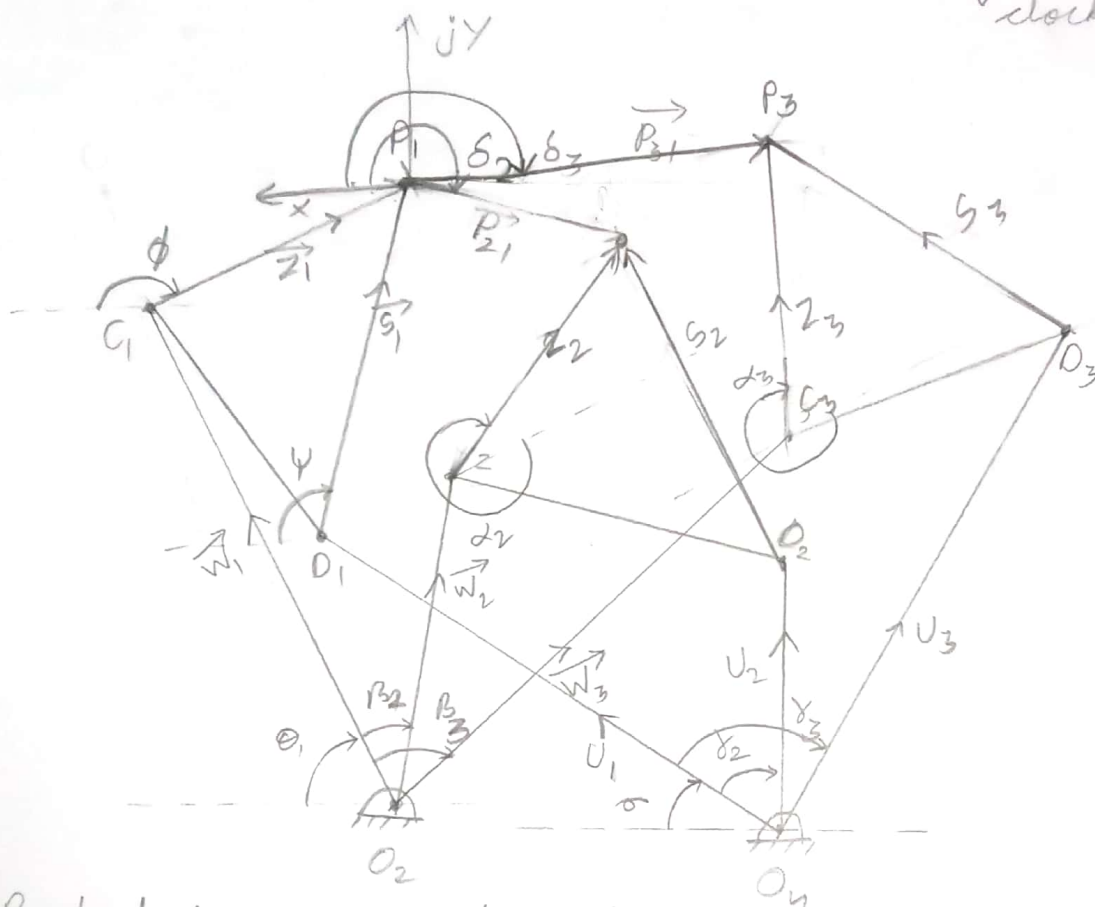


# Assignment-4

1)

every angle  
clockwise



By loop closure equations for left dyad we get

$$\left. \begin{aligned} w e^{i\theta} (e^{i\beta_2} - 1) + z e^{i\phi} (e^{i\alpha_2} - 1) &= p_2 e^{i\delta_2} \\ w e^{i\theta} (e^{i\beta_3} - 1) + z e^{i\phi} (e^{i\alpha_3} - 1) &= p_3 e^{i\delta_3} \end{aligned} \right\} \text{--- (1)}$$

$$\left( \begin{aligned} \vec{w}_2 + \vec{z}_2 - \vec{p}_{21} - \vec{z}_1 - \vec{w}_1 &= 0 & \& \\ \vec{w}_3 + \vec{z}_3 - \vec{p}_{31} - \vec{z}_1 - \vec{w}_1 &= 0 \end{aligned} \right)$$

