1 Question 1

Given We are given three different vectors to try to map through a given function. We are then to plot everything.

1. $\mathbf{A} = \begin{bmatrix} 3 & 0 \\ 0 & -2 \end{bmatrix}$
2. $T : \mathbb{R}^2 \to \mathbb{R}^2$
3. $T(\mathbf{x}) = \mathbf{A}\mathbf{x}$

Find

1. The image of u under T where $\mathbf{u} = \begin{bmatrix} 3 \\ -1 \end{bmatrix}$
2. The image of c under T where $\mathbf{v} = \begin{bmatrix} 0 \\ 1.5 \end{bmatrix}$
3. The image of $\mathbf{u} + \mathbf{v}$

1.1 Work

Images The image under is just going to be the result of having the function applied. We can do as such like so, for each of the given terms

1. $T(\mathbf{u}) = A\mathbf{u} = \begin{bmatrix} 3 & 0 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} 3 \\ -1 \end{bmatrix} = \begin{bmatrix} 9 \\ 2 \end{bmatrix}$
2. $T(\mathbf{v}) = A\mathbf{v} = \begin{bmatrix} 3 & 0 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} 0 \\ 1.5 \end{bmatrix} = \begin{bmatrix} 0 \\ -3 \end{bmatrix}$
3. $T(\mathbf{u} + \mathbf{v}) = A(\mathbf{u} + \mathbf{v}) = \begin{bmatrix} 3 & 0 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} 0 \\ 1.5 \end{bmatrix} = \begin{bmatrix} 0 \\ -3 \end{bmatrix}$

1.2 Illustration

Scaling Throughout we should expect to see a few things. The origin should remain constant, and relationships about perpendicularity and being parallel should contiue to hold.