Spatstat Quick Reference guide

December 31, 2014

spatstat-package

The Spatstat Package

Description

This is a summary of the features of **spatstat**, a package in R for the statistical analysis of spatial point patterns.

Details

spatstat is a package for the statistical analysis of spatial data. Currently, it deals mainly with the analysis of spatial patterns of points in two-dimensional space. The points may carry auxiliary data ('marks'), and the spatial region in which the points were recorded may have arbitrary shape.

The package supports

- creation, manipulation and plotting of point patterns
- exploratory data analysis
- · simulation of point process models
- parametric model-fitting
- · hypothesis tests and model diagnostics

Apart from two-dimensional point patterns and point processes, **spatstat** also supports point patterns in three dimensions, point patterns in multidimensional space-time, point patterns on a linear network, patterns of line segments in two dimensions, and spatial tessellations and random sets in two dimensions.

The package can fit several types of point process models to a point pattern dataset:

- Poisson point process models (by Berman-Turner approximate maximum likelihood or by spatial logistic regression)
- Gibbs/Markov point process models (by Baddeley-Turner approximate maximum pseudolikelihood, Coeurjolly-Rubak logistic likelihood, or Huang-Ogata approximate maximum likelihood)

 Cox/cluster process models (by Waagepetersen's two-step fitting procedure and minimum contrast, or by composite likelihood)

The models may include spatial trend, dependence on covariates, and complicated interpoint interactions. Models are specified by a formula in the R language, and are fitted using a function analogous to lm and glm. Fitted models can be printed, plotted, predicted, simulated and so on.

Getting Started

For a quick introduction to **spatstat**, see the package vignette *Getting started with spatstat* installed with **spatstat**. (To see this document online, start R, type help.start() to open the help browser, and navigate to Packages > spatstat > Vignettes).

For a complete 2-day course on using **spatstat**, see the workshop notes by Baddeley (2010), available on the internet. (This is now somewhat out-of-date but it will get you started.)

Type demo(spatstat) for a demonstration of the package's capabilities. Type demo(data) to see all the datasets available in the package.

For information about handling data in **shapefiles**, see the Vignette *Handling shapefiles in the spat-stat package* installed with **spatstat**.

To learn about spatial point process methods, see the short book by Diggle (2003) and the handbook Gelfand et al (2010).

Updates

New versions of **spatstat** are produced about once a month. Users are advised to update their installation of **spatstat** regularly.

Type latest.news to read the news documentation about changes to the current installed version of **spatstat**.

See the Vignette *Summary of recent updates*, installed with **spatstat**, which describes the main changes to **spatstat** since the workshop notes were published in 2010,

Type news(package="spatstat") to read news documentation about all previous versions of the package.

FUNCTIONS AND DATASETS

Following is a summary of the main functions and datasets in the **spatstat** package. Alternatively an alphabetical list of all functions and datasets is available by typing library(help=spatstat).

For further information on any of these, type help(name) where name is the name of the function or dataset.

CONTENTS:

- I. Creating and manipulating data
- II. Exploratory Data Analysis
- III. Model fitting (cluster models)
- IV. Model fitting (Poisson and Gibbs models)
- V. Model fitting (spatial logistic regression)
- VI. Simulation

VII. Tests and diagnosticsVIII. Documentation

I. CREATING AND MANIPULATING DATA

Types of spatial data:

The main types of spatial data supported by **spatstat** are:

ppp point pattern
owin window (spatial region)
im pixel image
psp line segment pattern
tess tessellation
pp3 three-dimensional point pattern
ppx point pattern in any number of dimensions
1pp point pattern on a linear network

To create a point pattern:

ppp create a point pattern from (x,y) and window information ppp(x, y, xlim, ylim) for rectangular window ppp(x, y, poly) for polygonal window ppp(x, y, mask) for binary image window as.ppp convert other types of data to a ppp object clickppp interactively add points to a plot attach/reassign marks to a point pattern

