Report

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Introduction

Dataset

hurrican
703.csv collected the track data of 702 hurricanes in the North Atlantic area from 1950 to 2013. For
 all the storms, their location (longitude & latitude) and maximum wind speed were recorded every 6 hours.
 The data includes the following variables

- 1. **ID**: ID of the hurricans
- 2. Season: In which year the hurricane occurred
- 3. Month: In which month the hurricane occurred
- 4. Nature: Nature of the hurricane
- ET: Extra Tropical
- DS: Disturbance
- NR: Not Rated
- SS: Sub Tropical
- TS: Tropical Storm
- 5. time: dates and time of the record
- 6. Latitude and Longitude: The location of a hurricane check point
- 7. Wind.kt Maximum wind speed (in Knot) at each check point

From the original dataset, we built a new dataset with contains five more variables, including:

- 1. Wind_prev: wind speed at 6 hours ago
- 2. Wind_prev_prev: wind speed at 12 hours ago
- 3. Lat_change: latitude change compared to 6 hours earlier
- 4. Long_change: longitude change compared to 6 hours earlier
- 5. Wind change: wind speed change at 6 hours earlier compared to 12 hours earlier

These variables will help us to build the model in the following part.

The hurricanoutcome 2.csv recorded the damages and death caused by 46 hurricanes in the U.S, and some features extracted from the hurricane records. The variables include:

- 1. **ID**: ID of the hurricans
- 2. Season: In which year the hurricane occurred
- 3. Month: In which month the hurricane occurred
- 4. Nature: Nature of the hurricane
 - ET: Extra Tropical
 - DS: Disturbance
 - NR: Not Rated
 - SS: Sub Tropical
 - TS: Tropical Storm
- 5. Damage: Financial loss (in Billion U.S. dollars) caused by hurricanes
- 6. **Deaths**: Number of death caused by hurricanes
- 7. Maxspeed: Maximum recorded wind speed of the hurricane
- 8. Meanspeed: average wind speed of the hurricane
- 9. Maxpressure: Maximum recorded central pressure of the hurricane
- 10. **Meanpressure**: average central pressure of the hurricane
- 11. Hours: Duration of the hurricane in hours
- 12. **Total.Pop**: Total affected population
- 13. **Percent.Poor**: % affected population that reside in low GDP countres (i.e. GDP per Capita <= 10.000)
- 14. Percent.USA: % affected population that reside in the United States

EDA

We use a bar plot to examine the number of hurricanes in each month. From Figure 1, we can see that September is the month with the most hurricanes, while there are no hurricanes in February and March. Hurricanes in September also have the highest average wind speed as we can see in Figure 2.

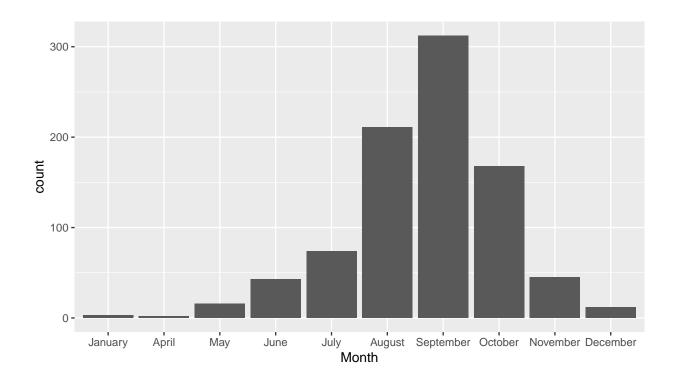


Figure 1. Count of Hurricanes in Each Month

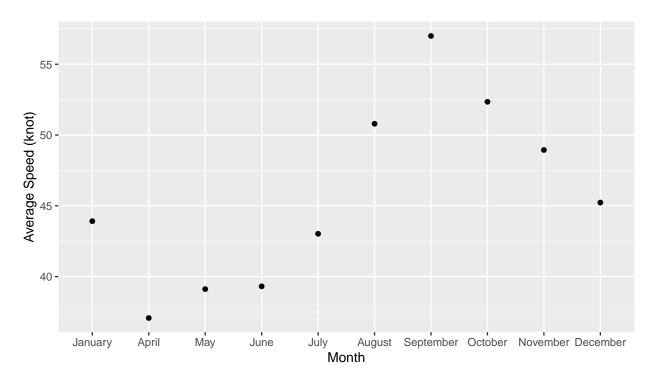


Figure 2. Average Speed (knot) of Hurricanes in Each Month

If we group the hurricanes by years, we can see in general, we have more observations in recently years compared to 50 years ago as shown in Figure 3. However, from Figure 4, the average wind speed seems to have a decreasing trend.

