

## Chapter 6

# A SURVEY OF TEXT CLASSIFICATION ALGORITHMS

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**Abstract** The problem of classification has been widely studied in the data mining, machine learning, database, and information retrieval communities with applications in a number of diverse domains, such as target marketing, medical diagnosis, news group filtering, and document organization. In this paper we will provide a survey of a wide variety of text classification algorithms.

**Keywords:** Text Classification

## 1. Introduction

The problem of classification has been widely studied in the database, data mining, and information retrieval communities. The problem of classification is defined as follows. We have a set of training records  $\mathcal{D} = \{X_1, \dots, X_N\}$ , such that each record is labeled with a class value drawn from a set of  $k$  different discrete values indexed by  $\{1 \dots k\}$ . The training data is used in order to construct a *classification model*, which relates the features in the underlying record to one of the class labels. For a given *test instance* for which the class is unknown, the training model

is used to predict a class label for this instance. In the *hard version* of the classification problem, a particular label is explicitly assigned to the instance, whereas in the *soft version* of the classification problem, a probability value is assigned to the test instance. Other variations of the classification problem allow ranking of different class choices for a test instance, or allow the assignment of multiple labels [52] to a test instance.

The classification problem assumes categorical values for the labels, though it is also possible to use continuous values as labels. The latter is referred to as the regression modeling problem. The problem of text classification is closely related to that of classification of records with set-valued features [28]; however, this model assumes that only information about the presence or absence of words is used in a document. In reality, the frequency of words also plays a helpful role in the classification process, and the typical domain-size of text data (the entire lexicon size) is much greater than a typical set-valued classification problem. A broad survey of a wide variety of classification methods may be found in [42, 62], and a survey which is specific to the text domain may be found in [111]. A relative evaluation of different kinds of text classification methods may be found in [132]. A number of the techniques discussed in this chapter have also been converted into software and are publicly available through multiple toolkits such as the *BOW* toolkit [93], Mallot [96], WEKA <sup>1</sup>, and LingPipe <sup>2</sup>.

The problem of text classification finds applications in a wide variety of domains in text mining. Some examples of domains in which text classification is commonly used are as follows:

- **News filtering and Organization:** Most of the news services today are electronic in nature in which a large volume of news articles are created very single day by the organizations. In such cases, it is difficult to organize the news articles manually. Therefore, automated methods can be very useful for news categorization in a variety of web portals [78]. This application is also referred to as *text filtering*.
- **Document Organization and Retrieval:** The above application is generally useful for many applications beyond news filtering and organization. A variety of supervised methods may be used for document organization in many domains. These include large digital libraries of documents, web collections, scientific literature,

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<sup>1</sup><http://www.cs.waikato.ac.nz/ml/weka/>

<sup>2</sup><http://alias-i.com/lingpipe/>

or even social feeds. Hierarchically organized document collections can be particularly useful for browsing and retrieval [19].

- **Opinion Mining:** Customer reviews or opinions are often short text documents which can be mined to determine useful information from the review. Details on how classification can be used in order to perform opinion mining are discussed in [89] and Chapter 13 in this book.
- **Email Classification and Spam Filtering:** It is often desirable to classify email [23, 27, 85] in order to determine either the subject or to determine junk email [113] in an automated way. This is also referred to as *spam filtering* or *email filtering*.

A wide variety of techniques have been designed for text classification. In this chapter, we will discuss the broad classes of techniques, and their uses for classification tasks. We note that these classes of techniques also generally exist for other data domains such as quantitative or categorical data. Since text may be modeled as quantitative data with frequencies on the word attributes, it is possible to use most of the methods for quantitative data directly on text. However, text is a particular kind of data in which the word attributes are sparse, and high dimensional, with low frequencies on most of the words. Therefore, it is critical to design classification methods which effectively account for these characteristics of text. In this chapter, we will focus on the specific changes which are applicable to the text domain. Some key methods, which are commonly used for text classification are as follows:

- **Decision Trees:** Decision trees are designed with the use of a hierarchical division of the underlying data space with the use of different text features. The hierarchical division of the data space is designed in order to create class partitions which are more skewed in terms of their class distribution. For a given text instance, we determine the partition that it is most likely to belong to, and use it for the purposes of classification.
- **Pattern (Rule)-based Classifiers:** In rule-based classifiers we determine the word patterns which are most likely to be related to the different classes. We construct a set of rules, in which the left-hand side corresponds to a word pattern, and the right-hand side corresponds to a class label. These rules are used for the purposes of classification.
- **SVM Classifiers:** SVM Classifiers attempt to partition the data space with the use of linear or non-linear delineations between the

different classes. The key in such classifiers is to determine the optimal boundaries between the different classes and use them for the purposes of classification.

- **Neural Network Classifiers:** Neural networks are used in a wide variety of domains for the purposes of classification. In the context of text data, the main difference for neural network classifiers is to adapt these classifiers with the use of word features. We note that neural network classifiers are related to SVM classifiers; indeed, they both are in the category of discriminative classifiers, which are in contrast with the *generative classifiers* [102].
- **Bayesian (Generative) Classifiers:** In Bayesian classifiers (also called generative classifiers), we attempt to build a probabilistic classifier based on modeling the underlying word features in different classes. The idea is then to classify text based on the posterior probability of the documents belonging to the different classes on the basis of the word presence in the documents.
- **Other Classifiers:** Almost all classifiers can be adapted to the case of text data. Some of the other classifiers include nearest neighbor classifiers, and genetic algorithm-based classifiers. We will discuss some of these different classifiers in some detail and their use for the case of text data.

The area of text categorization is so vast that it is impossible to cover all the different algorithms in detail in a single chapter. Therefore, our goal is to provide the reader with an overview of the most important techniques, and also the pointers to the different variations of these techniques.

Feature selection is an important problem for text classification. In feature selection, we attempt to determine the features which are most relevant to the classification process. This is because some of the words are much more likely to be correlated to the class distribution than others. Therefore, a wide variety of methods have been proposed in the literature in order to determine the most important features for the purpose of classification. These include measures such as the gini-index or the entropy, which determine the level of which the presence of a particular feature skews the class distribution in the underlying data. We will also discuss the different feature selection methods which are commonly used for text classification.

The rest of this chapter is organized as follows. In the next section, we will discuss methods for feature selection in text classification. In section

3, we will describe decision tree methods for text classification. Rule-based classifiers are described in detail in section 4. We discuss naive Bayes classifiers in section 5. The nearest neighbor classifier is discussed in section 7. In section 7, we will discuss a number of linear classifiers, such as the SVM classifier, direct regression modeling and the neural network classifier. A discussion of how the classification methods can be adapted to text and web data containing hyperlinks is discussed in section 8. In section 9, we discuss a number of different meta-algorithms for classification such as boosting, bagging and ensemble learning. Section 10 contains the conclusions and summary.

## 2. Feature Selection for Text Classification

Before any classification task, one of the most fundamental tasks that needs to be accomplished is that of document representation and feature selection. While feature selection is also desirable in other classification tasks, it is especially important in text classification due to the high dimensionality of text features and the existence of irrelevant (noisy) features. In general, text can be represented in two separate ways. The first is as a bag of words, in which a document is represented as a set of words, together with their associated frequency in the document. Such a representation is essentially independent of the sequence of words in the collection. The second method is to represent text directly as *strings*, in which each document is a sequence of words. Most text classification methods use the bag-of-words representation because of its simplicity for classification purposes. In this section, we will discuss some of the methods which are used for feature selection in text classification.

The most common feature selection which is used in both supervised and unsupervised applications is that of stop-word removal and stemming. In stop-word removal, we determine the common words in the documents which are not specific or discriminatory to the different classes. In stemming, different forms of the same word are consolidated into a single word. For example, singular, plural and different tenses are consolidated into a single word. We note that these methods are not specific to the case of the classification problem, and are often used in a variety of unsupervised applications such as clustering and indexing. In the case of the classification problem, it makes sense to supervise the feature selection process with the use of the class labels. This kind of selection process ensures that those features which are highly skewed towards the presence of a particular class label are picked for the learning process. A wide variety of feature selection methods are discussed in [133, 135]. Many of these feature selection methods have been compared with one

another, and the experimental results are presented in [133]. We will discuss each of these feature selection methods in this section.

## 2.1 Gini Index

One of the most common methods for quantifying the discrimination level of a feature is the use of a measure known as the *gini-index*. Let  $p_1(w) \dots p_k(w)$  be the fraction of class-label presence of the  $k$  different classes for the word  $w$ . In other words,  $p_i(w)$  is the conditional probability that a document belongs to class  $i$ , given the fact that it contains the word  $w$ . Therefore, we have:

$$\sum_{i=1}^k p_i(w) = 1 \quad (6.1)$$

Then, the gini-index for the word  $w$ , denoted by  $G(w)$  is defined<sup>3</sup> as follows:

$$G(w) = \sum_{i=1}^k p_i(w)^2 \quad (6.2)$$

The value of the gini-index  $G(w)$  always lies in the range  $(1/k, 1)$ . Higher values of the gini-index  $G(w)$  represent indicate a greater discriminative power of the word  $w$ . For example, when all documents which contain word  $w$  belong to a particular class, the value of  $G(w)$  is 1. On the other hand, when documents containing word  $w$  are evenly distributed among the  $k$  different classes, the value of  $G(w)$  is  $1/k$ .

One criticism with this approach is that the global class distribution may be skewed to begin with, and therefore the above measure may sometimes not accurately reflect the discriminative power of the underlying attributes. Therefore, it is possible to construct a normalized gini-index in order to reflect the discriminative power of the attributes more accurately. Let  $P_1 \dots P_k$  represent the global distributions of the documents in the different classes. Then, we determine the normalized probability value  $p'_i(w)$  as follows:

$$p'_i(w) = \frac{p_i(w)/P_i}{\sum_{j=1}^k p_j(w)/P_j} \quad (6.3)$$

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<sup>3</sup>The gini-index is also sometimes defined as  $1 - \sum_{i=1}^k p_i(w)^2$ , with lower values indicating greater discriminative power of the feature  $w$ .

Then, the gini-index is computed in terms of these normalized probability values.

$$G(w) = \sum_{i=1}^k p'_i(w)^2 \quad (6.4)$$

The use of the global probabilities  $P_i$  ensures that the gini-index more accurately reflects class-discrimination in the case of biased class distributions in the whole document collection. For a document corpus containing  $n$  documents,  $d$  words, and  $k$  classes, the complexity of the information gain computation is  $O(n \cdot d \cdot k)$ . This is because the computation of the term  $p_i(w)$  for all the different words and the classes requires  $O(n \cdot d \cdot k)$  time.

## 2.2 Information Gain

Another related measure which is commonly used for text feature selection is that of information gain or entropy. Let  $P_i$  be the global probability of class  $i$ , and  $p_i(w)$  be the probability of class  $i$ , given that the document contains the word  $w$ . Let  $F(w)$  be the fraction of the documents containing the word  $w$ . The information gain measure  $I(w)$  for a given word  $w$  is defined as follows:

$$\begin{aligned} I(w) = & - \sum_{i=1}^k P_i \cdot \log(P_i) + F(w) \cdot \sum_{i=1}^k p_i(w) \cdot \log(p_i(w)) + \\ & + (1 - F(w)) \cdot \sum_{i=1}^k (1 - p_i(w)) \cdot \log(1 - p_i(w)) \end{aligned}$$

The greater the value of the information gain  $I(w)$ , the greater the discriminatory power of the word  $w$ . For a document corpus containing  $n$  documents and  $d$  words, the complexity of the information gain computation is  $O(n \cdot d \cdot k)$ .

## 2.3 Mutual Information

This *mutual information measure* is derived from information theory [31], and provides a formal way to model the mutual information between the features and the classes. The pointwise mutual information  $M_i(w)$  between the word  $w$  and the class  $i$  is defined on the basis of the level of co-occurrence between the class  $i$  and word  $w$ . We note that the expected co-occurrence of class  $i$  and word  $w$  on the basis of mutual independence is given by  $P_i \cdot F(w)$ . The true co-occurrence is of course given by  $F(w) \cdot p_i(w)$ . In practice, the value of  $F(w) \cdot p_i(w)$  may be much

larger or smaller than  $P_i \cdot F(w)$ , depending upon the level of correlation between the class  $i$  and word  $w$ . The mutual information is defined in terms of the ratio between these two values. Specifically, we have:

$$M_i(w) = \log \left( \frac{F(w) \cdot p_i(w)}{F(w) \cdot P_i} \right) = \log \left( \frac{p_i(w)}{P_i} \right) \quad (6.5)$$

Clearly, the word  $w$  is positively correlated to the class  $i$ , when  $M_i(w) > 0$ , and the word  $w$  is negatively correlated to class  $i$ , when  $M_i(w) < 0$ . We note that  $M_i(w)$  is specific to a particular class  $i$ . We need to compute the overall mutual information as a function of the mutual information of the word  $w$  with the different classes. These are defined with the use of the average and maximum values of  $M_i(w)$  over the different classes.

$$M_{avg}(w) = \sum_{i=1}^k P_i \cdot M_i(w)$$

$$M_{max}(w) = \max_i \{M_i(w)\}$$

Either of these measures may be used in order to determine the relevance of the word  $w$ . The second measure is particularly useful, when it is more important to determine high levels of positive correlation of the word  $w$  with any of the classes.

