

A dissertation report on

“Interactive Learning Platform for Orbital Mechanics Using Python”

Submitted to



In partial fulfilment of the requirements for the award of degree

Bachelor of Technology In Aerospace Engineering

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CERTIFICATE

This is to certify that **Mr. Ramkiran L. (17030141AE007)**, **Mr. Manjunath (17030141AE009)**, **Ms. Monisha Patel A. (17030141AE012)** and **Ms. Thoshitha R. Kumar (17030141AE027)** students of **Aerospace Engineering, Bachelor of Technology 2017-21** batch at **Alliance College of Engineering and Design (ACED), Alliance University, Bengaluru** has completed the project report titled ***“Interactive Learning Platform for Orbital Mechanics Using Python”*** under our guidance in partial fulfillment for the award of Bachelor of Technology degree in Aerospace Engineering, Alliance University, Bangalore during the year 2020-2021.

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DECLARATION

We, Ramkiran L, Manjunath, Monisha Patel A, Thoshitha R. Kumar students of 8th Semester Bachelor of Technology in Aerospace Engineering, Alliance College of Engineering and Design (ACED), Alliance University, Bengaluru, hereby declare that the entire project work entitled “**Interactive Learning Platform for Orbital Mechanics Using Python**” is an authentic record of the work that has been carried out independently by us during final year of our B.Tech at ACED, under the esteemed guidance of **Prof. Gisa G.S** and **Prof. Yadu Krishnan S.**, Assistant Professors, Department of Aerospace Engineering, Alliance college of Engineering and Design, Alliance University.

This project report is submitted in partial fulfillment of requirements for the award of the degree of Bachelor of Technology in Aerospace Engineering. The results embodied in this dissertation are original and it has not been submitted in part or full for any degree in any University.

Place: Bengaluru
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1 Introduction

MOPy, a learning tool designed to learn and practice various orbital mechanics concepts. It is designed in a way such that it can be a user-friendly tool that can be operated with ease even by the user who has very limited knowledge about the concepts of orbital mechanics. It provides users to learn about a particular concept with a brief explanation so the user can gain the theoretical knowledge required through visualizations. The sophisticated 3D environment benefits the user to visualize the fundamental concepts easily. It assists the user to verify manually calculated data. It serves as advanced virtual calculator. MOPy is an open source software with GNU-GPL v3 license¹ which anyone can use or work with. It runs on windows platforms at present.

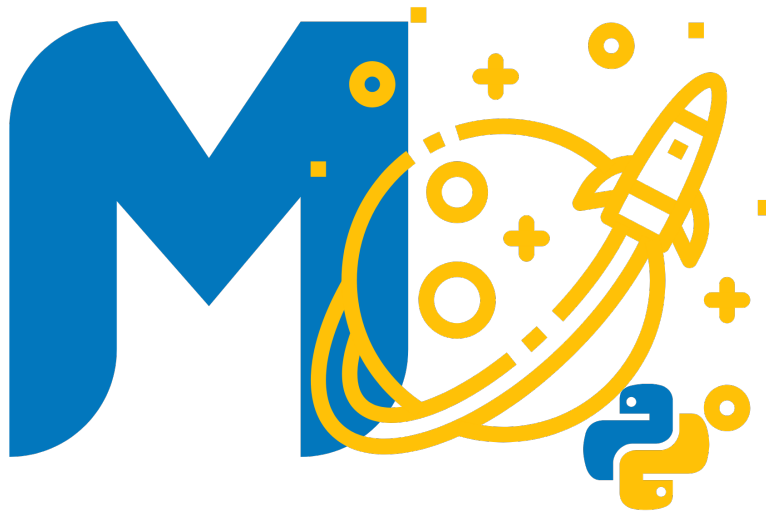


Figure 1: MOPy

1.1 Features

Sl. No	Section
1	Calculation of Orbital Elements
2	2D and 3D orbit
3	Various Parameters at any given point
4	2D and 3D Orbits
5	Calculation of Julian Day
5	Euler Angles
6	Sphere Of Influence
7	Sensitivity Analysis
8	Position of one Spacecraft w.r.t Another
9	Calculation of State and Velocity Vector
10	Orbital Transfer

Table 1: List of Features present in MOPy

1.2 Libraries Used

1. **NumPy**: This brings MATLAB like functionality of using Matrices and their operations to python. This enables us to do a lot of stuff without much hassle.
2. **SciPy** - This enables us to add many features involving more complex computing scenarios as it has features for scientific and technical computing. For example, it has different kinds of solvers for integration which we can use for solving acceleration vector equation to obtain the position vector for an orbit.
3. **Matplotlib** - This is a plotting tool that is an extension on NumPy that gives the functionality of plotting many different kinds of graph. This library is somewhat similar to the plotting feature of MATLAB.
4. **Panda3D** - This is a Game Engine based on C++ that takes in syntax from both C++ and Python. This provides real-time 3D visualizations and simulations based on the code.
5. **SQLite3** - The entire details of the planetary bodies like the orbital elements, planetary ephemeris and others are stored in a local database. SQLite is used as it enables the offline functionality.
6. **Qt Designer** - This enables MATLAB's App Designer like feature of dragging and dropping the UI elements and creating the GUI. This is based on Qt, a cross platform GUI toolkit developed by the Qt Company
7. **PyQt5 & PySide2** - These both are the python binding libraries of Qt.
8. **PyInstaller** - This library lets us convert our python code(.py) into executable file(.exe)

1.3 Market Research

There are mainly two kinds of softwares.