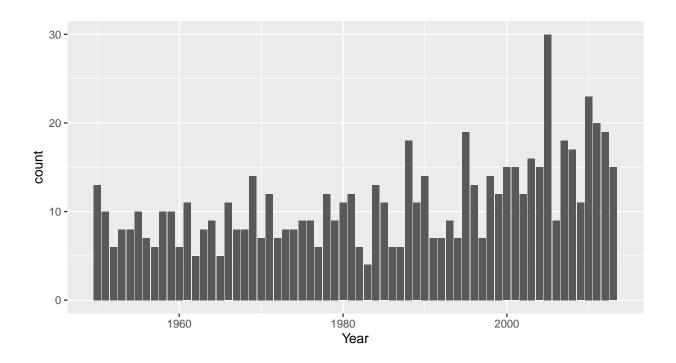


Figure 3. Count of Hurricanes in Each Year

'geom_smooth()' using formula 'y ~ x'

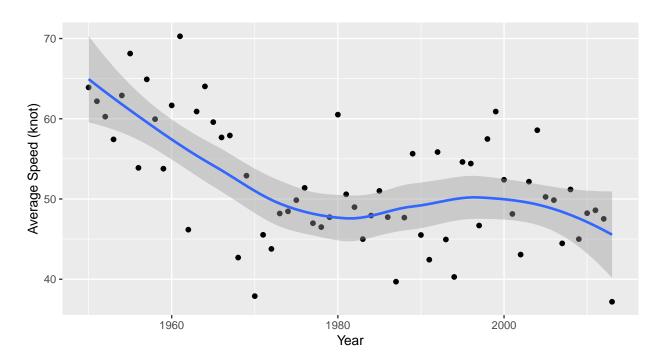


Figure 4. Average Speed (knot) of Hurricanes in Each Year

We also compare the hurricanes with different natures. In our dataset, there are 1214 different nature ratings. This number is larger than the number of hurricanes because some hurricanes are in different natures at

different time. From Figure 5, we know that more than half of the natures are in Tropical Storm category. This nature also have the highest average wind speed at about 60 knot, while the disturbance and not rated hurricanes have average wind speed at round 20 knot as Figure 6 illustrates.

