## 12.10.4

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## EE22BTECH11008 - Annapureddy Siva Meenakshi\*

Q:A system has transfer function

$$\frac{Y(s)}{X(s)} = \frac{s - \pi}{s + \pi}$$

let u(t) be the unit step function. The input x(t) that results in a steady-state output  $y(t) = sin(\pi t)$  is \_\_\_. **Solution:** 

Variable	Description	Value
x(t)	input function	none
y(t)	output function	$\sin(\pi t)$
H(s)	Transfer-function	$\frac{s-\pi}{s+\pi}$

TABLE 0

INPUT PARAMETERS

$$H(s) = \frac{s - \pi}{s + \pi} \tag{1}$$

Converting transfer function to frequency response, we get

$$H(j\omega) = \frac{j\omega - \pi}{j\omega + \pi} \tag{2}$$

$$|H(j\omega)| = \frac{\sqrt{(j\omega)^2 + (\pi)^2}}{\sqrt{(j\omega)^2 + (\pi)^2}} = 1$$
 (3)

$$\angle H(j\omega) = 180 - 2\tan^{-1}\frac{\omega}{\pi} \tag{4}$$

Here,  $\omega = \pi$ 

$$\angle H(j\omega)\big|_{\omega=\pi} = 90^{\circ} \tag{5}$$

$$y(t) = \sin(\pi t) = -\cos(\pi t + \frac{\pi}{2}) \qquad (6)$$

$$\cos(\omega t) \stackrel{H(j\omega)}{\to} |H(j\omega)| \cos(\omega t + \angle H(j\omega))$$
 (7)

Therefore by (6) and (7), we get

$$x(t) = -\cos(\pi t) \tag{8}$$

$$=\sin\left(\pi t - \frac{\pi}{2}\right) \tag{9}$$