## 2.4 $\chi^2$ -Statistic

The  $\chi^2$  statistic is a different way to compute the lack of independence between the word  $w$  and a particular class  $i$ . Let  $n$  be the total number of documents in the collection,  $p_i(w)$  be the conditional probability of class  $i$  for documents which contain  $w$ ,  $P_i$  be the global fraction of documents containing the class  $i$ , and  $F(w)$  be the global fraction of documents which contain the word  $w$ . The  $\chi^2$ -statistic of the word between word  $w$  and class  $i$  is defined as follows:

$$\chi_i^2(w) = \frac{n \cdot F(w)^2 \cdot (p_i(w) - P_i)^2}{F(w) \cdot (1 - F(w)) \cdot P_i \cdot (1 - P_i)} \quad (6.6)$$

As in the case of the mutual information, we can compute a global  $\chi^2$  statistic from the class-specific values. We can use either the average of maximum values in order to create the composite value:

$$\chi_{avg}^2(w) = \sum_{i=1}^k P_i \cdot \chi_i^2(w)$$

$$\chi_{max}^2(w) = \max_i \chi_i^2(w)$$



We note that the  $\chi^2$ -statistic and mutual information are different ways of measuring the correlation between terms and categories. One major advantage of the  $\chi^2$ -statistic over the mutual information measure is that it is a normalized value, and therefore these values are more comparable across terms in the same category.

## 2.5 Feature Transformation Methods: Supervised LSI

While feature selection attempts to reduce the dimensionality of the data by picking from the original set of attributes, feature transformation methods create a new (and smaller) set of features as a function of the original set of features. A typical example of such a feature transformation method is Latent Semantic Indexing (LSI) [38], and its probabilistic variant pLSA [57]. The LSI method transforms the text space of a few hundred thousand word features to a new axis system (of size about a few hundred) which are a linear combination of the original word features. In order to achieve this goal, Principal Component Analysis techniques [69] are used to determine the axis-system which retains the greatest level of information about the variations in the underlying attribute values. The main disadvantage of using techniques such as LSI is that these are unsupervised techniques which are blind to the underlying class-distribution. Thus, the features found by LSI are not necessarily the directions along which the *class-distribution* of the underlying documents can be best separated. A modest level of success has been obtained in improving classification accuracy by using boosting techniques in conjunction with the conceptual features obtained from unsupervised pLSA method [17]. A more recent study has systematically compared pLSA and LDA (which is a Bayesian version of pLSA) in terms of their effectiveness in transforming features for text categorization and drawn a similar conclusion and found that pLSA and LDA tend to perform similarly.

A number of techniques have also been proposed to perform the feature transformation methods by using the class labels for effective supervision. The most natural method is to adapt LSI in order to make it work more effectively for the supervised case. A number of different methods have been proposed in this direction. One common approach is to perform local LSI on the subsets of data representing the individual classes, and identify the discriminative eigenvectors from the different reductions with the use of an iterative approach [123]. This method is known as SLSI (Supervised Latent Semantic Indexing), and the advantages of the method seem to be relatively limited, because the experiments in [123]

show that the improvements over a standard SVM classifier, which did not use a dimensionality reduction process, are relatively limited. The work in [129] uses a combination of class-specific LSI and global analysis. As in the case of [123], class-specific LSI representations are created. Test documents are compared against each LSI representation in order to create the most discriminative reduced space. One problem with this approach is that the different local LSI representations use a different subspace, and therefore it is difficult to compare the similarities of the different documents across the different subspaces. Furthermore, both the methods in [123, 129] tend to be computationally expensive.

A method called *sprinkling* is proposed in [21], in which artificial terms are added to (or “sprinkled” into) the documents, which correspond to the class labels. In other words, we create a term corresponding to the class label, and add it to the document. LSI is then performed on the document collection with these added terms. The sprinkled terms can then be removed from the representation, once the eigenvectors have been determined. The sprinkled terms help in making the LSI more sensitive to the class distribution during the reduction process. It has also been proposed in [21] that it can be generally useful to make the sprinkling process *adaptive*, in which all classes are not necessarily treated equally, but the relationships between the classes are used in order to regulate the sprinkling process. Furthermore, methods have also been proposed in [21] to make the sprinkling process adaptive to the use of a particular kind of classifier.

## 2.6 Supervised Clustering for Dimensionality Reduction

One technique which is commonly used for feature transformation is that of text clustering [7, 71, 83, 121]. In these techniques, the clusters are constructed from the underlying text collection, with the use of supervision from the class distribution. The exception is [83] in which supervision is not used. In the simplest case, each class can be treated as a separate cluster, though better results may be obtained by using the classes for supervision of the clustering process. The frequently occurring words in these supervised clusters can be used in order to create the new set of dimensions. The classification can be performed with respect to this new feature representation. One advantage of such an approach is that it retains interpretability with respect to the original words of the document collection. The disadvantage is that the optimum directions of separation may not necessarily be represented in the form of clusters of words. Furthermore, the underlying axes are not necessarily orthonor-

mal to one another. The use of supervised methods [1, 7, 71, 121] has generally led to good results either in terms of improved classification accuracy, or significant performance gains at the expense of a small reduction in accuracy. The results with the use of unsupervised clustering [83, 87] are mixed. For example, the work in [83] suggests that the use of unsupervised term-clusters and phrases is generally not helpful [83] for the classification process. The key observation in [83] is that the loss of granularity associated with the use of phrases and term clusters is not necessarily advantageous for the classification process. The work in [8] has shown that the use of the information bottleneck method for feature distributional clustering can create clustered pseudo-word representations which are quite effective for text classification.

## 2.7 Linear Discriminant Analysis

Another method for feature transformation is the use of linear discriminants, which explicitly try to construct directions in the feature space, along which there is best separation of the different classes. A common method is the *Fisher's linear discriminant* [46]. The main idea in the Fisher's discriminant method is to determine the directions in the data along which the points are as well separated as possible. The subspace of lower dimensionality is constructed by iteratively finding such unit vectors  $\alpha_i$  in the data, where  $\alpha_i$  is determined in the  $i$ th iteration. We would also like to ensure that the different values of  $\alpha_i$  are orthonormal to one another. In each step, we determine this vector  $\alpha_i$  by discriminant analysis, and project the data onto the remaining orthonormal subspace. The next vector  $\alpha_{i+1}$  is found in this orthonormal subspace. The quality of vector  $\alpha_i$  is measured by an objective function which measures the separation of the different classes. This objective function reduces in each iteration, since the value of  $\alpha_i$  in a given iteration is the optimum discriminant in that subspace, and the vector found in the next iteration is the optimal one from a smaller search space. The process of finding linear discriminants is continued until the class separation, as measured by an objective function, reduces below a given threshold for the vector determined in the current iteration. The power of such a dimensionality reduction approach has been illustrated in [18], in which it has been shown that a simple decision tree classifier can perform much more effectively on this transformed data, as compared to more sophisticated classifiers.

Next, we discuss how the Fisher's discriminant is actually constructed. First, we will set up the objective function  $J(\bar{\alpha})$  which determines the level of separation of the different classes along a given direction (unit-

vector)  $\bar{\alpha}$ . This sets up the crisp optimization problem of determining the value of  $\bar{\alpha}$  which maximizes  $J(\bar{\alpha})$ . For simplicity, let us assume the case of binary classes. Let  $D_1$  and  $D_2$  be the two sets of documents belonging to the two classes. Then, the projection of a document  $\bar{X} \in D_1 \cup D_2$  along  $\bar{\alpha}$  is given by  $\bar{X} \cdot \bar{\alpha}$ . Therefore, the squared class separation  $S(D_1, D_2, \bar{\alpha})$  along the direction  $\bar{\alpha}$  is given by:

$$S(D_1, D_2, \bar{\alpha}) = \left( \frac{\sum_{\bar{X} \in D_1} \bar{\alpha} \cdot \bar{X}}{|D_1|} - \frac{\sum_{\bar{X} \in D_2} \bar{\alpha} \cdot \bar{X}}{|D_2|} \right)^2 \quad (6.7)$$

In addition, we need to normalize this absolute class separation with the use of the underlying class variances. Let  $Var(D_1, \bar{\alpha})$  and  $Var(D_2, \bar{\alpha})$  be the individual class variances along the direction  $\alpha$ . In other words, we have:

$$Var(D_1, \bar{\alpha}) = \frac{\sum_{\bar{X} \in D_1} (\bar{X} \cdot \bar{\alpha})^2}{|D_1|} - \left( \frac{\sum_{\bar{X} \in D_1} \bar{X} \cdot \bar{\alpha}}{|D_1|} \right)^2 \quad (6.8)$$

The value of  $Var(D_2, \bar{\alpha})$  can be defined in a similar way. Then, the normalized class-separation  $J(\bar{\alpha})$  is defined as follows:

$$J(\bar{\alpha}) = \frac{S(D_1, D_2, \bar{\alpha})}{Var(D_1, \bar{\alpha}) + Var(D_2, \bar{\alpha})} \quad (6.9)$$

The optimal value of  $\alpha$  needs to be determined subject to the constraint that  $\bar{\alpha}$  is a unit vector. Let  $\mu_1$  and  $\mu_2$  be the means of the two data sets  $D_1$  and  $D_2$ , and  $C_1$  and  $C_2$  be the corresponding covariance matrices. It can be shown that the optimal (unscaled) direction  $\bar{\alpha} = \bar{\alpha}^*$  can be expressed in closed form, and is given by the following:

$$\bar{\alpha}^* = \left( \frac{C_1 + C_2}{2} \right)^{-1} (\mu_1 - \mu_2) \quad (6.10)$$

The main difficulty in computing the above equation is that this computation requires the inversion of the covariance matrix, which is sparse and computationally difficult in the high-dimensional text domain. Therefore, a gradient descent approach can be used in order to determine the value of  $\bar{\alpha}$  in a more computationally effective way. Details of the approach are presented in [18].

Another related method which attempts to determine projection directions that maximize the topical differences between different classes is the *Topical Difference Factor Analysis* method proposed in [72]. The problem has been shown to be solvable as a generalized eigenvalue problem. The method was used in conjunction with a  $k$ -nearest neighbor

classifier, and it was shown that the use of this approach significantly improves the accuracy over a classifier which uses the original set of features.

## 2.8 Generalized Singular Value Decomposition

While the method discussed above finds one vector  $\bar{\alpha}_i$  at a time in order to determine the relevant dimension transformation, it is possible to be much more direct in finding the optimal subspaces simultaneously by using a generalized version of dimensionality reduction [58, 59]. It is important to note that this method has really been proposed in [58, 59] as an *unsupervised* method which preserves the underlying *clustering* structure, assuming the data has already been clustered in a pre-processing phase. Thus, the generalized dimensionality reduction method has been proposed as a much more aggressive dimensionality reduction technique, which preserves the underlying clustering structure rather than the individual points. This method can however also be used as a *supervised* technique in which the different classes are used as input to the dimensionality reduction algorithm, instead of the clusters constructed in the pre-processing phase [131]. This method is known as the *Optimal Orthogonal Centroid Feature Selection Algorithm (OCFS)*, and it directly targets at the maximization of inter-class scatter. The algorithm is shown to have promising results for supervised feature selection in [131].

## 2.9 Interaction of Feature Selection with Classification

Since the classification and feature selection processes are dependent upon one another, it is interesting to test how the feature selection process interacts with the underlying classification algorithms. In this context, two questions are relevant:

- Can the feature-specific insights obtained from the intermediate results of some of the classification algorithms be used for creating feature selection methods that can be used more generally by other classification algorithms?
- Do the different feature selection methods work better or worse with different kinds of classifiers?

Both these issues were explored in some detail in [99]. In regard to the first question, it was shown in [99] that feature selection which was derived from *linear* classifiers, provided very effective results. In regard to the second question, it was shown in [99] that the sophistication of

the feature selection process itself was more important than the specific pairing between the feature selection process and the classifier.

