

# Computer Vision - 2025

## A Tiny Lecture #2. Room for Doubt

Lectures by Alexei Kornaev <sup>1,2,3</sup>

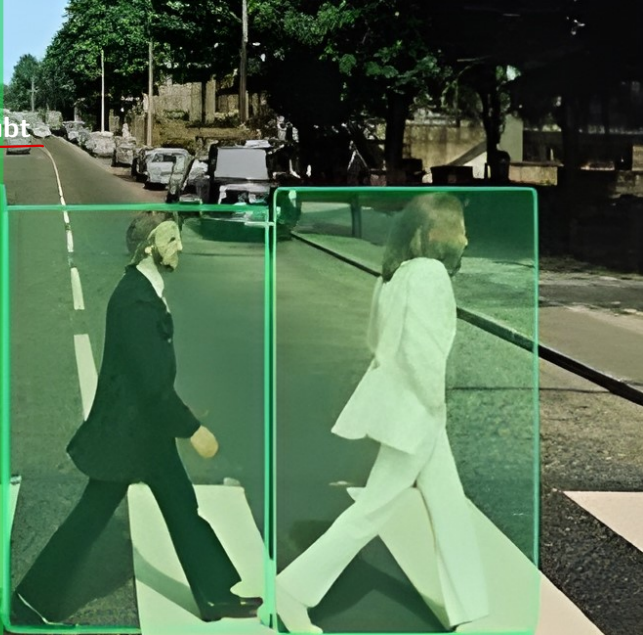
Practical sessions by Kirill Yakovlev <sup>2</sup>

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# Agenda

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K.Yakovlev

On  
uncertainty in  
AI

Recap

Uncertainty-  
aware Loss  
Intuition

Conclusion

- ① On uncertainty in AI
- ② Recap
- ③ Uncertainty-aware Loss Intuition
- ④ Conclusion

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# Section 1. On uncertainty in AI

# All models are wrong, but models that know when they are wrong, are useful /George Box + some corrections/

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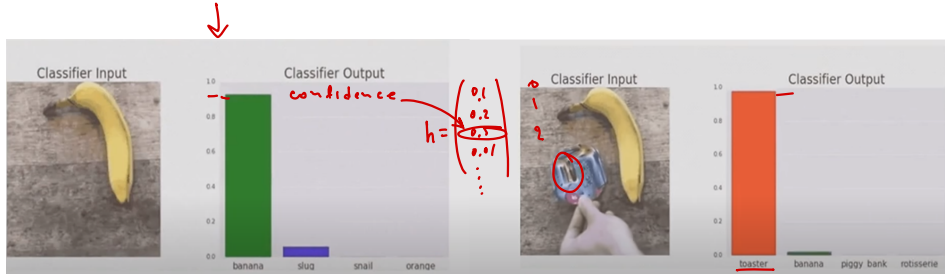
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Overconfidence effect (first line ) and some uncertainty domains (second line).

# Goals

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The goal of this lecture is:

- 1 To teach students how to incorporate uncertainty into account in an ML model

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## Section 2. Recap

# Binary Cross-Entropy (BCE) Loss Intuition

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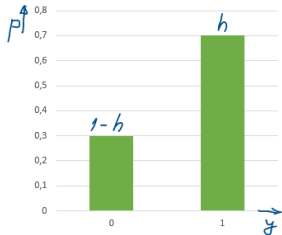


Figure: The Bernoulli distribution  
Bishop and Nasrabadi (2006); Prince  
(2023).

## Derivation of BCE Loss from MLE

For a pair  $(x_i, y_i)$ , the Bernoulli distribution takes the form:

$$p(y_i | h_i) = h_i^{y_i} (1 - h_i)^{1-y_i}.$$

This represents the probability of observing  $y_i$  given the predicted probability  $h_i$ .

