#### A dissertation report on

## "Interactive Learning Platform for Orbital Mechanics Using Python"

Submitted to



In partial fulfilment of the requirements for the award of degree

# **Bachelor of Technology** In **Aerospace Engineering**

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#### **CERTIFICATE**

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## **DECLARATION**

We, Ramkiran L, Manjunath, Monisha Patel A, Thoshitha R. Kumar students of 8<sup>th</sup> Semester Bachelor of Technology in Aerospace Engineering, Alliance College of Engineering and Design (ACED), Alliance University, Bengaluru, hereby declare that the entire project work entitled "Interactive Learning Platform for Orbital Mechanics Using Python" is an authentic record of the work that has been carried out independently by us during final year of our B.Tech at ACED, under the esteemed guidance of Prof. Gisa G.S and Prof. Yadu Krishnan S., Assistant Professors, Department of Aerospace Engineering, Alliance college of Engineering and Design, Alliance University.

This project report is submitted in partial fulfillment of requirements for the award of the degree of Bachelor of Technology in Aerospace Engineering. The results embodied in this dissertation are original and it has not been submitted in part or full for any degree in any University.

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## 1 Introduction

MOPy, a learning tool designed to learn and practice various orbital mechanics concepts. It is designed in a way such that it can be a user-friendly tool that can be operated with ease even by the user who has very limited knowledge about the concepts of orbital mechanics. It provides users to learn about a particular concept with a brief explanation so the user can gain the theoretical knowledge required through visualizations. The sophisticated 3D environment benefits the user to visualize the fundamental concepts easily. It assists the user to verify manually calculated data. It serves as advanced virtual calculator. MOPy is an open source software with GNU-GPL v3 licenselic which anyone can use or work with. It runs on windows platforms at present.

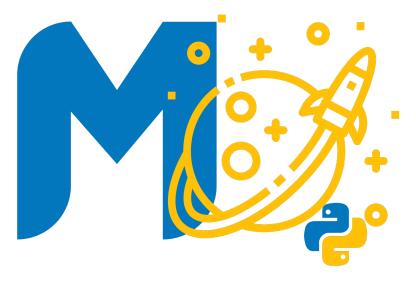


Figure 1: MOPy

#### 1.1 Features

Sl. No	Section
1	Calculation of Orbital Elements
2	2D and 3D orbit
3	Various Parameters at any given point
4	2D and 3D Orbits
5	Calculation of Julian Day
5	Euler Angles
6	Sphere Of Influence
7	Sensitivity Analysis
8	Position of one Spacecraft w.r.t Another
9	Calculation of State and Velocity Vector
10	Orbital Transfer

Table 1: List of Features present in MOPy

#### 1.2 Libraries Used

- 1. **NumPy**: This brings MATLAB like functionality of using Matrices and their operations to python. This enables us to do a lot of stuff without much hassle.
- 2. SciPy This enables us to add many features involving more complex computing scenarios as it has features for scientific and technical computing. For example, it has different kinds of solvers for integration which we can use for solving acceleration vector equation to obtain the position vector for an orbit.
- 3. **Matplotlib** This is a plotting tool that is a extension on NumPy that gives the functionality of plotting many different kinds of graph. This library is somewhat similar to the plotting feature of MATLAB.
- 4. **Panda3D** This is a Game Engine based on C++ that takes in syntax from both C++ and Python. This provides real-time 3D visualizations and simulations based on the code.
- 5. **SQLite3** The entire details of the planetary bodies like the orbital elements, planetary ephemeris and others are stored in a local database. SQLite is used as it enables the offline functionality.
- 6. **Qt Deisgner** This enables MATLAB's App Designer like feature of dragging and dropping the UI elements and creating the GUI. This is based on Qt, a cross platform GUI toolkit developed by the Qt Company
- 7. **PyQt5** & **PySide2** These both are the python binding libraries of Qt.
- 8. **PyInstaller** This library lets us convert our python code(.py) into executable file(.exe)

#### 1.3 Market Research

There are mainly two kinds of softwares.

- 1. Simulation Based programs like STK, FreeFlyer etc.,
- 2. Sandbox Based programs like Universe SandBox, Kerbal Space Program etc.,

The simulation based programs are mainly used to simulate missions and solve problems based on the instance. Both the applications given in the example are used in the industry for all kinds of missions, ranging from very small scale missions that are performed by the students to complicated missions that are performed by NASA and ISRO.

The Sandbox based programs are the stuff that are run by the physics engine that are baked into it. They use a 3D visualization toolkit or engine which lets the user easily interact with the UI, and change the parameters directly from the environment.

In the analysis done by Morgan Stanley named "Investing in Space Exploration", it is stated as - The revenue generated by the global space industry may increase to more than \$1 trillion by 2040. **morgan** 

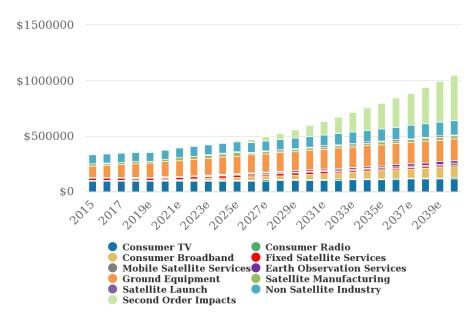


Figure 2: Global Market Trend according to Morgan Stanley.

