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EE5609 Assignment 3

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Abstract—This assignment involves solving a system of equations using matrix method

The python solution code for this problem can be downloaded from

https://github.com/vimalkb007/EE5609/blob/master/Assignment_3/codes/assignment3_solution.py

The python verification code for this problem can be downloaded from

https://github.com/vimalkb007/EE5609/blob/master/Assignment_3/codes/assignment3_solution_verify.py

1 PROBLEM STATEMENT

Solve the system of linear equatios, using matrix method.

$$2x - y = -2 \tag{1.0.1}$$

$$3x + 4y = 3 \tag{1.0.2}$$

2 THEORY

Given a set of linear equations we can use Guass Jordan Elimination method in order to find the the unknown variables.

3 Solution

Given 1.0.1 can be repsented in a matrix form as:

$$\begin{pmatrix} 2 & -1 \\ 3 & 4 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} -2 \\ 3 \end{pmatrix} \tag{3.0.1}$$

The corresponding augmented matrix is

$$\begin{pmatrix} 2 & -1 & | & -2 \\ 3 & 4 & | & 3 \end{pmatrix} \tag{3.0.2}$$

We use the Guass Jordan Elimination method as:

$$\begin{pmatrix} 2 & -1 & | & -2 \\ 3 & 4 & | & 3 \end{pmatrix} \tag{3.0.3}$$

$$\xrightarrow{R_2 \leftarrow R_2 - \frac{3}{2}R_1} \begin{pmatrix} 2 & -1 & | & -2 \\ 0 & \frac{11}{2} & | & 6 \end{pmatrix}$$
 (3.0.4)

$$\stackrel{R_2 \leftarrow \frac{2}{11}R_2}{\longleftrightarrow} \begin{pmatrix} 2 & -1 & | & -2 \\ 0 & 1 & | & \frac{12}{11} \end{pmatrix} \tag{3.0.5}$$

$$\stackrel{R_1 \leftarrow R_1 + R_2}{\longleftrightarrow} \begin{pmatrix} 2 & 0 & \frac{-10}{\frac{1}{2}} \\ 0 & 1 & \frac{1}{2} \end{pmatrix}$$
 (3.0.6)

$$\stackrel{R_1 \leftarrow \frac{1}{2}R_1}{\longleftrightarrow} \begin{pmatrix} 1 & 0 & \left| & \frac{-5}{11} \right| \\ 0 & 1 & \left| & \frac{1}{11} \right| \end{pmatrix} \tag{3.0.7}$$

Therefore, the values of x and y are:

$$x = \frac{-5}{11} \tag{3.0.8}$$

$$y = \frac{12}{11} \tag{3.0.9}$$