*Linear Classifiers* are those for which the output of the linear predictor is defined to be  $p = \bar{A} \cdot \bar{X} + b$ , where  $\bar{X} = (x_1 \dots x_n)$  is the normalized document word frequency vector,  $\bar{A} = (a_1 \dots a_n)$  is a vector of linear coefficients with the same dimensionality as the feature space, and  $b$  is a scalar. Both the basic neural network and basic SVM classifiers [65] (which will be discussed later in this chapter) belong to this category. The idea here is that if the coefficient  $a_i$  is close to zero, then the corresponding feature does not have a significant effect on the classification process. On the other hand, since large absolute values of  $a_j$  may significantly influence the classification process, such features should be selected for classification. In the context of the SVM method, which attempts to determine linear planes of separation between the different classes, the vector  $\bar{A}$  is essentially the normal vector to the corresponding plane of separation between the different classes. This intuitively explains the choice of selecting features with large values of  $|a_j|$ . It was shown in [99] that this class of feature selection methods was quite robust, and performed well even for classifiers such as the Naive Bayes method, which were unrelated to the linear classifiers from which these features were derived. Further discussions on how SVM and maximum margin techniques can be used for feature selection may be found in [51, 56].

### 3. Decision Tree Classifiers

A decision tree [106] is essentially a hierarchical decomposition of the (training) data space, in which a *predicate* or a condition on the attribute value is used in order to divide the data space hierarchically. In the context of text data, such predicates are typically conditions on the presence or absence of one or more words in the document. The division of the data space is performed recursively in the decision tree, until the leaf nodes contain a certain minimum number of records, or some conditions on class purity. The majority class label (or cost-weighted majority label) in the leaf node is used for the purposes of classification. For a given test instance, we apply the sequence of predicates at the nodes, in order to traverse a path of the tree in top-down fashion and determine the relevant leaf node. In order to further reduce the overfitting, some of the nodes may be pruned by holding out a part of the data, which are not used to construct the tree. The portion of the data which is held out is used in order to determine whether or not the constructed leaf node should be pruned or not. In particular, if the class distribution in the

training data (for decision tree construction) is very different from the class distribution in the training data which is used for pruning, then it is assumed that the node overfits the training data. Such a node can be pruned. A detailed discussion of decision tree methods may be found in [15, 42, 62, 106].

In the particular case of text data, the predicates for the decision tree nodes are typically defined in terms of the terms in the underlying text collection. For example, a node may be partitioned into its children nodes depending upon the presence or absence of a particular term in the document. We note that different nodes at the same level of the tree may use different terms for the partitioning process.

Many other kinds of predicates are possible. It may not be necessary to use individual terms for partitioning, but one may measure the similarity of documents to correlated sets of terms. These correlated sets of terms may be used to further partition the document collection, based on the similarity of the document to them. The different kinds of splits are as follows:

- **Single Attribute Splits:** In this case, we use the presence or absence of particular words (or even phrases) at a particular node in the tree in order to perform the split. At any given level, we pick the word which provides the maximum discrimination between the different classes. Measures such as the gini-index or information gain can be used in order to determine the level of entropy. For example, the DT-min10 algorithm [81] is based on this approach.
- **Similarity-based multi-attribute split:** In this case, we use documents (or meta-documents such as frequent word clusters), and use the similarity of the documents to these words clusters in order to perform the split. For the selected word cluster, the documents are further partitioned into groups by rank ordering the documents by similarity value, and splitting at a particular threshold. We select the word-cluster for which rank-ordering by similarity provides the best separation between the different classes.
- **Discriminant-based multi-attribute split:** For the multi-attribute case, a natural choice for performing the split is to use discriminants such as the Fisher discriminant for performing the split. Such discriminants provide the directions in the data along which the classes are best separated. The documents are projected on this discriminant vector for rank ordering, and then split at a particular coordinate. The choice of split point is picked in order to maximize the discrimination between the different classes.

The work in [18] uses a discriminant-based split, though this is done indirectly because of the use of a feature transformation to the discriminant representation, before building the classifier.

Some of the earliest implementation of classifiers may be found in [80, 81, 87, 127]. The last of these is really a rule-based classifier, which can be interpreted either as a decision tree or a rule-based classifier. Most of the decision tree implementations in the text literature tend to be small variations on standard packages such as ID3 and C4.5, in order to adapt the model to text classification. Many of these classifiers are typically designed as baselines for comparison with other learning models [65].

A well known implementation of the decision tree classifier is based on the C4.5 taxonomy of algorithms [106] is presented in [87]. More specifically, the work in [87] uses the successor to the C4.5 algorithm, which is also known as the C5 algorithm. This algorithm uses single-attribute splits at each node, where the feature with the highest information gain [31] is used for the purpose of the split. Decision trees have also been used in conjunction with boosting techniques. An adaptive boosting technique [48] is used in order to improve the accuracy of classification. In this technique, we use  $n$  different classifiers. The  $i$ th classifier is constructed by examining the errors of the  $(i - 1)$ th classifier. A voting scheme is applied among these classifiers in order to report the final label. Other boosting techniques for improving decision tree classification accuracy are proposed in [116].

The work in [43] presents a decision tree algorithm based on the Bayesian approach developed in [22]. In this classifier, the decision tree is grown by recursive greedy splits, where the splits are chosen using Bayesian posterior probability of model structure. The structural prior penalizes additional model parameters at each node. The output of the process is a class probability rather than a deterministic class label for the test instance.

## 4. Rule-based Classifiers

Decision trees are also generally related to *rule-based classifiers*. In rule-based classifiers, the data space is modeled with a set of rules, in which the left hand side is a condition on the underlying feature set, and the right hand side is the class label. The rule set is essentially the model which is generated from the training data. For a given test instance, we determine the set of rules for which the test instance satisfies the condition on the left hand side of the rule. We determine the predicted class label as a function of the class labels of the rules which are satisfied by the test instance. We will discuss more on this issue slightly later.



In its most general form, the left hand side of the rule is a boolean condition, which is expressed in Disjunctive Normal Form (DNF). However, in most cases, the condition on the left hand side is much simpler and represents a set of terms, all of which must be present in the document for the condition to be satisfied. The *absence* of terms is rarely used, because such rules are not likely to be very informative for sparse text data, in which most words in the lexicon will typically not be present in it by default (sparseness property). Also, while the *set intersection* of conditions on term presence is used often, the union of such conditions is rarely used in a single rule. This is because such rules can be split into two separate rules, each of which is more informative on its own. For example, the rule  $Honda \cup Toyota \Rightarrow Cars$  can be replaced by two separate rules  $Honda \Rightarrow Cars$  and  $Toyota \Rightarrow Cars$  without any loss of information. In fact, since the confidence of each of the two rules can now be measured separately, this can be more useful. On the other hand, the rule  $Honda \cap Toyota \Rightarrow Cars$  is certainly much more informative than the individual rules. Thus, in practice, for sparse data sets such as text, rules are much more likely to be expressed as a simple conjunction of conditions on term presence.

We note that decision trees and decision rules both tend to encode rules on the feature space, except that the decision tree tends to achieve this goal with a hierarchical approach. In fact, the original work on decision tree construction in C4.5 [106] studied the decision tree problem and decision rule problem within a single framework. This is because a particular path in the decision tree can be considered a rule for classification of the text instance. The main difference is that the decision tree framework is a strict hierarchical partitioning of the data space, whereas rule-based classifiers allow for overlaps in the decision space. The general principle is to create a rule set, such that all points in the decision space are covered by *at least* one rule. In most cases, this is achieved by generating a set of targeted rules which are related to the different classes, and one default *catch-all* rule, which can cover all the remaining instances.

A number of criteria can be used in order to generate the rules from the training data. Two of the most common conditions which are used for rule generation are those of *support* and *confidence*. These conditions are common to all rule-based pattern classifiers [88] and may be defined as follows:

- **Support:** This quantifies the **absolute number** of instances in the training data set which are relevant to the rule. For example, in a corpus containing 100,000 documents, a rule in which **both** the left-hand set and right-hand side are satisfied by 50,000 documents

is more important than a rule which is satisfied by 20 documents. Essentially, this quantifies the statistical *volume* which is associated with the rule. However, it does not encode the strength of the rule.

- **Confidence:** This quantifies the **conditional probability** that the right hand side of the rule is satisfied, if the left-hand side is satisfied. This is a more direct measure of the strength of the underlying rule.

We note that the afore-mentioned measures are not the only measures which are possible, but are widely used in the data mining and machine learning literature [88] for both textual and non-textual data, because of their intuitive nature and simplicity of interpretation. One criticism of the above measures is that they do not normalize for the a-priori presence of different terms and features, and are therefore prone to misinterpretation, when the feature distribution or class-distribution in the underlying data set is skewed.

The training phase constructs all the rules, which are based on measures such as the above. For a given test instance, we determine all the rules which are relevant to the test instance. Since we allow overlaps, it is possible that more than one rule may be relevant to the test instance. If the class labels on the right hand sides of all these rules are the same, then it is easy to pick this class as the relevant label for the test instance. On the other hand, the problem becomes more challenging when there are conflicts between these different rules. A variety of different methods are used to rank-order the different rules [88], and report the most relevant rule as a function of these different rules. For example, a common approach is to rank-order the rules by their confidence, and pick the top- $k$  rules as the most relevant. The class label on the right-hand side of the most number of these rules is reported as the relevant one.

An interesting rule-based classifier for the case of text data has been proposed in [5]. This technique uses an iterative methodology, which was first proposed in [128] for generating rules. Specifically, the method determines the single best rule related to any particular class in the training data. The best rule is defined in terms of the confidence of the rule, as defined above. This rule along with its corresponding instances are removed from the training data set. This approach is continuously repeated, until it is no longer possible to find strong rules in the training data, and complete predictive value is achieved.

The transformation of decision trees to rule-based classifiers is discussed generally in [106], and for the particular case of text data in [68]. For each path in the decision tree a rule can be generated, which repre-

sents the conjunction of the predicates along that path. One advantage of the rule-based classifier over a decision tree is that it is not restricted to a strict hierarchical partitioning of the feature space, and it allows for overlaps and inconsistencies among the different rules. Therefore, if a new set of training examples are encountered, which are related to a new class or new part of the feature space, then it is relatively easy to modify the rule set for these new examples. Furthermore, rule-based classifiers also allow for a tremendous interpretability of the underlying decision space. In cases in which domain-specific expert knowledge is known, it is possible to encode this into the classification process by manual addition of rules. In many practical scenarios, rule-based techniques are more commonly used because of their ease of maintenance and interpretability.

One of the most common rule-based techniques is the *RIPPER* technique discussed in [26–28]. The *RIPPER* technique essentially determines frequent combinations of words which are related to a particular class. The *RIPPER* method has been shown to be especially effective in scenarios where the number of training examples is relatively small [25]. Another method called *sleeping experts* [26, 49] generates rules which take the placement of the words in the documents into account. Most of the classifiers such as *RIPPER* [26–28] treat documents as set-valued objects, and generate rules based on the co-presence of the words in the documents. The rules in *sleeping experts* are different from most of the other classifiers in this respect. In this case [49, 26], the left hand side of the rule consists of a *sparse phrase*, which is a group of words close to one another in the document (though not necessarily completely sequential). Each such rule has a weight, which depends upon its classification specificity in the training data. For a given test example, we determine the sparse phrases which are present in it, and perform the classification by combining the weights of the different rules that are fired. The *sleeping experts* and *RIPPER* systems have been compared in [26], and have been shown to have excellent performance on a variety of text collections.

## 5. Probabilistic and Naive Bayes Classifiers

Probabilistic classifiers are designed to use an implicit mixture model for generation of the underlying documents. This mixture model typically assumes that each class is a component of the mixture. Each mixture component is essentially a generative model, which provides the probability of sampling a particular term for that component or class. This is why this kind of classifiers are often also called generative classifier. The naive Bayes classifier is perhaps the simplest and also the most

commonly used generative classifiers. It models the distribution of the documents in each class using a probabilistic model with independence assumptions about the distributions of different terms. Two classes of models are commonly used for naive Bayes classification. Both models essentially compute the posterior probability of a class, based on the distribution of the words in the document. These models ignore the actual position of the words in the document, and work with the “bag of words” assumption. The major difference between these two models is the assumption in terms of taking (or not taking) word frequencies into account, and the corresponding approach for sampling the probability space:

- **Multivariate Bernoulli Model:** In this model, we use the presence or absence of words in a text document as features to represent a document. Thus, the frequencies of the words are not used for the modeling a document, and the word features in the text are assumed to be binary, with the two values indicating presence or absence of a word in text. Since the features to be modeled are binary, the model for documents in each class is a multivariate Bernoulli model.
- **Multinomial Model:** In this model, we capture the frequencies of terms in a document by representing a document with a bag of words. The documents in each class can then be modeled as samples drawn from a multinomial word distribution. As a result, the conditional probability of a document given a class is simply a product of the probability of each observed word in the corresponding class.

