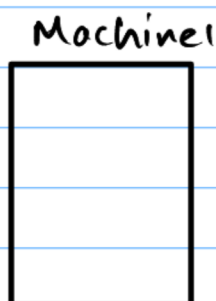
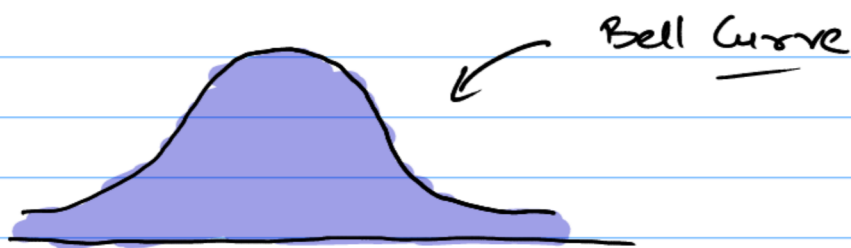


## The Normal Distribution



← Backup

{ Vanilla, Chocolate, Strawberry }

### Scenario:

Complaint: Sashi got a complaint that the quantity of ice-cream served was less compared to last time!

Sol<sup>n</sup>: Sashi should measure the weight of each ice-cream OR she can set an acceptable limit & check if the prob. of weight of ice-cream is falling within or outside the acceptable range.

Manufacturer: " Mean Weight = 95 gm  
S.D. = 11 gm

if acceptable range  $\in [84, 117]$  gm

Then, Prob. of weight of ice-cream falling

within 2 outside this range?

Sol<sup>n</sup>:

