

Lecture Objectives



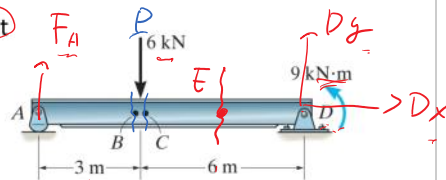
Internal Forces

1

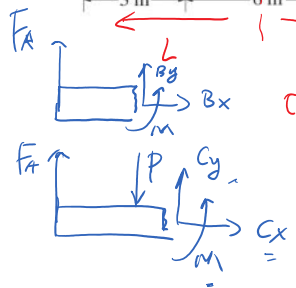
Procedure for analysis

1. Find support reactions (free-body diagram of entire structure)
2. Pass an imaginary section through the member
3. Draw a free-body diagram of the segment that has the least number of loads on it
4. Apply the equations of equilibrium

Find the internal forces and moments at B (just to the left of P) and at C (just to the right of P)

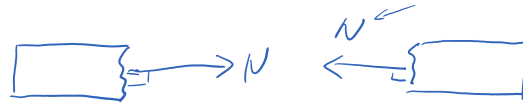


$$\begin{aligned} \sum F_x &= 0 \\ \sum F_y &= 0 \\ \sum M_E &= 0 \end{aligned} \Rightarrow \begin{cases} E_x = ? \\ E_y = ? \\ M = ? \end{cases}$$

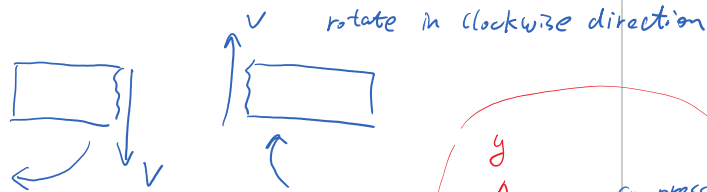


Sign conventions

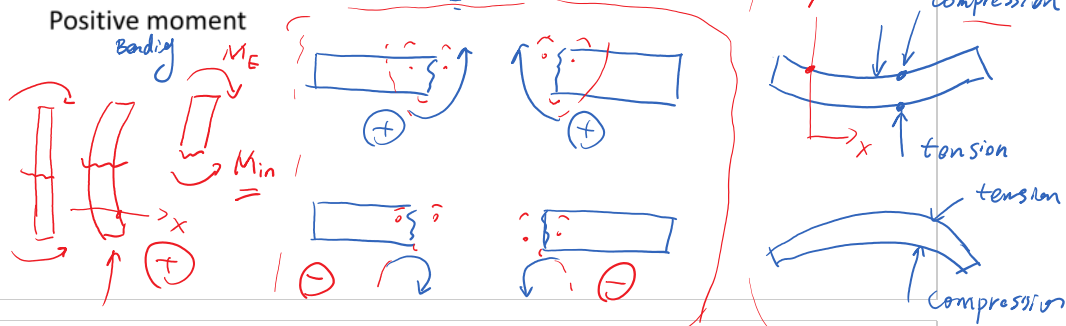
Positive normal force



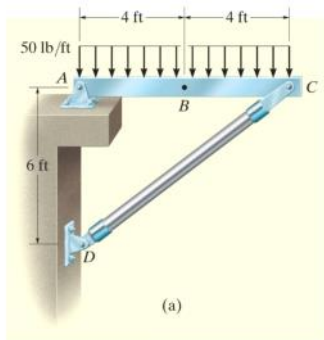
Positive shear force



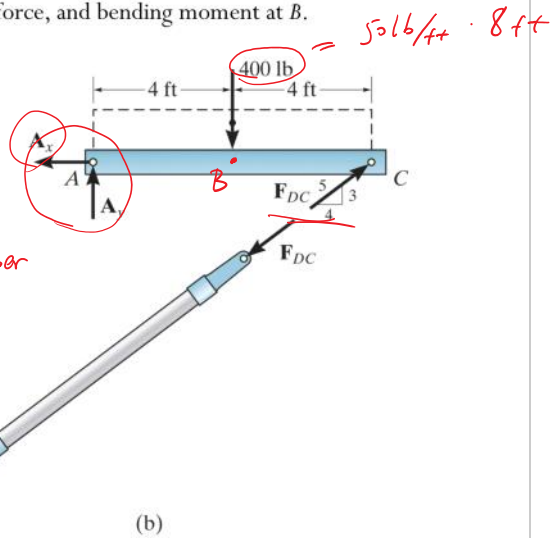
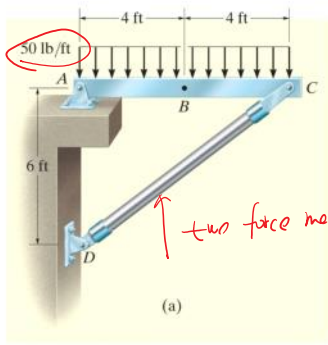
Positive moment



Determine the normal force, shear force, and bending moment at B.