1. Simulation Based programs like STK, FreeFlyer etc.,
2. Sandbox Based programs like Universe SandBox, Kerbal Space Program etc.,

The simulation based programs are mainly used to simulate missions and solve problems based on the instance. Both the applications given in the example are used in the industry for all kinds of missions, ranging from very small scale missions that are performed by the students to complicated missions that are performed by NASA and ISRO.

The Sandbox based programs are the stuff that are run by the physics engine that are baked into it. They use a 3D visualization toolkit or engine which lets the user easily interact with the UI, and change the parameters directly from the environment.

In the analysis done by Morgan Stanley named “Investing in Space Exploration”, it is stated as - The revenue generated by the global space industry may increase to more than \$1 trillion by 2040. **morgan**

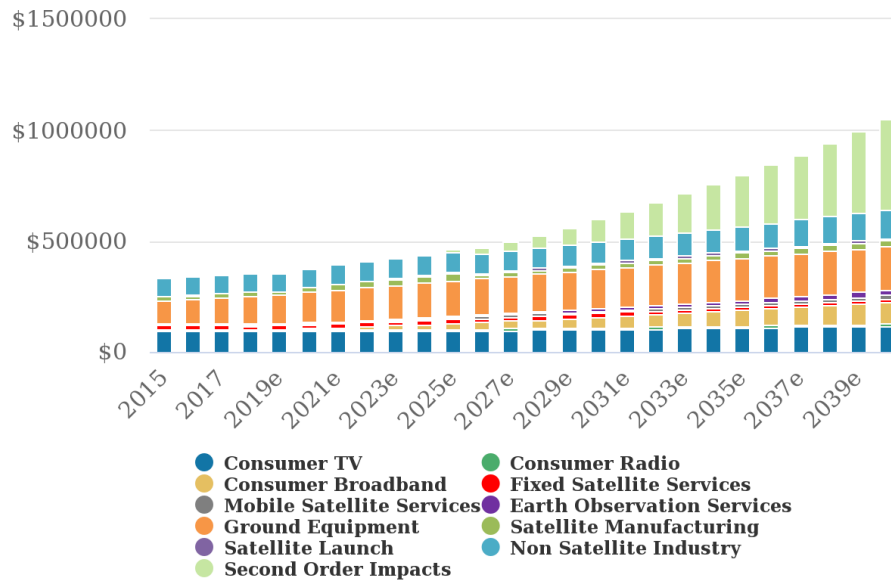


Figure 2: Global Market Trend according to Morgan Stanley.

A report by Antrix and PwC, it is stated that the indian space sector can become a \$50 Billion industry, or about one per cent of India’s projected \$5 Trillion economy, by 2024 from the current \$7 billion, according to a report by the Antrix and PwC.**indiaspace**

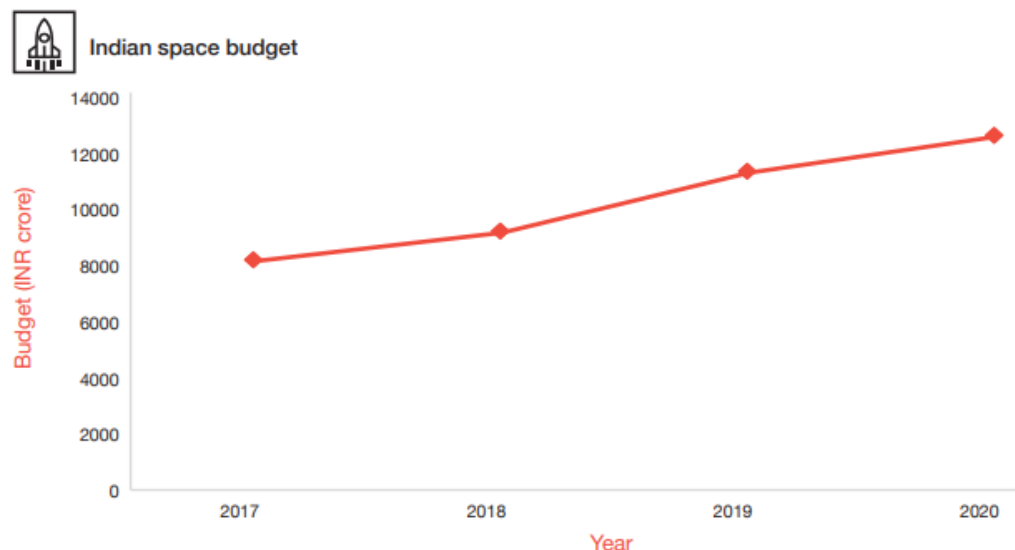


Figure 3: Indian Space Budget over the years.