To simulate a random point pattern:

runifpoint	generate n independent uniform random points
rpoint	generate n independent random points
rmpoint	generate n independent multitype random points
rpoispp	simulate the (in)homogeneous Poisson point process
rmpoispp	simulate the (in)homogeneous multitype Poisson point process
runifdisc	generate n independent uniform random points in disc
rstrat	stratified random sample of points
rsyst	systematic random sample of points
rjitter	apply random displacements to points in a pattern
rMaternI	simulate the Matérn Model I inhibition process
rMaternII	simulate the Matérn Model II inhibition process
rSSI	simulate Simple Sequential Inhibition process
rStrauss	simulate Strauss process (perfect simulation)
rHardcore	simulate Hard Core process (perfect simulation)
rDiggleGratton	simulate Diggle-Gratton process (perfect simulation)
rDGS	simulate Diggle-Gates-Stibbard process (perfect simulation)
rNeymanScott	simulate a general Neyman-Scott process

rPoissonCluster simulate a general Poisson cluster process simulate the Matérn Cluster process rThomas simulate the Thomas process

rGaussPoisson simulate the Gauss-Poisson cluster process rCauchy simulate Neyman-Scott Cauchy cluster process

rVarGamma simulate Neyman-Scott Variance Gamma cluster process

rthin random thinning

rcell simulate the Baddeley-Silverman cell process

rmh simulate Gibbs point process using Metropolis-Hastings simulate.ppm simulate Gibbs point process using Metropolis-Hastings generate n random points along specified line segments generate Poisson random points along specified line segments

To randomly change an existing point pattern:

rshift random shifting of points

rjitter apply random displacements to points in a pattern

rthin random thinning

rlabel random (re)labelling of a multitype point pattern

quadratresample block resampling

Standard point pattern datasets:

Datasets in **spatstat** are lazy-loaded, so you can simply type the name of the dataset to use it; there is no need to type data(amacrine) etc.

Type demo(data) to see a display of all the datasets installed with the package.

amacrine
Austin Hughes' rabbit amacrine cells
anemones
Upton-Fingleton sea anemones data
Harkness-Isham ant nests data
Transical print process transport

bei Tropical rainforest trees

betacells Waessle et al. cat retinal ganglia data

bramblecanes Bramble Canes data
bronzefilter Bronze Filter Section data

cells Crick-Ripley biological cells data

chicago Chicago street crimes
chorley Chorley-Ribble cancer data
clmfires Castilla-La Mancha forest fires

copper Berman-Huntington copper deposits data

demohyperSynthetic point patternsdemopatSynthetic point patternfinpinesFinnish Pines datafluInfluenza virus proteins

gordon People in Gordon Square, London

gorillas Gorilla nest sites

hamster Aherne's hamster tumour data

humberside North Humberside childhood leukaemia data

hyytiala Mixed forest in Hyytiälä, Finland

Japanese Pines data japanesepines lansing Lansing Woods data Longleaf Pines data longleaf Cells in gastric mucosa mucosa murchison Murchison gold deposits nbfires New Brunswick fires data nztrees Mark-Esler-Ripley trees data Osteocyte lacunae (3D, replicated) osteo Kimboto trees in Paracou, French Guiana paracou Getis-Franklin ponderosa pine trees data ponderosa pyramidal Pyramidal neurons from 31 brains Strauss-Ripley redwood saplings data redwood redwoodfull Strauss redwood saplings data (full set) Data from Baddeley et al (2005) residualspaper Galaxies in an astronomical survey shapley

simulated point pattern (inhomogeneous, with interaction)

sporophores Mycorrhizal fungi around a tree

spruces Spruce trees in Saxonia

swedishpines Strand-Ripley Swedish pines data

urkiola Urkiola Woods data

waka Trees in Waka national park waterstriders Insects on water surface

To manipulate a point pattern:

plot.ppp	plot a point pattern (e.g. plot(X))
iplot	plot a point pattern interactively

