

FUNCIÓN DELTA DE DIRAC - $\delta(t)$

1	$\delta(t) = \begin{cases} 0 & \text{si } t \neq 0 \\ \infty & \text{si } t = 0 \end{cases}$	$\int_{-\infty}^{\infty} \delta(t) dt = \int_{-a}^a \delta(t) dt = 1, \quad a > 0$
2	$\phi(t)$ es una función continua en un intervalo I y cero fuera de ella $\int_{-\infty}^{\infty} \delta(t) \phi(t) dt = \phi(0), \quad 0 \in I$	
3	$\int_{-\infty}^{\infty} \delta(t - t_0) \phi(t) dt = \int_{-\infty}^{\infty} \delta(t) \phi(t + t_0) dt = \phi(t_0), \quad t_0 \in I$	
4	$\int_{-\infty}^{\infty} \delta(t - t_0) g(t) dt = \begin{cases} g(t_0) & \text{si } a < t_0 < b \\ 0 & \text{si } t_0 \notin [a, b] \end{cases}$	
5	$\int_a^b \delta(t - t_0) dt = \begin{cases} 1 & \text{si } a < t_0 < b \\ 0 & \text{si } t_0 \notin [a, b] \end{cases}$	
6	$f(t) \delta(t) = f(0) \delta(t)$, siendo $f(t)$ continua en $t = 0$	
7	$t \delta(t) = 0, \quad \delta(at) = \frac{1}{ a } \delta(t), \quad \delta(-t) = \delta(t)$	
8	$\int_{-\infty}^{\infty} \delta'(t) \phi(t) dt = - \int_{-\infty}^{\infty} \delta(t) \phi'(t) dt = -\phi'(0)$	
9	$\int_{-\infty}^{\infty} \delta'(t - t_0) \phi(t) dt = -\phi'(t_0)$	
10	$\int_{-\infty}^{\infty} \delta^{(n)}(t) \phi(t) dt = (-1)^n \int_{-\infty}^{\infty} \delta(t) \phi^{(n)}(t) dt = (-1)^n \phi^{(n)}(0)$	
11	$\int_{-\infty}^{\infty} f'(t) \phi(t) dt = - \int_{-\infty}^{\infty} f(t) \phi'(t) dt$	
12	$[f(t) \delta(t)]' = f(t) \delta'(t) + f'(t) \delta(t)$	
13	$f(t) \delta'(t) = f(0) \delta'(t) - f'(0) \delta(t)$	
14	$\delta(t) = \frac{d u(t)}{dt}$	$\delta^{(n)}(t) = \frac{d^n \delta(t)}{dt^n}, \quad n = 1, 2, \dots$

ALGUNAS FÓRMULAS DE LA MATEMÁTICA

1	$\begin{aligned}\operatorname{sen}(a+b) &= \operatorname{sen}(a)\cos(b) + \operatorname{sen}(b)\cos(a) \\ \operatorname{sen}(a-b) &= \operatorname{sen}(a)\cos(b) - \operatorname{sen}(b)\cos(a) \\ \cos(a+b) &= \cos(a)\cos(b) - \operatorname{sen}(a)\operatorname{sen}(b) \\ \cos(a-b) &= \cos(a)\cos(b) + \operatorname{sen}(a)\operatorname{sen}(b)\end{aligned}$	
2	$\begin{aligned}\operatorname{sen}(a+b) + \operatorname{sen}(a-b) &= 2\operatorname{sen}(a)\cos(b) \\ \operatorname{sen}(a+b) - \operatorname{sen}(a-b) &= 2\operatorname{sen}(b)\cos(a) \\ \cos(a+b) + \cos(a-b) &= 2\cos(a)\cos(b) \\ \cos(a+b) - \cos(a-b) &= -2\operatorname{sen}(a)\operatorname{sen}(b)\end{aligned}$	
3	$\begin{aligned}\cos(2a) &= \cos^2(a) - \operatorname{sen}^2(a) \\ \cos(2a) &= 2\cos^2(a) - 1 \\ \cos(2a) &= 1 - 2\operatorname{sen}^2(a)\end{aligned}$	$\operatorname{sen}(2a) = 2\operatorname{sen}(a)\cos(a)$
4	$\int_a^b f(x)dx = - \int_b^a f(x)dx$	$\int_a^b f(x)dx = - \int_{-a}^{-b} f(-y)dy$
5	$\int_{-L}^L f(x)dx = 0 \quad \text{si } f \text{ es } \mathbf{impar} \text{ en } [-L, L]$	
6	$\int_{-L}^L f(x)dx = 2 \int_0^L f(x)dx \quad \text{si } f \text{ es } \mathbf{par} \text{ en } [-L, L]$	
7	$\int te^{bt}dt = \frac{e^{bt}(bt-1)}{b^2} + C$	
8	$\int t^2 e^{bt}dt = \frac{e^{bt}(b^2 t^2 - 2bt + 2)}{b^2} + C$	
9	$\int t \cos(at)dt = \frac{\cos(at) + at \operatorname{sen}(at)}{a^2} + C$	
10	$\int t \operatorname{sen}(at)dt = \frac{\operatorname{sen}(at) - at \cos(at)}{a^2} + C$	
11	$\int e^{bt} \cos(at)dt = \frac{e^{bt}(a \operatorname{sen}(at) + b \cos(at))}{a^2 + b^2} + C$	
12	$\int e^{bt} \operatorname{sen}(at)dt = \frac{-e^{bt}(a \cos(at) - b \operatorname{sen}(at))}{a^2 + b^2} + C$	