1.4 Objective

The development in the field of space technology is constantly increasing as shown in the aforementioned studies. Such being the case, many students are showing interest to learn more and more about space technology and its related concepts. Considering all such possibilities, we have come up with an idea to develop a learning tool beneficial to learn more about Orbital Mechanics. The main objectives of this project are as follows:

1. Design and develop a software to learn concepts and solve Problems related orbital mechanics to understand the basics.
2. Provide a user friendly learning tool such that the user can operate even with the minimum knowledge about the concepts of orbital mechanics.
3. Help user to visualize the virtual view of the space mission.

1.5 Front End Development

1.5.1 Introduction

Front-end development deals with the Graphical User-Interface aspect of the software. It is the key developmental process that defines how the user experiences the features we have developed. The interface between the user and the back end code is GUI. The inputs from the user is taken from the GUI. So the design must be intuitive and clear. There are many libraries that can be used to develop a GUI like PyQt, Pyside, Kivy, Tkinter, etc. In our case, we have opted for PyQt5, Pyside2 and designed GUI in Qt-Designer. Then linked the Back-End scripts through the Integrated Development Environment(IDE) by Microsoft i.e, Visual Studio Code.

1.5.2 Home Page

When the application opens the Home Page will load. In it, there is a Dropdown box containing all the features available, from which the user can choose which feature they want to use. When the user selects any of the features from the drop-down and clicks on the go button at the bottom, they are navigated to that screen where they can use the feature they selected. And then if they want to navigate back to the Home-Page they can click on the Home button provided at the top left corner of the screen. All the features are listed in the upper-mentioned table.



Figure 4: Home Page of MOPy

2 Details of the Features

2.1 Calculation of Orbital Elements

This can convert state velocity vector into orbital elements and vice versa. The inputs are as follows

Inputs	State and Velocity Vectors
	Orbital Elements
Outputs	Orbital Elements
	State and Velocity Vectors

Table 2: Inputs and outputs for Calculation of Orbital Elements

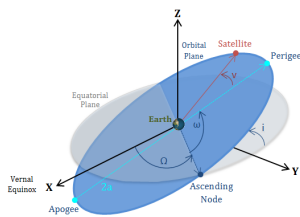


Figure 5: Classical Orbital Elements

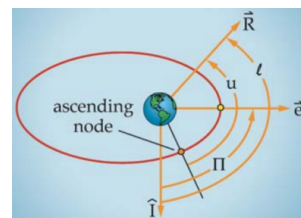


Figure 6: Alternate Orbital Elements

2.2 2D and 3D Orbits

Based on the inputs given the application can plot either 2D or 3D or both. If the inputs are just Semi major axis and eccentricity or Radius of perigee and apogee or, r_1 , v_1 , γ_1 then the resultant plot will be in the perifocal frame. If the inputs are state and velocity vector or orbital elements then the resultant will be a 3D orbit.

Inputs	For 2D - $a, e/r_a, r_p/r_1, v_1, \gamma_1$
	For 3D - Orbital Elements, State Vectors
Outputs	Orbit in the Perifocal Frame
	Orbit in a virtual 3D Environment

Table 3: I/O for 2D and 3D orbits

2.3 Euler Angle

The inputs for this are as in table(4). This code can be fed the model in 3D environment and the orientation of the model can be manipulated with this.

Inputs	Directional Cosine Matrix
	Euler Angles
Outputs	Euler Angles
	Directional Cosine Matrix

Table 4: I/O for conversion between Euler angle and DCM

2.4 Sphere of Influence

In this section, the user can either input the values or interact with the model in the 3D environment to see the corresponding output.

Inputs	Minor Body
Outputs	Radius of SOI in desired units
	3D visualization of sphere of influence in virtual environment

Table 5: I/O for Sphere of Influence

2.5 Orbital Transfer

This feature simulates the orbital transfer using various numerical methods. For now, this can perform Hohmann Transfer. The Inputs and outputs are as in table(6)

Inputs	Minor Body, Major Body, Orbital parameters of both initial and final orbit.
Outputs	Values such as Radius of apogee, Radius of perigee, DeltaV, Time-period of the orbit etc 3D visualization of desired orbital transfer

Table 6: I/O for Orbital transfer

2.6 Calculation of Julian Day

In this section the user can choose between Gregorian calendar and Julian calendar and with the other inputs they can obtain the Julian day of the corresponding date.