A report by Antrix and PwC, it is stated that the indian space sector can become a \$50 Billion industry, or about one per cent of India's projected \$5 Trillion economy, by 2024 from the current \$7 billion, according to a report by the Antrix and PwC.indiaspace

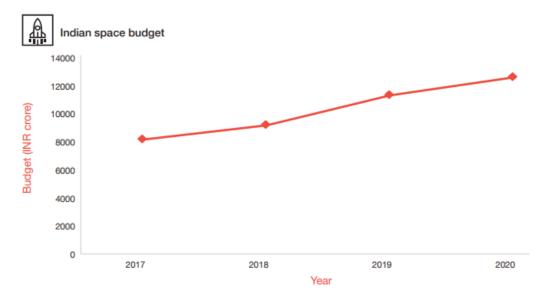


Figure 3: Indian Space Budget over the years.

## 1.4 Objective

The development in the field of space technology is constantly increasing as shown in the aforementioned studies. Such being the case, many students are showing interest to learn more and more about space technology and its related concepts. Considering all such possibilities, we have come up with an idea to develop a learning tool beneficial to learn more about Orbital Mechanics The main objectives of this project are as follows:

- 1. Design and develop a software to learn concepts and solve Problems related orbital mechanics to understand the basics.
- 2. Provide a user friendly learning tool such that the user can operate even with the minimum knowledge about the concepts of orbital mechanics.
- 3. Help user to visualize the virtual view of the space mission.

## 1.5 Front End Development

#### 1.5.1 Introduction

Front-end development deals with the Graphical User-Interface aspect of the software. It is the key developmental process that defines how the user experiences the features we have developed. The interface between the user and the back end code is GUI. The inputs from the user is taken from the GUI. So the design must be intuitive and clear. There are many libraries that can be used to develop a GUI like PyQt, Pyside, Kivy, Tkinter, etc. In our case, we have opted for PyQt5, Pyside2 and designed GUI in Qt-Designer. Then linked the Back-End scripts through the Integrated Development Environment(IDE) by Microsoft i.e. Visual Studio Code.

#### 1.5.2 Home Page

When the application opens the Home Page will load. In it, there is a Dropdown box containing all the features available, from which the user can choose which feature they want to use. When the user selects any of the features from the drop-down and clicks on the go button at the bottom, they are navigated to that screen where they can use the feature they selected. And then if they want to navigate back to the Home-Page they can click on the Home button provided at the top left corner of the screen. All the features are listed in the upper-mentioned table.



Figure 4: Home Page of MOPy

## 2 Details of the Features

## 2.1 Calculation of Orbital Elements

This can convert state velocity vector into orbital elements and vice versa. The inputs are as follows

Inputs	State and Velocity Vectors
inputs	Orbital Elements
Outputs	Orbital Elements
Outputs	State and Velocity Vectors

Table 2: Inputs and outputs for Calculation of Orbital Elements

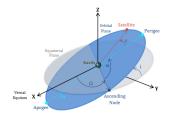


Figure 5: Classical Orbital Elements

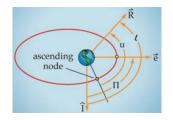


Figure 6: Alternate Orbital Elements

#### **Classical Orbital Elements**

1. **Semi-major Axis**(a): This is a constant that defines the size of the orbit. In Circular it is the radius of the circle. It is the longest diameter of an ellipse.

$$a = \frac{r_a + r_p}{2} \tag{1}$$

$$a = \frac{h^2/\mu}{1 - e^2} \tag{2}$$

where,

 $r_a = Radius \ of \ Apogee(F_1B)$ 

 $r_p = Radius \ of \ Perigee(F_1A)$ 

 $\mu = Standard\ Gravitational\ Parameter,$ 

2. **Eccentricity**(*e*): This the parameter of the conic section which determines its shape. It is defined as the ratio of distance b/w two foci to the Major-axis.

$$e = -\frac{c}{a} \tag{3}$$

$$e = \frac{1}{\mu} \left[ \left( \frac{v^2 - \mu}{r} \right) \times \overrightarrow{r} - (\overrightarrow{r} \cdot \overrightarrow{v}) \times \overrightarrow{v} \right]$$
 (4)

where,

 $r_a \& r_p = Radius \ of \ Apogee \& \ Perigee \ respectively,$ 

 $\mu = Standard\ Gravitational\ Parameter,$ 

 $\overrightarrow{v} \& v = Velocity\ vector\ \&\ Magnitude\ of\ Velocity\ Vector\ at\ r,$ 

 $\overrightarrow{r}$  &  $r = Radius\ Vector\ \&\ Magnitude\ of\ Radius\ Vector.$ 

3. **Inclination**(e): It is the tilt of the orbit w.r.t the equatorial plane, measured at ascending node. It can also be defined as the angle from  $\hat{K}$  unit vector to the specific angular momentum vector  $\vec{h}$ .

$$i = \cos^{-1}\left(\frac{\overrightarrow{h}.\overrightarrow{K}}{|h|}\right) \tag{5}$$

where,

 $\overrightarrow{h} = Specific Angular Momentum,$ 

 $\overrightarrow{K} = Unit\ Vector\ in\ Z\ direction,$ 

 $|h|=Magnitude\ of\ Specific\ Angular\ Momentum.$ 

4. **Right Ascension of Ascending Node**( $\Omega$ ): RAAN horizontally orients the ascending node of the orbit w.r.t the Equatorial plane's vernal equinox, measured in an equatorial plane This is not defined when the inclination is 0 or 180 degree. It lies between 0 to 360 degrees.

$$\Omega = \cos^{-1}\left(\frac{\overrightarrow{I}.\overrightarrow{n}}{|n|}\right) \tag{6}$$

where,

 $\overrightarrow{n} = Nodal \ vector$ 

It's the vector that joins the ascending node and the descending node.

