

Intro to Computing

ES112

Lecture 3

Some drawings and material from CS101 course pages
and lectures of various universities, esp. IITB and
OCW@MIT

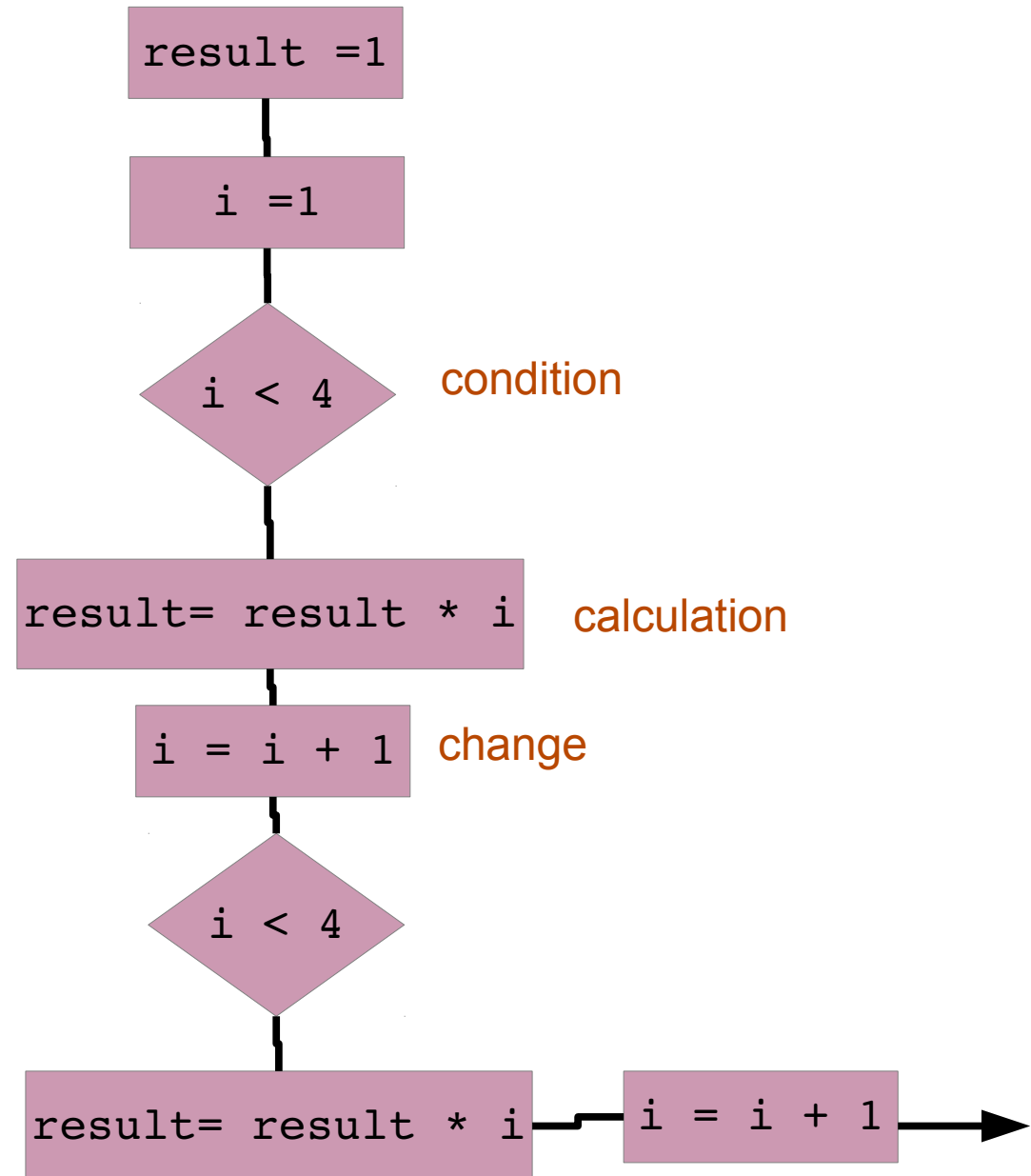
Iteration: while loop

```
result = 1
i = 1
while i < 4:
    result = result * i
    i = i + 1
print "result =", result
```