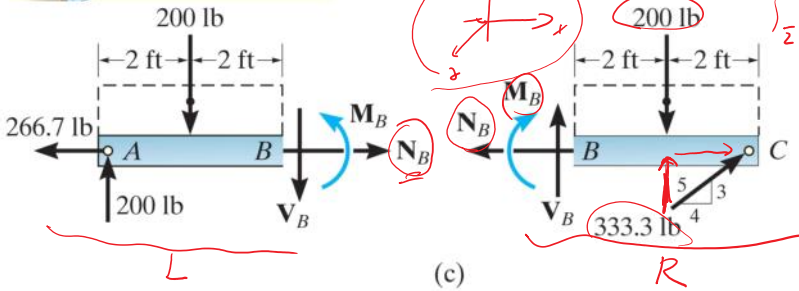
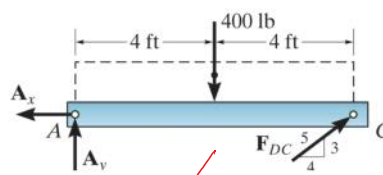
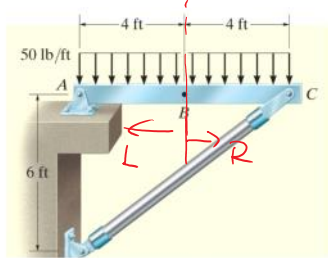


Determine the normal force, shear force, and bending moment at B.



$$\begin{cases} \sum F_x = 0 \\ \sum F_y = 0 \\ \sum M_A = 0 \end{cases} \Rightarrow \begin{cases} F_{DC} = ? \\ A_x = ? \\ A_y = ? \end{cases}$$

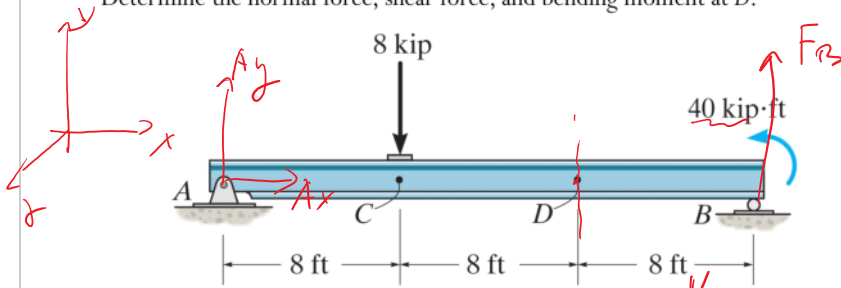
Determine the normal force, shear force, and bending moment at B.



$$\begin{cases} \sum F_x = 0 \\ \sum F_y = 0 \\ \sum M_B = 0 \end{cases} \Rightarrow \begin{cases} -N_B + 333.3 \frac{4}{5} = 0 \\ -200 + V_B + 333.3 \frac{3}{5} = 0 \\ -M_B - 200 \cdot 2 + 333.3 \cdot \frac{3}{5} \cdot 4 = 0 \end{cases}$$

$$\Rightarrow \begin{cases} N_B = ? (+) \\ V_B = ? (+) \\ M_B = ? \end{cases}$$

Determine the normal force, shear force, and bending moment at D.

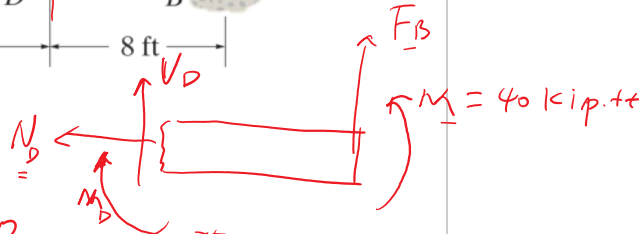


$$\sum F_x = A_x = 0$$

$$\sum F_y = A_y - 8 + F_B = 0$$

$$\sum M_A = -8 \cdot 8 + F_B \cdot 24 + 40 = 0$$

$$\Rightarrow \begin{cases} A_y = ? \\ F_B = ? \end{cases}$$

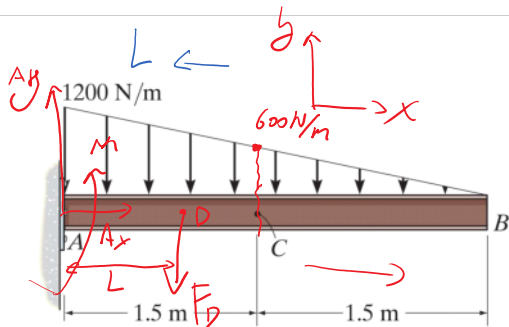


$$\sum F_x = N_D = 0$$

$$\sum F_y = F_B + V_D = 0$$

$$\sum M_D = -M_D + F_B \cdot 8 + \overset{V}{M} = 0$$

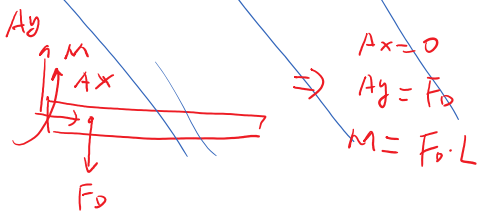
$$\Rightarrow \begin{cases} V_D = ? \\ M_D = ? \end{cases}$$



Determine the normal force, shear force, and bending moment at C of the beam.

$$F_D = \frac{1}{2} \cdot 1200 \cdot 3 = 1800 \text{ N}$$

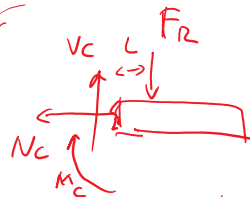
$$L = \frac{1}{3} \cdot 3 = 1 \text{ m}$$



$$A_x = 0$$

$$A_y = F_D$$

$$M = F_D \cdot L$$



$$F_R = \frac{1}{2} \cdot 600 \cdot 1.5 = 450 \text{ N}$$

$$L = \frac{1}{3} \cdot 1.5 = 0.5 \text{ m}$$

$$N_C = ?$$

$$V_C = ?$$

$$M_C = ?$$

Determine the normal force, shear force, and bending moment at C .

