

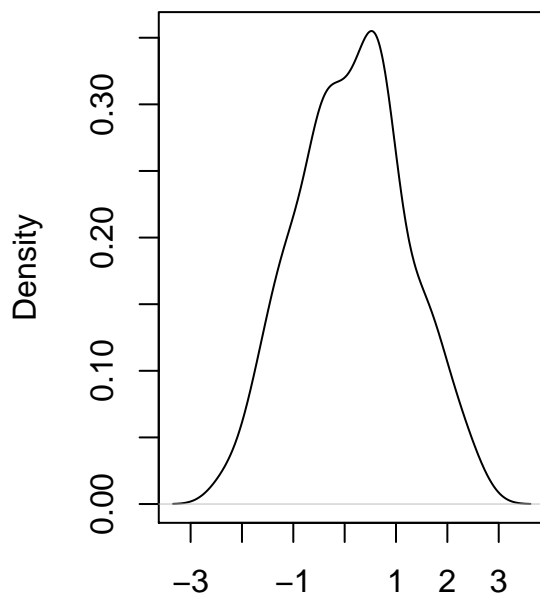
2352-Statistical Computing Assignment

Simulating the Central Limit Theorem

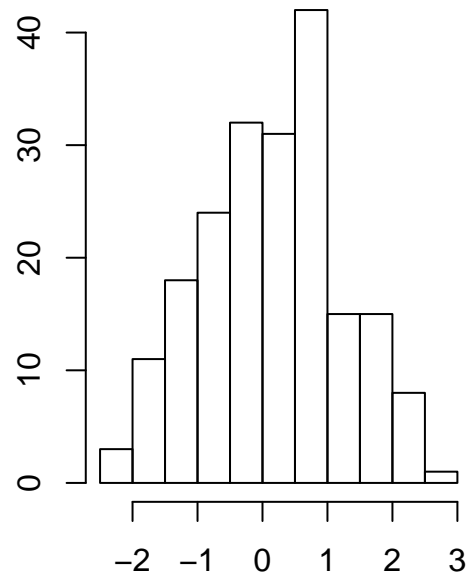
We can sample from a variety of distributions in R. To sample from a normal distribution we would use **rnorm**. `rnorm()` takes in parameters of the distribution: `n` (the number of observations), `mean` (the mean of the sample), and `sd` (the standard deviation) to randomly draw from the distribution. The example below creates a sample of size = 200 with mean = 0 and standard deviation = 1.

```
# Set seed allows for reproducible results and for the document to produce  
# the exact sample numbers and samples  
set.seed(12345)  
  
# A sample of 200 observations from a normal distribution with mean = 0 and  
# sd = 1.  
dat1 <- rnorm(200, 0, 1)  
  
# We can visualize our data using the R functions plot(), density(), and  
# hist()  
par(mfrow = c(1, 2)) #This creates matrix of m rows by n columns to be able to plot more than one plot  
plot(density(dat1), main = "Density Plot of random sample", cex.main = 0.8) # Creates a density plot of  
hist(dat1, main = "Histogram of random sample", ylab = "", xlab = "", cex.main = 0.8) # Creates a hist
```

Density Plot of random sample



Histogram of random sample



N = 200 Bandwidth = 0.3204

```
# Draw 20 observations and take the mean of the draw  
  
N <- 20 # Storing the number of observations  
draw1 <- sample(dat1, N) # Randomly drawing from the above simulated data N number of times and storing  
mean(draw1) # Computes the mean of the draw
```

```
## [1] 0.3039873
```

```
var(draw1)/sqrt(1) #
```