[.ppp extract or replace a subset of a point pattern

pp[subset] or pp[subwindow]

subset.ppp extract subset of point pattern satisfying a condition

superimpose combine several point patterns

by .ppp apply a function to sub-patterns of a point pattern

cut.ppp classify the points in a point pattern split.ppp divide pattern into sub-patterns

unmark remove marks

npoints count the number of points

coords extract coordinates, change coordinates
marks extract marks, change marks or attach marks

rotate rotate pattern shift translate pattern

flipxy swap x and y coordinates reflect reflect in the origin

periodify make several translated copies affine apply affine transformation scalardilate apply scalar dilation

density.ppp kernel estimation of point pattern intensity
Smooth.ppp kernel smoothing of marks of point pattern

nnmark mark value of nearest data point

sharpen.ppp data sharpening

identify.ppp interactively identify points remove duplicate points unique.ppp determine which points are duplicates duplicated.ppp connected.ppp find clumps of points dirichlet compute Dirichlet-Voronoi tessellation delaunay compute Delaunay triangulation delaunay.distance graph distance in Delaunay triangulation convexhull compute convex hull discretise discretise coordinates pixellate.ppp approximate point pattern by pixel image as.im.ppp approximate point pattern by pixel image

See spatstat.options to control plotting behaviour.

To create a window:

An object of class "owin" describes a spatial region (a window of observation).

Create a window object owin owin(xlim, ylim) for rectangular window owin(poly) for polygonal window owin(mask) for binary image window Window Extract window of another object Extract the containing rectangle ('frame') of another object Frame as.owin Convert other data to a window object make a square window square disc make a circular window Ripley-Rasson estimator of window, given only the points ripras compute convex hull of something convexhull polygonal window in the shape of the R logo letterR interactively draw a polygonal window clickpoly interactively draw a rectangle clickbox

To manipulate a window:

plot.owin	plot a window.
	plot(W)
boundingbox	Find a tight bounding box for the window
erosion	erode window by a distance r
dilation	dilate window by a distance r
closing	close window by a distance r
opening	open window by a distance r
border	difference between window and its erosion/dilation
complement.owin	invert (swap inside and outside)
simplify.owin	approximate a window by a simple polygon
rotate	rotate window
flipxy	swap x and y coordinates
shift	translate window
periodify	make several translated copies
affine	apply affine transformation

Digital approximations:

as.mask Make a discrete pixel approximation of a given window convert window to pixel image as.im.owin pixellate.owin convert window to pixel image commonGrid find common pixel grid for windows map continuous coordinates to raster locations nearest.raster.point raster x coordinates raster.x raster y coordinates raster.y as.polygonal convert pixel mask to polygonal window

See spatstat.options to control the approximation

Geometrical computations with windows:

```
edges
                   extract boundary edges
                   intersection of two windows
intersect.owin
union.owin
                   union of two windows
setminus.owin
                   set subtraction of two windows
                   determine whether a point is inside a window
inside.owin
                   compute area
area.owin
                   compute perimeter length
perimeter
diameter.owin
                   compute diameter
incircle
                   find largest circle inside a window
                   find connected components of window
connected.owin
eroded.areas
                   compute areas of eroded windows
                   compute areas of dilated windows
dilated.areas
bdist.points
                   compute distances from data points to window boundary
                   compute distances from all pixels to window boundary
bdist.pixels
bdist.tiles
                   boundary distance for each tile in tessellation
distmap.owin
                   distance transform image
distfun.owin
                   distance transform
                   compute centroid (centre of mass) of window
centroid.owin
                   determine whether one window contains another
is.subset.owin
                   determine whether a window is convex
is.convex
convexhull
                   compute convex hull
                   pixel approximation of window
as.mask
as.polygonal
                   polygonal approximation of window
is.rectangle
                   test whether window is a rectangle
is.polygonal
                   test whether window is polygonal
                   test whether window is a mask
is.mask
                   spatial covariance function of window
setcov
                   extract centres of pixels in mask
pixelcentres
```

Pixel images: An object of class "im" represents a pixel image. Such objects are returned by some of the functions in **spatstat** including Kmeasure, setcov and density.ppp.