- While loop has three parts:
 - **the condition**: which tells us when the loop should end
 - the actual **calculation**
 - somewhere where we are actual **changing** the variable

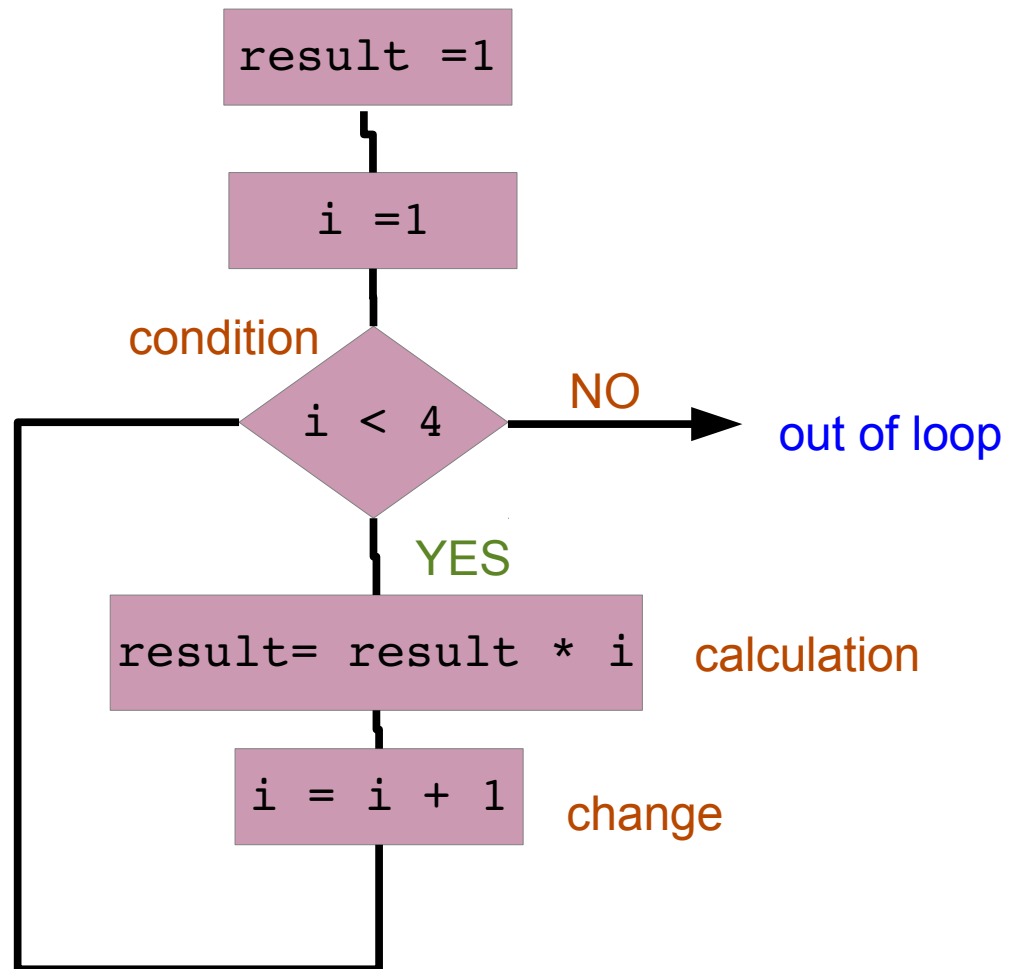
Iteration: while loop

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result = 1
i = 1
while i < 4:
    result = result * i
    i = i + 1
print "result =", result
```



Iteration: while loop

```
result = 1
i = 1
while i < 4:
    result = result * i
    i = i + 1
print "result =", result
```



Iteration: while loop

```
i = 1
while True:
    print "i = ", i
    i = i + 1
print result
```

- What will happen above?

Iteration: while loop

