## 1

## 12.10.4

## EE22BTECH11008 - Annapureddy Siva Meenakshi\*

Q:A system has transfer function

$$\frac{Y(s)}{X(s)} = \frac{s - \pi}{s + \pi}$$

let u(t) be the unit step function. The input x(t) that results in a steady-state output  $y(t) = \sin(\pi t)$  is \_\_. Solution:

Variable	Description	Value
x(t)	input function	none
y(t)	output function	$\sin(\pi t)$
H(s)	Transfer-function	$\frac{s-\pi}{s+\pi}$

TABLE 0: input parameters

$$H(s) = \frac{s - \pi}{s + \pi} \tag{1}$$

Converting transfer function to frequency response, we get

$$H(j\omega) = \frac{j\omega - \pi}{j\omega + \pi} \tag{2}$$

Here,  $\omega = \pi$ 

$$H(j\pi) = \frac{j-1}{j+1} = j$$
 (3)

$$|H(j\pi)| = 1\tag{4}$$

$$\angle H(j\pi) = 90^{\circ} \tag{5}$$

$$y(t) = \sin(\pi t) = \cos(\pi t + \frac{3\pi}{2}) \tag{6}$$

$$|X|\cos(\omega t + \phi) \stackrel{H(j\omega)}{\longrightarrow} |X||H(j\omega)|\cos(\omega t + \phi + \angle H(j\omega))$$
(7)

$$\cos(\pi t + \pi) \xrightarrow{H(j\omega)} |H(j\omega)| \sin(\pi t + \pi + \angle H(j\omega))$$
(8)

Therefore by (6) and (7), we get

$$x(t) = \cos(\pi t + \pi) \tag{9}$$

$$=\sin\left(\pi t - \frac{\pi}{2}\right) \tag{10}$$

$$\frac{\sin(\pi t - \frac{\pi}{2})}{H(s)} \longrightarrow H(s)$$

Fig. 0: Block diagram of the System