Inputs	YYYY-MM-DD , hh:mm:ss, Type of calender
Outputs	Julian-day

Table 7: I/O for Julian-day

2.7 Calculation of Parameters of the Orbit

The user can obtain various parameters by giving the details that they know of. If necessary they can plot the orbit too.

Inputs	$a, e/r_a, r_p/r_1, v_1, \gamma_1$ / Orbital Elements/State and velocity vectors
Outputs	μ, h, ϵ , Forces and Velocity at significant position Mean Motion, Time Period

Table 8: I/O for Various Parameters of the Orbit

2.8 Sensitivity Analysis

User has to select the type of calendar and the in the input section they have to select date and time and accuracy of digits and then by clicking on calculate button we will get Julian days in the output section. This takes in the required values an outputs how much of an error will that small change in the velocity or radius in the 3D environment.

Input	State Vector, Velocity Vector and two delta-v with slight difference
Output	Percentage difference caused to the final orbit parameters due to slight difference in delta-v

Table 9: I/O for Sensitivity Analysis

2.9 Position of One Spacecraft Relative To Another

Based on the inputs of the user the relative velocity and orbit can be visualized in this section.

Input	Major Body, State Vector and Velocity Vector of Minor Body
Output	Graph Showing the Minor bodies in the orbit around Major Body

Table 10: I/O for Position of One Spacecraft Relative To Another

2.10 Lagrangian Points

The Lagrangian points are points near two large orbiting bodies, the two objects exert an unbalanced gravitational force at a point, altering the orbit of whatever is at that point. At the Lagrange points, the gravitational forces of the two large bodies and the centrifugal force balance each other, The inputs and outputs are as follows.

Input	Major Body, Minor Body and Distance Between them
Output	Lagrangian points polar coordinates and Graph showing them

Table 11: I/O for Lagrangian Points

3 Database Management System

3.1 Introduction

Database is a collection of set of related data or information of any particular concept, generally stored using any electronic gadget . Database Management system is a system which uses integrated software to connect frontend user to connect to the database to access , modify and manage the data stored in it. There are two types of Databases:

1. Relational Database - Organizes data into one or more table. each table comprising of number of rows and columns with each row identifiable with unique key.

2. Non - Relational database - Organizes data in any form other than table. Such as graphs, flexible tables, documents etc.

In this project we have used Relational database management system with structured Query Language (SQL) to interact with the RDBMS. SQLite is the database engine used to run SQL query to perform CRUD (Create , Retrieve, Update or Delete) operation in the database.

This database contains the data of planetary bodies such as Mass, radius, density, gravity, temperature, orbital parameters, number of moons etc., of all planets of our solar system.

4 Conclusion

The outcome of the project is the lessons we learnt during the project. Communication is the key for collaborative work. This is one of the main aspect that we learned during this project. The other aspects that we were able to learn are:

1. Project Management
2. Time Management
3. Prioritize the list that is at hand based on various parameters

5 Future Scope

MOPy is a open source application with GNU - GPL v3 License, with this anyone who is interested in using this application can freely download and use it, and even modify the contents to their requirements. If they wish to contribute to this application they can fork the repository on GitHub[3] and add their contribution by sending a pull request. The reason GNU-GPL v3 license is used is that we aim to keep a quality control to the features that gets added to the application. We are always open to contributors.

There is a list of features with corresponding priorities that are planned to be added down the line. This will be constantly updated indefinitely. And if the user is not able to add a feature then they can request a feature that would be added to the list with a appropriate priority. There is discord server in which anyone can join and hold discussions with other participants. Contributors can hold discussions about the feature they are planning to add, others can discuss about the concepts and request features to be added.

As of now this runs on Windows only. This could be made to run on other platforms and even as a web application which would negate the need of a moderately powerful hardware. The database could be expanded with much more data than present.

This entire code can be converted into a library that anyone can download from PyPI. This would enable the user to utilize the features directly from the command line or their python projects. This would simplify their projects.