From diagram

$$p_{21} = 3 \text{ cm}$$

$$p_{31} = 5 \text{ cm}$$

$$\delta_2 = 195^\circ$$

$$\delta_3 = 174^\circ$$

$$\alpha_2 = 332^\circ$$

$$\alpha_3 = 295^\circ$$

choose:

$$\beta_2 = 30^\circ$$

$$\beta_3 = 45^\circ$$

$$\rightarrow \text{Let } W = w e^{i\theta} \quad S_2 = e^{i\beta_2} - 1 \quad T_2 = e^{i\alpha_2} - 1 \quad U_2 = P_{21} e^{i\delta_2} \\ Z = z e^{i\phi} \quad S_3 = e^{i\beta_3} - 1 \quad T_3 = e^{i\alpha_3} - 1 \quad U_3 = P_{31} e^{i\delta_3} \quad \} - (2)$$

By ① & ②

$$\Rightarrow \begin{cases} WS_2 + ZT_2 = U_2 \\ WS_3 + ZT_3 = U_3 \end{cases} - (4)$$

By elimination we get

$$\Rightarrow W = \frac{U_2 T_3 - U_3 T_2}{S_2 T_3 - S_3 T_2}$$

solving in MATLAB we get

$$W = -0.0203 + i 0.0214$$

$$\Rightarrow W \cos \theta = -0.0203$$

$$W \sin \theta = 0.0214 \Rightarrow W = \frac{0.0214}{\sin \theta} \quad - (3)$$

$$\Rightarrow \frac{0.0214}{\sin \theta} \cos \theta = -0.0203$$

$$\Rightarrow \cot \theta = -0.95$$

$$\Rightarrow \theta = -46.5^\circ$$

$$\Rightarrow \underline{\underline{\theta = 46.5^\circ \text{ Clockwise as in diagram}}}$$

from ③

$$W = \frac{0.0214}{\sin 46.5^\circ} = 0.03 \text{ m} = 3 \text{ cm}$$

$$\underline{\underline{W = 3 \text{ cm}}}$$

Using (ii) we also get

$$\bar{Z} = \frac{U_2 S_3 - U_3 S_2}{T_2 S_3 - T_3 S_2}$$

Using MATLAB,

$$\bar{Z} = -0.0447i \quad \bar{Z} = ze^{i\phi}$$

$$\angle \phi = 0$$

$[\phi = 90^\circ]$  Clockwise  $\rightarrow$  Refer Dia

$$Z = 0.0447 m$$

$$[Z = 4.47 \mu m]$$

Similarly by loop closure equations for right Dyad we get

$$U e^{i\sigma} (e^{i\gamma_2} - 1) + S e^{i\psi} (e^{i\alpha_2} - 1) = P_2 e^{i\delta_2}$$

$$\underbrace{U e^{i\sigma}}_U \underbrace{(e^{i\gamma_2} - 1)}_{S_2} + \underbrace{S e^{i\psi}}_S \underbrace{(e^{i\alpha_2} - 1)}_{T_2} = \underbrace{P_2 e^{i\delta_2}}_{U_2}$$

Choose

$$\gamma_2 = 70^\circ$$

$$\gamma_3 = 100^\circ$$

$$\Rightarrow U S_2 + S T_2 = U_2$$

$$U S_3 + S T_3 = U_3$$

$$U = \frac{U_2 T_3 - U_3 T_2}{S_2 T_3 - S_3 T_2}$$

Using MATLAB ;  $U = -0.004 + 0.0103i$

$$\Rightarrow U \cos \sigma = -0.004$$

$$U \sin \sigma = 0.0103$$

$$\Rightarrow \tan \sigma = \frac{0.0103}{-0.004}$$

$$\Rightarrow \left[ \begin{array}{l} \sigma = 68.78^\circ \text{ clockwise} \\ U = 1.11 \text{ cm} \end{array} \right] \rightarrow \text{Refer dia}$$