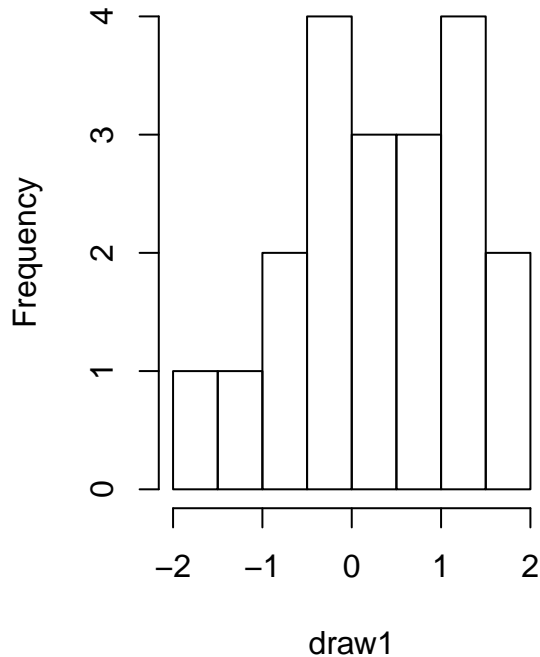
```
## [1] 1.006714
```

```
par(mfrow = c(1, 2))
```

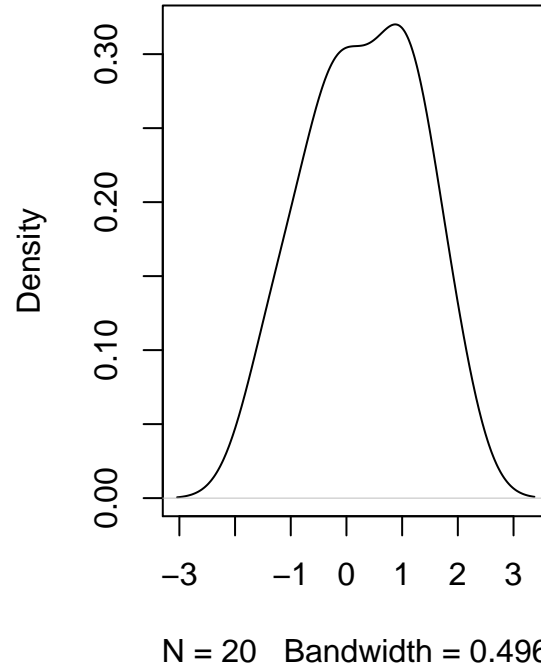
```
hist(draw1) # Plots a histogram of the draw
```

```
plot(density(draw1)) # Creates a density plot of the draw
```

Histogram of draw1



density.default(x = draw1)



Now let's create a sampling distribution of the mean of size 50.

```
N <- 20 # Set the size of sample
```

```
ITER <- 50 # Set the number of iterations
```

```
# Create empty vector of length ITER to store results
```

```
draw_mean1 <- rep(NA, length = ITER)
```

```
# Creates a loop to draw 20 observations from the original sample (dat1),  
# takes the mean of the 20 observations, and stores the mean and iterates  
# over the loop ITER times (in this case 50 times)
```

```
for (i in 1:ITER) {  
  draw_mean1[i] <- mean(sample(dat1, N))  
}
```