A Code for the Features

A.1 Calculation Of Orbital Elements

```
1 from numpy.linalg import norm
2 from numpy import dot, pi, cross, multiply as multi
3 from math import acos
4
5 class Calculate:
6     I = [1, 0, 0]
7     J = [0, 1, 0]
8     K = [0, 0, 1]
9     G = 6.67e-20 #units are in km3 kg-1 s-2
10
11     @classmethod
12     def muvalue(cls, major_body):
13         major_body_list = pandas.read_csv("Major_and_Minor_Bodies.csv")
14         major_bodies = list(major_body_list.Major_Body)
15         major_bodies_mass = list(major_body_list.Mass)
16         major_bodies_radius = list(major_body_list.Radius)
17         sel_major_body = major_bodies.index(major_body)
18         major_body_mass = major_bodies_mass[sel_major_body]
19         major_body_radius = major_bodies_radius[sel_major_body]
20         mu = cls.G * major_body_mass
21         return [mu, major_body_radius]
22
23     @classmethod
24     def correct_ohm(cls, ohm, n_vec):
25         if n_vec[0] > 0 and n_vec[1] > 0:
26             print("This is a Prograde Elliptical Orbit and is in first Quadrant.")
27             if ohm > 90:
28                 ohm -= 360
29         elif n_vec[0] < 0 and n_vec[1] > 0:
30             print("This is a Retrograde Elliptical Orbit and is in second Quadrant.")
31         )
32             if ohm > 180:
33                 ohm -= 360
34         elif n_vec[0] < 0 and n_vec[1] < 0:
35             print("This is a Retrograde Elliptical Orbit and is in Third Quadrant.")
36             if ohm < 180:
37                 ohm -= 360
38         elif n_vec[0] > 0 and n_vec[1] < 0:
39             print("This is a Prograde Elliptical Orbit and is in fourth Quadrant.")
40             if ohm < 90:
41                 ohm -= 360
42         return ohm
43
44     @classmethod
45     def other_var(cls, pos_vec, vel_vec):
46         h_vec = cross(pos_vec, vel_vec)
47         n_vec = cross(cls.K, h_vec)
48         return [h_vec, n_vec]
49
50     @classmethod
51     def OE(cls, pos_vec, vel_vec, mu):
```

```

51     [h_vec, n_vec] = Calculate.other_var(pos_vec, vel_vec)
52     e_vec = (multi((norm(vel_vec)*norm(vel_vec)-(mu/norm(pos_vec))),pos_vec)-
multi(dot(pos_vec,vel_vec),vel_vec))/(mu)
53     call.ecc_o.setText(str(norm(e_vec)))
54     inc = (acos((dot(h_vec, cls.K))/norm(h_vec))) * 180/pi
55     call.inc_o.setText(str(inc))
56     sma = 1/((2/norm(pos_vec))-((norm(vel_vec)*norm(vel_vec))/mu))
57     call.sma_o.setText(str(sma))
58     return [sma, inc, e_vec]
59
60 @classmethod
61 def ACOE(cls, pos_vec, vel_vec, e_vec, inc):
62     [h_vec, n_vec] = Calculate.other_var(pos_vec, vel_vec)
63     if inc != 0 or 180 and norm(e_vec) > 0: #Nothing is Zero/180
64         ohm = (acos((dot(cls.I,n_vec))/norm(n_vec)))
65         ohm = Calculate.correct_ohm(ohm, n_vec)
66         call.ohm_o.setText(str(ohm))
67         nu = (acos((dot(e_vec,pos_vec))/(norm(e_vec)*norm(pos_vec))))
68         call.nu_u_o.setText(str(nu))
69         omega = (acos((dot(n_vec,e_vec))/multi(norm(n_vec),norm(e_vec))))
70         call.omega_l_o.setText(str(omega))
71         return [ohm, omega, nu]
72     elif inc == 0 or 180: #Inclination is Zero
73         if norm(e_vec) > 0: #Elliptical Orbit
74             nu = (acos((dot(e_vec,pos_vec))/(norm(e_vec)*norm(pos_vec))))
75             call.nu_u_o.setText(str(nu))
76             Long_of_peri_pi = acos(dot(cls.I,e_vec)/(norm(cls.I)*norm(e_vec)))
77             return [Long_of_peri_pi, nu]
78         elif norm(e_vec) == 0: #Circular Orbit
79             Tr_long_l = acos(dot(cls.I,pos_vec)/(norm(pos_vec)*norm(cls.I)))
80             return [Tr_long_l]
81     elif norm(e_vec) == 0: #Circular orbit with inclination non-zero/pi
82         Arg_of_latitude_u = acos(dot(n_vec,pos_vec)/(norm(n_vec)*norm(pos_vec))
)
83     return [Arg_of_latitude_u]
84
85 @classmethod
86 def possibility(cls, major_body, pos_vec, vel_vec):
87     [mu, major_body_radius] = Calculate.muvalue(major_body)
88     pos = norm(pos_vec)
89     vel = norm(vel_vec)
90     sma = 1/((2/pos)-(vel*vel/mu))
91     e_vec = (multi((norm(vel_vec)*norm(vel_vec)-(mu/norm(pos_vec))),pos_vec)-
multi(dot(pos_vec,vel_vec),vel_vec))/(mu)
92     r_peri = sma*(1-norm(e_vec))
93     if r_peri <= major_body_radius:
94         print("The Orbit is not possible as radius of perigee is less than
radius of the major Body")
95         return False
96     return True

