



Minimum Subset Sum Difference

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Problem Statement#

Given a set of positive numbers, partition the set into two subsets with a minimum difference between their subset sums.

Example 1:#

Input: {1, 2, 3, 9}

Output: 3

Explanation: We can partition the given set into two subsets where the minimum absolute difference



between the sum of numbers is '3'. Following are the two subsets: {1, 2, 3} & {9}.



Example 2:#

Input: {1, 2, 7, 1, 5}

Output: 0

Explanation: We can partition the given set into two subsets where the minimum absolute difference

between the sum of numbers is '0'. Following are the two subsets: {1, 2, 5} & {7, 1}.

Example 3:#

Input: {1, 3, 100, 4}

Output: 92

Explanation: We can partition the given set into two subsets where the minimum absolute difference

between the sum of numbers is '92'. Here are the two subsets: {1, 3, 4} & {100}.

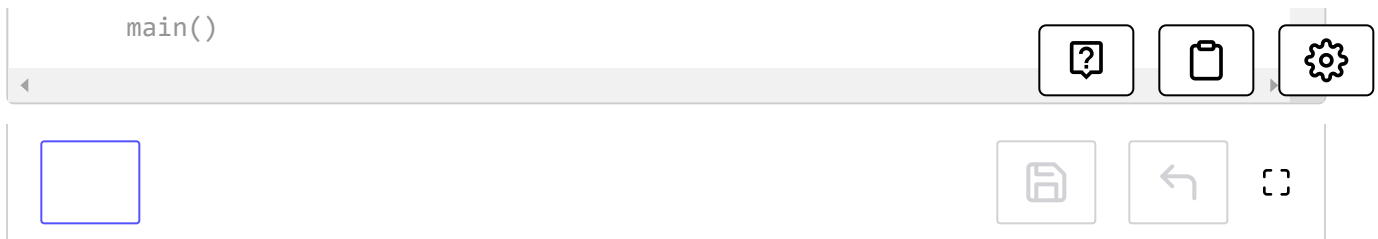
Try it yourself#

Try solving this question here:



```
def can_partition(num):  
    # TODO: Write your code here  
    return -1  
  
def main():  
    print("Can partition: " + str(can_partition([1, 2, 3, 9])))  
    print("Can partition: " + str(can_partition([1, 2, 7, 1, 5])))  
    print("Can partition: " + str(can_partition([1, 3, 100, 4])))
```





Basic Solution#

This problem follows the **0/1 Knapsack pattern** and can be converted into a [Subset Sum](#) problem.

Let's assume S1 and S2 are the two desired subsets. A basic brute-force solution could be to try adding each element either in S1 or S2, to find the combination that gives the minimum sum difference between the two sets.

So our brute-force algorithm will look like:

```
for each number 'i'
    add number 'i' to S1 and recursively process the remaining numbers
    add number 'i' to S2 and recursively process the remaining numbers
return the minimum absolute difference of the above two sets
```

Code#

Here is the code for the brute-force solution:

 Python3

```
def can_partition(num):
    return can_partition_recursive(num, 0, 0, 0)

def can_partition_recursive(num, currentIndex, sum1, sum2):
    # base check
    if currentIndex == len(num):
        return abs(sum1 - sum2)
```

```

# recursive call after including the number at the currentIndex in the first subset
diff1 = can_partition_recursive(
    num, currentIndex + 1, sum1 + num[currentIndex], sum2)

# recursive call after including the number at the currentIndex in the second subset
diff2 = can_partition_recursive(
    num, currentIndex + 1, sum1, sum2 + num[currentIndex])

return min(diff1, diff2)

def main():
    print("Can partition: " + str(can_partition([1, 2, 3, 9])))
    print("Can partition: " + str(can_partition([1, 2, 7, 1, 5])))
    print("Can partition: " + str(can_partition([1, 3, 100, 4])))

main()

```



The time complexity of the above algorithm is exponential $O(2^n)$, where 'n' represents the total number. The space complexity is $O(n)$ which is used to store the recursion stack.

Top-down Dynamic Programming with Memoization#

We can use memoization to overcome the overlapping sub-problems.

