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### Homeomorphic Graph

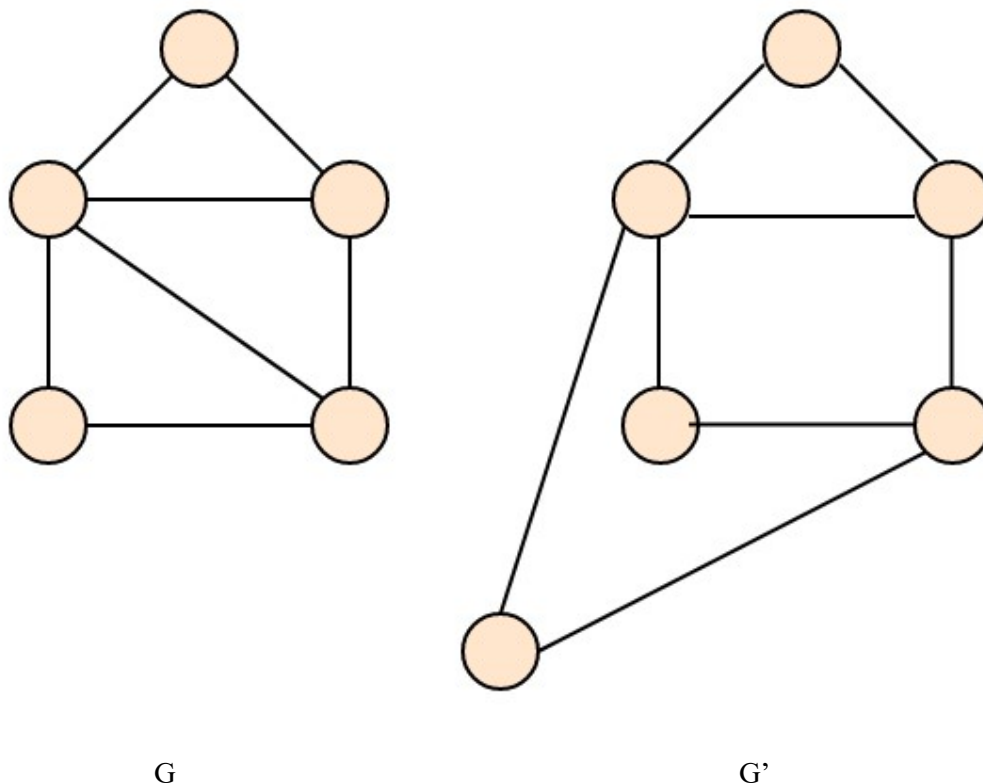
A graph homomorphism  $F$  from a graph  $G = (V, E)$  to a graph  $G' = (V', E')$  is written as:  $f: G \rightarrow G'$ . It is a mapping  $f: V \rightarrow V'$  from the vertex set of  $G$  to the vertex set of  $G'$  such that  $\{u, v\} \in E \Rightarrow \{f(u), f(v)\} \in E'$ .

In simple words, If another graph  $G^*$  can be formed by dividing the edge of  $G$  with additional vertices, or if a Graph  $G^*$  can be obtained by introducing vertices of degree 2 in any edge of a Graph  $G$ , then the graph  $G^*$  is complete. Both the graphs  $G$  and  $G^*$  are known as Homeomorphic graphs.

### Properties of Homeomorphic Graph

- Homomorphism always retains a graph's edges and connectedness.
- If a homomorphism is a bijective mapping, then it is an isomorphism.
- The compositions of homomorphisms are also homomorphisms.
- Finding out if there is any homomorphic graph of another graph is an NP-complete problem.

### Example



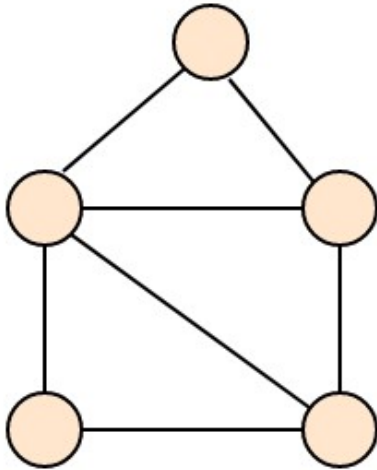


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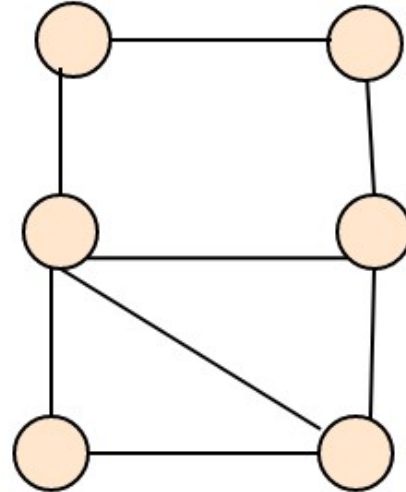
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H



H'

As we can see in both examples,  $G'$  can be derived from  $G$ , and  $H'$  can be derived from  $H$  by introducing a vertex of degree 2.