similarly

$$S = \frac{U_2 S_3 - U_3 S_2}{T_2 S_3 - T_3 S_2}$$

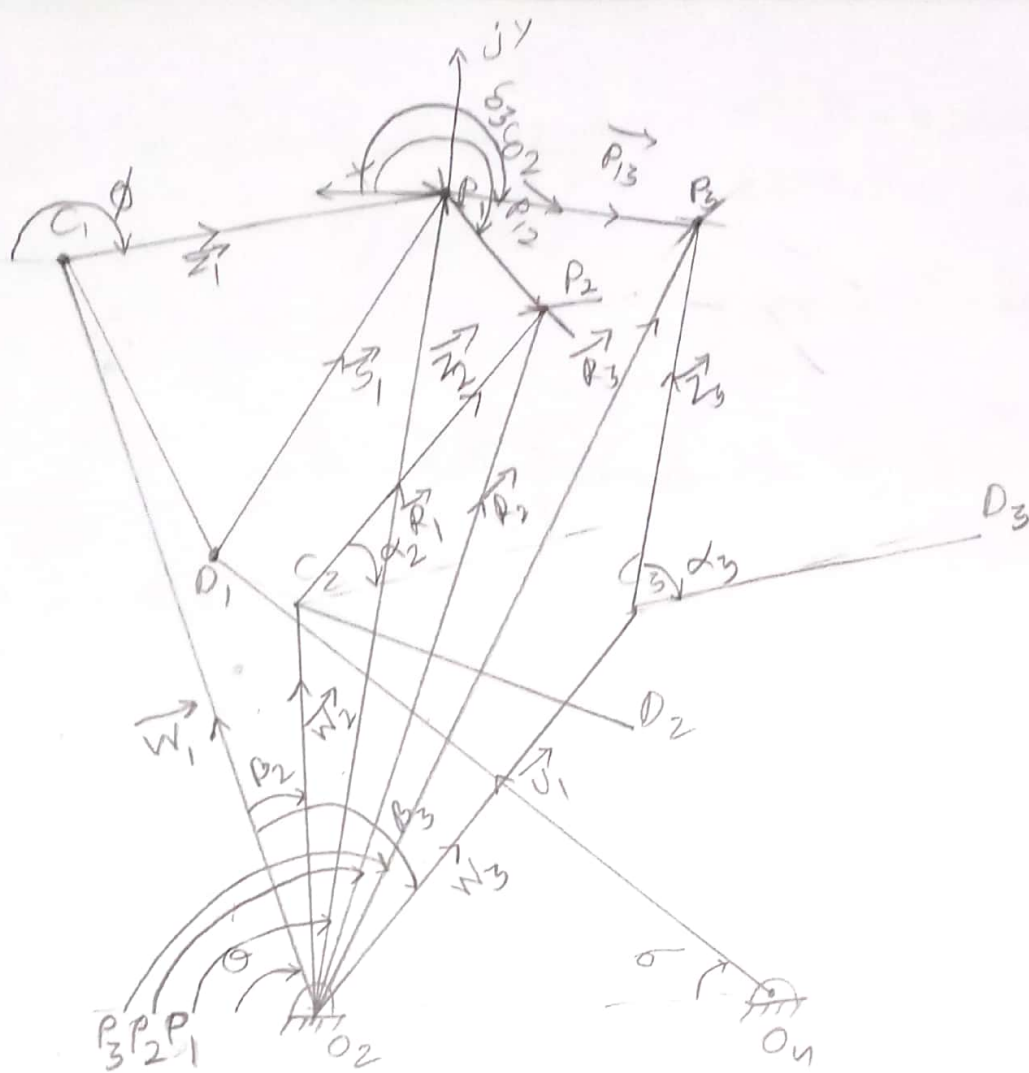
$$= 0.0055 - 0.0453;$$

$$S \cos \psi = 0.0055$$

$$S \sin \psi = -0.0453$$

$$\left[ \begin{array}{l} \psi = 83^\circ \text{ clockwise} \\ S = 4.564 \text{ cm} \end{array} \right] \rightarrow \text{Refer dia}$$

2)



Using loop closure equations

$$\begin{aligned} \vec{w}_1 + \vec{z}_1 &= \vec{R}_1 \\ e^{i\beta_2} \vec{w}_1 + e^{i\alpha_2} \vec{z}_1 &= \vec{R}_2 \\ e^{i\beta_3} \vec{w}_1 + e^{i\alpha_3} \vec{z}_1 &= \vec{R}_3 \end{aligned}$$

$$\begin{aligned} \Rightarrow w e^{i\theta} + z e^{i\phi} &= R e^{iP_1} \\ e^{i\beta_2} w e^{i\theta} + e^{i\alpha_2} z e^{i\phi} &= R e^{iP_2} \\ e^{i\beta_3} w e^{i\theta} + e^{i\alpha_3} z e^{i\phi} &= R e^{iP_3} \end{aligned}$$