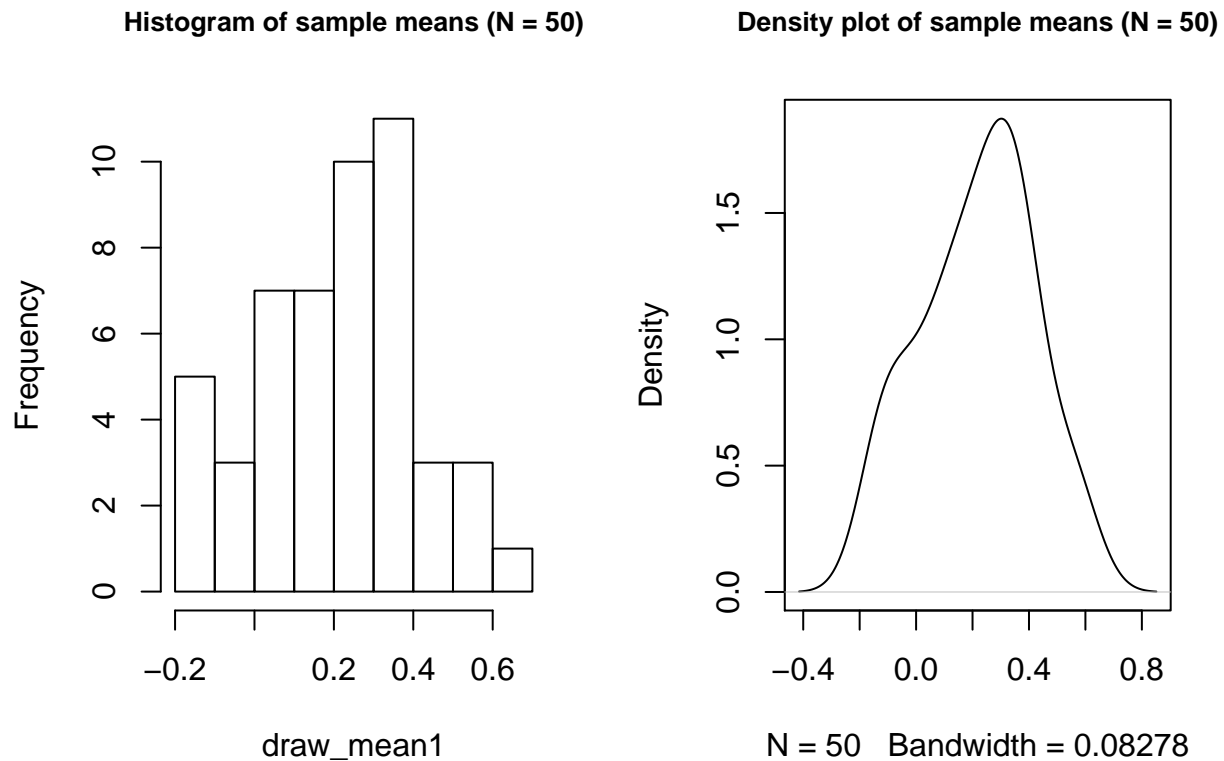
```
mean(draw_mean1)
```

```
## [1] 0.2171342
```

```
par(mfrow = c(1, 2))
```

```
hist(draw_mean1, main = "Histogram of sample means (N = 50)", cex.main = 0.8) # Plots a histogram of t
```

```
plot(density(draw_mean1), main = "Density plot of sample means (N = 50)", cex.main = 0.8) # Creates a
```



Next we can increase the number of iterations to 100, 1000, and 4000 and see what happens to the sampling distribution as we increase the number of iterations.

```
N <- 20 # Set the size of sample
ITER <- 100 # Set the number of iterations

# Create empty vector of length ITER to store results
draw_mean2 <- rep(NA, length = ITER)

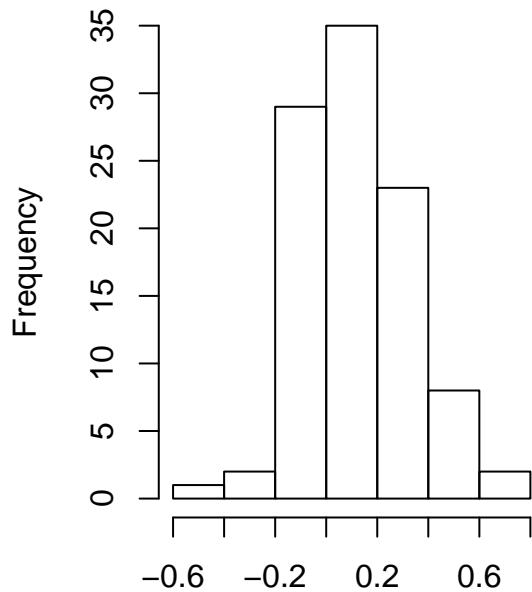
# Creates a loop to draw 20 observations from the original sample (dat1),
# takes the mean of the 20 observations, and stores the mean and iterates
# over the loop ITER times (in this case 100 times)
for (i in 1:ITER) {
  draw_mean2[i] <- mean(sample(dat1, N))
}

mean(draw_mean2)

## [1] 0.1198831

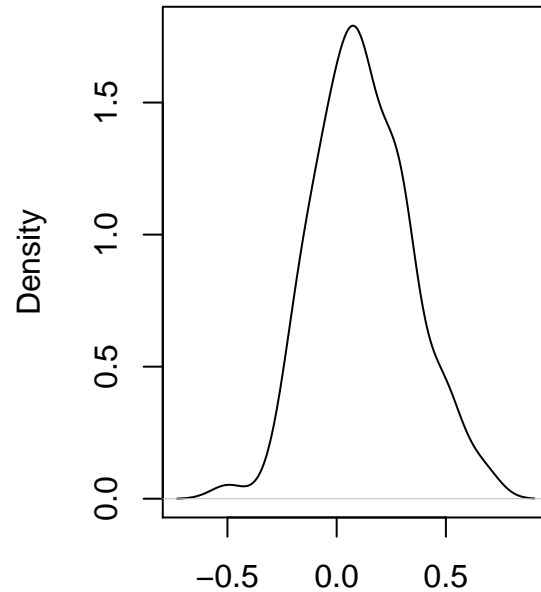
par(mfrow = c(1, 2))
hist(draw_mean2, main = "Histogram of sample means (N = 100)", cex.main = 0.8) # Plots a histogram of
plot(density(draw_mean2), main = "Density plot of sample means (N = 100)", cex.main = 0.8) # Creates a
```