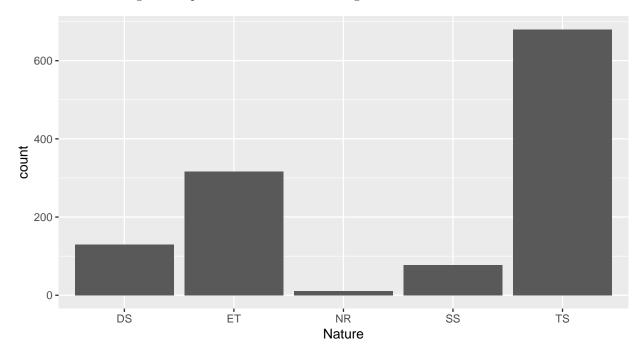


Figure 5. Count of Hurricanes in Each Nature

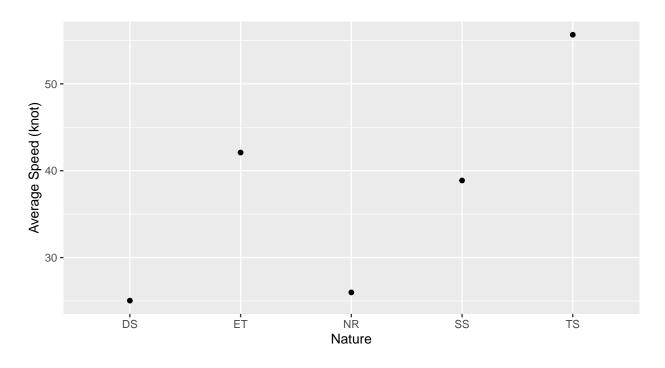


Figure 6. Average Speed (knot) of Hurricanes in Each Nature

MCMC

Markov Chain Monte Carlo is combined by two methods, Markov Chain and Monte Carlo Method. Monte Carlo is a random sampling method for approximating a desired quantity, whereas Markov Chain generates a sequence of random variables where the current state only depends on the nearest past in the chain. MCMC algorithm draws samples from Markov Chain successively leading us close to the desired posterior. Two commonly used MCMC algorithm are the Metropolis-Hastings Algorithm and the Gibbs Sampler. Here, we implement the Gibbs Sampler here since we can save much computation cost compared to Metropolis-Hastings Algorithm.

Gibbs Sampler

Gibbs Sampler is one of Bayesian MCMC approaches with known conditional distributions. By sampling from each random variables given all the others, and changing one random variable at a time, Gibbs Sampler is able to draw parameter samples from the joint distribution. Then given proper starting value, the Markov Chain can reach its stationary distribution.

Model Performance

We evaluate the performance of predictive ability by calculating the RMSE and the R^2 values for each hurricane. The residuals of Bayesian estimates that converged after iterations from MCMC will be used to predict the wind speed of test dataset. The overall R^2 is 0.822 and overall RMSE is 4.51. The valid R^2 is filtered with values between 0 and 1 and we get 77.5% hurricanes (540) indicating that 22.5% of the estimated Bayesian models do not track hurricanes well and have negative R^2 . One of the reason may be the limited number of observations of the hurricanes. Figure 7 shows the 10 hurricanes with the least 10 RMSE. R^2 are also large enough to indicates that the estimated model track most hurricanes well and the smallest RMSE is GUSTAV.1996 with R^2 being 0.952.

ID	r_square	rmse
GUSTAV.1996	0.952	0.537
LORENZO.2001	0.914	0.733
ERIN.2013	0.878	0.823
JOSE.2011	0.970	0.872
GRETA.1970	0.980	0.876
DELTA.1972	0.825	0.904
EDITH.1967	0.826	0.983
FABIAN.1997	0.955	1.002
DEBBY.2006	0.984	1.045
CRISTOBAL.2002	0.956	1.053

Figure 7. R-square and RMSE for prediction result on test data

Figure 8 shows the actual wind speed and the estimated wind speed of randomly selected four hurricanes. We can see that most parts of the two curves overlapped indicating that the predicted values are close to the actual values. In DEBBY.2006, we can see that this is a very good model prediction with small deviation.

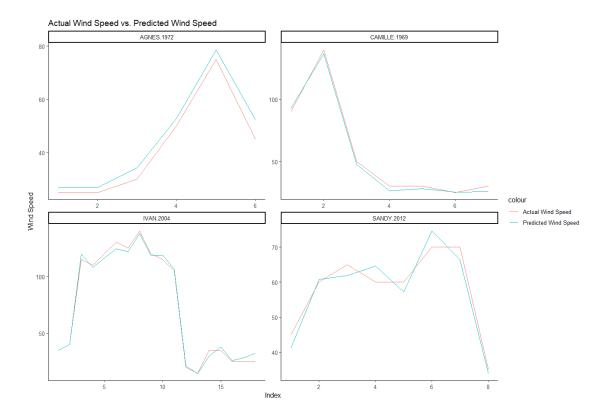


Figure 8. Actual Wind Speed vs. Predicted Wind Speed

Explore the seasonal differences and wind speed change

Now based on the estimated Bayesion model from previous questions, we need to explore the seasonal difference. We can fit 5 models using 5 estimated beta values against the three predictors: $X_{i,1}$: the month of the year the ith hurricane started, $X_{i,2}$:the year of the ith hurricane and $X_{i,3}$: the nature of the ith hurricane. The beta values obtained from previous Gibbs Sampler MCMC method contains the mean value of $\beta_{0,i}$, $\beta_{1,i}$, $\beta_{2,i}$, $\beta_{3,i}$ and $\beta_{4,i}$ for each of the 697 unique hurricanes, which is of the size 697 * 5.