```
result = 1
i = 1
while i < 4:
    result = result * i
print result
```

- What will happen above?

Iteration: while loop

```
result = 1
i = 1
while i < 4:
    result = result * i
    i = i - 1
print result
```

- What will happen above?

break statement

```
result = 1
i = 10
while True:
    result = result * i
    i = i - 1
    if i < 0:
        break
print result
```

- **break** is a way to get out of a loop
- What happens above then?

Iteration: `while`

- Let's write a function to find out the cube root of a number:
 - Take `x` as input and pass `x` as a parameter to this function
 - If there exists `x`, such that `y**3` equals `x`, then output `y`
 - Else output `"not a perfect cube"`
- `Hint: use a while loop to look for y`
- Also print out the count of how many `y` values did you try

for loop

- Another way of writing the program we did before

```
result = 1
i = 1
for i in range(4):
    result = result * i
print "result = ", result
```



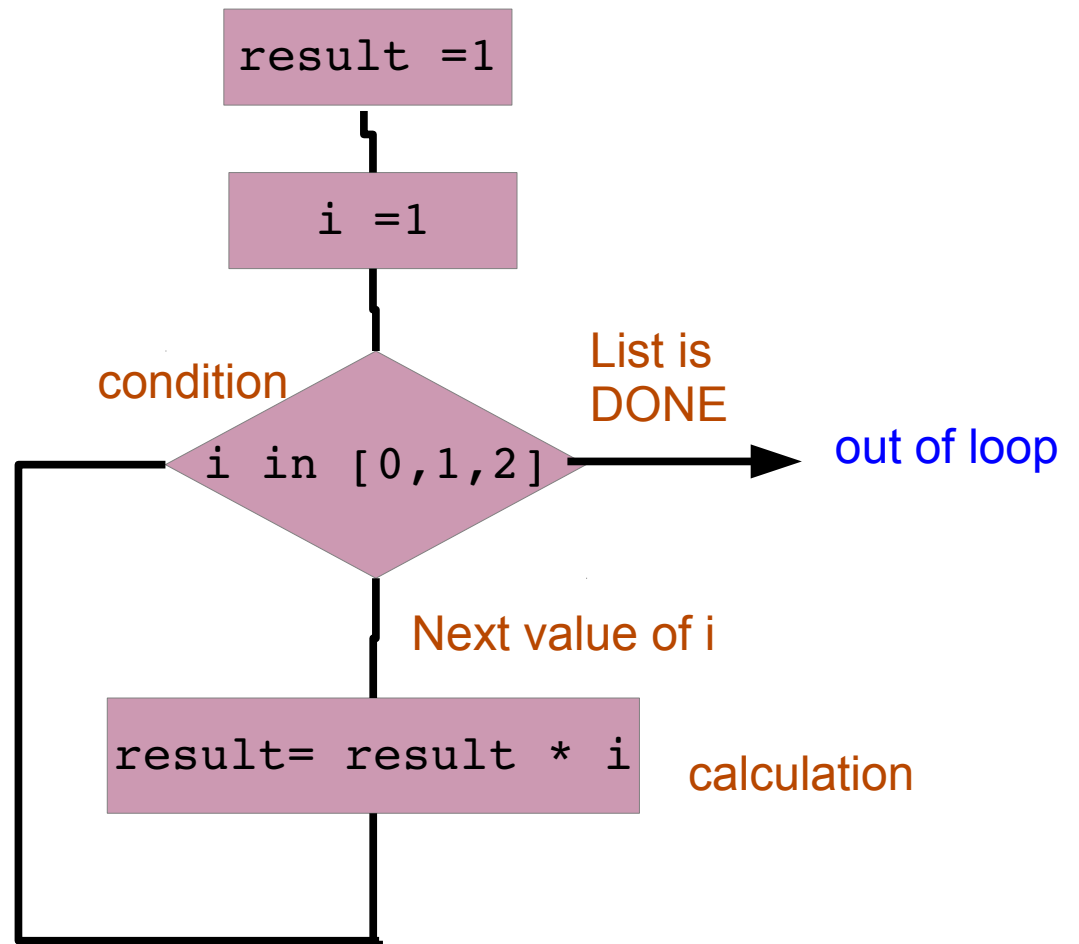
range(4) = [0, 1, 2, 3]

The loop code is executed for every value of *i* in the list.

So what is *result*?

for loop