Histogram of sample means (N = 100)



draw_mean2

Density plot of sample means (N = 100)



N = 100 Bandwidth = 0.07763

```
N <- 20 # Set the size of sample
ITER <- 1000 # Set the number of iterations

# Create empty vector of length ITER to store results
draw_mean3 <- rep(NA, length = ITER)

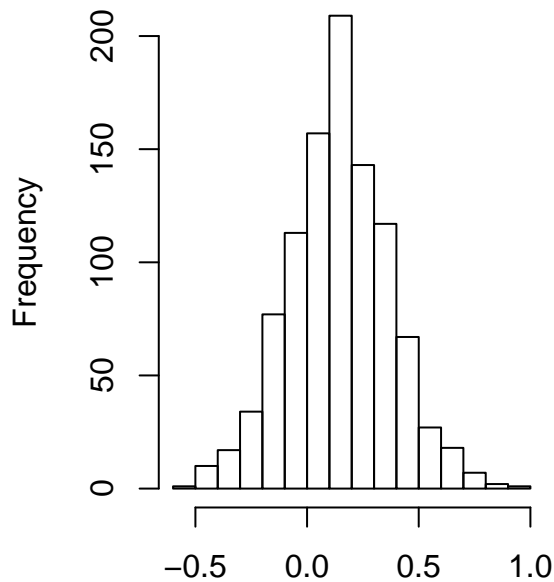
# Creates a loop to draw 20 observations from the original sample (dat1),
# takes the mean of the 20 observations, and stores the mean and iterates
# over the loop ITER times (in this case 1000 times)
for (i in 1:ITER) {
  draw_mean3[i] <- mean(sample(dat1, N))
}

mean(draw_mean3)

## [1] 0.1424135

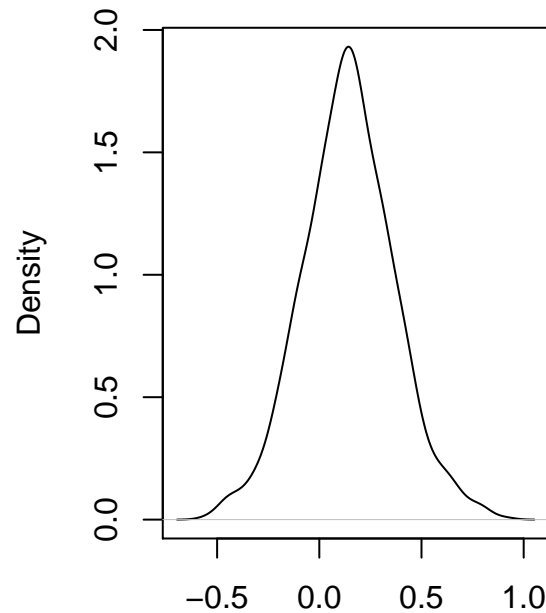
par(mfrow = c(1, 2))
hist(draw_mean3, main = "Histogram of sample means (N = 1000)", cex.main = 0.8) # Plots a histogram of
plot(density(draw_mean3), main = "Density plot of sample means (N = 1000)",
     cex.main = 0.8) # Creates a density plot of the sample means
```