im create a pixel image as.im convert other data to a pixel image

pixellate	convert other data to a pixel image
as.matrix.im	convert pixel image to matrix
as.data.frame.im	convert pixel image to data frame
plot.im	plot a pixel image on screen as a digital image
contour.im	draw contours of a pixel image
persp.im	draw perspective plot of a pixel image
rgbim	create colour-valued pixel image
hsvim	create colour-valued pixel image
[.im	extract a subset of a pixel image
[<im< td=""><td>replace a subset of a pixel image</td></im<>	replace a subset of a pixel image
rotate.im	rotate pixel image
shift.im	apply vector shift to pixel image
affine.im	apply affine transformation to image
Χ	print very basic information about image X
<pre>summary(X)</pre>	summary of image X
hist.im	histogram of image
mean.im	mean pixel value of image
integral.im	integral of pixel values
quantile.im	quantiles of image
cut.im	convert numeric image to factor image
is.im	test whether an object is a pixel image
interp.im	interpolate a pixel image
blur	apply Gaussian blur to image
Smooth.im	apply Gaussian blur to image
connected.im	find connected components
compatible.im	test whether two images have compatible dimensions
harmonise.im	make images compatible
commonGrid	find a common pixel grid for images
eval.im	evaluate any expression involving images
scaletointerval	rescale pixel values
zapsmall.im	set very small pixel values to zero
levelset	level set of an image
solutionset	region where an expression is true
imcov	spatial covariance function of image
convolve.im	spatial convolution of images
transect.im	line transect of image
pixelcentres	extract centres of pixels

Line segment patterns

An object of class "psp" represents a pattern of straight line segments.

psp create a line segment pattern	
as.psp convert other data into a line segment p	attern
edges extract edges of a window	
is.psp determine whether a dataset has class "	psp"
plot.psp plot a line segment pattern	
print.psp print basic information	
summary.psp print summary information	

[.psp	extract a subset of a line segment pattern
as.data.frame.psp	convert line segment pattern to data frame
marks.psp	extract marks of line segments
marks <psp< td=""><td>assign new marks to line segments</td></psp<>	assign new marks to line segments
unmark.psp	delete marks from line segments
midpoints.psp	compute the midpoints of line segments
endpoints.psp	extract the endpoints of line segments
lengths.psp	compute the lengths of line segments
angles.psp	compute the orientation angles of line segments
superimpose	combine several line segment patterns
flipxy	swap x and y coordinates
rotate.psp	rotate a line segment pattern
shift.psp	shift a line segment pattern
periodify	make several shifted copies
affine.psp	apply an affine transformation
<pre>pixellate.psp</pre>	approximate line segment pattern by pixel image
as.mask.psp	approximate line segment pattern by binary mask
distmap.psp	compute the distance map of a line segment pattern
distfun.psp	compute the distance map of a line segment pattern
density.psp	kernel smoothing of line segments
selfcrossing.psp	find crossing points between line segments
crossing.psp	find crossing points between two line segment patterns
nncross	find distance to nearest line segment from a given point
nearestsegment	find line segment closest to a given point
project2segment	find location along a line segment closest to a given point
pointsOnLines	generate points evenly spaced along line segment
rpoisline	generate a realisation of the Poisson line process inside a window
rlinegrid	generate a random array of parallel lines through a window

Tessellations

An object of class "tess" represents a tessellation.

tess	create a tessellation
quadrats	create a tessellation of rectangles
hextess	create a tessellation of hexagons
as.tess	convert other data to a tessellation
plot.tess	plot a tessellation
tiles	extract all the tiles of a tessellation
[.tess	extract some tiles of a tessellation
[<tess< td=""><td>change some tiles of a tessellation</td></tess<>	change some tiles of a tessellation
intersect.tess	intersect two tessellations
	or restrict a tessellation to a window
chop.tess	subdivide a tessellation by a line
dirichlet	compute Dirichlet-Voronoi tessellation of points
delaunay	compute Delaunay triangulation of points
rpoislinetess	generate tessellation using Poisson line process
tile.areas	area of each tile in tessellation
bdist.tiles	boundary distance for each tile in tessellation

