





Solution Review: Problem Challenge



We'll cover the following ^

- Minimum Height Trees (hard)
- Solution
 - Code
- Time complexity
- Space complexity

Minimum Height Trees (hard)#

We are given an undirected graph   characteristics of a **k-ary tree**. In such a graph, we can choose any node as the root to make a k-ary tree. The root (or the tree) with the minimum height will be called **Minimum Height Tree (MHT)**. There can be multiple MHTs for a graph. In this problem, we need to find all those roots which give us MHTs. Write a method to find all MHTs of the given graph and return a list of their roots.

Example 1:

Input: vertices: 5, Edges: [[0, 1], [1, 2], [1, 3], [2, 4]]

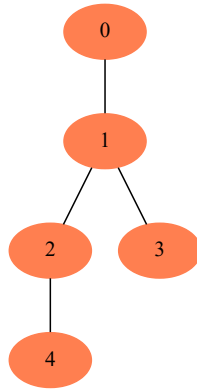
Output:[1, 2]

Explanation: Choosing '1' or '2' as roots give us MHTs. In the below diagram, we can see that the height of the trees with roots '1' or '2' is three which is minimum.

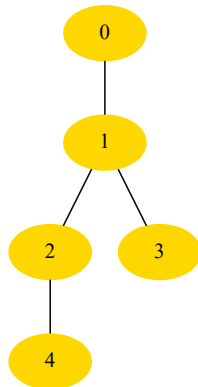




Given graph ==>

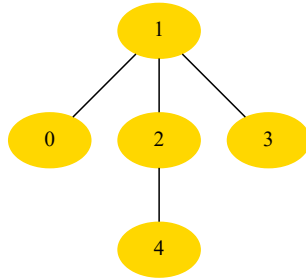


With '0' as the root



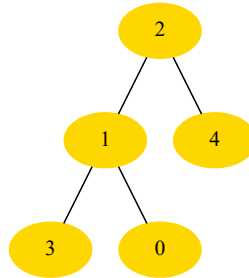
Height = 4

With '1' as the root



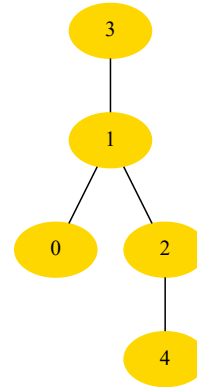
Height = 3

With '2' as the root



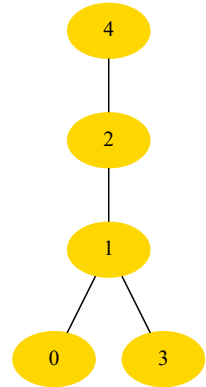
Height = 3

With '3' as the root



Height = 4

With '4' as the root



Height = 4

Example 2:

Input: vertices: 4, Edges: `[[0, 1], [0, 2], [2, 3]]`

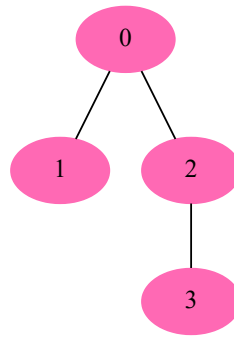
Output: `[0, 2]`

Explanation: Choosing '0' or '2' as roots give us MHTs. In the below diagram, we can see that the height of the trees with roots '0' or '2' is three which is minimum.

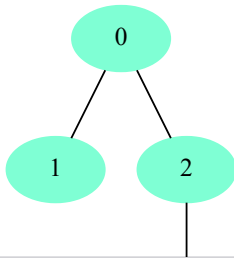




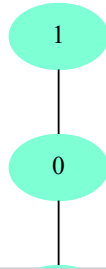
Given graph ==>



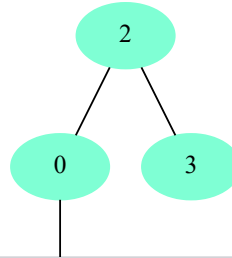
With '0' as the root



With '1' as the root



With '2' as the root



With '3' as the root



Example 3:

Input: vertices: 4, Edges: [[0, 1], [1, 2], [1, 3]]

Output:[1]

Solution#

From the above-mentioned examples, we can clearly see that any leaf node (i.e., node with only one edge) can never give us an MHT because its adjacent non-leaf nodes will always give an MHT with a smaller height. All the adjacent non-leaf nodes will consider the leaf node as a subtree. Let's understand this with another example. Suppose we have a tree with root 'M' and height '5'. Now, if we take another node, say 'P', and make the 'M' tree as its subtree, then the height of the overall tree with root 'P' will be '6' ($=5+1$). Now, this whole tree can be considered a graph, where 'P' is a leaf as it has only one edge (connection with 'M'). This clearly shows that the leaf node ('P') gives us a tree of height '6' whereas its adjacent non-leaf node ('M') gives us a tree with smaller height '5' - since 'P' will be a child of 'M'.



This gives us a strategy to find MHTs. Since leaves can't give us MHT, we can remove them from the graph and remove their edges too. Once we remove the leaves, we will have new leaves. Since these new leaves can't give us MHT, we will repeat the process and remove them from the graph too. We will prune the leaves until we are left with one or two nodes which will be our answer and the roots for MHTs.

We can implement the above process using the topological sort. Any node with only one edge (i.e., a leaf) can be our source and, in a stepwise fashion, we can remove all sources from the graph to find new sources. We will repeat this process until we are left with one or two nodes in the graph, which will be our answer.

Code#

Here is what our algorithm will look like:

C++

```
1 using namespace std;
2
3 #include <deque>
4 #include <iostream>
5 #include <string>
6 #include <unordered_map>
7 #include <vector>
8
9 class MinimumHeightTrees {
10 public:
11     static vector<int> findTrees(int nodes, vector<vector<int>>& edges) {
12         vector<int> minHeightTrees;
13         if (nodes <= 0) {
14             return minHeightTrees;
15         }
16
17         // with only one node, since its in-degree will be 0, therefore, we need to handle
18         if (nodes == 1) {
19             minHeightTrees.push_back(0);
20             return minHeightTrees;
21         }
22
23         // a. Initialize the graph
```

```

24 unordered_map<int, int> inDegree; // count of incoming edges
25 unordered_map<int, vector<int>> graph; // adjacency list
26 for (int i = 0; i < nodes; i++) {
27     inDegree[i] = 0;
28     graph[i] = vector<int>();
29 }
30
31 // b. Build the graph

```



Time complexity#

In step 'd', each node can become a source only once and each edge will be accessed and removed once. Therefore, the time complexity of the above algorithm will be $O(V + E)$, where 'V' is the total nodes and 'E' is the total number of the edges.

Space complexity#

The space complexity will be $O(V + E)$, since we are storing all of the edges for each node in an adjacency list.

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Problem Challenge 2

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Kth Smallest Number (hard)



Mark as Completed



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