5. **Argument of Perigee**( $\omega$ ): Argument of Perigee defines the orientation of the ellipse in the orbital plane, as an angle measured from the ascending node to the periapsis measure in the direction of the spacecraft's motion. This is not defined when inclination is 0 or 180 degree or eccentricity is 0. It lies between 0 to 360 degree.

$$\omega = \cos^{-1}\left(\frac{\overrightarrow{n} \cdot \overrightarrow{e}}{|n||e|}\right)$$

$$where,$$

$$\overrightarrow{e} = EccentricityVector.$$
(7)

6. **True Anomaly**( $\nu$ ): True Anomaly defines the position of the spacecraft w.r.t perigee. It's the angle between the spacecraft and the perigee of the orbit. It lies between 0 to 360 degree.

$$\nu = \cos^{-1}\left(\frac{\overrightarrow{e} \cdot \overrightarrow{r}}{|e||r|}\right)$$

$$where,$$

$$\overrightarrow{r} = RadiusVector$$
(8)

#### **Alternate Orbital Elements**

1. **Longitude of Perigee**(Pi) is the angle from the principle direction to perigee. This is used whenever inclination is either  $0^o$  or  $180^o$  as there is no ascending node. It's lies between  $0^0$  to  $360^0$ . In the figure(6) Longitude of perigee is represented as " $\Pi$ ".

$$\Pi = \cos^{-1}\left(\frac{\overrightarrow{I} \cdot \overrightarrow{e}}{|e|}\right) \tag{9}$$

2. **True Longitude** is the angle from the principle direction to the spacecraft's position. This is used whenever there is no perigee and the inclination is either 0° or 180°. It's lies between 0° to 360°. It lies between 0 to 360 degree. In the figure(6)True Longitude is represented as "l" In the figure(6)True Longitude is represented as "l". In the figure(6) Longitude of perigee is represented as "Π".

$$l = \cos^{-1}\left(\frac{\overrightarrow{I}.\overrightarrow{r'}}{|r|}\right) \tag{10}$$

3. **Argument of Latitude**(u) is the angle from ascending to the spacecraft's position. This is used whenever a perigee is absent(i.e., e=0,Circular Orbit). It's lies between  $0^0$  to  $360^0$ . In the figure(6) Argument of latitude is represented as "u".

$$u = \cos^{-1}\left(\frac{\overrightarrow{n} \cdot \overrightarrow{r}}{|n||r|}\right) \tag{11}$$

#### 2.2 2D and 3D Orbits

Based on the inputs given the application can plot either 2D or 3D or both. If the inputs are just Semi major axis and eccentricity or Radius of perigee and apogee or,  $r_1$ ,  $v_1$ ,  $v_1$ ,  $v_1$ , then the resultant plot will be in the perifocal frame. If the inputs are state and velocity vector or orbital elements then the resultant will be a 3D orbit.

Inputs	For 2D - $a, e/r_a, r_p/r_1, v_1, \gamma_1$
inputs	For 3D - Orbital Elements, State Vectors
Outputs	Orbit in the Perifocal Frame
Outputs	Orbit in a virtual 3D Environment

Table 3: I/O for 2D and 3D orbits

There are two ways to plot a orbit, if the plot is on a 2D plane, i.e., Perifocal Plane, the the trajectory equation can be used to plot it easily.

$$r = \frac{h^2/\mu}{1 - e\cos(\theta)}$$

If the plot is 3D then solving for the trajectory analytically can be tricky and expensive computing wise depending on the orbit. But, solving it numerically will yeild the orbit with wide range of accuracy depending on the numerical method. The method has mainly two properties to be considered for at this level, the computing speed and the accuracy. A good compromise between these both is desirable for most of the cases. In this case we need a ODE solver. Here are a few types of numerical methods:

- 1. Euler Method
- 2. Backward Euler Method
- 3. First-order Exponential integrator Method
- 4. Generalizations
- 5. Parallel-in-time Methods
- 6. Integrals over Infinite intervals

In a programming language based on these methods ODE solvers are written. The most popular ones are:

- 1. **Isoda** This automatically selects a solver which is appropriate for the given equation.
- 2. **Isode** Since Isoda turns out to be slow, then the DE might need a stiff solver(i.e., very small time steps), this will choose only the stiff solvers
- 3. **ode23** Simultaneously uses fourth and fifth order RK formulas to make error estimates and adjust the time step accordingly. For nonstiff ODEs

4. **ode45** - Uses simultaneously second and third order Runge Kutta formulas to make estimates of the error, and calculate the time step size. Since the second and third order RK require less steps, ode23 is "less expensive" in terms of computation demands than ode45, but is also lower order. Use for nonstiff ODEs

For MOPy Isoda is sufficient enough for now. So Isoda is used to solve for the acceleration vector. If the acceleration vector is solved twice then we obtain the position vectors using which a 3D plot can be plotted. The acceleration vector is:

Enter the acceleration vector

## 2.3 Euler Angle

The inputs for this are as in table(4). This code can be fed the model in 3D environment and the orientation of the model can be manipulated with this.

Inputs	Directional Cosine Matrix
Imputs	Euler Angles
Outputs	Euler Angles
Carpais	Directional Cosine Matrix

Table 4: I/O for conversion between Euler angle and DCM

## 2.4 Sphere of Influence

In this section, the user can either input the values or interact with the model in the 3D environment to see the corresponding output.

Inputs	Minor Body
Outputs	Radius of SOI in desired units
Catpats	3D visualization of sphere of influence in virtual environment

Table 5: I/O for Sphere of Influence

The sun is the dominant celestial body in the solar system. It has a mass of over 300,000 earths. The sun's gravitational pull holds all the planets in its hold according to Newton's law of gravity. However, near a given planet, the influence of its own gravity exceeds that of the sun. For example, at its surface the earth's gravitational force is over 1600 times greater than the sun's. The inversesquare nature of the law of gravity means that the force of gravity  $F_g$  drops off rapidly with distance r from the center of attraction. If

 $F_{g0}$  is the gravitational force at the surface of a planet with radius  $r_0$ , then Figure 8.5 shows how rapidly the force diminishes with distance. At ten body radii, the force is 1% of its value at the surface. Eventually, the force of the sun's gravitational field overwhelms that of the planet.