Acceptable range  $\in [84, 117]$  gm

$\Rightarrow$  it is a cont. distribution

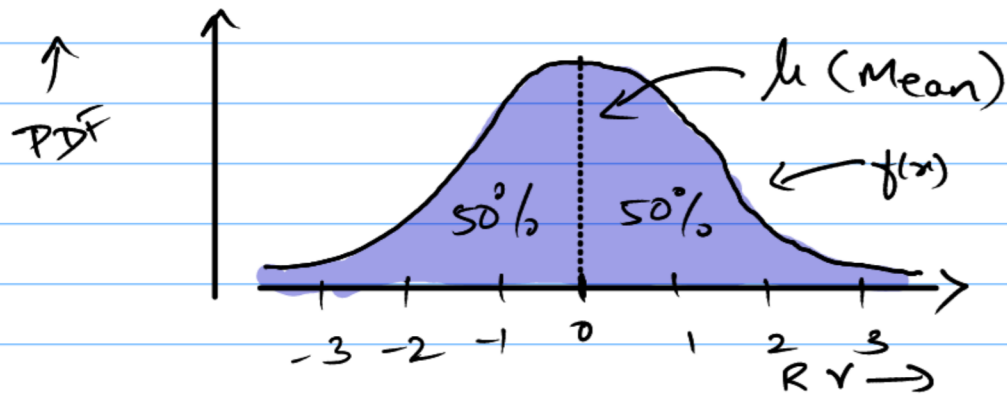
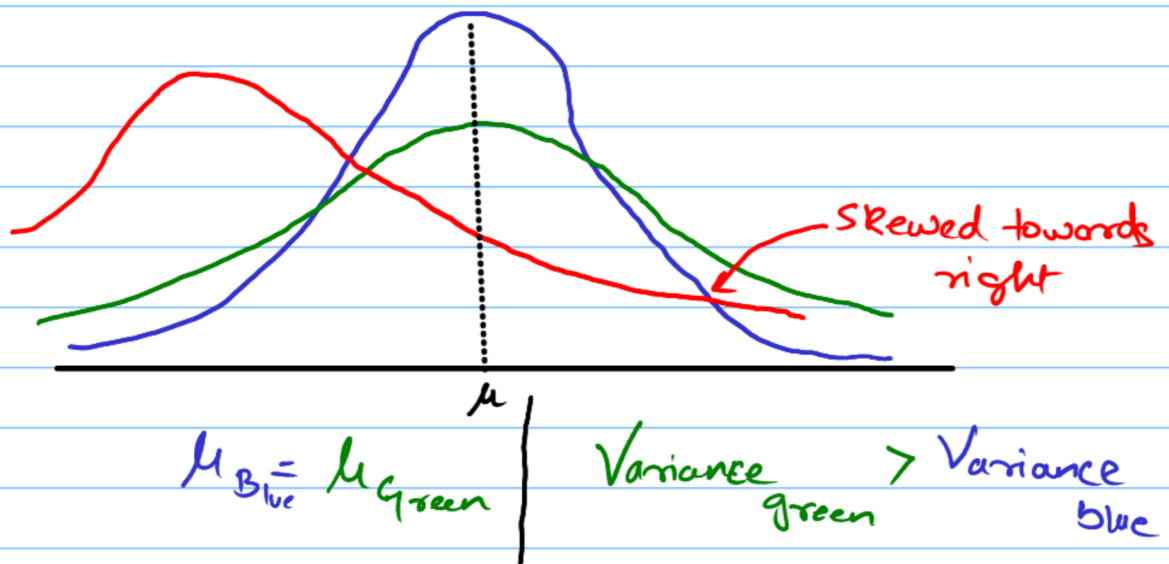
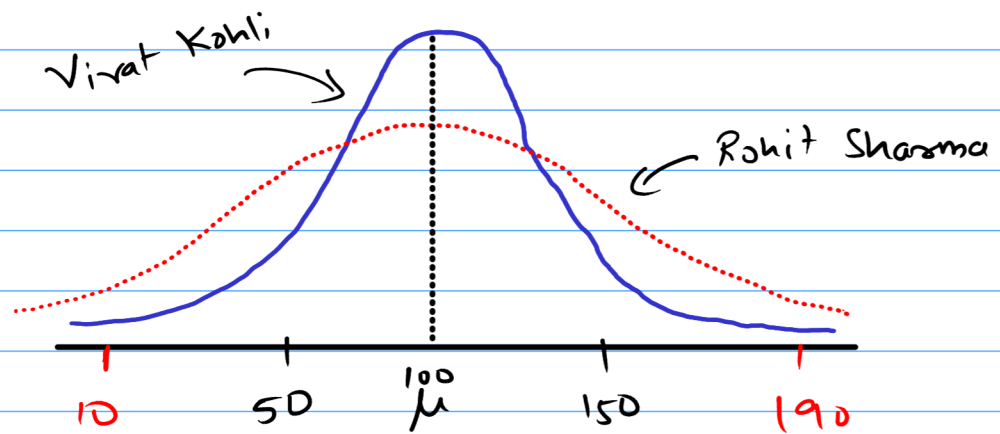


Fig. Normal Dist.

$$\text{Area} = \int_{-\infty}^{\infty} f(x) dx = 1$$





Assuming  $\mu_V = \mu_R = 100$  Runs

Variance<sub>R</sub> > Variance<sub>V</sub>

The PDF (Normally distributed RV) :