Three-dimensional point patterns

An object of class "pp3" represents a three-dimensional point pattern in a rectangular box. The box is represented by an object of class "box3".

pp3 create a 3-D point pattern plot a 3-D point pattern plot.pp3 coords extract coordinates as.hyperframe extract coordinates subset.pp3 extract subset of 3-D point pattern name of unit of length unitname.pp3 npoints count the number of points generate uniform random points in 3-D runifpoint3 rpoispp3 generate Poisson random points in 3-D generate simulation envelopes for 3-D pattern envelope.pp3 create a 3-D rectangular box box3 convert data to 3-D rectangular box as.box3 name of unit of length unitname.box3 diameter of box diameter.box3 volume.box3 volume of box shortest side of box shortside.box3 eroded.volumes volumes of erosions of box

Multi-dimensional space-time point patterns

An object of class "ppx" represents a point pattern in multi-dimensional space and/or time.

create a multidimensional space-time point pattern ррх coords extract coordinates as.hyperframe extract coordinates subset.ppx extract subset unitname.ppx name of unit of length count the number of points npoints generate uniform random points runifpointx rpoisppx generate Poisson random points boxx define multidimensional box diameter of box diameter.boxx volume.boxx volume of box shortside.boxx shortest side of box eroded.volumes.boxx volumes of erosions of box

Point patterns on a linear network

An object of class "linnet" represents a linear network (for example, a road network).

linnet create a linear network
clickjoin interactively join vertices in network
simplenet simple example of network
lineardisc disc in a linear network
methods.linnet methods for linnet objects

An object of class "lpp" represents a point pattern on a linear network (for example, road accidents on a road network).

lpp	create a point pattern on a linear network
methods.lpp	methods for 1pp objects
subset.lpp	method for subset
rpoislpp	simulate Poisson points on linear network
runiflpp	simulate random points on a linear network
chicago	Chicago street crime data

Hyperframes

A hyperframe is like a data frame, except that the entries may be objects of any kind.

```
hyperframe create a hyperframe
as.hyperframe convert data to hyperframe
plot.hyperframe plot hyperframe
with.hyperframe evaluate expression using each row of hyperframe
cbind.hyperframe combine hyperframes by columns
rbind.hyperframe combine hyperframes by rows
as.data.frame.hyperframe
```

Layered objects

A layered object represents data that should be plotted in successive layers, for example, a background and a foreground.

```
layered create layered object
plot.layered plot layered object
[.layered extract subset of layered object
```

Colour maps

A colour map is a mechanism for associating colours with data. It can be regarded as a function, mapping data to colours. Using a colourmap object in a plot command ensures that the mapping from numbers to colours is the same in different plots.

colourmap	create a colour map
plot.colourmap	plot the colour map only
tweak.colourmap	alter individual colour values
<pre>interp.colourmap</pre>	make a smooth transition between colours
beachcolourmap	one special colour map

II. EXPLORATORY DATA ANALYSIS

Inspection of data:

summary(X)	print useful summary of point pattern X
X	print basic description of point pattern X

> check for duplicated points in pattern X any(duplicated(X)) Interactive exploratory analysis istat(X)

Classical exploratory tools:

clarkevans Clark and Evans aggregation index

fryplot Fry plot

miplot Morisita Index plot

Smoothing:

kernel smoothed density/intensity density.ppp kernel estimate of relative risk relrisk Smooth.ppp spatial interpolation of marks

bw.diggle cross-validated bandwidth selection for density.ppp

bw.ppl likelihood cross-validated bandwidth selection for density.ppp

Scott's rule of thumb for density estimation bw.scott cross-validated bandwidth selection for relrisk bw.relrisk bw.smoothppp cross-validated bandwidth selection for Smooth.ppp bandwidth selection using window geometry bw.frac

bw.stoyan Stoyan's rule of thumb for bandwidth for pcf

Modern exploratory tools:

clusterset Allard-Fraley feature detection Byers-Raftery feature detection nnclean Choi-Hall data sharpening sharpen.ppp Kernel estimate of covariate effect rhohat rho2hat Kernel estimate of covariate effect Spatial cumulative distribution function spatialcdf