To estimate the planets Sphere of Influence, the three body problem system comprising of planet p of mass MiB\_ mass, the sun s and its mass MaB\_ mass with the distance between then being R and the equation on hand is:

$$r_{SOI} = R \left( \frac{MiB\_mass}{MaB\_mass} \right)^{2/5}$$

#### 2.5 Orbital Transfer

This feature simulates the orbital transfer using various numerical methods. For now, this can perform Hohmann Transfer. The Inputs and outputs are as in table(6)

Inputs	Minor Body, Major Body, Orbital parameters of both initial and final orbit.
Outputs	Values such as Radius of apogee, Radius of perigee, DeltaV, Time-period of the orbit etc
outputs	3D visualization of desired orbital transfer

Table 6: I/O for Orbital transfer

#### 2.6 Calculation of Julian Day

In this section the user can choose between Gregorian calendar and Julian calendar and with the other inputs they can obtain the Julian day of the corresponding date.

Inputs	YYYY-MM-DD , hh:mm:ss, Type of calender
Outputs	Julian-day

Table 7: I/O for Julian-day

The Julian day is the continuous count of days since the beginning of the Julian period i.e., January 1, 4713 B.C. at 12 Noon, and is used primarily by astronomers for easily calculating elapsed days between two events. To calculate a Julian Day there are many formulae, but the generalised formula is:

To convert from Gregorian calendar:

$$JDN = \frac{1461\left(Y + 4800 + \frac{M - 14}{12}\right)}{4} + \frac{367\left(M - 2 - 12\frac{M - 14}{12}\right)}{12} - \frac{3\left(\frac{Y + 4900 + \frac{M - 14}{12}}{100}\right)}{4} + D - 32075$$

To convert from Julian Calendar:

$$JDN = 367 \times Y - \frac{7\left(Y + 5001 + \frac{M - 9}{7}\right)}{4} + \frac{275M}{9} + D + 1729777$$

Once the Julian Day Number is obtained the time is taken into account. So, The Julian day becomes:

$$JD = JDN + \frac{HH - 12}{24} + \frac{MM}{1440} + \frac{SS}{86400}$$

#### 2.7 Calculation of Parameters of the Orbit

The user can obtain various parameters by giving the details that they know of. If necessary they can plot the orbit too.

Inputs	$a,e/r_a,r_p/r_1,\ v_1,\ \gamma_1$ / Orbital Elements/State and velocity vectors
Outputs	$\mu,\ ,h\ ,\epsilon,$ Forces and Velocity at significant position
Guipuis	Mean Motion, Time Period

Table 8: I/O for Various Parameters of the Orbit

## 2.8 Sensitivity Analysis

User has to select the type of calendar and the in the input section they have to select date and time and accuracy of digits and then by clicking on calculate button we will get Julian days in the output section. This takes in the required values an outputs how much of an error will that small change in the velocity or radius in the 3D environment.

Input	State Vector, Velocity Vector and two delta-v with slight difference
Output	Percentage difference caused to the final orbit parameters due to slight difference in delta-v

Table 9: I/O for Sensitivity Analysis

## 2.9 Position of One Spacecraft Relative To Another

Based on the inputs of the user the relative velocity and orbit can be visualized in this section.

Input	Major Body, State Vector and Velocity Vector of Minor Body
Output	Graph Showing the Minor bodies in the orbit around Major Body

Table 10: I/O for Position of One Spacecraft Relative To Another

## 2.10 Lagrangian Points

The Lagrangian points are points near two large orbiting bodies, the two objects exert an unbalanced gravitational force at a point, altering the orbit of whatever is at that point. At the Lagrange points, the gravitational forces of the two large bodies and the centrifugal force balance each other, The inputs and outputs are as follows.

Input	Major Body, Minor Body and Distance Between them
Output	Lagrangian points polar coordinates and Graph showing them

Table 11: I/O for Lagrangian Points

## 3 Database Management System

#### 3.1 Introduction

Database is a collection of set of related data or information of any particular concept, generally stored using any electronic gadget . Database Management system is a system which uses integrated software to connect frontend user to connect to the database to access , modify and manage the data stored in it. There are two types of Databases:

- 1. Relational Database Organizes data into one or more table. each table comprising of number of rows and columns with each row identifiable with unique key.
- 2. Non Relational database Organizes data in any form other than table. Such as graphs, flexible tables, documents etc.

In this project we have used Relational database management system with structured Query Language (SQL) to interact with the RDBMS. SQLite is the database engine used to run SQL query to perform CRUD (Create, Retrieve, Update or Delete) operation in the database.

This database contains the data of planetary bodies such as Mass, radius, density, gravity, temperature, orbital parameters, number of moons etc., of all planets of our solar system.

## 4 Conclusion

The outcome of the project is the lessons we learnt during the project. Communication is the key for collaborative work. This is one of the main aspect that we learned during this project. The other aspects that we were able to learn are:

- 1. Project Management
- 2. Time Management
- 3. Prioritize the list that is at hand based on various parameters

## **5** Future Scope

MOPy is a open source application with GNU - GPL v3 License, with this anyone who is interested in using this application can freely download and use it, and even modify the contents to their requirements. If they wish to contribute to this application they can fork the repository on GitHub[3] and add their contribution by sending a pull request. The reason GNU-GPL v3 license is used is that we aim to keep a quality control to the features that gets added to the application. We are always open to contributors.