Given:

- $R = 5 \text{ cm}$
- $P_1 = 43^\circ$
- $P_2 = 95^\circ$
- $P_3 = 97^\circ$
- $\alpha_2 = 35^\circ$
- $\alpha_3 = 70^\circ$

To find:

$w, \theta, \beta_1, \beta_2, z, \phi$   
6 variables

3 complex  $\Rightarrow$  6 equations

measured from the dimensions given in the text book figures

summary of calculations:

$$\text{let } A = e^{i\alpha_2} \vec{P}_3 - e^{i\alpha_3} \vec{P}_2$$

$$B = e^{i\alpha_3} \vec{P}_1 - \vec{P}_3$$

$$C = \vec{P}_2 - e^{i\alpha_2} \vec{P}_1$$

&

$$a = \bar{A}B, b = A\bar{A} + B\bar{B} - C\bar{C} \text{ \& } c = A\bar{B}$$

then

$$e^{i\beta_2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = t_{1,2}$$

&

$$e^{i\beta_3} = \frac{-A + B t_{1,2}}{C}$$

↓

we get  $\beta_2$  &  $\beta_3$  from above ←

then use

$$\vec{W}_1 + \vec{Z}_1 = \vec{R}_1 \text{ \& }$$

$$e^{i\beta_2} \vec{W}_1 + e^{i\alpha_2} \vec{Z}_1 = \vec{P}_2 \quad \underline{\text{my 2}}$$

$$e^{i\beta_3} \vec{W}_1 + e^{i\alpha_3} \vec{Z}_1 = \vec{P}_3$$

to get  $\omega, \theta, z$  &  $\phi$

⇒ For MATLAB implementation, run A3.m with input array as [5 93 95 97 35 70]

we get

$$\left[ \begin{array}{l} \beta_2 = 2^\circ \text{ clockwise} \\ \beta_3 = 163.4564^\circ \text{ clockwise} \end{array} \right]$$



Using

$$W_1 + Z_1 = R_1$$

$$e^{i\beta_2} W_1 + e^{i\alpha_2} Z_1 = R_2$$

we will get  $w, \theta, z$  &  $\phi$

$$e^{i\beta_2} (R_1 - Z_1) + e^{i\alpha_2} Z_1 = R_2$$

$$R_1 e^{i\beta_2} - Z_1 e^{i\beta_2} + Z_1 e^{i\alpha_2} = R_2$$

$$Z_1 = \frac{R_2 - R_1 e^{i\beta_2}}{e^{i\alpha_2} - e^{i\beta_2}} = z e^{i\phi}$$