$$f(x, \mu, \sigma^2) = \frac{1}{\sigma\sqrt{2\pi}} e^{-(x-\mu)^2/2\sigma^2}$$

where  $x \in \mathbb{R} \Rightarrow (-\infty, \infty)$

$x$  is a Normal RV

$\mu$  = mean

$\sigma$  = standard Deviation

$\pi = 3.14$

$e = 2.718$

# Standard Normal Distribution - PDF

$$\ast \mu = 0$$

$$\ast \sigma = 1$$

$$\text{PDF: } f(x) = \frac{1}{\sqrt{2\pi}} \cdot e^{-x^2/2}$$

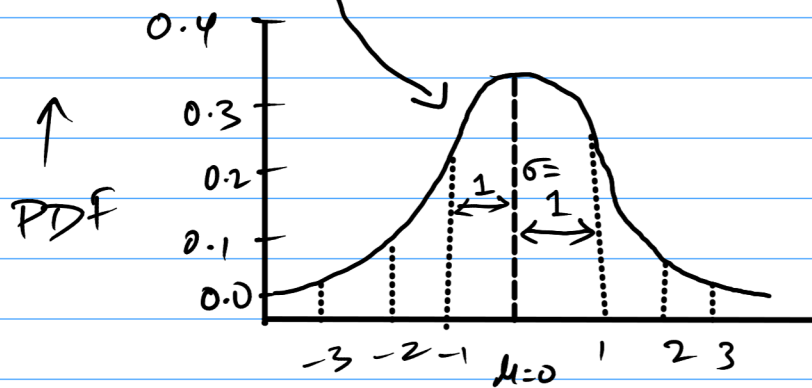
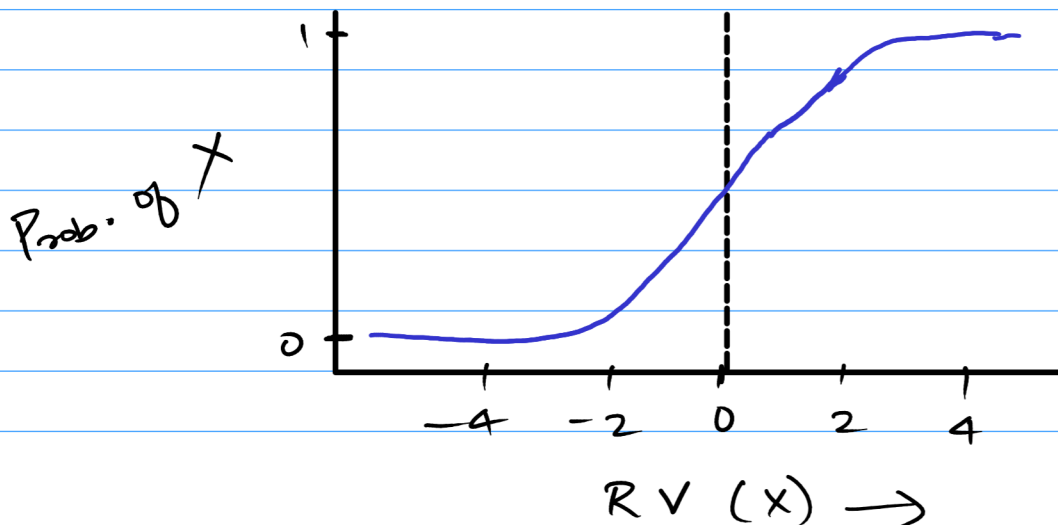


Fig. Standard Normal Dist.

CDF of a Normal Dist:

$$F(x) = \int_{-\infty}^x f(x) dx = \int_{-\infty}^x \frac{1}{\sqrt{2\pi}} \cdot e^{-x^2/2} dt$$



- Weight ( $x$ ) :  $0 < x < 84$
- $w(x)$  :  $117 < x < \infty$
- weight( $x$ ) :  $84 \leq x \leq 117$

Z-score (Standard Score) = total # of S.D.'s from the mean by a RV.