```

Listing 1: CoOE.py

A.2 Euler Angles

```

1 from math import *
2 from numpy import *
3
4 class EA():
5
6     def RxRyRz(pitch_theta, roll_phi, yaw_si):
7         Rx = matrix([[ 1, 0 , 0 ],
8                       [ 0, cos(roll_phi),sin(roll_phi)],
9                       [ 0,-sin(roll_phi), cos(roll_phi)]]))
10
11         Ry = matrix([[ cos(pitch_theta), 0,-sin(pitch_theta)],
12                       [ 0 ,1, 0],
13                       [sin(pitch_theta), 0, cos(pitch_theta)]]))
14
15         Rz = matrix([[ cos(yaw_si), sin(yaw_si), 0 ],
16                       [-sin(yaw_si), cos(yaw_si) , 0 ],
17                       [ 0, 0, 1]])
18         return [Rx, Ry, Rz]
19
20     def DCMtoEA(DCM, order):
21         if order=='321':
22             theta=-asin(DCM[0][2])
23             phi=atan(DCM[1][2]/DCM[2][2])
24             si=atan(DCM[0][1]/DCM[0][0])
25         elif order=='123':
26             theta=asin(DCM[2][0])
27             phi=atan(DCM[2][1]/DCM[2][2])
28             si=atan(DCM[1][0]/DCM[0][0])
29         elif order=='132':
30             theta=atan(DCM[2][0]/DCM[0][0])
31             phi=atan(DCM[1][2]/DCM[1][1])
32             si=-asin(DCM[1][0])
33         elif order=='312':
34             theta=atan(DCM[0][2]/DCM[2][2])
35             phi=asin(DCM[1][2])
36             si=atan(DCM[1][0]/DCM[1][1])
37         elif order=='213':
38             theta=atan(DCM[2][0]/DCM[2][2])
39             phi=-asin(DCM[2][1])
40             si=atan(DCM[0][1]/DCM[1][1])
41         elif order=='231':
42             theta=atan(DCM[0][2]/DCM[0][0])
43             phi=atan(DCM[2][1]/DCM[1][1])
44             si=asin(DCM[0][1])
45         return [theta, si, phi]
46
47     def EAtoDCM(theta, si, phi, order):
48         [Rx, Ry, Rz] = EA.RxRyRz(theta, si, phi)
49         if order=='321':
50             RxRy = dot(Rx,Ry)
51             return (dot(RxRy,Rz))
52         elif order == '123':
53             x = Rx(phi*pi/180)
54             y = Ry(theta*pi/180)
55             z = Rz(si*pi/180)
56             zy = dot(z,y)
57             return (dot(zy,x))

```

```

58     elif order == '213':
59         x = Rx(phi*pi/180)
60         y = Ry(theta*pi/180)
61         z = Rz(si*pi/180)
62         zx = dot(z,x)
63         return (dot(zx,y))
64     elif order == '312':
65         x = Rx(phi*pi/180)
66         y = Ry(theta*pi/180)
67         z = Rz(si*pi/180)
68         yx = dot(y,x)
69         return (dot(yx,z))
70     elif order == '132':
71         x = Rx(phi*pi/180)
72         y = Ry(theta*pi/180)
73         z = Rz(si*pi/180)
74         yz = dot(y,z)
75         return (dot(yz,x))
76     elif order == '231':
77         x = Rx(phi*pi/180)
78         y = Ry(theta*pi/180)
79         z = Rz(si*pi/180)
80         xz = dot(x,z)
81         return (dot(xz,y))
82     else:
83         return ('No transformation matrix')
84
85 order = '321' #input("Enter the order:")
86 DCM = [[0.6405, 0.75319, -0.15038],[0.76736, -0.63531, 0.086824],[-0.030154,
87         -0.17101, -0.98481]]
88 print(EA.DCMtoEA(DCM,order))
89 print(EA.EAtoDCM(8.6489 * 180/pi, 49.619 * 180/pi, -5.039 * 180/pi, order))

```

Listing 2: EA.py

A.3 Sphere of Influence

```

1 from math import *
2 import numpy as np
3 import matplotlib.pyplot as plt
4 from mpl_toolkits.mplot3d import Axes3D
5 import sqlite3
6
7 def SoI(MiB_mass, MiB_radius, r_maj_to_min):
8     MaB_mass = 1.989e30
9     rSOI = (r_maj_to_min*(MiB_mass/MaB_mass)**(2/5))
10    return [rSOI, rSOI/MiB_radius]