No matter how we model the documents in each class (be it a multivariate Bernoulli model or a multinomial model), the component class models (i.e., generative models for documents in each class) can be used in conjunction with the Bayes rule to compute the posterior probability of the class for a given document, and the class with the highest posterior probability can then be assigned to the document.

There has been considerable confusion in the literature on the differences between the multivariate Bernoulli model and the multinomial model. A good exposition of the differences between these two models may be found in [94]. In the following, we describe these two models in more detail.

## 5.1 Bernoulli Multivariate Model

This class of techniques treats a document as a set of distinct words with no frequency information, in which an element (term) may be either present or absent. The seminal work on this approach may be found in [82].

Let us assume that the lexicon from which the terms are drawn are denoted by  $V = \{t_1 \dots t_n\}$ . Let us assume that the bag-of-words (or text document) in question contains the terms  $Q = \{t_{i_1} \dots t_{i_m}\}$ , and the class is drawn from  $\{1 \dots k\}$ . Then, our goal is to model the posterior probability that the document (which is assumed to be generated from the term distributions of one of the classes) belongs to class  $i$ , given that it contains the terms  $Q = \{t_{i_1} \dots t_{i_m}\}$ . The best way to understand the Bayes method is by understanding it as a sampling/generative process from the underlying mixture model of classes. The Bayes probability of class  $i$  can be modeled by sampling a set of terms  $T$  from the term distribution of the classes:

*If we sampled a term set  $T$  of any size from the term distribution of one of the randomly chosen classes, and the final outcome is the set  $Q$ , then what is the posterior probability that we had originally picked class  $i$  for sampling? The a-priori probability of picking class  $i$  is equal to its fractional presence in the collection.*

We denote the class of the sampled set  $T$  by  $C^T$  and the corresponding posterior probability by  $P(C^T = i | T = Q)$ . This is essentially what we are trying to find. It is important to note that since we do not allow replacement, we are essentially picking a subset of terms from  $V$  with no frequencies attached to the picked terms. Therefore, the set  $Q$  may not contain duplicate elements. Under the naive Bayes assumption of independence between terms, this is essentially equivalent to either selecting or not selecting each term with a probability that depends upon the underlying term distribution. Furthermore, it is also important to note that this model has no restriction on the number of terms picked. As we will see later, these assumptions are the key differences with the multinomial Bayes model. The Bayes approach classifies a given set  $Q$  based on the posterior probability that  $Q$  is a sample from the data distribution of class  $i$ , i.e.,  $P(C^T = i | T = Q)$ , and it requires us to compute the following two probabilities in order to achieve this:

- 1 What is the prior probability that a set  $T$  is a sample from the term distribution of class  $i$ ? This probability is denoted by  $P(C^T = i)$ .

- 2 If we sampled a set  $T$  of any size from the term distribution of class  $i$ , then what is the probability that our sample is the set  $Q$ ? This probability is denoted by  $P(T = Q|C^T = i)$ .

We will now provide a more mathematical description of Bayes modeling. In other words, we wish to model  $P(C^T = i|Q \text{ is sampled})$ . We can use the Bayes rule in order to write this conditional probability in a way that can be *estimated* more easily from the underlying corpus. In other words, we can simplify as follows:

$$\begin{aligned} P(C^T = i|T = Q) &= \frac{P(C^T = i) \cdot P(T = Q|C^T = i)}{P(T = Q)} \\ &= \frac{P(C^T = i) \cdot \prod_{t_j \in Q} P(t_j \in T|C^T = i) \cdot \prod_{t_j \notin Q} (1 - P(t_j \in T|C^T = i))}{P(T = Q)} \end{aligned}$$

We note that the last condition of the above sequence uses the *naive independence assumption*, because we are assuming that the probabilities of occurrence of the different terms are independent of one another. This is practically necessary, in order to transform the probability equations to a form which can be estimated from the underlying data.

The class assigned to  $Q$  is the one with the highest posterior probability given  $Q$ . It is easy to see that this decision is not affected by the denominator, which is the marginal probability of observing  $Q$ . That is, we will assign the following class to  $Q$ :

$$\begin{aligned} \hat{i} &= \arg \max_i P(C^T = i|T = Q) \\ &= \arg \max_i P(C^T = i) \cdot \\ &\quad \prod_{t_j \in Q} P(t_j \in T|C^T = i) \cdot \prod_{t_j \notin Q} (1 - P(t_j \in T|C^T = i)). \end{aligned}$$

It is important to note that all terms in the right hand side of the last equation can be estimated from the training corpus. The value of  $P(C^T = i)$  is estimated as the global fraction of documents belonging to class  $i$ , the value of  $P(t_j \in T|C^T = i)$  is the fraction of documents in the  $i$ th class which contain term  $t_j$ , and the value of  $P(t_j \in T)$  is the fraction of documents (in the whole corpus) containing the term  $t_j$ . We note that all of the above are maximum likelihood estimates of the corresponding probabilities. In practice, Laplacian smoothing [124] is used, in which small values are added to the frequencies of terms in order to avoid zero probabilities of sparsely present terms.

In most applications of the Bayes classifier, we only care about the *identity of the* class with the highest probability value, rather than the

actual probability value associated with it, which is why we do not need to compute the normalizer  $P(T = Q)$ . In fact, in the case of **binary** classes, a number of simplifications are possible in computing these Bayes “probability” values by using the logarithm of the Bayes expression, and removing a number of terms which do not affect the ordering of class probabilities. We refer the reader to [108] for details.

Although for classification, we do not need to compute  $P(T = Q)$ , some applications necessitate the exact computation of the posterior probability  $P(C^T = i|T = Q)$ . For example, in the case of supervised anomaly detection (or rare class detection), the exact posterior probability value  $P(C^T = i|T = Q)$  is needed in order to fairly compare the probability value over different test instances, and rank them for their anomalous nature. In such cases, we would need to compute  $P(T = Q)$ . One way to achieve this is simply to take a sum over all the classes:

$$P(T = Q) = \sum_i P(T = Q|C^T = i)P(C^T = i).$$

This is based on the conditional independence of features for each class. Since the parameter values are estimated for each class separately, we may face the problem of data sparseness. An alternative way of computing it, which may alleviate the data sparseness problem, is to further make the assumption of (global) independence of terms, and compute it as:

$$P(T = Q) = \prod_{j \in Q} P(t_j \in T) \cdot \prod_{t_j \notin Q} (1 - P(t_j \in T))$$

where the term probabilities are based on global term distributions in *all* the classes.

A natural question arises, as to whether it is possible to design a Bayes classifier which does not use the naive assumption, and models the dependencies between the terms during the classification process. Methods which generalize the naive Bayes classifier by not using the independence assumption do not work well because of the higher computational costs and the inability to estimate the parameters accurately and robustly in the presence of limited data. The most interesting line of work in relaxing the independence assumption is provided in [112]. In this work, the tradeoffs in spectrum of allowing different levels of dependence among the terms have been explored. On the one extreme, an assumption of complete dependence results in a Bayesian network model which turns out to be computationally very expensive. On the other hand, it has been shown that allowing limited levels of dependence can provide good tradeoffs between accuracy and computational costs. We note that while the independence assumption is a practical approximation, it has been

shown in [29, 39] that the approach does have some theoretical merit. Indeed, extensive experimental tests have tended to show that the naive classifier works quite well in practice.

A number of papers [19, 64, 74, 79, 108, 113] have used the naive Bayes approach for classification in a number of different application domains. The classifier has also been extended to modeling temporally aware training data, in which the importance of a document may decay with time [114]. As in the case of other statistical classifiers, the naive Bayes classifier [113] can easily incorporate *domain-specific knowledge* into the classification process. The particular domain that the work in [113] addresses is that of filtering junk email. Thus, for such a problem, we often have a lot of additional domain knowledge which helps us determine whether a particular email message is junk or not. For example, some common characteristics of the email which would make an email to be more or less likely to be junk are as follows:

- The domain of the sender such as *.edu* or *.com* can make an email to be more or less likely to be junk.
- Phrases such as “*Free Money*” or over emphasized punctuation such as “!!!” can make an email more likely to be junk.
- Whether the recipient of the message was a particular user, or a mailing list.

The Bayes method provides a natural way to incorporate such additional information into the classification process, by creating new features for each of these characteristics. The standard Bayes technique is then used in conjunction with this augmented representation for classification. The Bayes technique has also been used in conjunction with the incorporation of other kinds of domain knowledge, such as the incorporation of hyperlink information into the classification process [20, 104].

The Bayes method is also suited to hierarchical classification, when the training data is arranged in a taxonomy of topics. For example, the Open Directory Project (ODP), *Yahoo!* Taxonomy, and a variety of news sites have vast collections of documents which are arranged into hierarchical groups. The hierarchical structure of the topics can be exploited to perform more effective classification [19, 74], because it has been observed that context-sensitive feature selection can provide more useful classification results. In hierarchical classification, a Bayes classifier is built at *each node*, which then provides us with the next branch to follow for classification purposes. Two such methods are proposed in [19, 74], in which node specific features are used for the classification process. Clearly, much fewer features are required at a particular node



in the hierarchy, because the features which are picked are relevant to that branch. An example in [74] suggests that a branch of the taxonomy which is related to *Computer* may have no relationship with the word “cow”. These node-specific features are referred to as *signatures* in [19]. Furthermore, it has been observed in [19] that in a given node, the most discriminative features for a given class may be different from their parent nodes. For example, the word “health” may be discriminative for the *Yahoo!* category @*Health*, but the word “baby” may be much more discriminative for the category @*Health@Nursing*. Thus, it is critical to have an appropriate feature selection process at each node of the classification tree. The methods in [19, 74] use different methods for this purpose.

- The work in [74] uses an information-theoretic approach [31] for feature selection which takes into account the dependencies between the attributes [112]. The algorithm greedily eliminates the features one-by-one so as the least disrupt the conditional class distribution at that node.
- The node-specific features are referred to as *signatures* in [19]. These node-specific signatures are computed by calculating the ratio of intra-class variance to inter-class variance for the different words at each node of the tree. We note that this measure is the same as that optimized by the Fisher’s discriminant, except that it is applied to the original set of words, rather than solved as a general optimization problem in which arbitrary directions in the data are picked.

A Bayesian classifier is constructed at each node in order to determine the appropriate branch. A small number of context-sensitive features provide One advantage of these methods is that Bayesian classifiers work much more effectively with a much smaller number of features. Another major difference between the two methods is that the work in [74] uses the Bernoulli model, whereas that in [19] uses the multinomial model, which will be discussed in the next subsection. This approach in [74] is referred to as the *Pachinko Machine classifier* and that in [19] is known as *TAPER* (*T*axonomy and *P*ath *E*nhanced *R*etrieval *S*ystem).

Other noteworthy methods for hierarchical classification are proposed in [11, 130, 95]. The work [11] addresses two common problems associated with hierarchical text classification: (1) error propagation; (2) non-linear decision surfaces. The problem of error propagation occurs when the classification mistakes made at a parent node are propagated to its children node. This problem was solved in [11] by using cross validation to obtain a training data set for a child node that is more similar

to the actual test data passed to the child node from its parent node than the training data set normally used for training a classifier at the child node. The problem of non-linear decision surfaces refers to that the decision boundary of a category at a higher level is often non-linear (since its members are the union of the members of its children nodes). This problem is addressed by using the tentative class labels obtained at the children nodes as features for use at a parent node. These are general strategies that can be applied to any base classifier, and the experimental results in [11] show that both strategies are effective.

## 5.2 Multinomial Distribution

This class of techniques treats a document as a set of words with frequencies attached to each word. Thus, the set of words is allowed to have duplicate elements.

As in the previous case, we assume that the set of words in document is denoted by  $Q$ , drawn from the vocabulary set  $V$ . The set  $Q$  contains the distinct terms  $\{t_{i_1} \dots t_{i_m}\}$  with associated frequencies  $F = \{F_{i_1} \dots F_{i_m}\}$ . We denote the terms and their frequencies by  $[Q, F]$ . The total number of terms in the document (or document length) is denoted by  $L = \sum_{j=1}^m F(i_j)$ . Then, our goal is to model the posterior probability that the document  $T$  belongs to class  $i$ , given that it contains the terms in  $Q$  with the associated frequencies  $F$ . The Bayes probability of class  $i$  can be modeled by using the following sampling process:

*If we sampled  $L$  terms sequentially from the term distribution of one of the randomly chosen classes (allowing repetitions) to create the term set  $T$ , and the final outcome for sampled set  $T$  is the set  $Q$  with the corresponding frequencies  $F$ , then what is the posterior probability that we had originally picked class  $i$  for sampling? The a-priori probability of picking class  $i$  is equal to its fractional presence in the collection.*

The aforementioned probability is denoted by  $P(C^T = i | T = [Q, F])$ . An assumption which is commonly used in these models is that the length of the document is independent of the class label. While it is easily possible to generalize the method, so that the document length is used as a prior, independence is usually assumed for simplicity. As in the previous case, we need to estimate two values in order to compute the Bayes posterior.