According to the summary, the R squared value for all the five fitted linear models are quite small, which may indicate bad fit. In addition, most coefficients for the model are not significant with a p-value larger than 0.05. However, for those significant coefficients, we could infer a potential relationship between the certain predictors and the beta coefficients respectively. We should consult the previous Bayesion model:

$$Y_i(t+6) = \beta_{0,i} + \beta_{1,i}Y_i(t) + \beta_{2,i}\Delta_{i,1}(t) + \beta_{3,i}\Delta_{i,2}(t) + \beta_{4,i}\Delta_{i,3}(t) + \epsilon_i(t)$$

to interpret the change of the influence on $Y_{i,t+6}$ as the value of the predictor changes.

For the fitted coefficients of β_0 to β_4 , the intercept cannot show information about seasonal difference since they indicate when holding all the predictors zero, the value for the corresponding β . We can only observe that the year is quite significant in the model for β_0 , β_1 with both negative estimates close to zero. Therefore, as the year increase, the coefficient of the intercept and $Y_{i,t}$ may decrease a little, which means for the Bayesian model, the wind speed when holding all the variables zero and the effect the previous wind speed has will decrease over years. Apart from seasonal difference, some other predictors are quite significant, such as natureET for β_2 , natureTS for β_3 .

##

Attaching package: 'kableExtra'

	Estimate	Pr(> t)								
(Intercept)	4.481	0.000	1.343	0.000	0.041	0.951	-0.834	0.019	0.289	0.448
monthApril	0.023	0.835	0.015	0.670	0.017	0.931	0.042	0.680	0.036	0.739
monthMay	0.026	0.783	0.000	0.997	0.071	0.660	0.063	0.458	-0.016	0.859
monthJune	0.028	0.765	0.005	0.851	-0.007	0.964	0.056	0.505	0.024	0.792
monthJuly	0.013	0.891	0.015	0.590	-0.009	0.954	0.036	0.664	0.013	0.884
monthAugust	-0.020	0.828	0.023	0.412	-0.052	0.738	0.012	0.881	0.031	0.726
monthSeptember	-0.007	0.938	0.026	0.359	-0.036	0.817	0.021	0.797	0.044	0.618
monthOctober	0.009	0.919	0.021	0.459	-0.029	0.855	0.034	0.680	0.035	0.694
monthNovember	0.015	0.875	0.025	0.393	0.024	0.879	0.026	0.753	0.021	0.817
monthDecember	0.006	0.953	0.009	0.772	-0.054	0.745	0.042	0.633	0.011	0.905
year	0.000	0.072	0.000	0.000	0.000	0.910	0.000	0.203	0.000	0.625
natureET	0.001	0.977	0.004	0.688	-0.070	0.169	-0.026	0.329	-0.021	0.473
natureNR	0.001	0.987	-0.015	0.333	0.006	0.943	0.003	0.944	-0.022	0.646
natureSS	0.014	0.490	-0.003	0.602	-0.001	0.969	0.013	0.496	-0.024	0.234
natureTS	0.012	0.479	-0.006	0.249	-0.015	0.588	-0.023	0.126	-0.017	0.283

response	coefficient	Estimate	Pr(> t)
β_0	Intercept	3.837	0.000
β_0	seasonSummer	-0.031	0.205
β_0	seasonAutumn	-0.024	0.325
β_0	seasonWinter	-0.019	0.654
β_1	Intercept	0.894	0.000
β_1	seasonSummer	0.015	0.044
β_1	season Autumn	0.021	0.005
β_1	seasonWinter	0.003	0.794
β_2	Intercept	0.161	0.000
β_2	seasonSummer	-0.098	0.017
β_2	seasonAutumn	-0.091	0.025
β_2	seasonWinter	-0.098	0.164
β_3	Intercept	-0.350	0.000
β_3	seasonSummer	-0.047	0.034
β_3	seasonAutumn	-0.043	0.046
β_3	seasonWinter	-0.009	0.802
β_4	Intercept	0.442	0.000
β_4	seasonSummer	0.036	0.120
β_4	season Autumn	0.049	0.035
β_4	seasonWinter	0.015	0.711

```
## The following object is masked from 'package:dplyr':
##
group_rows
```

Table 99. Coefficients of the fitted β model against three predictors

We also try to represent the months as four seasons and fit a model for β against them. Each model has three dummy variables corresponding to the three seasons except Spring. The latter three rows of estimate shows how the value of β differentiate between Spring and the other three seasons respectively. If with a rather small p-value, we can conclude the existence of seasonal difference. Therefore, by constructing model in this way, we find that β_1 and β_4 will increase a little as season changes from Spring to Summer, then to Autumn, which means a season difference of the effect $Y_{i,t}$ and $\Delta_{i,3}(t)$ has on the wind speed. For β_2 , β_3 , Summer and Autumn may lead to a slightly smaller effect of $\Delta_{i,1}(t)$, $\Delta_{i,2}(t)$ have on the wind speed compared to Spring.

