Homework & Meer Mod: 01/29/2024 A=21,2,34 B= 22,34 C=2A,BY D= 2'a'4 E=280,43} (Q1) (a) (A,B) EC -> Faise (f) & E P(B) - False Power of a set returns a set (b) (1,3) ∈ Ax13 → true with sets inside of th 21,2,37 x 22,39 Hence 2 has no chances of = δ (1,2), (1,3), (2,2), (2,3). being in P(B) (3,2),(3,3) } (1,3) & & (1,2),(1,3), (2,2),(2,3), (9) & 29 = 9(B) + False &2y € & {2,3y, \$2},\$33, @} (3,2),(3,3)4 (c) (1,3) = A×B + Syntax error (h) 2 = P(B) + Syntax 2 cms $(1,3) \rightarrow \text{tople}$ 2 is not a set (d) (1,3) € C + Faise (e) \$23 € P(B) -> True 529 € { 2,39, 52,3, 534, Ø3 (i) { 53,233 ⊆ 3(A) + true \$ ₹ 3,23 4 € \$ \$ 1,2,33, \$ 1,3,523, according to thm [J(B)] = 2 1B) 233, Ø, E1, 23, \$2,33, \$1,339 19(8) 1 = 2 = 4 the order within a 229E 2 82,33, 223, 883, Ø9 set does not matter 23,29 = 22,39

hence true

- (i) { { 3, 2 } } ⊆ 8 (c) > false D(c): \$ EAB, EBB, EABB, @3 \$ 23,233 € \$ 2A3, 2B3, 2A, B3, Ø4
- (K) { \$2,33 } € 9(c) > Faise ₹ 2,333 € { 2 8 A3, 8 B3, 8 A, B4, \$ B
- (02)

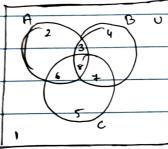
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- (9) BxA 22,33 x 21,2,33

 - = \(\((2,1) \) (2,2) \, (2,3) \, (3,1), (3,2), (3,3)
- (e) ExBxD
 - 820,439 x 22,39 x 2'a'3
 - P (80,43,8), (80,43,3) 3 x { 'a' 3 \$ (({\(\xi_0,43,2\), 'a'\), (({\(\xi_0,43,3\), 'a'\)}
- (b) A x D P(D) Power set of D (f)
 - £1,2,33 x 2 'a' 3 D = & 'a' 3
 - 9(0) = } {3,803} = { (1,'a'), (2,'a'),
 - (3, '0') 4
- 9(E) ~ @ E= } {0,439 (9)
- 9(E) = \$ &3, 80,43 g (c) Ø x B $\phi \times 22,39 = \phi$
- 7 (h) D(B) = \$ {23, {33, \$, \$2,339} (d) cxc
 - [A,B] x [A,BY
- 1 = § (A,A), (A,B), (B,A),
 - (B, B) q

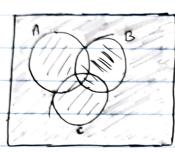
- (a) { (x,y) | x & N & x < 5 & y = 0 } = $\{(1,0),(2,0),(3,0),(4,0)\}$
- (b) & 4x | x & 24 6 -1 & x & 1 } = \$ -4,0,43
- € a+6 | a ∈ NI & a < 3 & 6 ∈ € 5,63 } = \$ 6,7,8 3

(O4)

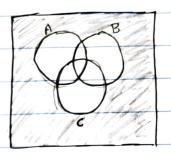


- (9) (AUB) OC = AU(BOC)
 - 5 2,3,4,56,7,83= \$ 2,3,4,5,6,7,89
- (b) AUB = BOA {2,6,3,8,4,7} = {2,6,3, 1,4,7}

(OS) AUBUC = AnBne



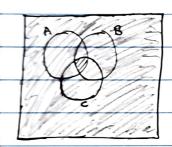
= > AUBUC >> AUBUC



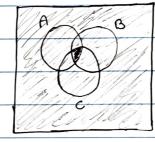
⇒ → あっるのこ

AUBUC = AnBno Hence

AOBOC = AUBUC *(P)*



= -> ANBOC = > AnBnc



· → Ã UBOC

Primes, divisors, modulo

(O) Prime Factorization

5 5

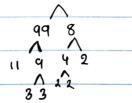
7

-

2 7

1

(b)



(C)31

3 × 31

5×17

85

2×2 xx x 3×3×11 2×2×2×5

 $2^3 \times 3^2 \times 11$

-> 98, 85 are relatively prime. (02) Defination (Quotient Remainder Thm): let n, d be 74 d>0 there are integers qur such that n= d·q+r and osred (e) ol12 (a) 417 7 - 1.75 \$ 2 12 gundefined False (f) 12/0 N=0 d=12 (b) 4/12 0 = 0 E Z n= 12 d= 4 True True (g) (c) 4 | -12 n=-12 d=4 (h) 12=3(i) Q - 0 True (i) 12 > undefined (d) 12/4 n=4 d=12 4 _ 0.B3 & ZL False