- 1 What is the prior probability that a set  $T$  is a sample from the term distribution of class  $i$ ? This probability is denoted by  $P(C^T = i)$ .

- 2 If we sampled  $L$  terms from the term distribution of class  $i$  (with repetitions), then what is the probability that our sampled set  $T$  is the set  $Q$  with associated frequencies  $F$ ? This probability is denoted by  $P(T = [Q, F] | C^T = i)$ .

Then, the Bayes rule can be applied to this case as follows:

$$P(C^T = i | T = [Q, F]) = \frac{P(C^T = i) \cdot P(T = [Q, F] | C^T = i)}{P(T = [Q, F])} \\ \propto P(C^T = i) \cdot P(T = [Q, F] | C^T = i) \quad (6.11)$$

As in the previous case, it is not necessary to compute the denominator,  $P(T = [Q, F])$ , for the purpose of deciding the class label for  $Q$ . The value of the probability  $P(C^T = i)$  can be estimated as the fraction of documents belonging to class  $i$ . The computation of  $P([Q, F] | C^T = i)$  is much more complicated. When we consider the sequential order of the  $L$  different samples, the number of possible ways to sample the different terms so as to result in the outcome  $[Q, F]$  is given by  $\frac{L!}{\prod_{i=1}^m F_i!}$ . The probability of *each* of these sequences is given by  $\prod_{t_j \in Q} P(t_j \in T)^{F_j}$ , by using the naive independence assumption. Therefore, we have:

$$P(T = [Q, F] | C^T = i) = \frac{L!}{\prod_{i=1}^m F_i!} \cdot \prod_{t_j \in Q} P(t_j \in T | C^T = i)^{F_j} \quad (6.12)$$

We can substitute Equations 6.12 in Equation 6.11 to obtain the class with the highest Bayes posterior probability, where the class priors are computed as in the previous case, and the probabilities  $P(t_j \in T | C^T = i)$  can also be easily estimated as previously with Laplacian smoothing [124]. We note that the probabilities of class absence are not present in the above equations because of the way in which the sampling is performed.

A number of different variations of the multinomial model have been proposed in [53, 70, 84, 95, 97, 103]. In the work [95], it is shown that a category hierarchy can be leveraged to improve the estimate of multinomial parameters in the naive Bayes classifier to significantly improve classification accuracy. The key idea is to apply shrinkage techniques to smooth the parameters for data-sparse child categories with their common parent nodes. As a result, the training data of related categories are essentially "shared" with each other in a weighted manner, which helps improving the robustness and accuracy of parameter estimation when there are insufficient training data for each individual child category. The work in [94] has performed an extensive comparison between

the bernoulli and the multinomial models on different corpora, and the following conclusions were presented:

- The multi-variate Bernoulli model can sometimes perform better than the multinomial model at small vocabulary sizes.
- The multinomial model outperforms the multi-variate Bernoulli model for large vocabulary sizes, and almost always beats the multi-variate Bernoulli when vocabulary size is chosen optimally for both. On the average a 27% reduction in error was reported in [94].

The afore-mentioned results seem to suggest that the two models may have different strengths, and may therefore be useful in different scenarios.

### 5.3 Mixture Modeling for Text Classification

We note that the afore-mentioned Bayes methods simply assume that each component of the mixture corresponds to the documents belonging to a class. A more general interpretation is one in which the components of the mixture are created by a clustering process, and the class membership probabilities are modeled in terms of this mixture. Mixture modeling is typically used for unsupervised (probabilistic) clustering or topic modeling, though the use of clustering can also help in enhancing the effectiveness of probabilistic classifiers [86, 103]. These methods are particularly useful in cases where the amount of training data is limited. In particular, clustering can help in the following ways:

- The Bayes method implicitly estimates the word probabilities  $P(t_i \in T | C^T = i)$  of a large number of terms in terms of their fractional presence in the corresponding component. This is clearly noisy. By treating the clusters as separate entities from the classes, we now only need to relate (a much smaller number of) cluster membership probabilities to class probabilities. This reduces the number of parameters and greatly improves classification accuracy [86].
- The use of clustering can help in incorporating unlabeled documents into the training data for classification. The premise is that unlabeled data is much more copiously available than labeled data, and when labeled data is sparse, it should be used in order to assist the classification process. While such unlabeled documents do not contain class-specific information, they do contain a lot of information about the clustering behavior of the underlying data. This can

be very useful for more robust modeling [103], when the amount of training data is low. This general approach is also referred to as *co-training* [9, 13, 37].

The common characteristic of both the methods [86, 103] is that they both use a form of supervised clustering for the classification process. While the goal is quite similar (limited training data), the approach used for this purpose is quite different. We will discuss both of these methods in this section.

In the method discussed in [86], the document corpus is modeled with the use of supervised word clusters. In this case, the  $k$  mixture components are clusters which are correlated to, but are distinct from the  $k$  groups of documents belonging to the different classes. The main difference from the Bayes method is that the term probabilities are computed indirectly by using clustering as an intermediate step. For a sampled document  $T$ , we denote its class label by  $C^T \in \{1 \dots k\}$ , and its mixture component by  $M^T \in \{1 \dots k\}$ . The  $k$  different mixture components are essentially word-clusters whose frequencies are generated by using the frequencies of the terms in the  $k$  different classes. This ensures that the word clusters for the mixture components are correlated to the classes, but they are not assumed to be drawn from the same distribution. As in the previous case, let us assume that the a document contains the set of words  $Q$ . Then, we would like to estimate the probability  $P(T = Q|C^T = i)$  for each class  $i$ . An interesting variation of the work in [86] from the Bayes approach is that it does not attempt to determine the posterior probability  $P(C^T = i|T = Q)$ . Rather, it simply reports the class with the highest likelihood  $P(T = Q|C^T = i)$ . This is essentially equivalent to assuming in the Bayes approach, that the prior distribution of each class is the same.

The other difference of the approach is in terms of how the value of  $P(T = Q|C^T = i)$  is computed. As before, we need to estimate the value of  $P(t_j \in T|C^T = i)$ , according to the naive Bayes rule. However, unlike the standard Bayes classifier, this is done very indirectly with the use of mixture modeling. Since the mixture components do not directly correspond to the class, this term can only be estimated by summing up the expected value over all the mixture components:

$$P(t_j \in T|C^T = i) = \sum_{s=1}^k P(t_j \in T|M^T = s) \cdot P(M^T = s|C^T = i) \quad (6.13)$$

The value of  $P(t_j \in T|M^T = s)$  is easy to estimate by using the fractional presence of term  $t_j$  in the  $s$ th mixture component. The main unknown here are the set of model parameters  $P(M^T = s|C^T = i)$ .

Since a total of  $k$  classes and  $k$  mixture-components are used, this requires the estimation of only  $k^2$  model parameters, which is typically quite modest for a small number of classes. An EM-approach has been used in [86] in order to estimate this small number of model parameters in a robust way. It is important to understand that the work in [86] is an interesting combination of supervised topic modeling (dimensionality reduction) and Bayes classification after reducing the effective dimensionality of the feature space to a much smaller value by clustering. The scheme works well because of the use of supervision in the topic modeling process, which ensures that the use of an intermediate clustering approach does not lose information for classification. We also note that in this model, the number of mixtures can be made to vary from the number of classes. While the work in [86] does not explore this direction, there is really no reason to assume that the number of mixture components is the same as the number of classes. Such an assumption can be particularly useful for data sets in which the classes may not be contiguous in the feature space, and a natural clustering may contain far more components than the number of classes.

Next, we will discuss the second method [103] which uses unlabeled data. The approach in [103] uses the unlabeled data in order to improve the training model. Why should unlabeled data help in classification at all? In order to understand this point, recall that the Bayes classification process effectively uses  $k$  mixture components, which are assumed to be the  $k$  different classes. If we had an infinite amount of training data, it would be possible to create the mixture components, but it would not be possible to assign labels to these components. However, the most data-intensive part of modeling the mixture, is that of determining the shape of the mixture components. The actual assignment of mixture components to class labels can be achieved with a relatively small number of class labels. It has been shown in [24] that the accuracy of assigning components to classes increases exponentially with the number of labeled samples available. Therefore, the work in [103] designs an EM-approach [36] to simultaneously determine the relevant mixture model and its class assignment.

It turns out that the EM-approach, as applied to this problem is quite simple to implement. It has been shown in [103] that the EM-approach is equivalent to the following iterative methodology. First, a naive Bayes classifier is constructed by estimating the model parameters from the labeled documents only. This is used in order to assign probabilistically-weighted class labels to the unlabeled documents. Then, the Bayes classifier is re-constructed, except that we also use the newly labeled documents in the estimation of the underlying model

parameters. We again use this classifier to re-classify the (originally unlabeled) documents. The process is continually repeated till convergence is achieved.

The ability to significantly improve the quality of text classification with a small amount of labeled data, and the use of clustering on a large amount of unlabeled data has been a recurring theme in the text mining literature. For example, the method in [122] performs purely unsupervised clustering (with no knowledge of class labels), and then as a final step assigns all documents in the cluster to the *dominant* class label of that cluster (as an evaluation step for the unsupervised clustering process in terms of its ability in matching clusters to known topics).<sup>4</sup> It has been shown that this approach is able to achieve a comparable accuracy of matching clusters to topics as a supervised Naive Bayes classifier trained over a small data set of about 1000 documents. Similar results were obtained in [47] where the quality of the unsupervised clustering process were shown to comparable to an SVM classifier which was trained over a small data set.

## 6. Linear Classifiers

*Linear Classifiers* are those for which the output of the linear predictor is defined to be  $p = \overline{A} \cdot \overline{X} + b$ , where  $\overline{X} = (x_1 \dots x_n)$  is the normalized document word frequency vector,  $\overline{A} = (a_1 \dots a_n)$  is a vector of linear coefficients with the same dimensionality as the feature space, and  $b$  is a scalar. A natural interpretation of the predictor  $p = \overline{A} \cdot \overline{X} + b$  in the *discrete scenario* (categorical class labels) would be as a *separating hyperplane* between the different classes. *Support Vector Machines* [30, 125] are a form of classifiers which attempt to determine “good” linear separators between the different classes. One characteristic of linear classifiers is that they are closely related to many *feature transformation methods* (such as the Fisher discriminant), which attempt to use these directions in order to transform the feature space, and then use other classifiers on this transformed feature space [51, 56, 99]. Thus, linear classifiers are intimately related to linear feature transformation methods as well.

Regression modeling (such as the least squares method) is a more direct and traditional statistical method for text classification. However, it is generally used in cases where the target variable to be learned is numerical rather than categorical. A number of methods have been

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<sup>4</sup>In a supervised application, the last step would require only a small number of class labels in the cluster to be known to determine the dominant label very accurately.

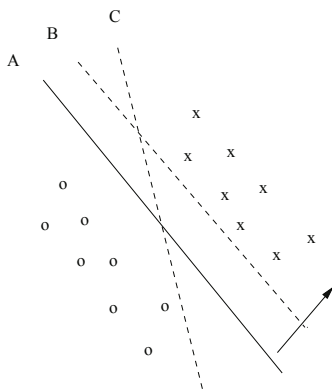


Figure 6.1. What is the Best Separating Hyperplane?

proposed in the literature for adapting such methods to the case of text data classification [134]. A comparison of different linear regression techniques for classification including SVM, may be found in [138].

Finally, simple neural networks are also a form of linear classifiers, since the function computed by a set of neurons is essentially linear. The simplest form of neural network, known as the *perceptron* (or single layer network) are essentially designed for linear separation, and work well for text. However, by using multiple layers of neurons, it is also possible to generalize the approach for non-linear separation. In this section, we will discuss the different linear methods for text classification.