```
result = 1
i = 1
for i in range(4):
    result = result * i
    print "result = ", result
```



Difference between `for` and `while` loops

```
result = 1
i = 1
for i in range(4):
    result = result * i
print "result = ", result
```

```
result = 1
i = 1
while i < 4:
    result = result * i
    i = i + 1
print "result =", result
```

- Notice that a `for` loop a programmer does not change the loop variable separately, it automatically takes the next value
- For a while loop, we have to change it
- Which one to use is a matter of taste, either is fine

Rewrite using `for` loop

- Let's write a program to find out the cube root of a number:
 - Take `x` as input
 - If there exists `x`, such that `y**3 = x`, then output `y`
 - Else output `"not a perfect cube"`

Rewrite using `for` loop

- Let's write a program to find out the cube root of a number:
 - Take `x` as input
 - If there exists `x`, such that `y**3 == x`, then output `y`
 - Else output `"not a perfect cube"`
- Change your function to find out approximate cube root
 - i.e. find out the integer `y` such that `math.abs(y**3 - x)` is the smallest among all possible `y`

Factorial

- Write down a function `factorial(n)` to compute the factorial of n

Approximating sin by a series

- Let's write a program to find out the $\sin(x)$ for any x
 - Take as input the number n and the value x
 - Use your function that calculate the factorial of a number n
 - Use the above function to calculate

$$\text{mysin}(n, x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} + \dots + (-1)^n \frac{x^{2n+1}}{(2n+1)!}$$

- Print out both the value of $\text{math.sin}(x)$ and $\text{mysin}(x)$

Creating new functions – syntax

```
def <functionname> ( <parameters> ):
```




```
<statements>
```

spaces

- Note that we **must indent**
- Function block ends in the line when the indentation finishes

Function Block

```
def print_lyrics():  
    print "Papa kehte hain"  
    print "Beta engineer banega"  
print "Lyrics of an all-time favorite"  
print_lyrics()
```



Function block

- The last two statements are **not** part of the function

Indentation

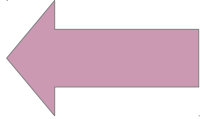
```
def print_lyrics():  
    print "Papa kehte hain"  
    print "Beta engineer banega"  
  
print "Lyrics of an all-time favorite"  
print_lyrics()
```

IndentationError: expected an indented block

- If you do not keep the indentation consistent, you will get this error

Calling a function

```
def print_lyrics():  
    print "Papa kehte hain"  
    print "Beta engineer banega"  
print_lyrics()
```



- After a function has been defined it has to be called
- The code inside the function block is executed only when it is called

Parameters to the function

```
def print_lyrics(x):  
    print "Papa kehte hain"  
    print "Beta ", x, " banega"  
print_lyrics("engineer")
```

- Notice that there is no “x” outside the function, we only provide a value to the function, not a variable
- Best way to think about this:
 - Each variable represents a container
 - Each time the function is called, new containers are created with the variables names of the parameters

Parameters to functions

```
def print_lyrics(x):  
    print "Papa kehte hain"  
    print "Beta ", x, " banega"
```

```
print_lyrics("engineer")  
print x
```

- What do you think happens above? Why?

Local variables are temporary

- Variables defined inside functions are not available outside
 - They are created each time the function is called and destroyed immediately

```
def addone(x):  
    x = x + 1  
    print "x + 1 = ", x + 1  
a = 5  
addone(a)  
addone(a + 1)
```

What will this output ?

Local variables are temporary

```
def addone(x):  
    x = x + 1  
    print "x = ", x  
a = 5  
addone(a)  
addone(a)
```

What will this output ?

Scopes

- Local variables inside a function exist in a separate namespace or scope

```
def f(x):  
    y = 1  
    x = x + y  
    print 'x = ', x  
    return x  
  
x = 3  
y = 2  
z = f(x)  
print 'z = ', z  
print 'x = ', x  
print 'y = ', y
```

What does the code print?

Scopes in terms of stack frames

- At the top level, there is a **symbol table** that stores the names and memory bindings of all variables
- When each function is called, a **new symbol table** (also called **stack frame**) is created
 - Contains all local variables and the parameters passed
 - This is destroyed when the function exits
 - If another function is called from this function, another stack frame is created

Creating stack frames

- What stack frames are created for the following code?