Table 99. Coefficients of the fitted β model against season

Now fit linear models for β against the season variables (corresponding to the year) to seek for potential evidence of the statement: "the wind speed has been increasing over years". In order to analyze this question, need to inspect on model which corresponds to the wind speed and the year. For β_2 model, the estimate of year is significant, although it's really close to zero. Therefore, we can infer that as the year increases, the impact past wind speed has on the current wind speed may decrease a little, which cannot provide support for the statement. However, it's quite match with the results shown in the figures in the initial EDA session, which indicates the mean wind speed tends to decrease over years.

response	coefficient	Estimate	$\Pr(> t)$
β_0	Intercept	4.514	0.000
β_0	year	0.000	0.050
β_1	Intercept	1.345	0.000
β_1	year	0.000	0.000
β_2	Intercept	-0.106	0.863
β_2	year	0.000	0.776
β_3	Intercept	-1.027	0.002
β_3	year	0.000	0.053
β_4	Intercept	0.305	0.382
β_4	year	0.000	0.607

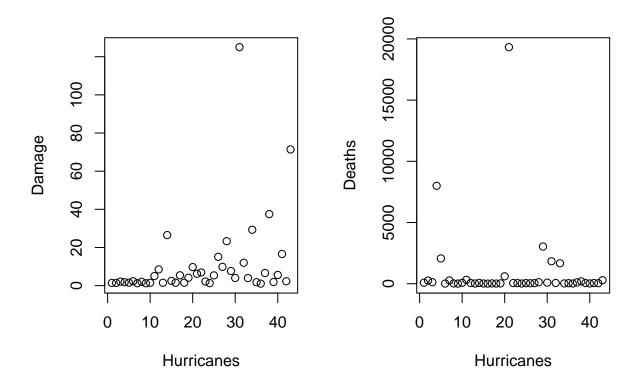
Table 99. Coefficients of the fitted β model against year

In conclusion, for different months, there is no significant differences observed. Over years, the effect the wind speed 6 months ago has on the current wind speed may decrease a little. And there is no evidence to support the statement in task 5.

Predict the hurricane-induced damage and deaths

Firstly, we plot deaths and financial loss separately. Figure 99. shows the distributions of deaths and damage. We could easily find a few points which are far away from most of the points indicate serious damage of society. In predictions of disasters, these extreme points are important because they enable the model to predict the worst outcome. Therefore, we keep these points in model building.

Figure 99. Distributions of Damage and Deaths



In order to build a model that combines information in original data and the estimated coefficients from the Bayesian model, we extract the coefficients from the previous results. By taking the average of β_i at different time points, we obtain $\beta_0 \sim \beta_4$ of each hurricane. Part of the results is shown in Table 99.

Table 99. Coefficients of Each Hurricane

id	intercept	beta1	beta2	beta3	beta4
agnes.1972	3.950974	0.9224097	0.0059532	-0.3103372	0.5453543
alex.2010	3.798737	0.9370333	0.0698849	-0.3937358	0.5400187
alicia.1983	3.897408	0.9036878	-0.0748341	-0.3994486	0.5477718
allen.1980	3.687070	0.9655304	0.1306393	-0.5460144	0.5466129
andrew.1992	3.676279	0.9375384	-0.2843257	-0.5782973	0.5370158
betsy.1965	3.808396	0.9513766	-0.4500720	-0.3890718	0.4244575
bob.1991	3.629466	0.9232143	0.0279527	-0.5751636	0.4382048
camille.1969	3.994355	0.9355674	0.0729188	-0.5734830	0.6703910
charley.2004	3.638829	0.9482764	-0.1797332	-0.6955016	0.1818395
david.1979	3.789678	0.9579657	-0.0461134	-0.3823658	0.6853938

Fortunately, 43 hurricanes recorded in *hurricanoutcome2.csv* are also in *hurrican703.csv*. Thus, we merge two data frame by hurricane id to predict the deaths and damage caused by hurricanes.