## 6.1 SVM Classifiers

Support-vector machines were first proposed in [30, 124] for numerical data. The main principle of SVMs is to determine separators in the search space which can best separate the different classes. For example, consider the example illustrated in Figure 6.1, in which we have two classes denoted by 'x' and 'o' respectively. We have denoted three different separating hyperplanes, which are denoted by A, B, and C respectively. It is evident that the hyperplane A provides the best separation between the different classes, because the *normal distance* of any of the data points from it is the largest. Therefore, the hyperplane A represents the maximum *margin of separation*. We note that the normal vector to this hyperplane (represented by the arrow in the figure) is a direction in the feature space along which we have the maximum discrimination. One advantage of the SVM method is that since it attempts to determine the optimum direction of discrimination in the feature space by examining the appropriate combination of features, it is quite robust to high dimen-



sionality. It has been noted in [64] that text data is ideally suited for SVM classification because of the sparse high-dimensional nature of text, in which few features are irrelevant, but they tend to be correlated with one another and generally organized into linearly separable categories. We note that it is not necessary to use a linear function for the SVM classifier. Rather, with the kernel trick [6], SVM can construct a non-linear *decision surface* in the original feature space by mapping the data instances non-linearly to an inner product space where the classes can be separated linearly with a hyperplane. However, in practice, linear SVM is used most often because of their simplicity and ease of interpretability. The first set of SVM classifiers, as adapted to the text domain were proposed in [64–66]. A deeper theoretical study of the SVM method has been provided in [67]. In particular, it has been shown why the SVM classifier is expected to work well under a wide variety of circumstances. This has also been demonstrated experimentally in a few different scenarios. For example, the work in [41] applied the method to email data for classifying it as spam or non-spam data. It was shown that the SVM method provides much more robust performance as compared to many other techniques such as boosting decision trees, the rule based RIPPER method, and the Rocchio method. The SVM method is flexible and can easily be combined with interactive user-feedback methods [107].

We note that the problem of finding the best separator is essentially an optimization problem, which can typically be reduced to a Quadratic Programming problem. For example, many of these methods use Newton's method for iterative minimization of a convex function. This can sometimes be slow, especially for high dimensional domains such as text data. It has been shown [43] that by breaking a large Quadratic Programming problem (QP problem) to a set of smaller problems, an efficient solution can be derived for the task. The SVM approach has also been used successfully [44] in the context of a hierarchical organization of the classes, as often occurs in web data. In this approach, a different classifier is built at different positions of the hierarchy.

The SVM classifier has also been shown to be useful in large scale scenarios in which a large amount of unlabeled data and a small amount of labeled data is available [120]. This is essentially a semi-supervised approach because of its use of unlabeled data in the classification process. This technique is also quite scalable because of its use of a number of modified quasi-newton techniques, which tend to be efficient in practice.

## 6.2 Regression-Based Classifiers

Regression modeling is a method which is commonly used in order to learn the relationships between real-valued attributes. Typically, these methods are designed for real valued attributes, as opposed to binary attributes. This is however not an impediment to its use in classification, because the binary value of a class may be treated as a rudimentary special case of a real value, and some regression methods such as logistic regression can also naturally model discrete response variables.

An early application of regression to text classification is the Linear Least Squares Fit (LLSF) method [134], which works as follows. Suppose the predicted class label be  $p_i = \bar{A} \cdot \bar{X}_i + b$ , and  $y_i$  is known to be the true class label, then our aim is to learn the values of  $A$  and  $b$ , such that the *Linear Least Squares Fit (LLSF)*  $\sum_{i=1}^n (p_i - y_i)^2$  is minimized. In practice, the value of  $b$  is set to 0 for the learning process. let  $P$  be  $1 \times n$  vector of binary values indicating the binary class to which the corresponding class belongs. Thus, if  $X$  be the  $n \times d$  term-matrix, then we wish to determine the  $1 \times d$  vector of regression coefficients  $A$  for which  $\|A \cdot X^T - P\|$  is minimized, where  $\|\cdot\|$  represents the Froebinus norm. The problem can be easily generalized from the binary class scenario to the multi-class scenario with  $k$  classes, by using  $P$  as a  $k \times n$  matrix of binary values. In this matrix, exactly one value in each column is 1, and the corresponding row identifier represents the class to which that instance belongs. Similarly, the set  $A$  is a  $k \times d$  vector in the multi-class scenario. The LLSF method has been compared to a variety of other methods [132, 134, 138], and has been shown to be very robust in practice.

A more natural way of modeling the classification problem with regression is the logistic regression classifier [102], which differs from the LLSF method in that the objective function to be optimized is the likelihood function. Specifically, instead of using  $p_i = \bar{A} \cdot \bar{X}_i + b$  directly to fit the true label  $y_i$ , we assume that the probability of observing label  $y_i$  is:

$$p(C = y_i | X_i) = \frac{\exp(\bar{A} \cdot \bar{X}_i + b)}{1 + \exp(\bar{A} \cdot \bar{X}_i + b)}.$$

This gives us a conditional generative model for  $y_i$  given  $X_i$ . Putting it in another way, we assume that the logit transformation of  $p(C = y_i | X_i)$  can be modeled by the linear combination of features of the instance  $X_i$ , i.e.,

$$\log \frac{p(C = y_i | X_i)}{1 - p(C = y_i | X_i)} = \bar{A} \cdot \bar{X}_i + b.$$

Thus logistic regression is also a linear classifier as the decision boundary is determined by a linear function of the features. In the case of binary classification,  $p(C = y_i|X_i)$  can be used to determine the class label (e.g., using a threshold of 0.5). In the case of multi-class classification, we have  $p(C = y_i|X_i) \propto \exp(\bar{A} \cdot \bar{X}_i + b)$ , and the class label with the highest value according to  $p(C = y_i|X_i)$  would be assigned to  $X_i$ . Given a set of training data points  $\{(X_1, y_1), \dots, (X_n, y_n)\}$ , the logistic regression classifier can be trained by choosing parameters  $\bar{A}$  to maximize the conditional likelihood  $\prod_{i=1}^n p(y_i|X_i)$ .

In some cases, the domain knowledge may be of the form, where some sets of words are more important than others for a classification problem. For example, in a classification application, we may know that certain domain-words (*Knowledge Words (KW)*) may be more important to classification of a particular target category than other words. In such cases, it has been shown [35] that it may be possible to encode such domain knowledge into the logistic regression model in the form of prior on the model parameters and use Bayesian estimation of model parameters.

It is clear that the regression classifiers are extremely similar to the SVM model for classification. Indeed, since LLSF, Logistic Regression, and SVM are all linear classifiers, they are thus identical at a conceptual level; the main difference among them lies in the details of the optimization formulation and implementation. As in the case of SVM classifiers, training a regression classifier also requires an expensive optimization process. For example, fitting LLSF requires expensive matrix computations in the form of a singular value decomposition process.

### 6.3 Neural Network Classifiers

The basic unit in a neural network is a *neuron* or *unit*. Each unit receives a set of inputs, which are denoted by the vector  $\bar{X}_i$ , which in this case, correspond to the term frequencies in the  $i$ th document. Each neuron is also associated with a set of weights  $A$ , which are used in order to compute a function  $f(\cdot)$  of its inputs. A typical function which is often used in the neural network is the linear function as follows:

$$p_i = A \cdot \bar{X}_i \quad (6.14)$$

Thus, for a vector  $\bar{X}_i$  drawn from a lexicon of  $d$  words, the weight vector  $A$  should also contain  $d$  elements. Now consider a binary classification problem, in which all labels are drawn from  $\{+1, -1\}$ . We assume that the class label of  $\bar{X}_i$  is denoted by  $y_i$ . In that case, the sign of the predicted function  $p_i$  yields the class label.

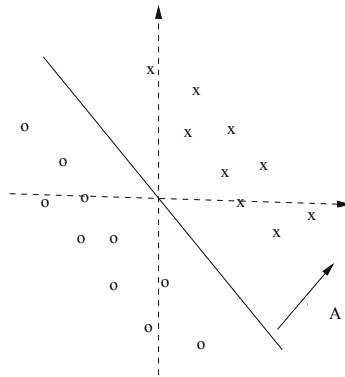


Figure 6.2. The sign of the projection onto the weight vector  $A$  yields the class label

In order to illustrate this point, let us consider a simple example in a 2-dimensional feature space, as illustrated in Figure 6.2. In this case, we have illustrated two different classes, and the plane corresponding to  $Ax = 0$  is illustrated in the same figure. It is evident that the sign of the function  $A \cdot \bar{X}_i$  yields the class label. Thus, the goal of the approach is to *learn* the set of weights  $A$  with the use of the training data. The idea is that we start off with random weights and gradually update them when a mistake is made by applying the current function on the training example. The magnitude of the update is regulated by a learning rate  $\mu$ . This forms the core idea of the *perceptron algorithm*, which is as follows:

### Perceptron Algorithm

**Inputs:** Learning Rate:  $\mu$

Training Data  $(\bar{X}_i, y_i) \forall i \in \{1 \dots n\}$

Initialize weight vectors in  $A$  to 0 or small random numbers

**repeat**

Apply each training data to the neural network to check if the  
sign of  $A \cdot \bar{X}_i$  matches  $y_i$ ;

if sign of  $A \cdot \bar{X}_i$  does **not** match  $y_i$ , then

update weights  $A$  based on learning rate  $\mu$

**until** weights in  $A$  converge

The weights in  $A$  are typically updated (increased or decreased) proportionally to  $\mu \cdot \bar{X}_i$ , so as to reduce the direction of the error of the neuron. We further note that many different update rules have been proposed in the literature. For example, one may simply update each weight by  $\mu$ , rather than by  $\mu \cdot \bar{X}_i$ . This is particularly possible in domains such

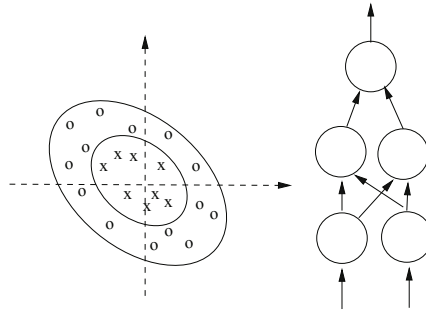


Figure 6.3. Multi-Layered Neural Networks for Nonlinear Separation

as text, in which all feature values take on small non-negative values of relatively similar magnitude. A number of implementations of neural network methods for text data have been studied in [34, 90, 101, 117, 129].

A natural question arises, as to how a neural network may be used, if all the classes may not be neatly separated from one another with a linear separator, as illustrated in Figure 6.2. For example, in Figure 6.3, we have illustrated an example in which the classes may not be separated with the use of a single linear separator. The use of *multiple layers of neurons* can be used in order to induce such non-linear classification boundaries. The effect of such multiple layers is to induce multiple piece-wise linear boundaries, which can be used to approximate enclosed regions belonging to a particular class. In such a network, the outputs of the neurons in the earlier layers feed into the neurons in the later layers. The training process of such networks is more complex, as the errors need to be back-propagated over different layers. Some examples of such classifiers include those discussed in [75, 110, 126, 132]. However, the general observation [117, 129] for text has been that linear classifiers generally provide comparable results to non-linear data, and the improvements of non-linear classification methods are relatively small. This suggests that the additional complexity of building more involved non-linear models does not pay for itself in terms of significantly better classification.

## 6.4 Some Observations about Linear Classifiers

While the different linear classifiers have been developed independently from one another in the research literature, they are surprisingly similar at a basic conceptual level. Interestingly, these different lines of work have also resulted in a number of similar conclusions in terms of

the effectiveness of the different classifiers. We note that the main difference between the different classifiers is in terms of the details of the objective function which is optimized, and the iterative approach used in order to determine the optimum direction of separation. For example, the SVM method uses a Quadratic Programming (QP) formulation, whereas the LLSF method uses a closed-form least-squares formulation. On the other hand, the perceptron method does not try to formulate a closed-form objective function, but works with a softer iterative hill climbing approach. This technique is essentially inherited from the iterative learning approach used by neural network algorithms. However, its goal remains quite similar to the other two methods. Thus, the differences between these methods are really at a detailed level, rather than a conceptual level, in spite of their very different research origins.

Another general observation about these methods is that all of them can be implemented with non-linear versions of their classifiers. For example, it is possible to create non-linear decision surfaces with the SVM classifier, just as it is possible to create non-linear separation boundaries by using layered neurons in a neural network [132]. However, the general consensus has been that the linear versions of these methods work very well, and the additional complexity of non-linear classification does not tend to pay for itself, except for some special data sets. The reason for this is perhaps because text is a high dimensional domain with highly correlated features and small non-negative values on sparse features. For example, it is hard to easily create class structures such as that indicated in [Figure 6.3](#) for a sparse domain such as text containing only small non-negative values on the features. On the other hand, the high dimensional nature of correlated text dimensions is especially suited to classifiers which can exploit the redundancies and relationships between the different features in separating out the different classes. Common text applications have generally resulted in class structures which are linearly separable over this high dimensional domain of data. This is one of the reasons that linear classifiers have shown an unprecedented success in text classification.

