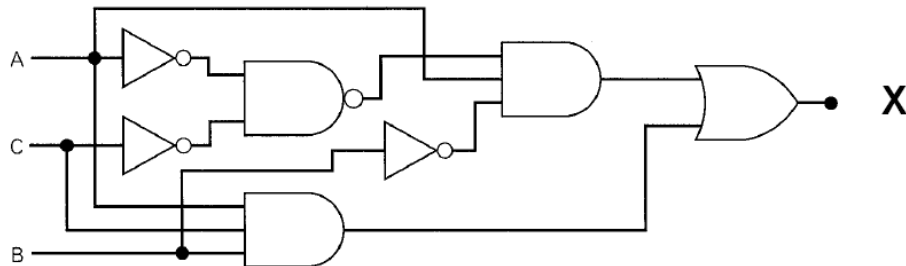
1. Draw the logic gate circuit corresponding to the following Boolean expression

$$F = (A' \cdot B' + A \cdot B) + (C' \cdot D' + C \cdot D)$$

2. Write the Boolean expression of the following circuit diagram. Set up the truth table



3. Write the Boolean expression of the following circuit diagram. Set up the truth table



4. Compare X of exercise 2 and exercise 3. The Boolean expression of X in exercise 3 can be simplified to the one of exercise 2.

5. Find the Boolean expression of a function $f(x,y,z)$ with three inputs and one output; $f(x,y,z)$ produces 1 when at least two of the inputs are 1, otherwise it produces 0

Step1: set up the truth table

x	y	z	$f(x, y, z)$
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

Step2: find all the Boolean sub-expressions only when $f(x,y,z)=1$, e.g., when $(x=0,y=1,z=1)$. The sub-expression is generated by inverting the inputs with zero and keeping the rest as they are, e.g., the subexpression for $(x=0,y=1,z=1)$ is $x'yz$.

Step3: $f(x,y,z)$ is given by adding all the sub-expressions found in step2.

Step4 (optional - not assessed): Simplify $f(x,y,z)$ using Boolean algebra. For those who are interested in how to simplify Boolean expressions, they can read the following link (Karnaugh maps) <https://www.geeksforgeeks.org/k-mapkarnaugh-map/>

6. Revisit and study the 4-bit ripple carry adder shown in the slides. Draw the circuit for an 8-bit ripple carry adder

Further Reading:

- Chapter 1 in 'Foundation of Digital Electronics and Logic Design', available at https://moodle.tktk.ee/pluginfile.php/270008/mod_resource/content/1/Foundation%20of%20Digital%20Electronics%20and%20Logic%20Design%20%5B2014%5D.pdf
- Chapter 11 in 'Computer Organization and architecture' available at http://home.ustc.edu.cn/~louwenqi/reference_books_tools/Computer%20Organization%20and%20Architecture%2010th%20-%20William%20Stallings.pdf