```
def f(x):  
    def g():  
        x = 'abc'  
        print 'x =', x  
    def h():  
        z = x  
        print 'z =', z  
    x = x + 1  
    print 'x =', x  
    h()  
    g()  
    print 'x =', x  
    return g
```

```
x = 3  
z = f(x)  
print 'x =', x  
print 'z =', z  
z()
```

More about scopes: locals vs. globals

```
def somefunc(a):  
    a = 2  
    print "a = ", a + 1  
a = 5  
somefunc(a)  
print a  
a = a + 1  
somefunc(a)
```

Local variables vs. global

```
def somefunc(a):  
    a = 2  
    print "a = ", a  
a = 5  
somefunc(a)  
a = a + 1  
somefunc(a)
```

When the function `somefunc` is called, there is already a global variable named `a`

However, if there is a variable of same name, the function always uses that

In the above example, the parameter `a` creates a local variable that is used by the function

More about scopes

- Understanding when variables are created in symbol tables is often important to avoid confusion

```
def f():  
    print x
```

```
def g():  
    print x  
    x = 1
```

```
x = 3  
f()  
x = 3  
g()
```

What does this code print?

Accessing global variables

```
def g():  
    global x          # accesses global symboltable for X  
    print x  
    x = 1  
x = 3  
g()
```

Here, because of the global keyword, the global variable X is being accessed.

Scopes

- Important to remember concepts:
 - Separate symbol table created for each function call (not definition)
 - An entry for a variable name exists **only if it appears in the LHS of an expression** (i.e. is being assigned)
 - Local symbol table searched first before global symbol table, local definitions override global definitions
 - **global** keyword forces looking into global symbol table

Return values

- Functions can often return a value

```
def myfunction ( x ):  
    a = x + 1  
    return a
```

```
Val = myfunction(5)  
print "Val = ",Val
```

```
def myfunction2 ( x ):  
    return x + 1
```

```
Val = myfunction(5)  
print "Val = ",Val
```

- `return` statement returns the values after it

Return values

- Functions can often return a value

```
def myfunction ( x ):  
    a = x + 1  
    return a
```

```
Val = myfunction(5)  
print "Val = ",Val
```

```
def myfunction2 ( x ):  
    return x + 1
```

```
Val = myfunction(5)  
print "Val = ",Val
```

- `return` statement returns the values after it
- If it is a mathematical expression, then the resulting value is returned

Return values

```
def myfunction ( x ):  
    return x + 1
```

```
Val = myfunction(myfunction(5)) + myfunction(6)  
print "Val = ",Val
```

- What is printed as Val?

Exercise

- Write down the following program
 - Input n numbers a_1, a_2, \dots, a_n
 - Has a function `am(list1)` that calculates the AM of the numbers in the list `list1`
 - Has a function `gm(list1)` that calculates the GM of the numbers in `list1`
 - The program calculates AM and GM of the given numbers and prints them out

Exercise

We will write some to spot-check whether a function is a bijection. Write down a python function to implement the function $f : (0,1) \rightarrow \mathbb{R}$ where

$$f(x) = (x - \frac{1}{2}) / (x - x^2)$$

- Write down the code for the inverse function g of the above function
- Write down a program that does the following:
 - Takes an input x in $(0, 1)$ from the user
 - Calculate $y = f(x)$
 - Calculate $z = g(y)$
 - Checks whether z is equal to x (beware of floating point comparisons), also print the values of x , $f(x)$ and $g(f(x))$