## 7. Proximity-based Classifiers

Proximity-based classifiers essentially use distance-based measures in order to perform the classification. The main thesis is that documents which belong to the same class are likely to be close to one another based on similarity measures such as the dot product or the cosine metric [115]. In order to perform the classification for a given test instance, two possible methods can be used:

- We determine the  $k$ -nearest neighbors in the training data to the test instance. The majority (or most abundant) class from these  $k$  neighbors are reported as the class label. Some examples of such methods are discussed in [25, 54, 134]. The choice of  $k$  typically ranges between 20 and 40 in most of the afore-mentioned work, depending upon the size of the underlying corpus.
- We perform training data aggregation during pre-processing, in which clusters or groups of documents belonging to the same class are created. A representative meta-document is created from each group. The same  $k$ -nearest neighbor approach is applied as discussed above, except that it is applied to this new set of meta-documents (or *generalized instances* [76]) rather than to the original documents in the collection. A pre-processing phase of summarization is useful in improving the efficiency of the classifier, because it significantly reduces the number of distance computations. In some cases, it may also boost the accuracy of the technique, especially when the data set contains a large number of outliers. Some examples of such methods are discussed in [55, 76, 109].

A method for performing nearest neighbor classification in text data is the *WHIRL* method discussed in [25]. The *WHIRL* method is essentially a method for performing soft similarity joins on the basis of text attributes. By *soft* similarity joins, we refer to the fact that the two records may not be exactly the same on the joined attribute, but a notion of similarity used for this purpose. It has been observed in [25] that any method for performing a similarity-join can be adapted as a nearest neighbor classifier, by using the relevant text documents as the joined attributes.

One observation in [134] about nearest neighbor classifiers was that feature selection and document representation play an important part in the effectiveness of the classification process. This is because most terms in large corpora may not be related to the category of interest. Therefore, a number of techniques were proposed in [134] in order to learn the associations between the words and the categories. These are then used to create a feature representation of the document, so that the nearest neighbor classifier is more sensitive to the classes in the document collection. A similar observation has been made in [54], in which it has been shown that the addition of weights to the terms (based on their class-sensitivity) significantly improves the underlying classifier performance. The nearest neighbor classifier has also been extended to the temporally-aware scenario [114], in which the timeliness of a training document plays a role in the model construction process.

In order to incorporate such factors, a temporal weighting function has been introduced in [114], which allows the importance of a document to gracefully decay with time.

For the case of classifiers which use grouping techniques, the most basic among such methods is that proposed by Rocchio in [109]. In this method, a *single* representative meta-document is constructed from each of the representative classes. For a given class, the weight of the term  $t_k$  is the normalized frequency of the term  $t_k$  in documents belonging to that class, minus the normalized frequency of the term in documents which do not belong to that class. Specifically, let  $f_p^k$  be the expected weight of term  $t_k$  in a randomly picked document belonging to the positive class, and  $f_n^k$  be the expected weight of term  $t_k$  in a randomly picked document belonging to the negative class. Then, for weighting parameters  $\alpha_p$  and  $\alpha_n$ , the weight  $f_{roccchio}^k$  is defined as follows:

$$f_{roccchio}^k = \alpha_p \cdot f_p^k - \alpha_n \cdot f_n^k \quad (6.15)$$

The weighting parameters  $\alpha_p$  and  $\alpha_n$  are picked so that the positive class has much greater weight as compared to the negative class. For the relevant class, we now have a vector representation of the terms  $(f_{roccchio}^1, f_{roccchio}^2 \cdots f_{roccchio}^n)$ . This approach is applied separately to each of the classes, in order to create a separate meta-document for each class. For a given test document, the closest meta-document to the test document can be determined by using a vector-based dot product or other similarity metric. The corresponding class is then reported as the relevant label. The main distinguishing characteristic of the Rocchio method is that it creates a single profile of the entire class. This class of methods is also referred to as the *Rocchio framework*. The main disadvantage of this method is that if a single class occurs in multiple disjoint clusters which are not very well connected in the data, then the centroid of these examples may not represent the class behavior very well. This is likely to be a source of inaccuracy for the classifier. The main advantage of this method is its extreme simplicity and efficiency; the training phase is linear in the corpus size, and the number of computations in the testing phase are linear to the number of classes, since all the documents have already been aggregated into a small number of classes. An analysis of the Rocchio algorithm, along with a number of different variations may be found in [64].

In order to handle the shortcomings of the Rocchio method, a number of classifiers have also been proposed [1, 14, 55, 76], which explicitly perform the clustering of each of the classes in the document collection. These clusters are used in order to generate class-specific profiles. These profiles are also referred to as *generalized instances* in [76]. For a given



test instance, the label of the closest generalized instance is reported by the algorithm. The method in [14] is also a centroid-based classifier, but is specifically designed for the case of text documents. The work in [55] shows that there are some advantages in designing schemes in which the similarity computations take account of the dependencies between the terms of the different classes.

We note that the nearest neighbor classifier can be used in order to generate a ranked list of categories for each document. In cases, where a document is related to multiple categories, these can be reported for the document, as long as a thresholding method is available. The work in [136] studies a number of thresholding strategies for the  $k$ -nearest neighbor classifier. It has also been suggested in [136] that these thresholding strategies can be used to understand the thresholding strategies of other classifiers which use ranking classifiers.

## 8. Classification of Linked and Web Data

In recent years, the proliferation of the web and social network technologies has lead to a tremendous amount of document data, which is expressed in the form of linked networks. The simplest example of this is the web, in which the documents are linked to one another with the use of hyper-links. Social networks can also be considered a noisy example of such data, because the comments and text profiles of different users are connected to one another through a variety of links. Linkage information is quite relevant to the classification process, because documents of similar subjects are often linked together. This observation has been used widely in the *collective classification literature* [12], in which a subset of network nodes are labeled, and the remaining nodes are classified on the basis of the linkages among the nodes.

In general, a content-based network may be denoted by  $G = (N, A, C)$ , where  $N$  is the set of nodes,  $A$  is the set of edges between the nodes, and  $C$  is a set of text documents. Each node in  $N$  corresponds to a text document in  $C$ , and it is possible for a document to be the empty, when the corresponding node does not contain any content. A subset of the nodes in  $N$  are labeled. This corresponds to the training data. The classification problem in this scenario is to determine the labels of the remaining nodes with the use of the training data. It is clear that both the content and structure can play a useful and complementary role in the classification process.

An interesting method for combining linkage and content information for classification was discussed in [20]. In this paper, a hypertext categorization method was proposed, which uses the content and labels of

neighboring web pages for the classification process. When the labels of all the nearest neighbors are available, then a Bayesian method can be adapted easily for classification purposes. Just as the presence of a word in a document can be considered a Bayesian feature for a text classifier, the presence of a link between the target page, and a page (for which the label is known) can be considered a feature for the classifier. The real challenge arises when the labels of all the nearest neighbors are not available. In such cases, a relaxation labeling method was proposed in order to perform the classification. Two methods have been proposed in this work:

- **Fully Supervised Case of Radius one Enhanced Linkage Analysis:** In this case, it is assumed that all the neighboring class labels are known. In such a case, a Bayesian approach is utilized in order to treat the labels on the nearest neighbors as features for classification purposes. In this case, the linkage information is the sole information which is used for classification purposes.
- **When the class labels of the nearest neighbors are not known:** In this case, an iterative approach is used for combining text and linkage based classification. Rather than using the pre-defined labels (which are not available), we perform a first labeling of the neighboring documents with the use of document content. These labels are then used to classify the label of the target document, with the use of *both* the local text and the class labels of the neighbors. This approach is used iteratively for re-defining the labels of both the target document and its neighbors until convergence is achieved.

The conclusion from the work in [20] is that a combination of text and linkage based classification always improves the accuracy of a text classifier. Even when none of the neighbors of the document have known classes, it seemed to be always beneficial to add link information to the classification process. When the class labels of all the neighbors are known, then the advantages of using the scheme seem to be quite significant.

An additional idea in the paper is that of the use of *bridges* in order to further improve the classification accuracy. The core idea in the use of a bridge is the use of *2-hop* propagation for link-based classification. The results with the use of such an approach are somewhat mixed, as the accuracy seems to reduce with an increasing number of hops. The work in [20] shows results on a number of different kinds of data sets such as the *Reuters database*, *US patent database*, and *Yahoo!*. Since the *Reuters database* contains the least amount of noise, and pure text

classifiers were able to do a good job. On the other hand, the *US patent database* and the *Yahoo! database* contain an increasing amount of noise which reduces the accuracy of text classifiers. An interesting observation in [20] was that a scheme which simply absorbed the neighbor text into the current document performed *significantly worse* than a scheme which was based on pure text-based classification. This is because there are often significant cross-boundary linkages between topics, and such linkages are able to confuse the classifier. A publicly available implementation of this algorithm may be found in the *NetKit* tool kit available in [92].

Another relaxation labeling method for graph-based document classification is proposed in [4]. In this technique, the probability that the end points of a link take on a particular pair of class labels is quantified. We refer to this as the *link-class pair probability*. The posterior probability of classification of a node  $T$  into class  $i$  is expressed as sum of the probabilities of pairing all possible class labels of the neighbors of  $T$  with class label  $i$ . We note a significant percentage of these (exponential number of ) possibilities are pruned, since only the currently most probable<sup>5</sup> labelings are used in this approach. For this purpose, it is assumed that the class labels of the different neighbors of  $T$  (while dependent on  $T$ ) are independent of each other. This is similar to the naive assumption, which is often used in Bayes classifiers. Therefore, the probability for a particular combination of labels on the neighbors can be expressed as the product of the corresponding link-class pair probabilities. The approach starts off with the use of a standard content-based Bayes or SVM classifier in order to assign the initial labels to the nodes. Then, an iterative approach is used to refine the labels, by using the most probably label estimations from the previous iteration in order to refine the labels in the current iteration. We note that the link-class pair probabilities can be estimated as the smoothed fraction of edges in the last iteration which contain a particular pair of classes as the end points (hard labeling), or it can also be estimated as the average product of node probabilities over all edges which take on that particular class pair (soft labeling). This approach is repeated to convergence.

Another method which uses a naive Bayes classifier to enhance link-based classification is proposed in [104]. This method incrementally assigns class labels, starting off with a temporary assignment and then gradually making them permanent. The initial class assignment is based on a simple Bayes expression based on both the terms and links in the

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<sup>5</sup>In the case of *hard labeling*, the single most likely labeling is used, whereas in the case of *soft labeling*, a small set of possibilities is used.

document. In the final categorization, the method changes the term weights for Bayesian classification of the target document with the terms in the neighbor of the current document. This method uses a broad framework which is similar to that in [20], except that it differentiates between the classes in the neighborhood of a document in terms of their influence on the class label of the current document. For example, documents for which the class label was either already available in the training data, or for which the algorithm has performed a final assignment, have a different confidence weighting factor than those documents for which the class label is currently temporarily assigned. Similarly, documents which belong to a completely different subject (based on content) are also removed from consideration from the assignment. Then, the Bayesian classification is performed with the re-computed weights, so that the document can be assigned a final class label. By using this approach the technique is able to compensate for the noise and inconsistencies in the link structures among different documents.

One major difference between the work in [20] and [104], is that the former is focussed on using link information in order to propagate the labels, whereas the latter attempts to use the content of the neighboring pages. Another work along this direction, which uses the content of the neighboring pages more explicitly is proposed in [105]. In this case, the content of the neighboring pages is broken up into different fields such as titles, anchor text, and general text. The different fields are given different levels of importance, which is learned during the classification process. It was shown in [105] that the use of title fields and anchor fields is much more relevant than the general text. This accounts for much of the accuracy improvements demonstrated in [105].

The work in [2] proposes a method for dynamic classification in text networks with the use of a random-walk method. The key idea in the work is to *transform* the combination of structure and content in the network into a pure network containing only content. Thus, we transform the original network  $G = (N, A, C)$  into an *augmented* network  $G^A = (N \cup N_c, A \cup A_c)$ , where  $N_c$  and  $A_c$  are an additional set of nodes and edges added to the original network. Each node in  $N_c$  corresponds to a distinct word in the lexicon. Thus, the augmented network contains the original structural nodes  $N$ , and a new set of word nodes  $N_c$ . The added edges in  $A_c$  are undirected edges added between the structural nodes  $N$  and the word nodes  $N_c$ . Specifically, an edge  $(i, j)$  is added to  $A_c$ , if the word  $i \in N_c$  occurs in the text content corresponding to the node  $j \in N$ . Thus, this network is *semi-bipartite*, in that there are no edges between the different word nodes. An illustration of the semi-bipartite content-structure transformation is provided in [Figure 6.4](#).

