## 12.10.4

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## EE22BTECH11008 - Annapureddy Siva Meenakshi\*

Q:A system has transfer function

$$\frac{Y(s)}{X(s)} = \frac{s - \pi}{s + \pi}$$

let u(t) be the unit step function. The input x(t) that results in a steady-state output  $y(t) = sin(\pi t)$  is \_\_\_. **Solution:** 

Variable	Description	Value
x(t)	input function	none
y(t)	output function	$\sin(\pi t)$
H(s)	Transfer-function	$\frac{s-\pi}{s+\pi}$

TABLE 0

INPUT PARAMETERS

$$H(s) = \frac{s - \pi}{s + \pi} \tag{1}$$

Converting transfer function to frequency response, we get

$$H(j\omega) = \frac{j\omega - \pi}{j\omega + \pi} \tag{2}$$

$$|H(j\omega)| = \frac{\sqrt{j^2 + (\omega)^2}}{\sqrt{j^2 + (\omega)^2}} = 1$$
 (3)

$$\angle H(j\omega) = -2\tan^{-1}\frac{\omega}{\pi} \tag{4}$$

Here,  $\omega = \pi$ 

$$\angle H(j\omega)\Big|_{\omega=\pi} = -90^{\circ} \tag{5}$$

Using the magnitude and phase information, the input signal x(t) is given by:

$$x(t) = |H(j\omega)|\sin(\omega t + \angle H(j\omega)) \tag{6}$$

Substituting  $|H(j\pi)| = 1$  and  $\angle H(j\pi) = -\frac{\pi}{2}$ :

$$x(t) = 1\sin\left(\pi t - \frac{\pi}{2}\right) \tag{7}$$

$$\therefore x(t) = \sin\left(\pi t - \frac{\pi}{2}\right) \tag{8}$$