The death variable is a count variable, so we decided to use Poisson regression to analysis relationship between death and other variables excluding damage. We use Total.Pop and Hours as the offset, since the outcome of deaths is proportional and the results would be different in some dimension (different populations, different duration). The Poisson regression is:

$$log(E(Deaths)) = \beta_i X_i + offset$$

Where X_i indicates all predictors included in the model. We use glm function to achieve the Poisson model. The coefficients result is in Table 99.

Table 99. Coefficients of Deaths Prediction

	Estimate	Std. Error	z value	$\Pr(> z)$
(Intercept)	272.6548414	11.9772996	22.764300	0.0000000
intercept	12.8670811	0.2681866	47.978086	0.0000000
beta1	139.3302799	2.2527075	61.850143	0.0000000
beta2	6.2673041	0.1222299	51.274709	0.0000000
beta3	11.6385648	0.3090069	37.664416	0.0000000
beta4	-15.5433361	0.3093214	-50.249788	0.0000000
nobs	-0.0259659	0.0011052	-23.494615	0.0000000
Season	-0.0101636	0.0022226	-4.572917	0.0000048
MonthJuly	-2.6409629	0.1476034	-17.892292	0.0000000
MonthJune	-0.3043892	0.0911374	-3.339894	0.0008381
MonthNovember	-3.0007313	0.1534637	-19.553361	0.0000000
MonthOctober	-2.1031926	0.0625508	-33.623762	0.0000000
MonthSeptember	-0.6480044	0.0473666	-13.680606	0.0000000
NatureNR	2.1051263	0.1265128	16.639630	0.0000000
NatureTS	4.2677929	0.1266627	33.694166	0.0000000
Maxspeed	0.0099355	0.0010283	9.661642	0.0000000
Meanspeed	-0.0634120	0.0033070	-19.175107	0.0000000
Maxpressure	-0.4345774	0.0087466	-49.685178	0.0000000
Meanpressure	0.0092073	0.0002035	45.253527	0.0000000
Percent.Poor	0.0520424	0.0008541	60.929497	0.0000000
Percent.USA	-0.0206136	0.0005851	-35.231400	0.0000000

From the results, $\beta_0 \sim \beta_4$ indicate the relatively strong association. Especially, β_1 , which represents the earlier wind speed has the biggest coefficient. We could conclude that high wind speed of hurricane more easily leads to serious casualties. Also, months seem to be an important factor in prediction. Comparing to June and September, July, November and October have lower proportion of death given all other variables constant.

In order to obtain the integer data, we transform the units of Damage from billion to million. Thus, Damage could be regarded as a count variable which could also be fitted by Poisson regression. In order to adjust the exposure, we use Hours as the offset.

$$log(E(Damage * 1000)) = \beta_i X_i + offset$$

Where X_i presents all predictors included in the model. We use glm function to achieve the Poisson model. The coefficients results is in Table 99.