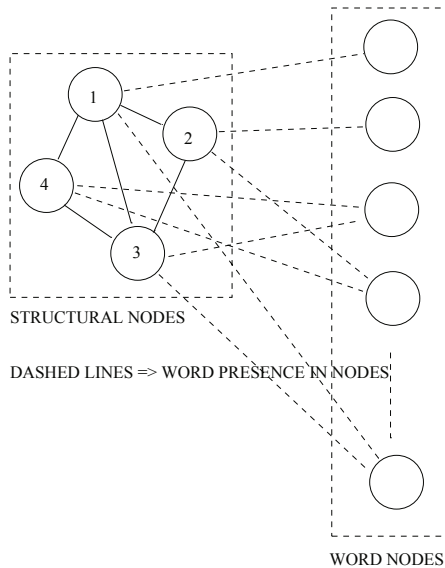


Figure 6.4. The Semi-bipartite Transformation

It is important to note that once such a transformation has been performed, any of the collective classification methods [12] can be applied to the structural nodes. In the work in [2], a random-walk method has been used in order to perform the collective classification of the underlying nodes. In this method, repeated random walks are performed starting at the unlabeled nodes which need to be classified. The random walks are defined only on the structural nodes, and each hop may either be a *structural* hop or a *content* hop. We perform  $l$  different random walks, each of which contains  $h$  nodes. Thus, a total of  $l \cdot h$  nodes are encountered in the different walks. The class label of this node is predicted to be the label with the highest frequency of presence in the different  $l \cdot h$  nodes encountered in the different walks. The error of this random walk-based sampling process has been bounded in [12]. In addition, the method in [12] can be adapted to dynamic content-based networks, in which the nodes, edges and their underlying content continuously evolve over time. The method in [2] has been compared to that proposed in [18] (based on the implementation in [92]), and it has been shown that the classification methods of [12] are significantly superior.

Another method for classification of linked text data is discussed in [139]. This method designs two separate regularization conditions; one is for the text-only classifier (also referred to as the *local* classifier), and

the other is for the link information in the network structure. These regularizers are expressed in the terms of the underlying kernels; the link regularizer is related to the standard graph regularizer used in the machine learning literature, and the text regularizer is expressed in terms of the kernel gram matrix. These two regularization conditions are combined in two possible ways. One can either use linear combinations of the regularizers, or linear combinations of the associated kernels. It was shown in [139] that both combination methods perform better than either pure structure-based or pure text-based methods. The method using a linear combination of regularizers was slightly more accurate and robust than the method which used a linear combination of the kernels.

A method in [32] designs a classifier which combines a Naive Bayes classifier (on the text domain), and a rule-based classifier (on the structural domain). The idea is to invent a set of predicates, which are defined in the space of links, pages and words. A variety of predicates (or relations) are defined depending upon the presence of the word in a page, linkages of pages to each other, the nature of the anchor text of the hyperlink, and the neighborhood words of the hyperlink. These essentially encode the graph structure of the documents in the form of boolean predicates, and can also be used to construct relational learners. The main contribution in [32] is to combine the relational learners on the structural domain with the Naive Bayes approach in the text domain. We refer the reader to [32, 33] for the details of the algorithm, and the general philosophy of such relational learners.

One of the interesting methods for collective classification in the context of email networks was proposed in [23]. The technique in [23] is designed to classify *speech acts* in email. Speech acts essentially characterize, whether an email refers to a particular kind of action (such as scheduling a meeting). It has been shown in [23] that the use of sequential thread-based information from the email is very useful for the classification process. An email system can be modeled as a network in several ways, one of which is to treat an email as a node, and the edges as the thread relationships between the different emails. In this sense, the work in [23] devises a network-based mining procedure which uses both the content and the structure of the email network. However, this work is rather specific to the case of email networks, and it is not clear whether the technique can be adapted (effectively) to more general networks.

A different line of solutions to such problems, which are defined on a heterogeneous feature space is to use latent space methods in order to simultaneously homogenize the feature space, and also determine the latent factors in the underlying data. The resulting representation can

be used in conjunction with any of the text classifiers which are designed for latent space representations. A method in [140] uses a matrix factorization approach in order to construct a latent space from the underlying data. Both supervised and unsupervised methods were proposed for constructing the latent space from the underlying data. It was then shown in [140] that this feature representation provides more accurate results, when used in conjunction with an SVM-classifier.

Finally, a method for web page classification is proposed in [119]. This method is designed for using intelligent agents in web page categorization. The overall approach relies on the design of two functions which correspond to scoring web pages and links respectively. An advice language is created, and a method is proposed for mapping advice to neural networks. It has been shown in [119] how this general purpose system may be used in order to find home pages on the web.

## 9. Meta-Algorithms for Text Classification

Meta-algorithms play an important role in classification strategies because of their ability to enhance the accuracy of existing classification algorithms by combining them, or making a general change in the different algorithms to achieve a specific goal. Typical examples of classifier meta-algorithms include *bagging*, *stacking* and *boosting* [42]. Some of these methods change the underlying distribution of the training data, others combine classifiers, and yet others change the algorithms in order to satisfy specific classification criteria. We will discuss these different classes of methods in this section.

### 9.1 Classifier Ensemble Learning

In this method, we use *combinations* of classifiers in conjunction with a voting mechanism in order to perform the classification. The idea is that since different classifiers are susceptible to different kinds of over-training and errors, a combination classifier is likely to yield much more robust results. This technique is also sometimes referred to as *stacking* or *classifier committee construction*.

Ensemble learning has been used quite frequently in text categorization. Most methods simply use weighted combinations of classifier outputs (either in terms of scores or ranks) in order to provide the final classification result. For example, the work by Larkey and Croft [79] used weighted linear combinations of the classifier scores or ranks. The work by Hull [60] used linear combinations of probabilities for the same goal. A linear combination of the normalized scores was used for classification [137]. The work in [87] used classifier selection techniques and

voting in order to provide the final classification result. Some examples of such voting and selection techniques are as follows:

- In a binary-class application, the class label which obtains the majority vote is reported as the final result.
- For a given test instance, a specific classifier is selected, depending upon the performance of the classifier which are closest to that test instance.
- A weighted combination of the results from the different classifiers are used, where the weight is regulated by the performance of the classifier on validation instances which are most similar to the current test instance.

The last two methods above try to select the final classification in a smarter way by discriminating between the performances of the classifiers in different scenarios. The work by [77] used category-averaged features in order to construct a different classifier for each category.

The major challenge in ensemble learning is to provide the appropriate combination of classifiers for a particular scenario. Clearly, this combination can significantly vary with the scenario and the data set. In order to achieve this goal, the method in [10] proposes a method for probabilistic combination of text classifiers. The work introduces a number of variables known as *reliability variables* in order to regulate the importance of the different classifiers. These reliability variables are learned dynamically for each situation, so as to provide the best classification.

## 9.2 Data Centered Methods: Boosting and Bagging

While ensemble techniques focus on combining different classifiers, data-centered methods such as boosting and bagging typically focus on training the same classifier on different parts of the training data in order to create different models. For a given test instance, a combination of the results obtained from the use of these different models is reported. Another major difference between ensemble-methods and boosting methods is that the training models in a boosting method are not constructed independently, but are constructed sequentially. Specifically, after  $i$  classifiers are constructed, the  $(i + 1)$ th classifier is constructed on those parts of the training data which the first  $i$  classifiers are unable to accurately classify. The results of these different classifiers are combined together carefully, where the weight of each classifier is typically a function of its error rate. The most well known meta-algorithm for boosting is the



*AdaBoost* algorithm [48]. Such boosting algorithms have been applied to a variety of scenarios such as decision tree learners, rule-based systems, and Bayesian classifiers [49, 61, 73, 100, 116, 118].

We note that boosting is also a kind of ensemble learning methodology, except that we train the same model on different subsets of the data in order to create the ensemble. One major criticism of boosting is that in many data sets, some of the training records are noisy, and a classification model should be resistant to overtraining on the data. Since the boosting model tends to weight the error-prone examples more heavily in successive rounds, this can cause the classification process to be more prone to overfitting. This is particularly noticeable in the case of noisy data sets. Some recent results have suggested that all convex boosting algorithms may perform poorly in the presence of noise [91]. These results tend to suggest that the choice of boosting algorithm may be critical for a successful outcome, depending upon the underlying data set.

Bagging methods [16] are generally designed to reduce the model overfitting error which arises during the learning process. The idea in bagging is to pick *bootstrap samples* (samples with replacement) from the underlying collection, and train the classifiers in these samples. The classification results from these different samples are then combined together in order to yield the final result. Bagging methods are generally used in conjunction with decision trees, though these methods can be used in principle with any kind of classifier. The main criticism of the bagging method is that it can sometimes lead to a reduction in accuracy because of the smaller size of each individual training sample. Bagging is useful only if the model is unstable to small details of the training algorithm, because it reduces the overfitting error. An example of such an algorithm would be the decision tree model, which is highly sensitive to how the higher levels of the tree are constructed in a high dimensional feature space such as text. Bagging methods have not been used frequently in text classification.

### 9.3 Optimizing Specific Measures of Accuracy

We note that the use of the absolute classification accuracy is not the only measure which is relevant to classification algorithms. For example, in skewed-class scenarios, as often arise in the context of applications such as fraud detection, and spam filtering, it is more costly to misclassify examples of one class than another. For example, while it may be tolerable to misclassify a few spam emails (thereby allowing them into the inbox), it is much more undesirable to incorrectly mark

a legitimate email as spam. Cost-sensitive classification problems also naturally arise in cases in which one class is more rare than the other, and it is therefore more desirable to identify the rare examples. In such cases, it is desirable to optimize the *cost-weighted accuracy* of the classification process. We note that many of the broad techniques which have been designed for non-textual data [40, 42, 45] are also applicable to text data, because the specific feature representation is not material to how standard algorithms are modified to the cost-sensitive case. A good understanding of cost-sensitive classification both for the textual and non-textual case may be found in [40, 45, 3]. Some examples of how classification algorithms may be modified in straightforward ways to incorporate cost-sensitivity are as follows:

- In a decision-tree, the split condition at a given node tries to maximize the accuracy of its children nodes. In the cost-sensitive case, the split is engineered to maximize the cost-sensitive accuracy.
- In rule-based classifiers, the rules are typically quantified and ordered by measures corresponding to their predictive accuracy. In the cost-sensitive case, the rules are quantified and ordered by their *cost-weighted accuracy*.
- In Bayesian classifiers, the posterior probabilities are weighted by the cost of the class for which the prediction is made.
- In linear classifiers, the optimum hyperplane separating the classes is determined in a cost-weighted sense. Such costs can typically be incorporated in the underlying objective function. For example, the least-square error in the objective function of the LLSF method can be weighted by the underlying costs of the different classes.
- In a  $k$ -nearest neighbor classifier, we report the cost-weighted majority class among the  $k$  nearest neighbors of the test instance.

We note that the use of a cost-sensitive approach is essentially a change of the objective function of classification, which can also be formulated as an optimization problem. While the standard classification problem generally tries to optimize accuracy, the cost-sensitive version tries to optimize a cost-weighted objective function. A more general approach was proposed in [50] in which a meta-algorithm was proposed for optimizing a specific figure of merit such as the accuracy, precision, recall, or  $F_1$ -measure. Thus, this approach generalizes this class of methods to *any arbitrary objective function*, making it essentially an *objective-centered classification method*. A generalized probabilistic descent algorithm (with the desired objective function) is used in conjunc-

tion with the classifier of interest in order to derive the class labels of the test instance. The work in [50] shows the advantages of using the technique over a standard SVM-based classifier.

## 10. Conclusions and Summary

The classification problem is one of the most fundamental problems in the machine learning and data mining literature. In the context of text data, the problem can also be considered similar to that of classification of *discrete set-valued* attributes, when the frequencies of the words are ignored. The domains of these sets are rather large, as it comprises the entire lexicon. Therefore, text mining techniques need to be designed to effectively manage large numbers of elements with varying frequencies. Almost all the known techniques for classification such as decision trees, rules, Bayes methods, nearest neighbor classifiers, SVM classifiers, and neural networks have been extended to the case of text data. Recently, a considerable amount of emphasis has been placed on linear classifiers such as neural networks and SVM classifiers, with the latter being particularly suited to the characteristics of text data. In recent years, the advancement of web and social network technologies have lead to a tremendous interest in the classification of text documents containing links or other meta-information. Recent research has shown that the incorporation of linkage information into the classification process can significantly improve the quality of the underlying results.

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