& Homework & continued

8

- -

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-2 -2

-

13

2

(a)
$$n=28$$
 $d=7$ (e) $n=0$ $d=6$
 $28 = 7 \cdot 9 + \Gamma$ $0 = 6 \times 9 + \Gamma$
 $28 = 7 \cdot 9 + 0$ $0 = 6 \times 9 + 0$

$$-28 = 7 \cdot (-4) + 0$$
 $S = 6 \times 0 + 5$

(c)
$$n=31$$
 $d=7$ (g) $n=-5$ $d=6$

$$31 = 7 \cdot 9 + \Gamma \qquad -5 = 6 \times 9 + \Gamma$$

$$31 = 7 \cdot 4 + 3$$
 $-5 = 6 \times (-1) + 1$

(d)
$$n = -31 d = 7$$
 (h) $n = -10 d = 6$

$$-31 = 7 \cdot (-5) + 4$$
 $-10 = 6 \times (-2) + 2$

$$q = -5$$
 R24 $q = -2$ $r = 2$

$$-5R4$$
 $-2R2$

(04) (a) 7 mod 5 (e) 0 mod 5 7 = 5 × q + r 0 = 5 + q + f 7=5x1+2 0=5.0+0 Q = O R = 2 71.5=2 01.5=0 (b) -7 mad 5 (f) 0 mod 3 n=-7 d=5 n=0 d=3 $-7 = 5 \times (-2) + 3$ 0 = 3.0 +0 R=3 -7.105=3 01.3 (9) 48 mod 12 (c) 3 mocl 5 n= 48 d=12 n=3 d=5 $3 = 5 \times (0) + 3$ 48 = 12 · 4 + 6 R = 3 34.5=3 48 1.12=6 (d) -3 mod 5 (h) 48 mod 11 n = -3 d = 5 $u8 = u \times 4 + 4$ -3=5(-1)+2 R = 4 48 R=4 R = 2 -34.5 = 248 1.11 = 4

4

6

1

2

E

3

3

3

-

3

-

-3 -

-

-

10

19 T 3

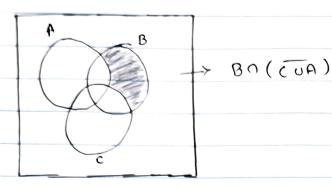
-3 7

3

$$\frac{1}{42}$$
 $\frac{1}{5}$ $\frac{1$

> section 1.1 82,25,56,77,96, 103 (Q22) V = { 0,1,2,3 } X = 2 1, 2, 3, 4, 5 4 $y = \{2n \mid n \in z^{\dagger}\} = \{0, 2, 4, 6, 8, 10 \dots \}$ XOY \(\times = all elements not in x but in the universe x = 20,6,1,8,9,10...3 y = {0,2,4,6,8,10 4 xny= &t|terbtexbtex3 (ODT) XU J & ý = au elements not in y but in universe X = ou element in x x = &1,2,3,4,5 3 > Finite y = 21,3,5,7 --- 3 + Infinite XUY = {t | tet b (tex or to y)}

1



(074) ZXR

-3

-3

3

- 3

-

-

24 Reprents all intigers & -1, 0, 1 3

R Represents an Real numbers & o 3

ZXR will return a set with touples inside of it which will have coordinates points (x,n) in them

ZXR = S(x,n) | x EZ and n ERY

(096) if x has n members how many proper subsets does

x have

let w = a gubset of x

Proper subset = wcx if wcx and w = y

n=1 ? -1 • •

(i) AUA = A (j) POA ZA { 3,38,63 U 22,3,8,64 2 A 21,3,8,63 n 22,3,8,63 2A (L) AUU2U (L) AT Ø = Ø 2 U (m) AU (AOB) = A (n) AO (AUB) = A {2,3,8,6} U (3,8) {2,3,8,6} \{2,3,8,6,4,7} { 2, 3, 8, 6, \$, \$ } = A $(\circ) \overline{A} = A \qquad (P) \overline{\emptyset} = U$ {1,4,5,73=} $\bar{A} = \{2,3,7,6\} = A$ (a) $\bar{U} = \emptyset$ £1,2,3,4,5,6,7,83 = {3 (R) (AUB) = A OB (S) (AOB) = A UB \$1,59 2 2 4,7,5,3 0 82,6,5,13 \$1,2,6,4,7,53 = \$1,2,6,4,7,54 81,53 2 21,53

3

3

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3

9

5

3