We will be using a two-dimensional array to store the results of the solved sub-problems. We can uniquely identify a sub-problem from 'currentIndex' and 'Sum1'; as 'Sum2' will always be the sum of the remaining numbers.

Code#



Here is the code:



 Python3



```
def can_partition(num):
    s = sum(num)
    dp = [[-1 for x in range(s+1)] for y in range(len(num))]
    return can_partition_recursive(dp, num, 0, 0, 0)

def can_partition_recursive(dp, num, currentIndex, sum1, sum2):
    # base check
    if currentIndex == len(num):
        return abs(sum1 - sum2)

    # check if we have not already processed similar problem
    if dp[currentIndex][sum1] == -1:
        # recursive call after including the number at the currentIndex in the first set
        diff1 = can_partition_recursive(
            dp, num, currentIndex + 1, sum1 + num[currentIndex], sum2)

        # recursive call after including the number at the currentIndex in the second set
        diff2 = can_partition_recursive(
            dp, num, currentIndex + 1, sum1, sum2 + num[currentIndex])

        dp[currentIndex][sum1] = min(diff1, diff2)




    return dp[currentIndex][sum1]

def main():
```



Bottom-up Dynamic Programming#

Let's assume 'S' represents the total sum of all the numbers. So what we are trying to achieve in this problem is to find a subset whose sum is as close to 'S/2' as possible, because if we can partition the given set into two subsets c ☾

an equal sum, we get the minimum difference i.e. zero. This    problem to [Subset Sum](#), where we try to find a subset whose sum is equal to a given number-- 'S/2' in our case. If we can't find such a subset, then we will take the subset which has the sum closest to 'S/2'. This is easily possible, as we will be calculating all possible sums with every subset.

Essentially, we need to calculate all the possible sums up to 'S/2' for all numbers. So how do we populate the array `dp[TotalNumbers][S/2+1]` in the bottom-up fashion?

For every possible sum 's' (where $0 \leq s \leq S/2$), we have two options:

1. Exclude the number. In this case, we will see if we can get the sum 's' from the subset excluding this number => `dp[index-1][s]`
2. Include the number if its value is not more than 's'. In this case, we will see if we can find a subset to get the remaining sum => `dp[index-1][s - num[index]]`

If either of the two above scenarios is true, we can find a subset with a sum equal to 's'. We should dig into this before we can learn how to find the closest subset.

Let's draw this visually, with the example input {1, 2, 3, 9}. Since the total sum is '15', therefore, we will try to find a subset whose sum is equal to the half of it i.e. '7'.





'0' sum can always be found through an empty set

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The above visualization tells us that it is not possible to find a subset whose sum is equal to '7'. So what is the closest subset we can find? We can find such a subset if we start moving backward in the last row from the bottom right corner to find the first 'T'. The first "T" in the above diagram is the sum '6', which means we can find a subset whose sum is equal to '6'. This means the other set will have a sum of '9', and the minimum difference will be '3'.

Code#

Here is the code for our bottom-up dynamic programming approach:

 Python3



```
def can_partition(num):
    s = sum(num)
    n = len(num)
    dp = [[False for x in range(int(s/2)+1)] for y in range(n)]

    # populate the s=0 columns, as we can always form '0' sum with an empty set
    for i in range(0, n):
        dp[i][0] = True

    # with only one number, we can form a subset only when the required sum is
    for j in range(1, int(s/2)+1):
        dp[0][j] = num[0] == j

    # process all subsets for all sums
    for i in range(1, n):
        for j in range(1, int(s/2)+1):
            # if we can get the sum 's' without the number at index 'i'
            if dp[i - 1][j]:
                dp[i][j] = dp[i - 1][j]
```

```

elif j >= num[i]:
    # else include the number and see if we can find a subset with sum less than or equal to j - num[i]
    dp[i][j] = dp[i - 1][j - num[i]]

sum1 = 0
# find the largest index in the last row which is true
for i in range(int(s/2), -1, -1):
    if dp[i][sum1]:
        sum1 += num[i]

```



The above solution has time and space complexity of $O(N * S)$, where 'N' represents total numbers and 'S' is the total sum of all the numbers.

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