There is a list of features with corresponding priorities that are planned to be added down the line. This will be constantly updated indefinitely. And if the user is not able to add a feature then they can request a feature that would be added to the list with a appropriate priority. There is discord server in which anyone can join and hold discussions with other participants. Contributors can hold discussions about the feature they are planning to add, others can discuss about the concepts and request features to be added.

As of now this runs on Windows only. This could be made to run on other platforms and even as a web application which would negate the need of a moderately powerful hardware. The database could be expanded with much more data than present.

This entire code can be converted into a library that anyone can download from PyPI. This would enable the user to utilize the features directly from the command line or their python projects. This would simplify their projects.

## A Code for the Features

#### **A.1** Calculation Of Orbital Elements

```
from numpy.linalg import norm
<sup>2</sup> from numpy import dot, pi, cross, multiply as multi
 from math import acos
5 class Calculate:
      I = [1, 0, 0]
      J = [0, 1, 0]
      K = [0, 0, 1]
      G = 6.67e-20 #units are in km3 kg-1 s-2
      @classmethod
11
      def muvalue(cls, major_body):
          major_body_list = pandas.read_csv("Major_and_Minor_Bodies.csv")
13
          major_bodies = list(major_body_list.Major_Body)
          major_bodies_mass = list(major_body_list.Mass)
          major_bodies_radius = list(major_body_list.Radius)
16
          sel_major_body = major_bodies.index(major_body)
          major_body_mass = major_bodies_mass[sel_major_body]
18
          major_body_radius = major_bodies_radius[sel_major_body]
19
          mu = cls.G * major_body_mass
20
21
          return [mu, major_body_radius]
22
      @classmethod
23
      def correct_ohm(cls, ohm, n_vec):
24
          if n_vec[0] > 0 and n_vec[1] > 0:
25
               print("This is a Prograde Elliptical Orbit and is in first Quadrant.")
26
              if ohm >90:
27
                   ohm -= 360
28
          elif n_{vec}[0] < 0 and n_{vec}[1] > 0:
29
               print("This is a Retrograde Elliptical Orbit and is in second Quadrant."
30
     )
               if ohm > 180:
31
                   ohm -= 360
32
          elif n_{vec}[0] < 0 and n_{vec}[1] < 0:
33
               print("This is a Retrograde Elliptical Orbit and is in Third Quadrant.")
34
               if ohm < 180:
35
                   ohm -= 360
          elif n_vec[0] > 0 and n_vec[1] < 0:</pre>
               print("This is a Prograde Elliptical Orbit and is in fourth Quadrant.")
               if ohm < 90:
39
                   ohm -= 360
40
          return ohm
41
42
      @classmethod
43
      def other_var(cls, pos_vec, vel_vec):
44
          h_vec = cross(pos_vec, vel_vec)
45
          n_vec = cross(cls.K,h_vec)
46
          return [h_vec, n_vec]
47
48
      @classmethod
49
      def OE(cls, pos_vec, vel_vec, mu):
50
```

```
[h_vec, n_vec] = Calculate.other_var(pos_vec, vel_vec)
51
          e_vec = (multi((norm(vel_vec)*norm(vel_vec)-(mu/norm(pos_vec))),pos_vec)-
52
     multi(dot(pos_vec,vel_vec),vel_vec))/(mu)
          call.ecc_o.setText(str(norm(e_vec)))
53
          inc = (acos((dot(h_vec, cls.K))/norm(h_vec))) * 180/pi
54
          call.inc_o.setText(str(inc))
55
          sma = 1/((2/norm(pos_vec))-((norm(vel_vec)*norm(vel_vec))/mu))
          call.sma_o.setText(str(sma))
57
          return [sma, inc, e_vec]
58
      @classmethod
      def ACOE(cls, pos_vec, vel_vec, e_vec, inc):
61
          [h_vec, n_vec] = Calculate.other_var(pos_vec, vel_vec)
62
          if inc != 0 or 180 and norm(e_vec) > 0: #Nothing is Zero/180
63
              ohm = (acos((dot(cls.I,n_vec))/norm(n_vec)))
              ohm = Calculate.correct_ohm(ohm, n_vec)
              call.ohm_o.setText(str(ohm))
              nu = (acos((dot(e_vec,pos_vec))/(norm(e_vec)*norm(pos_vec))))
              call.nu_u_o.setText(str(nu))
68
              omega = (acos((dot(n_vec,e_vec))/multi(norm(n_vec),norm(e_vec))))
69
              call.omega_l_o.setText(str(omega))
70
              return [ohm, omega, nu]
          elif inc == 0 or 180: #Inclination is Zero
              if norm(e_vec) > 0: #Elliptical Orbit
                  nu = (acos((dot(e_vec,pos_vec))/(norm(e_vec)*norm(pos_vec))))
                  call.nu_u_o.setText(str(nu))
                  Long_of_peri_pi = acos(dot(cls.I,e_vec)/(norm(cls.I)*norm(e_vec)))
76
                  return [Long_of_peri_pi, nu]
              elif norm(e_vec) == 0: #Circular Orbit
                  Tr_long_l = acos(dot(cls.I,pos_vec)/(norm(pos_vec)*norm(cls.I)))
                  return [Tr_long_1]
80
          elif norm(e_vec) == 0: #Circular orbit with inclination non-zero/pi
81
              Arg_of_lattitude_u = acos(dot(n_vec,pos_vec)/(norm(n_vec)*norm(pos_vec))
              return [Arg_of_lattitude_u]
83
84
      @classmethod
85
      def possibility(cls, major_body, pos_vec, vel_vec):
86
          [mu, major_body_radius] = Calculate.muvalue(major_body)
87
          pos = norm(pos_vec)
          vel = norm(vel_vec)
89
          sma = 1/((2/pos)-(vel*vel/mu))
90
          e_vec = (multi((norm(vel_vec)*norm(vel_vec)-(mu/norm(pos_vec))),pos_vec)-
91
     multi(dot(pos_vec,vel_vec),vel_vec))/(mu)
          r_peri = sma*(1-norm(e_vec))
92
          if r_peri <= major_body_radius:</pre>
93
              print("The Orbit is not possible as radius of perigee is less than
94
     radius of the major Body")
              return False
95
          return True
```

