

Functional Programming: Exercise 3

Sheet published: Thursday, May 2nd

Submission deadline: Wednesday, May 8th, 12:00 noon

Exercise 3.1 (Skeleton: `Lists.hs`). Solve the following tasks using the *List Design Pattern*, i.e. write recursive functions and do not use any library functions.

- a) Write a function $\text{prod} :: [Integer] \rightarrow Integer$ that computes the product of a list of numbers.
- b) Write a function $\text{contains} :: Integer \rightarrow [Integer] \rightarrow Bool$ that checks whether the given number is contained in the list.
- c) Write a function $\text{nth} :: Integer \rightarrow [a] \rightarrow Maybe a$ that takes an index n and a list of elements and returns the n th element of the list (if the index is valid) or *Nothing* if the index is invalid.
- d) Write a function $\text{remove} :: Integer \rightarrow [Integer] \rightarrow [Integer]$ that takes a number x and a list of numbers and returns the list where all occurrences of x are removed.
- e) Write a function $\text{suffixes} :: [a] \rightarrow [[a]]$ that takes a list and returns the list of all suffixes, starting with the list itself and ending with an empty list. For example:
 $\text{suffixes } [1, 2, 3] = [[1, 2, 3], [2, 3], [3], []]$.

Exercise 3.2 (Skeleton: `Comprehensions.hs`). Solve the following tasks using the *List Comprehensions*, do not use *map*, *filter* or *concat*.

- a) Write a function $f :: [(Bool, a)] \rightarrow [a]$ that takes a list of pairs and returns only those elements where the first component is *True*.
- b) Write a function $g :: [(a, b)] \rightarrow [(b, a)]$ that swaps the all pairs in the given list.
- c) Write a function $h :: [(Integer, a)] \rightarrow [a]$ that takes a list of components (n, x) and returns a list where each element x is repeated n times. For example:
 $h [(3, 'a'), (2, 'b'), (4, 'z')] = \text{"aaabbzzzz"}$. Do not use *replicate*, think of another way to repeat the elements.

Exercise 3.3 (Skeleton: `HigherOrder.hs`). Solve the previous task without list comprehensions, instead use the functions *map*, *filter* and *concat*.