For a dataset of  $N$  i.i.d. pairs, the joint probability is:

$$P(y_1, y_2, \dots, y_N | h_1, h_2, \dots, h_N) = \prod_{i=1}^N h_i^{y_i} (1 - h_i)^{1-y_i} \rightarrow \max.$$

Then we take the negative logarithm of the joint probability:

$$-\log P = -\sum_{i=1}^N [y_i \log h_i + (1 - y_i) \log(1 - h_i)] \rightarrow \min.$$

# Binary Cross-Entropy (BCE) Loss Intuition

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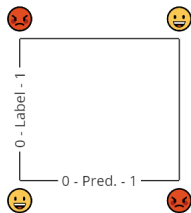


Figure: The BCE loss values intuition concerning the predictions and labels Prince (2023); Goodfellow et al. (2016).

## Derivation of BCE Loss from MLE

The Binary Cross-Entropy (BCE) loss can be derived from Maximum Likelihood Estimation (MLE) for binary classification problems. Given a set of predictions  $\hat{y}_i$  and true labels  $y_i$ , the BCE loss is defined as:

$$\mathcal{L}_{\text{BCE}} = -\frac{1}{N} \sum_{i=1}^N [y_i \log h_i + (1 - y_i) \log(1 - h_i)],$$

where:

- $N$  is the number of samples,
- $y_i \in \{0, 1\}$  is the true label,
- $h_i \in (0, 1)$  is the predicted probability.



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## Section 3. Uncertainty-aware Loss Intuition

# Uncertainty-aware Loss Intuition

$$h_i, u_i, y_i \quad \delta_i = (h_i - y_i)^2$$

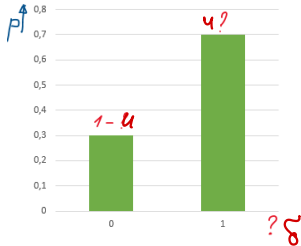


Figure: The Bernoulli distribution  
Bishop and Nasrabadi (2006); Prince  
(2023).

## Derivation of UA Loss from MLE

For a pair  $(x_i, y_i)$ , the Bernoulli distribution takes the form:

$$p(\cdot | \cdot) = u^\delta (1-u)^{1-\delta}$$

This represents the probability of observing ... given the predicted probability ...

For a dataset of  $N$  i.i.d. pairs, the joint probability  $P$  is:

$$P = \prod_{i=1}^N u_i^{\delta_i} (1-u_i)^{1-\delta_i} \rightarrow \max.$$

Then we take the negative logarithm of the joint probability:

$$-\log P = - \sum_{i=1}^N [\delta_i \log u_i + (1-\delta_i) \log (1-u_i)] \rightarrow \min.$$

# Uncertainty-Aware Loss Intuition

$u_i$  - uncertainty.

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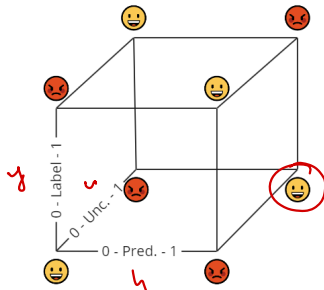
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**Figure:** The UA loss values intuition concerning the predictions, the labels, and the uncertainties.

## Derivation of UA Loss from MLE

The UA loss can be derived from Maximum Likelihood Estimation (MLE) for binary classification problems. Given a set of predictions  $\hat{y}_i$  and true labels  $y_i$ , the BCE loss is defined as:

$$\mathcal{L}_{UA} = -\frac{1}{N} \sum_{i=1}^N [\underbrace{\delta_i}_{\downarrow} \log \underbrace{u_i}_{\downarrow} + \underbrace{(1 - \delta_i)}_{\downarrow} \log \underbrace{(1 - u_i)}_{\downarrow}] \rightarrow \min,$$

$\delta_i = |h_i - y_i|$   
 $u_i \rightarrow 1 \quad h_i \rightarrow 1, \quad y_i \neq 0$   
 $\delta_i \rightarrow 1$

where:

- $N$  is the number of samples,
- $\delta_i = (y_i - h_i)^2 \in (0, 1)$  is the pseudo label,
- $y_i \in \{0, 1\}$  is the true label,
- $h_i \in (0, 1)$  is the prediction,
- $u_i \in (0, 1)$  is the uncertainty of the prediction.

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## Section 4. Conclusion

# Conclusion

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Taking the **uncertainty** into account makes a model slightly more complicated but also more flexible for real-world data. A more precise test of the research domain helps determine whether the application of uncertainty-aware models is necessary.

# Bibliography

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