Listing 1: CoOE.py

## A.2 Euler Angles

```
from math import *
2 from numpy import *
 class EA():
      def RxRyRz(pitch_theta, roll_phi, yaw_si):
          Rx = matrix([[ 1, 0, 0],
                           [ 0, cos(roll_phi), sin(roll_phi)],
                           [ 0,-sin(roll_phi), cos(roll_phi)]])
          Ry = matrix([[ cos(pitch_theta), 0,-sin(pitch_theta)],
                           [ 0 ,1, 0],
                           [sin(pitch_theta), 0, cos(pitch_theta)]])
          Rz = matrix([[ cos(yaw_si), sin(yaw_si), 0 ],
                           [-sin(yaw_si), cos(yaw_si), 0],
16
17
                           [0, 0, 1]
          return [Rx, Ry, Rz]
18
19
      def DCMtoEA(DCM, order):
20
21
          if order=='321':
               theta=-asin(DCM[0][2])
              phi=atan(DCM[1][2]/DCM[2][2])
              si=atan(DCM[0][1]/DCM[0][0])
24
25
          elif order=='123':
              theta=asin(DCM[2][0])
26
              phi=atan(DCM[2][1]/DCM[2][2])
              si=atan(DCM[1][0]/DCM[0][0])
          elif order=='132':
29
              theta=atan(DCM[2][0]/DCM[0][0])
30
31
              phi=atan(DCM[1][2]/DCM[1][1])
32
              si=-asin(DCM[1][0])
          elif order=='312':
              theta=atan(DCM[0][2]/DCM[2][2])
              phi=asin(DCM[1][2])
              si=atan(DCM[1][0]/DCM[1][1])
36
          elif order=='213':
37
              theta=atan(DCM[2][0]/DCM[2][2])
38
              phi=-asin(DCM[2][1])
              si=atan(DCM[0][1]/DCM[1][1])
40
          elif order=='231':
41
              theta=atan(DCM[0][2]/DCM[0][0])
42
              phi=atan(DCM[2][1]/DCM[1][1])
43
              si=asin(DCM[0][1])
44
          return [theta, si, phi]
45
46
47
      def EAtoDCM(theta, si, phi, order):
          [Rx, Ry, Rz] = EA.RxRyRz(theta, si, phi)
48
          if order=='321':
49
              RxRy = dot(Rx,Ry)
              return (dot(RxRy,Rz))
51
          elif order == '123':
52
53
              x = Rx(phi*pi/180)
              y = Ry(theta*pi/180)
              z = Rz(si*pi/180)
```

```
zy = dot(z,y)
               return (dot(zy,x))
57
          elif order == '213':
58
               x = Rx(phi*pi/180)
59
               y = Ry(theta*pi/180)
60
               z = Rz(si*pi/180)
61
               zx = dot(z,x)
62
               return (dot(zx,y))
63
          elif order == '312':
64
               x = Rx(phi*pi/180)
               y = Ry(theta*pi/180)
               z = Rz(si*pi/180)
67
               yx = dot(y,x)
68
69
               return (dot(yx,z))
70
          elif order == '132':
               x = Rx(phi*pi/180)
               y = Ry(theta*pi/180)
72
73
               z = Rz(si*pi/180)
74
               yz = dot(y,z)
               return (dot(yz,x))
75
          elif order == '231':
76
77
              x = Rx(phi*pi/180)
               y = Ry(theta*pi/180)
78
               z = Rz(si*pi/180)
79
               xz = dot(x,z)
80
               return (dot(xz,y))
81
82
               return ('No transformation matrix')
83
85 order = '321' #input("Enter the order:")
^{86} DCM = [[0.6405, 0.75319, -0.15038], [0.76736, -0.63531, 0.086824], [-0.030154,
      -0.17101, -0.98481]]
87 print(EA.DCMtoEA(DCM,order))
89 print(EA.EAtoDCM(8.6489 * 180/pi, 49.619 * 180/pi, -5.039 * 180/pi, order))
```

Listing 2: EA.py

## A.3 Sphere of Influence

```
from math import *
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
import sqlite3

def SoI(MiB_mass, MiB_radius, r_maj_to_min):
    MaB_mass = 1.989e30
    rSOI = (r_maj_to_min*(MiB_mass/MaB_mass)**(2/5))
    return [rSOI, rSOI/MiB_radius]
```

Listing 3: SoI

## A.4 Calculation of Julian Day

```
from math import *
class JulianDay():
     @classmethod
     def tb_method(cls,year, month, day, hour, minutes, seconds, accuracy):
         if 1901 <= year <= 2099:</pre>
             JDN = 367 * year + int((7 * (year + int((month + 9)/12)))/4) + int(275 *
     month/9) + day + 1721013.5
             UT = hour + round((minutes/60), accuracy) + round((seconds/3600),
     accuracy)
             JD = JDN + UT/24
             return [JDN, JD]
10
         else:
             #manju you can set limits when this option is selected between 1901 and
     2099
             print("Not Possible from this method")
14
     @classmethod
15
     def julian_day(cls,year, month, day, hour, minutes, seconds, accuracy,
16
     type_of_calender):
         if type_of_calender == "Gregorian":
             #julian day number from Gregorian calender date
18
             JDN = int((1461 * (year + 4800 + (month - 14)/12))/4) + int((367 * month))
19
      (100)(4) + day - 32075
         elif type_of_calender == "Julian":
20
             #julian day number from julian calender date
21
             JDN = 367 * year - int((7 * (year + 5001 + (month - 9)/7))/4) + int((275))
      * month)/9) + day + 1729777
         #JDN to JD
         JD = JDN + round(((hour - 12)/24),accuracy) + round((minutes/1440), accuracy
24
     ) + round((seconds/86400), accuracy)
         return [JDN, round(JD, accuracy)]
```