```

Listing 3: SoI

A.4 Calculation of Julian Day

```

1 from math import *
2 class JulianDay():
3
4     @classmethod
5     def tb_method(cls,year, month, day, hour, minutes, seconds, accuracy):
6         if 1901 <= year <= 2099:
7             JDN = 367 * year + int((7 * (year + int((month + 9)/12)))/4) + int(275 *
8             month/9) + day + 1721013.5
9             UT = hour + round((minutes/60), accuracy) + round((seconds/3600),
10             accuracy)
11             JD = JDN + UT/24
12             return [JDN, JD]
13         else:
14             #manju you can set limits when this option is selected between 1901 and
15             2099
16             print("Not Possible from this method")
17
18     @classmethod
19     def julian_day(cls,year, month, day, hour, minutes, seconds, accuracy,
20     type_of_calender):
21         if type_of_calender == "Gregorian":
22             #julian day number from Gregorian calender date
23             JDN = int((1461 * (year + 4800 + (month - 14)/12))/4) + int((367 * month
24             - 2 - 12 * ((month - 14)/12))/12) - int((3 * ((year + 4900 + (month - 14)/12)
25             /100))/4) + day - 32075
26         elif type_of_calender == "Julian":
27             #julian day number from julian calender date
28             JDN = 367 * year - int((7 * (year + 5001 + (month - 9)/7))/4) + int((275
29             * month)/9) + day + 1729777
30             #JDN to JD
31             JD = JDN + round(((hour - 12)/24),accuracy) + round((minutes/1440), accuracy
32             ) + round((seconds/86400), accuracy)
33             return [JDN, round(JD, accuracy)]

```

Listing 4: CJS.py

A.5 Calculation of Various Parameters of the Orbit

```

1 import numpy as np
2 from math import *
3
4 class GlobalCalculation():
5     I = [1, 0, 0]
6     J = [0, 1, 0]
7     K = [0, 0, 1]
8     G = 6.67e-20 #units are in km3 kg-1 s-2
9
10    @classmethod
11    def force_at_this_point(cls, r, major_body_mass, minor_body_mass):
12        F_r = cls.G * major_body_mass * minor_body_mass / r ** 2
13        return F_r
14
15
16 # all the units should be km
17 class CalculateCircularElliptical:

```

```

18 I = [1, 0, 0]
19 J = [0, 1, 0]
20 K = [0, 0, 1]
21 G = 6.67e-20 #units are in km3 kg-1 s-2
22 def __init__(self, major_body):
23
24     self.major_body = major_body
25     return
26
27 @classmethod
28 def semiecc(cls, sma, mag_e, major_body):
29     r_per = sma * (1 - mag_e)
30     r_apo = sma * (1 + mag_e)
31     [mean_motion, T_period, mag_h, sme, slr] = CalculateCircularElliptical.
orb_const(r_per, sma, mag_e, major_body)
32     return [r_per, r_apo, mean_motion, T_period, mag_h, sme, slr]
33
34 @classmethod
35 def perapo(cls, r_per, r_apo, major_body):
36     sma = (r_per + r_apo)/2
37     mag_e = (r_apo - r_per)/(r_apo + r_per)
38     [mean_motion, T_period, mag_h, sme, slr] = CalculateCircularElliptical.
orb_const(r_per, sma, mag_e, major_body)
39     return [mag_e, sma, mean_motion, T_period, mag_h, sme, slr]
40
41 @classmethod
42 def orb_const(cls, r_per, sma, mag_e, major_body):
43     major_body_mass = 5.972e24 #self.major_body * 1
44     mu = cls.G * major_body_mass
45     slr = sma*(1-mag_e**2)
46     mag_h = (r_per*(1+e)*mu)**0.5
47     T_period = sqrt(((4*pi**2)/mu)*sma**3)
48     mean_motion = T_period/(2*pi)
49     sme = -mu/(2* sma)
50     return [mean_motion, T_period, mag_h, sme, slr]
51
52 @classmethod
53 def time_since_periapsis(cls, mag_e, theta, T_period):
54     E_anomly = 2 * atan((sqrt((1 - mag_e)/(1 + mag_e)) * tan(theta/2)))
55     M_anomly = E_anomly - mag_e * sin(E_anomly)
56     t_since_perigee = T_period * M_anomly/(2*pi)
57     return t_since_perigee
58
59 @classmethod
60 def velocity_at_any_point(cls, sma, r, major_body):
61     major_body_mass = major_body * 1
62     mu = cls.G * major_body_mass
63     v_point = sqrt(((2 * mu)/r) - (mu/sma))
64     return v_point
65
66 class CalculateParabola():
67     I = [1, 0, 0]
68     J = [0, 1, 0]
69     K = [0, 0, 1]
70     G = 6.67e-20 #units are in km3 kg-1 s-2
71
72     @classmethod