Summary statistics for a point pattern: Type demo(sumfun) for a demonstration of many of the summary statistics.

intensity Mean intensity quadratcount Quadrat counts

intensity.quadratcount Mean intensity in quadrats empty space function FFest

nearest neighbour distribution function G Gest J-function J = (1 - G)/(1 - F)Jest

Ripley's K-function Kest Besag L-function Lest Third order T-function Tstat all four functions F, G, J, Kallstats pair correlation function pcf

K for inhomogeneous point patterns Kinhom Linhom L for inhomogeneous point patterns

pcfinhompair correlation for inhomogeneous patternsFinhomF for inhomogeneous point patternsGinhomG for inhomogeneous point patternsJinhomJ for inhomogeneous point patterns

localL Getis-Franklin neighbourhood density function

localK neighbourhood K-function localpcf local pair correlation function

Kest.fft fast K-function using FFT for large datasets

Kmeasure reduced second moment measure

envelope simulation envelopes for a summary function

variances and confidence intervals

for a summary function

lohboot bootstrap for a summary function

Related facilities:

plot.fv plot a summary function evaluate any expression involving summary functions eval.fv harmonise.fv make functions compatible eval.fasp evaluate any expression involving an array of functions evaluate an expression for a summary function with.fv Smooth.fv apply smoothing to a summary function deriv.fv calculate derivative of a summary function nndist nearest neighbour distances nnwhich find nearest neighbours distances between all pairs of points pairdist crossdist distances between points in two patterns nearest neighbours between two point patterns nncross exactdt distance from any location to nearest data point distance map image distmap distance map function distfun nearest point image nnmap nearest point function nnfun kernel smoothed density density.ppp Smooth.ppp spatial interpolation of marks kernel estimate of relative risk relrisk sharpen.ppp data sharpening theoretical distribution of nearest neighbour distance rknn

Summary statistics for a multitype point pattern: A multitype point pattern is represented by an object X of class "ppp" such that marks (X) is a factor.

relrisk

kernel estimation of relative risk

```
scan.test
                                     spatial scan test of elevated risk
                                     multitype nearest neighbour distributions G_{ij}, G_{i\bullet}
Gcross,Gdot,Gmulti
Kcross, Kdot, Kmulti
                                     multitype K-functions K_{ij}, K_{i\bullet}
Lcross, Ldot
                                     multitype L-functions L_{ij}, L_{i\bullet}
Jcross, Jdot, Jmulti
                                     multitype J-functions J_{ij}, J_{i\bullet}
pcfcross
                                     multitype pair correlation function g_{ij}
pcfdot
                                     multitype pair correlation function q_{i\bullet}
pcfmulti
                                     general pair correlation function
                                     marked connection function p_{ij}
markconnect
alltypes
                                     estimates of the above for all i, j pairs
Iest
                                     multitype I-function
Kcross.inhom,Kdot.inhom
                                     inhomogeneous counterparts of Kcross, Kdot
Lcross.inhom,Ldot.inhom
                                     inhomogeneous counterparts of Lcross, Ldot
pcfcross.inhom,pcfdot.inhom
                                     inhomogeneous counterparts of pcfcross, pcfdot
```

Summary statistics for a marked point pattern: A marked point pattern is represented by an object X of class "ppp" with a component X\$marks. The entries in the vector X\$marks may be numeric, complex, string or any other atomic type. For numeric marks, there are the following functions:

smoothed local average of marks markmean smoothed local variance of marks markvar mark correlation function markcorr markvario mark variogram markcorrint mark correlation integral mark independence diagnostic E(r)**Emark Vmark** mark independence diagnostic V(r)nearest neighbour mean index nnmean nnvario nearest neighbour mark variance index

For marks of any type, there are the following:

Alternatively use cut. ppp to convert a marked point pattern to a multitype point pattern.