Listing 4: CJSD.py

#### A.5 Calculation of Various Parameters of the Orbit

```
# all the units should be km
17 class CalculateCircularElliptical:
      I = [1, 0, 0]
18
      J = [0, 1, 0]
19
      K = [0, 0, 1]
20
      G = 6.67e-20 #units are in km3 kg-1 s-2
21
      def __init__(self, major_body):
          self.major_body = major_body
24
          return
      @classmethod
27
      def semiecc(cls, sma, mag_e, major_body):
28
          r_per = sma * (1 - mag_e)
29
30
          r_{apo} = sma * (1 + mag_e)
          [mean_motion, T_period, mag_h, sme, slr] = CalculateCircularElliptical.
31
     orb_const(r_per, sma, mag_e, major_body)
32
          return [r_per, r_apo, mean_motion, T_period, mag_h, sme, slr]
33
      @classmethod
34
      def perapo(cls, r_per, r_apo, major_body):
35
          sma = (r_per + r_apo)/2
36
37
          mag_e = (r_apo - r_per)/(r_apo + r_per)
          [mean_motion, T_period, mag_h, sme, slr] = CalculateCircularElliptical.
38
     orb_const(r_per, sma, mag_e, major_body)
          return [mag_e, sma, mean_motion, T_period, mag_h, sme, slr]
39
40
      @classmethod
41
      def orb_const(cls, r_per, sma, mag_e, major_body):
42
          major_body_mass = 5.972e24 #self.major_body * 1
43
          mu = cls.G * major_body_mass
44
          slr = sma*(1-mag_e**2)
45
          mag_h = (r_per*(1+e)*mu)**0.5
          T_{period} = sqrt(((4*pi**2)/mu)*sma**3)
47
          mean_motion = T_period/(2*pi)
48
          sme = -mu/(2* sma)
49
          return [mean_motion, T_period, mag_h, sme, slr]
50
51
      @classmethod
52
      def time_since_periapsis(cls, mag_e, theta, T_period):
53
          E_{anomly} = 2 * atan((sqrt((1 - mag_e)/(1 + mag_e))) * tan(theta/2)))
54
          M_anomly = E_anomly - mag_e * sin(E_anomly)
55
          t_since_perigee = T_period * M_anomly/(2*pi)
56
          return t_since_perigee
57
58
      @classmethod
59
      def velocity_at_any_point(cls, sma, r, major_body):
60
          major_body_mass = major_body * 1
61
          mu = cls.G * major_body_mass
62
          v_{point} = sqrt(((2 * mu)/r) - (mu/sma))
63
          return v_point
65
66 class CalculateParabola():
      I = [1, 0, 0]
67
      J = [0, 1, 0]
      K = [0, 0, 1]
69
   G = 6.67e-20 #units are in km3 kg-1 s-2
```

```
72
      @classmethod
      def const_values(cls, r_per, major_body):
73
           major_body_mass = major_body * 1
74
           mu = major_body_mass * cls.G
75
           slr = 2 * r_per
76
           v_{per} = sqrt((2*mu)/r_{per})
77
           mag_h = sqrt(mu*r_per * 2)
78
           return [slr, v_per, mag_h]
79
80
      @classmethod
      def velocity_at_any_point(cls, r, major_body):
82
           major_body_mass = major_body * 1
83
          mu = major_body_mass * cls.G
84
85
          v = sqrt((2*mu)/r)
          return v
86
87
  class CalculateHyperBola():
      I = [1, 0, 0]
89
      J = [0, 1, 0]
90
      K = [0, 0, 1]
91
      G = 6.67e-20 #units are in km3 kg-1 s-2
92
93
      @classmethod
94
      def const_values(cls,major_body,mag_e, sma):
           mu = cls.G * major_body
96
           theta_inf = acos(1/mag_e) #angle between asympotes
97
           beta = theta_inf
98
           delta = 2 * sin(1/mag_e) #turn angle
           mag_h = sqrt(sma * mu * (mag_e**2-1)) #specific angular momentum
100
           b = sma * mag_e * sin(theta_inf) #semi minor axis
101
          Delta = b #aiming radius
102
           v_inf = mu * mag_e*sin(theta_inf)/mag_h #velocity at r = infinity
103
           sme = mu/(2 * sma) #specific mechanical energy
104
           slr = -b**2/sma #semi latus rectum
105
           return [theta_inf, beta, delta, mag_h, b, Delta, v_inf, sme, slr]
106
107
      @classmethod
108
      def semiecc(cls,major_body,sma,mag_e):
109
           mu = cls.G * major_body
110
           [theta_inf, beta, delta, mag_h, b, Delta, v_inf, sme, slr] =
      CalculateHyperBola.const_values(major_body, sma, mag_e)
           r_{apo} = (mag_h**2/mu)/(1 - mag_e)
           r_{per} = (mag_h**2/mu)/(1 + mag_e)
           return [theta_inf, beta, delta, mag_h, b, Delta, v_inf, sme, slr, r_apo,
114
      r_per]
```