$$W_1 = R_1 - Z_1 = w e^{i\theta}$$

For solution using MATLAB A4.m with input array

as  $[5 \ 93 \ 95 \ 97 \ 35 \ 70]$  we get

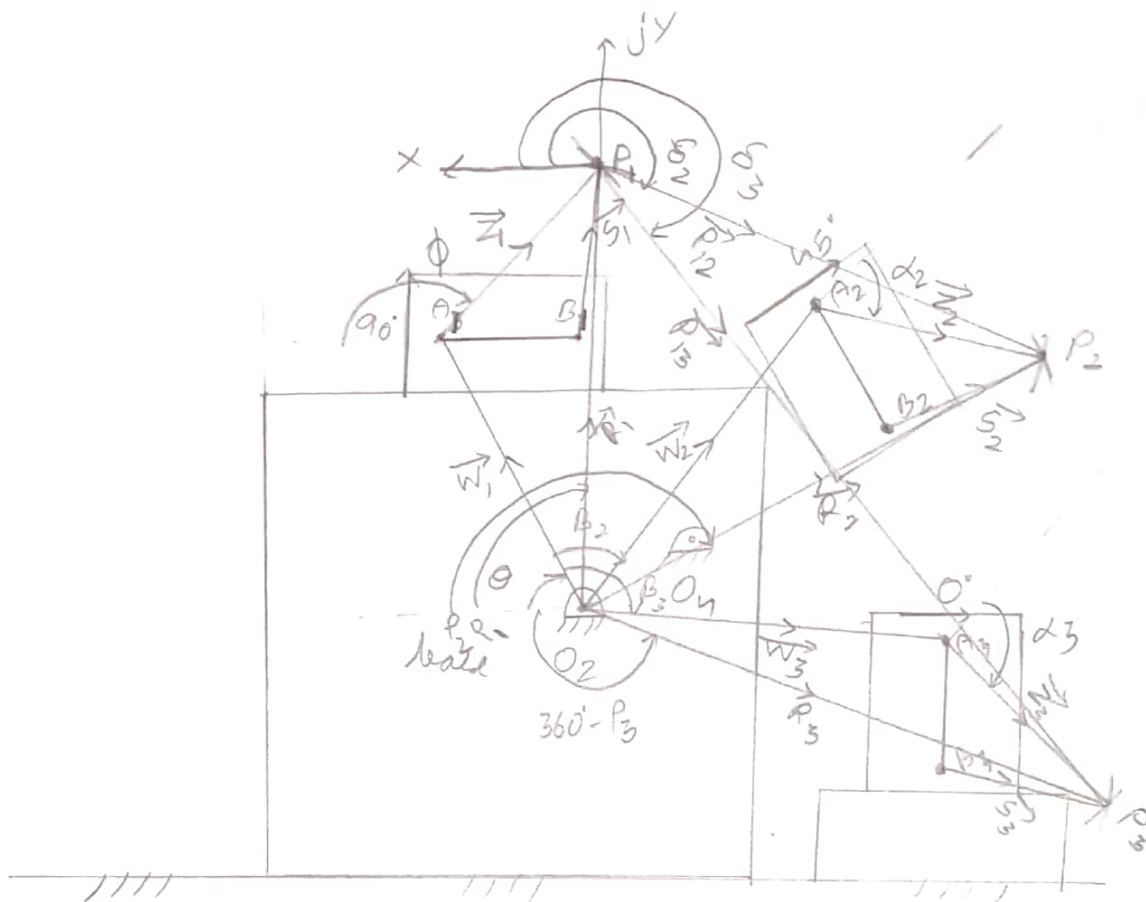
①

$$\left[ \begin{array}{l} Z = 5.618 \text{ cm} \\ \phi = 76.5^\circ \\ w = 2.8020 \text{ cm} \\ \theta = -179.5953^\circ \\ \beta_2 = -35^\circ \\ \beta_3 = 163.6002^\circ \end{array} \right]$$

②

$$\left[ \begin{array}{l} Z = 5.0345 \text{ cm} \\ \phi = 31.1196^\circ \\ w = 8.2186 \text{ cm} \\ \theta = 128.1498^\circ \\ \beta_2 = -2^\circ \\ \beta_3 = -163.4564^\circ \end{array} \right]$$

3)



In the above problem, we are constrained by the condition that the fixed pivot points should lie inside the base, as a result let us choose  $O_2$  &  $O_4$  as marked in the above diagram.

Hence once fixing  $O_2$  &  $O_4$  we will get input values from the dimensions mentioned in the textbook diagram.



As a result given input values are:

$$R = 1.86 \text{ cm}$$

$$P_1 = 62^\circ$$

$$P_2 = 150^\circ$$

$$P_3 = 200^\circ$$

$$\alpha_2 = 58^\circ$$

$$\alpha_3 = 94^\circ$$

Run A.h.m with input array as [1.8 62 150 200 58 94]  
we get the result:

①

$$Z = 2.5451 \text{ cm}$$

$$\phi = 77^\circ$$

$$w = 1.3285 \text{ cm}$$

$$\theta = -45.9366^\circ$$

$$\beta_2 = -88^\circ$$

$$\beta_3 = -156.8469^\circ$$

②

$$Z = 1.3499 \text{ cm}$$

$$\phi = 117.5633^\circ$$

$$w = 3.1273 \text{ cm}$$

$$\theta = 67.9442^\circ$$

$$\beta_2 = -58^\circ$$

$$\beta_3 = -134.0954^\circ$$

Alternative

Using Graphical Analysis we can create a Crank-Rocker Mechanism too as in 3<sup>rd</sup> Problem of Assignment 3