Warning: package 'broom' was built under R version 4.1.3

estimate	std.error	statistic	p.value
-206.5342295	2.0185627	-102.317470	0.00e+00
4.7792873	0.0279968	170.708107	0.00e+00
60.3768193	0.4513469	133.770326	0.00e+00
-1.0909958	0.0132414	-82.392801	0.00e+00
3.6396116	0.0259580	140.211430	0.00e+00
-1.6090883	0.0335258	-47.995549	0.00e+00
0.0308929	0.0002582	119.662746	0.00e+00
0.0757660	0.0003973	190.691693	0.00e+00
0.4806325	0.0187755	25.598871	0.00e+00
-3.2641224	0.0241511	-135.154056	0.00e+00
-1.8378419	0.0249958	-73.526098	0.00e+00
-1.3044789	0.0094414	-138.165832	0.00e+00
-1.7755988	0.0077805	-228.211660	0.00e+00
-4.2815939	0.0356423	-120.126833	0.00e+00
-1.9548375	0.0143805	-135.936287	0.00e+00
0.0507898	0.0002142	237.112410	0.00e+00
-0.0644452	0.0004911	-131.235042	0.00e+00
-0.0140045	0.0012224	-11.456463	0.00e+00
-0.0001769	0.0000407	-4.351453	1.35e-05
0.0000003	0.0000000	62.112535	0.00e+00
-0.0384685	0.0001886	-203.998906	0.00e+00
-0.0049715	0.0000729	-68.209623	0.00e+00
	4.7792873 60.3768193 -1.0909958 3.6396116 -1.6090883 0.0308929 0.0757660 0.4806325 -3.2641224 -1.8378419 -1.3044789 -1.7755988 -4.2815939 -1.9548375 0.0507898 -0.0644452 -0.0140045 -0.0001769 0.0000003 -0.0384685	-206.5342295 2.0185627 4.7792873 0.0279968 60.3768193 0.4513469 -1.0909958 0.0132414 3.6396116 0.0259580 -1.6090883 0.0335258 0.0308929 0.0002582 0.0757660 0.0003973 0.4806325 0.0187755 -3.2641224 0.0241511 -1.8378419 0.0249958 -1.3044789 0.0094414 -1.7755988 0.0077805 -4.2815939 0.0356423 -1.9548375 0.0143805 0.0507898 0.0002142 -0.0644452 0.0004911 -0.0140045 0.0012224 -0.0001769 0.0000000 -0.0384685 0.0001886	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$

The results of coefficients in predicting damage also show the importance of β_1 . From the model, we can see that serious casualties are also accompanied by serious financial losses which are strongly influenced by earlier wind speed and are slightly affected by months, latitude change, longitude change and wind speed change. $\beta_0 \sim \beta_4$ are generally powerful in damage and deaths prediction.

Appendix

Model Performance

```
beta.res.postmean = beta.res.postmean %>% rename(beta_0 = intercept,
                                                 beta_1 = Wind_prev,
                                                 beta_2 = Lat_change,
                                                 beta_3 = Long_change,
                                                 beta_4 = Wind_change)
dt_res = merge(dt_test_id, beta.res.postmean, by = "ID")
dt res = dt res %>%
 mutate(Wind_kt_pred = beta_0*intercept+beta_1*Wind_prev
         +beta_2*Lat_change+beta_3*Long_change+beta_4*Wind_change) %>%
  group_by(ID) %>%
 mutate(r_square = 1-(sum((Wind_kt_pred-Wind.kt)^2))/(sum((Wind.kt-mean(Wind.kt))^2)),
        rmse = rmse(Wind.kt,Wind_kt_pred))
 dt rmse=
 dt_res %>%
  dplyr::select(ID, r_square, rmse) %>%
  distinct() %>%
 mutate(r_square = round(r_square, 3),
         rmse = round(rmse,3)) %>%
 filter(r_square > 0 && r_square < 1) %>%
```