Histogram of sample means (N = 1000)



draw_mean3

Density plot of sample means (N = 1000)



N = 1000 Bandwidth = 0.04866

```
N <- 20 # Set the size of sample
ITER <- 4000 # Set the number of iterations

# Create empty vector of length ITER to store results
draw_mean4 <- rep(NA, length = ITER)

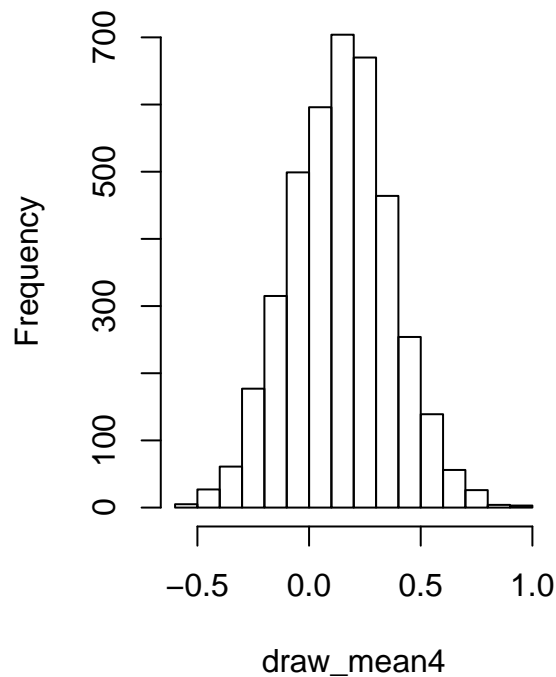
# Creates a loop to draw 20 observations from the original sample (dat1),
# takes the mean of the 20 observations, and stores the mean and iterates
# over the loop ITER times (in this case 4000 times)
for (i in 1:ITER) {
  draw_mean4[i] <- mean(sample(dat1, N))
}

mean(draw_mean4)

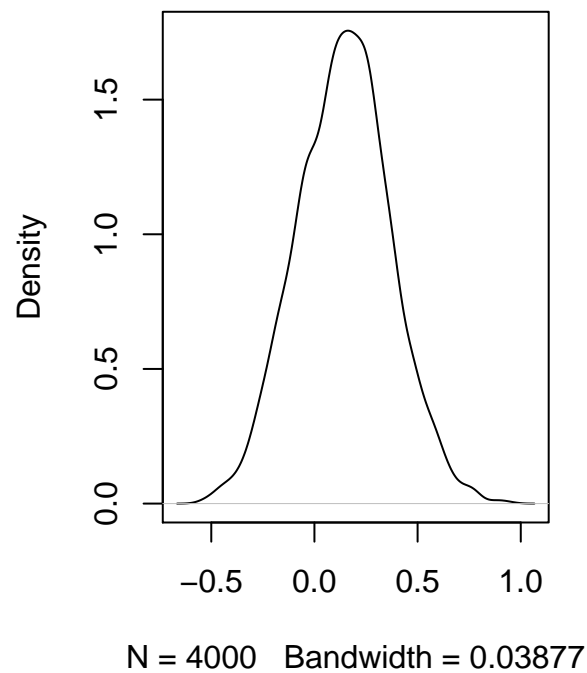
## [1] 0.1422502

par(mfrow = c(1, 2))
hist(draw_mean4, main = "Histogram of sample means (N = 4000)", cex.main = 0.8) # Plots a histogram of
plot(density(draw_mean4), main = "Density plot of sample means (N = 4000)",
     cex.main = 0.8) # Creates a density plot of the sample means
```