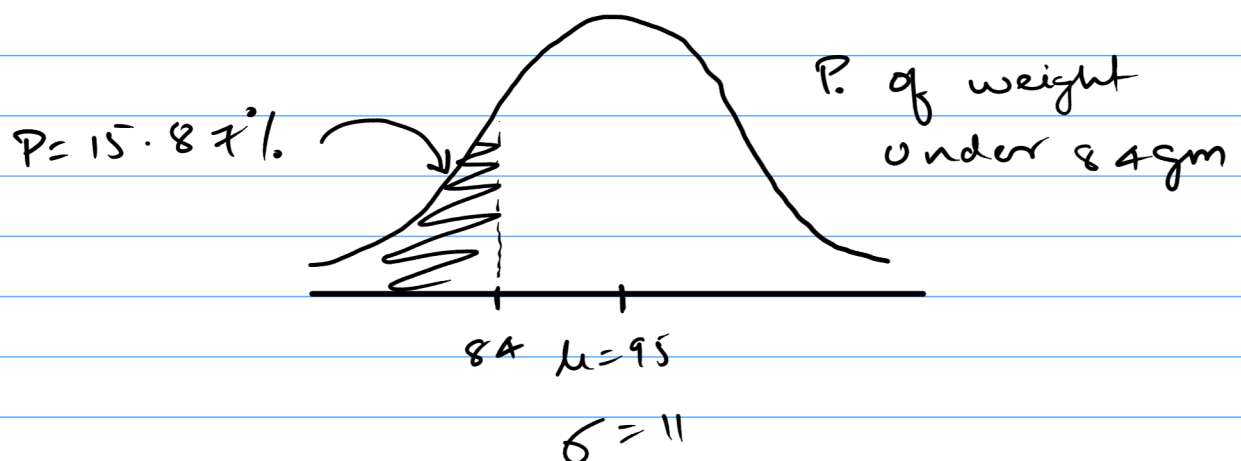
$$Z = \frac{x - \mu}{\sigma}$$

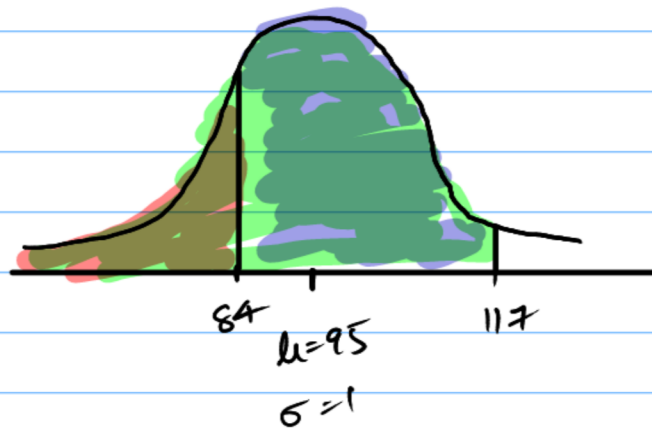
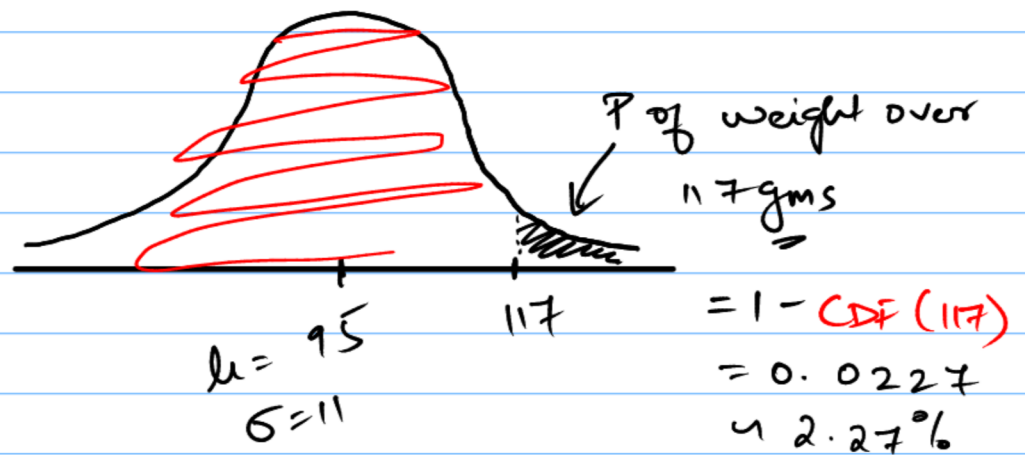
$$\mu = 95$$

$$\sigma = 11$$

- $P(\text{weight} < 84\text{gm})$  :

$$Z = \frac{x - \mu}{\sigma} = \frac{84 - 95}{11} = -1$$





● = ● - ● = 81.85%

### Empirical Rule:

- \* 68.27%  $\in$  1 SD of Mean
- \* 95.45%  $\in$  2 SD of Mean
- \* 99.73%  $\in$  3 SD of Mean