Listing 5: VPCO

## A.6 Sensitivity Analysis

```
class SA(Major_Body,R1_bod):
    def __init__(self):
        G = 6.67e-20
        mu_Major_Body = G * self.R1_bod * 1
        mu_R1 = G * self.R2_bod * 1

def SA(self, R1, R2):
        a = 2/(1-(R1*Vdv**2)/(2*self.mu_Major_Body))
        coeff_del_Rp_Rp = a * (self.mu_R1/(Vdv*Vi*Rp))
        coeff_del_Vp_Vp = a * ((Vi+(2*self.mu_R1/(Rp*Vi)))/Vdv)
        del_R2_R2 = coeff_del_Rp_Rp*(del_Rp_Rp) + coeff_del_Vp_Vp * (del_Vp_Vp)
        return [del_R2_R2]
```

Listing 6: SA.py

## A.7 Lagrangian Points

```
1 from math import pi
from numpy import arange
3 import matplotlib.pyplot as plt
4 from scipy.optimize import root_scalar
6 G = 6.67408e - 11
7 \text{ m1} = 5.972 \text{ e24}
m2 = 0.07346e24
9 1 = 384400000
10 \times 1 = m2 * 1 / (m1 + m2)
x2 = m1 * 1 / (m1 + m2)
velocity = (G * (m1 + m2)/ 1) ** 0.5
period = 2 * pi * 1 / velocity
theta_dot = 2*pi / period
16 def x_eqn(xs):
     return -G*m1/((xs + x1) * abs(xs + x1)) - G * m2 / ((xs - x2)*abs(xs - x2)) + \
               theta_dot**2 * xs
18
19
21 \text{ xvals} = \text{arange}(-2*1, 2*1, 1000)
yvals = x_eqn(xvals)
24 L1 = root_scalar(x_eqn, bracket=[2e8, 3.5e8])
25 print(L1.root+x1)
26 L2 = root_scalar(x_eqn, bracket=[3.9e8, 5e8])
27 print(L2.root+x1)
28 L3 = root_scalar(x_eqn, bracket=[-4e8, -2e8])
29 print(L3.root+x1)
plt.plot(xvals, yvals)
32 plt.grid()
33 plt.ylim(-0.01, 0.01)
34 plt.show()
```

Listing 7: LP.py

## **A.8 CRUD File Operations**

```
# import sqlite in ide
2 import sqlite3
4 # Create a database or connect to one
5 conn= sqlite3.connect('appdatabase.db')
7 # Create a Cursor
8 c= conn.cursor()
10 # Creat a table
c.execute(""" CREATE TABLE table_name(
         column_name datatype,
         column_name datatype
13
     )""")
14
15
# Insert data into table
19
20 c.executemany( "INSERT INTO table_name VALUES(?,?)",x)
21
22 #Retrieve or read data
23 c.execute("SELECT * FROM table_name")
24 print(c.fetchall())
26 # commit data to the database
27 conn.commit()
```

Listing 8: db.py

# A Database:

	Mercury	Venus	Earth	Moon	Mars	Jupiter	Saturn	Uranus	Neptune	Pluto
Mass $(10^{24}kg)$	0.330	4.87	5.97	0.073	0.642	1898	568	8.98	102	0.0146
Diameter(km)	4879	12,104	12,756	3475	6792	142,984	120,536	51,118	49,528	2370
<b>Density</b> $(kg/m^3)$	5427	5243	5514	3340	3933	1326	289	1271	1638	2095
<b>Gravity</b> $(m/s^2)$	3.7	8.9	8.6	1.6	3.7	23.1	0.6	8.7	11.0	0.7
Escape Velocity $(km/s)$	4.3	10.4	11.2	2.4	5.0	59.5	35.5	21.3	23.5	1.3
<b>Rotation Period</b> (hours)	1407.6	-5832.5	23.9	655.7	24.6	6.6	10.7	-17.2	16.1	-153.3
Length of Day(hours)	4222.6	2802.0	24.0	708.7	24.7	6.6	10.7	17.2	16.1	153.3
<b>Distance from Sun</b> ( $10^6 km$ )	57.9	108.2	149.6	0.384	227.9	9.877	1433.5	2872.5	4495.1	5906.4
<b>Perihelion</b> ( $10^6 km$ )	46.0	107.5	147.1	0.363	206.6	740.5	1352.6	2741.3	4444.5	4436.8
Apohelion	8.69	108.9	152.1	0.406	249.2	816.6	1514.5	3003.6	4545.7	7375.9
<b>Orbital Period</b> (days)	88.0	224.7	365.2	27.3	0.789	4331	10,747	30,589	59,800	90,560
<b>Orbital Velocity</b> $(km/s)$	47.4	35.0	29.8	1.0*	24.1	13.1	6.7	8.9	5.4	4.7
<b>Orbital Inclination</b> (degrees)	7.0	3.4	0.0	5.1	1.9	1.3	2.5	8.0	1.8	17.2
Orbital Eccentricity(e)	0.205	0.007	0.017	0.055	0.094	0.049	0.057	0.046	0.011	0.244
Obliquity to Orbit	0.034	177.4	23.4	6.7	25.2	3.1	26.7	8.76	28.3	122.5
Mean Temperature( ${}^{o}C$ )	167	464	15	-20	-65	-110	-140	-195	-200	-225
Surface Pressure(bars)	0	92	1	0	0.01	Unknown	Unknown	Unknown	Unknown	0.00001
Number of Moons	0	0	П	0	2	79	82	27	14	5
Global Magnetic Field	Yes	No	Yes	No	No	Yes	Yes	Yes	Yes	Unknown

Table 12: Planetary Details

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