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Assignnment-1

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Abstract—This document explain the concept of projection of vector by solving a problem.

Download all python codes from

https://github.com/vipulmalik8569/MT-EE5609

and latex-tikz codes from

https://github.com/vipulmalik8569/MT-EE5609

1 Problem

Find the projection of vector $\begin{pmatrix} 1\\3\\7 \end{pmatrix}$ on vector $\begin{pmatrix} 7\\-1\\8 \end{pmatrix}$

2 EXPLANATION

Projection of \mathbf{u} onto \mathbf{v} means the component of \mathbf{u} in the direction of \mathbf{v} .

This is given by the formula:

$$\mathbf{p} = \left(\frac{\mathbf{u}^T \mathbf{v}}{\|\mathbf{v}\|^2}\right) \mathbf{v} \tag{2.0.1}$$

where

$$\mathbf{u}^{T}\mathbf{v} = u_{1}v_{1} + u_{2}v_{2} + \dots + u_{n}v_{n}$$
 (2.0.2)

and

$$\|\mathbf{v}\| = \sqrt{v_1^2 + v_2^2 + \dots + v_n^2}$$
 (2.0.3)

3 Solution

We have,

$$\mathbf{u} = \begin{pmatrix} 1 \\ 3 \\ 7 \end{pmatrix}, \mathbf{v} = \begin{pmatrix} 7 \\ -1 \\ 8 \end{pmatrix}$$

Using equation (2.0.1)

$$\mathbf{p} = \begin{bmatrix} \begin{pmatrix} 1 \\ 3 \\ 7 \end{pmatrix}^T \begin{pmatrix} 7 \\ -1 \\ 8 \end{pmatrix} \\ \begin{bmatrix} 7 \\ -1 \\ 8 \end{bmatrix}^2 \end{bmatrix} \begin{pmatrix} 7 \\ -1 \\ 8 \end{pmatrix}$$
 (3.0.1)

$$\mathbf{p} = \left[\frac{(7-3+56)}{\left(\sqrt{7^2 + (-1)^2 + 8^2}\right)^2} \right] \begin{pmatrix} 7\\ -1\\ 8 \end{pmatrix}$$
 (3.0.2)

$$\mathbf{p} = \frac{13}{25} \begin{pmatrix} 7 \\ -1 \\ 8 \end{pmatrix} = \begin{pmatrix} \frac{92}{25} \\ -\frac{13}{25} \\ \frac{21}{5} \end{pmatrix}$$
 (3.0.3)

Hence the projection of \mathbf{u} on \mathbf{v} is

$$\mathbf{p} = \begin{pmatrix} \frac{92}{25} \\ -\frac{13}{25} \\ \frac{21}{5} \end{pmatrix}$$