Histogram of sample means (N = 4000)



Density plot of sample means (N = 4000)



```
par(mfrows=c(2,2))
```

```
## Warning in par(mfrows = c(2, 2)): "mfrows" is not a graphical parameter
```

The Central Limit Theorem

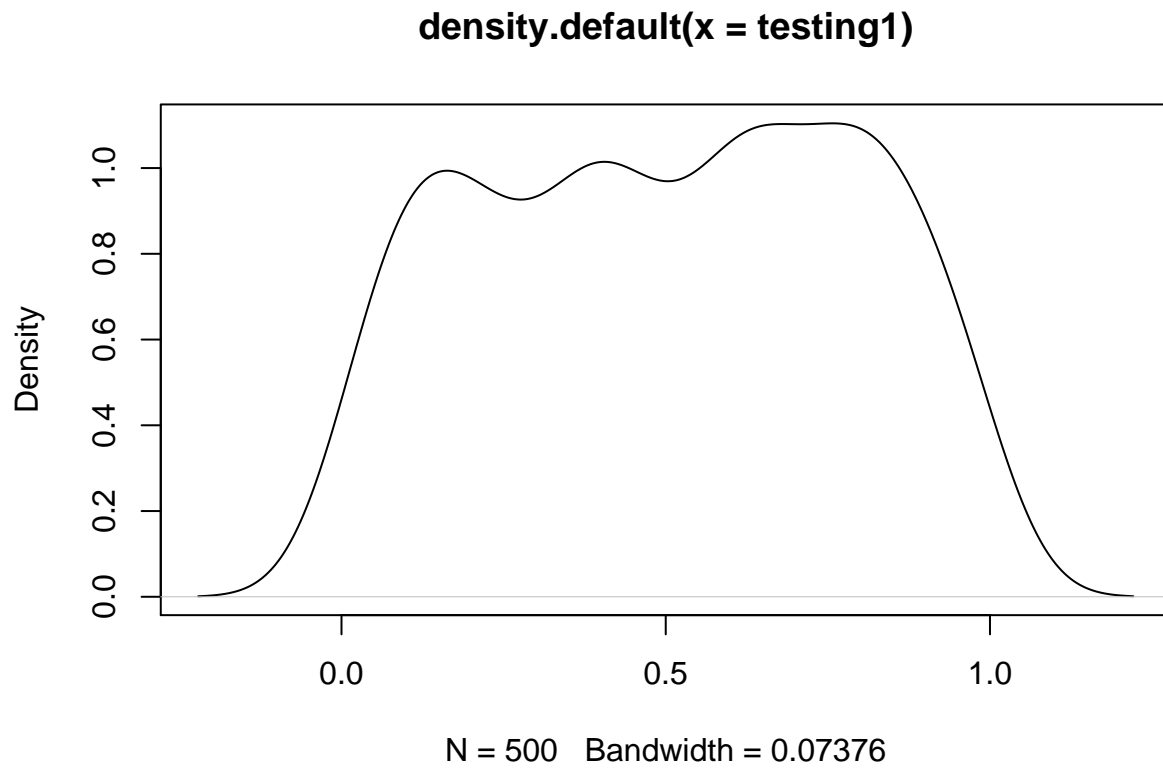
The **central limit theorem** states that given a population with mean of μ and a standard deviation of σ , the sampling distribution of the mean has a mean of μ and a standard deviation of $\frac{\sigma}{\sqrt{N}}$ and approaches a normal distribution as the sample size on which it is based, N , approaches infinity.

1. The mean of the sampling distribution of the mean

*** Describe what a uniform distribution is!!!!**** For a uniform distribution, the probability density function,

1. Sample from a uniform distribution (use runif) and store your sample.

```
testing1 <- runif(500, 0, 1)
plot(density(testing1))
```



2. Create a sampling distribution of the mean with 20, 100, 1000, and 4000 thousand draws