Seasonal Difference

arrange(rmse)
mean(dt_rmse\$r_square)
mean(dt_rmse\$rmse)

```
load("./dt_long.RData")
load("./ID_in.RData")
load("./beta.res.postmean.RData")
dt season <-
 dt_long %>%
 drop_na() %>%
 filter(ID %in% ID_in) %>%
 distinct(ID, .keep_all = TRUE) %>%
  select(ID, Season, Month, Nature) %>%
 mutate(Month = factor(Month, levels = month.name))
season diff <-
 merge(dt_season, beta.res.postmean, by = c("ID")) %>%
  janitor::clean names()
colnames(season_diff)[2] <- "year"</pre>
# BetaO
intercept.fit <- lm(intercept ~ month + year + nature, data = season_diff)</pre>
wind_prev.fit <- lm(wind_prev ~ month + year + nature, data = season_diff)</pre>
# Beta2
```

```
lat_change.fit <- lm(lat_change ~ month + year + nature, data = season_diff)</pre>
# Beta3
long_change.fit <- lm(long_change ~ month + year + nature, data = season_diff)</pre>
wind_change.fit <- lm(wind_change ~ month + year + nature, data = season_diff)</pre>
summary(intercept.fit)
summary(wind prev.fit)
summary(lat change.fit)
summary(long change.fit)
summary(wind_change.fit)
sum0 <- summary(intercept.fit)$coefficients[,c(1,4)]</pre>
sum1 <- summary(wind_prev.fit)$coefficients[,c(1,4)]</pre>
sum2 <- summary(lat_change.fit)$coefficients[,c(1,4)]</pre>
sum3 <- summary(long_change.fit)$coefficients[,c(1,4)]</pre>
sum4 <- summary(wind_change.fit)$coefficients[,c(1,4)]</pre>
kable(cbind(sum0, sum1, sum2, sum3, sum4)) %>%
 kable_styling(bootstrap_options = c("striped", "hover", "condensed")) %%
 add_header_above(c(" " = 1, "Beta 0" = 2, "Beta 1" = 2, "Beta 2" = 2, "Beta 3" = 2, "Beta 4" = 2))
# Try to fit the beta model only with the four seasons
season diff <- as.data.frame(season diff) %>%
  mutate(month = recode(month, April = "Spring"),
       month = recode(month, May = "Spring"),
       month = recode(month, June = "Summer"),
       month = recode(month, July = "Summer"),
       month = recode(month, August = "Summer"),
       month = recode(month, September = "Autumn"),
       month = recode(month, October = "Autumn"),
       month = recode(month, November = "Autumn"),
       month = recode(month, December = "Winter"),
       month = recode(month, January = "Winter"),
       month = factor(month, levels = c("Spring", "Summer", "Autumn", "Winter")))
colnames(season diff)[3] <- "season"</pre>
# Beta0
intercept.fit.2 <- lm(intercept ~ season, data = season_diff)</pre>
wind_prev.fit.2 <- lm(wind_prev ~ season, data = season_diff)</pre>
# Beta2
lat_change.fit.2 <- lm(lat_change ~ season, data = season_diff)</pre>
# Beta3
long_change.fit.2 <- lm(long_change ~ season, data = season_diff)</pre>
wind_change.fit.2 <- lm(wind_change ~ season, data = season_diff)</pre>
sum0_2 <- summary(intercept.fit.2)$coefficients[,c(1,4)]</pre>
sum1_2 <- summary(wind_prev.fit.2)$coefficients[,c(1,4)]</pre>
sum2_2 <- summary(lat_change.fit.2)$coefficients[,c(1,4)]</pre>
sum3 2 <- summary(long change.fit.2)$coefficients[,c(1,4)]</pre>
sum4_2 <- summary(wind_change.fit.2)$coefficients[,c(1,4)]</pre>
```

```
kable(cbind(sum0_2, sum1_2, sum2_2, sum3_2, sum4_2)) %>%
  kable_styling(bootstrap_options = c("striped", "hover", "condensed")) %>%
  add_header_above(c(" " = 1, "Beta 0" = 2, "Beta 1" = 2, "Beta 2" = 2, "Beta 3" = 2, "Beta 4" = 2))
# Try to fit the beta model only with the year
# Beta0
intercept.fit.new <- lm(intercept ~ year, data = season_diff)</pre>
wind_prev.fit.new <- lm(wind_prev ~ year, data = season_diff)</pre>
lat_change.fit.new <- lm(lat_change ~ year, data = season_diff)</pre>
# Beta3
long_change.fit.new <- lm(long_change ~ year, data = season_diff)</pre>
#Beta4
wind_change.fit.new <- lm(wind_change ~ year, data = season_diff)</pre>
summary(intercept.fit.new)
summary(wind_prev.fit.new)
summary(lat_change.fit.new)
summary(long_change.fit.new)
summary(wind_change.fit.new)
sum0.new <- summary(intercept.fit.new)$coefficients[,c(1,4)]</pre>
sum1.new <- summary(wind_prev.fit.new)$coefficients[,c(1,4)]</pre>
sum2.new <- summary(lat_change.fit.new)$coefficients[,c(1,4)]</pre>
sum3.new <- summary(long_change.fit.new)$coefficients[,c(1,4)]</pre>
sum4.new <- summary(wind_change.fit.new)$coefficients[,c(1,4)]</pre>
kable(cbind(sum0.new, sum1.new, sum2.new, sum3.new, sum4.new)) %>%
  kable_styling(bootstrap_options = c("striped", "hover", "condensed")) %>%
  add_header_above(c(" " = 1, "Beta 0" = 2, "Beta 1" = 2, "Beta 2" = 2, "Beta 3" = 2, "Beta 4" = 2))
```