```

```

73     def const_values(cls, r_per, major_body):
74         major_body_mass = major_body * 1
75         mu = major_body_mass * cls.G
76         slr = 2 * r_per
77         v_per = sqrt((2*mu)/r_per)
78         mag_h = sqrt(mu*r_per * 2)
79         return [slr, v_per, mag_h]
80
81     @classmethod
82     def velocity_at_any_point(cls, r, major_body):
83         major_body_mass = major_body * 1
84         mu = major_body_mass * cls.G
85         v = sqrt((2*mu)/r)
86         return v
87
88 class CalculateHyperBola():
89     I = [1, 0, 0]
90     J = [0, 1, 0]
91     K = [0, 0, 1]
92     G = 6.67e-20 #units are in km3 kg-1 s-2
93
94     @classmethod
95     def const_values(cls, major_body, mag_e, sma):
96         mu = cls.G * major_body
97         theta_inf = acos(1/mag_e) #angle between asymptotes
98         beta = theta_inf
99         delta = 2 * sin(1/mag_e) #turn angle
100        mag_h = sqrt(sma * mu * (mag_e**2-1)) #specific angular momentum
101        b = sma * mag_e * sin(theta_inf) #semi minor axis
102        Delta = b #aiming radius
103        v_inf = mu * mag_e*sin(theta_inf)/mag_h #velocity at r = infinity
104        sme = mu/(2 * sma) #specific mechanical energy
105        slr = -b**2/sma #semi latus rectum
106        return [theta_inf, beta, delta, mag_h, b, Delta, v_inf, sme, slr]
107
108     @classmethod
109     def semiecc(cls, major_body, sma, mag_e):
110         mu = cls.G * major_body
111         [theta_inf, beta, delta, mag_h, b, Delta, v_inf, sme, slr] =
CalculateHyperBola.const_values(major_body, sma, mag_e)
112         r_apo = (mag_h**2/mu)/(1 - mag_e)
113         r_per = (mag_h**2/mu)/(1 + mag_e)
114         return [theta_inf, beta, delta, mag_h, b, Delta, v_inf, sme, slr, r_apo,
r_per]

```

Listing 5: VPCO

A.6 Sensitivity Analysis

```

1 class SA(Major_Body, R1_bod):
2     def __init__(self):
3         G = 6.67e-20
4         mu_Major_Body = G * self.R1_bod * 1
5         mu_R1 = G * self.R2_bod * 1
6

```

```

7     def SA(self, R1, R2):
8         a = 2/(1-(R1*Vdv**2)/(2*self.mu_Major_Body))
9         coeff_del_Rp_Rp = a * (self.mu_R1/(Vdv*Vi*Rp))
10        coeff_del_Vp_Vp = a * ((Vi+(2*self.mu_R1/(Rp*Vi)))/Vdv)
11        del_R2_R2 = coeff_del_Rp_Rp*(del_Rp_Rp) + coeff_del_Vp_Vp * (del_Vp_Vp)
12        return [del_R2_R2]

```

Listing 6: SA.py

A.7 Lagrangian Points

```

1  from math import pi
2  from numpy import arange
3  import matplotlib.pyplot as plt
4  from scipy.optimize import root_scalar
5
6  G = 6.67408e-11
7  m1 = 5.972e24
8  m2 = 0.07346e24
9  l = 384400000
10 x1 = m2 * l / (m1 + m2)
11 x2 = m1 * l / (m1 + m2)
12 velocity = (G * (m1 + m2)/ l) ** 0.5
13 period = 2 * pi * l / velocity
14 theta_dot = 2*pi / period
15
16 def x_eqn(xs):
17     return -G*m1/((xs + x1) * abs(xs +x1)) - G * m2 / ((xs - x2)*abs(xs-x2)) + \
18         theta_dot**2 * xs
19
20
21 xvals = arange(-2*l, 2*l, 1000)
22 yvals = x_eqn(xvals)
23
24 L1 = root_scalar(x_eqn, bracket=[2e8, 3.5e8])
25 print(L1.root+x1)
26 L2 = root_scalar(x_eqn, bracket=[3.9e8, 5e8])
27 print(L2.root+x1)
28 L3 = root_scalar(x_eqn, bracket=[-4e8, -2e8])
29 print(L3.root+x1)
30
31 plt.plot(xvals, yvals)
32 plt.grid()
33 plt.ylim(-0.01, 0.01)
34 plt.show()

```

Listing 7: LP.py

A.8 CRUD File Operations

```

1  # import sqlite in ide
2  import sqlite3

```



```

3
4 # Create a database or connect to one
5 conn= sqlite3.connect('appdatabase.db')
6
7 # Create a Cursor
8 c= conn.cursor()
9
10 # Creat a table
11 c.execute(""" CREATE TABLE table_name(
12         column_name datatype,
13         column_name datatype
14     )""")
15
16 # Insert data into table
17 x = [('column 1', 'column 2')
18      ('column 1', 'column 2')
19      ]
20 c.executemany( "INSERT INTO table_name VALUES(?,?)",x)
21
22 #Retrieve or read data
23 c.execute("SELECT * FROM table_name")
24 print(c.fetchall())
25
26 # commit data to the database
27 conn.commit()

```

Listing 8: db.py