Programming tools:

```
applynbd apply function to every neighbourhood in a point pattern
apply function to the marks of neighbours in a point pattern
tabulate the marks of neighbours in a point pattern
find the optimal match between two point patterns
```

Summary statistics for a point pattern on a linear network:

These are for point patterns on a linear network (class 1pp). For unmarked patterns:

linearK	K function on linear network
linearKinhom	inhomogeneous K function on linear network
linearpcf	pair correlation function on linear network
linearpcfinhom	inhomogeneous pair correlation on linear network

For multitype patterns:

linearKcross	K function between two types of points
linearKdot	K function from one type to any type
linearKcross.inhom	Inhomogeneous version of linearKcross
linearKdot.inhom	Inhomogeneous version of linearKdot
linearmarkconnect	Mark connection function on linear network
linearmarkequal	Mark equality function on linear network
linearpcfcross	Pair correlation between two types of points
linearpcfdot	Pair correlation from one type to any type
linearpcfcross.inhom	Inhomogeneous version of linearpcfcross
linearpcfdot.inhom	Inhomogeneous version of linearpcfdot

Related facilities:

pairdist.lpp	distances between pairs
crossdist.lpp	distances between pairs
nndist.lpp	nearest neighbour distances
nncross.lpp	nearest neighbour distances
nnwhich.lpp	find nearest neighbours
nnfun.lpp	find nearest data point
distfun.lpp	distance transform
envelope.lpp	simulation envelopes
rpoislpp	simulate Poisson points on linear network
runiflpp	simulate random points on a linear network

It is also possible to fit point process models to 1pp objects. See Section IV.

Summary statistics for a three-dimensional point pattern:

These are for 3-dimensional point pattern objects (class pp3).

F3est	empty space function F
G3est	nearest neighbour function G
K3est	K-function
pcf3est	pair correlation function

Related facilities:

envelope.pp3	simulation envelopes
pairdist.pp3	distances between all pairs of points
crossdist.pp3	distances between points in two patterns
nndist.pp3	nearest neighbour distances
nnwhich.pp3	find nearest neighbours

nncross.pp3 find nearest neighbours in another pattern

Computations for multi-dimensional point pattern:

These are for multi-dimensional space-time point pattern objects (class ppx).

```
pairdist.ppx distances between all pairs of points crossdist.ppx distances between points in two patterns nearest neighbour distances find nearest neighbours
```

Summary statistics for random sets:

These work for point patterns (class ppp), line segment patterns (class psp) or windows (class owin).

```
Hest spherical contact distribution H Gfox Foxall G-function Jfox Foxall J-function
```

III. MODEL FITTING (CLUSTER MODELS)

Cluster process models (with homogeneous or inhomogeneous intensity) and Cox processes can be fitted by the function kppm. Its result is an object of class "kppm". The fitted model can be printed, plotted, predicted, simulated and updated.

kppm	Fit model
plot.kppm	Plot the fitted model
fitted.kppm	Compute fitted intensity
predict.kppm	Compute fitted intensity
update.kppm	Update the model
improve.kppm	Refine the estimate of trend
simulate.kppm	Generate simulated realisations
vcov.kppm	Variance-covariance matrix of coefficients
Kmodel.kppm	K function of fitted model
pcfmodel.kppm	Pair correlation of fitted model

The theoretical models can also be simulated, for any choice of parameter values, using rThomas, rMatClust, rCauchy, rVarGamma, and rLGCP.

Lower-level fitting functions include:

```
fit a log-Gaussian Cox process model
lgcp.estK
lgcp.estpcf
                    fit a log-Gaussian Cox process model
                    fit the Thomas process model
thomas.estK
thomas.estpcf
                    fit the Thomas process model
                    fit the Matern Cluster process model
matclust.estK
                    fit the Matern Cluster process model
matclust.estpcf
cauchy.estK
                    fit a Neyman-Scott Cauchy cluster process
                    fit a Neyman-Scott Cauchy cluster process
cauchy.estpcf
                    fit a Neyman-Scott Variance Gamma process
vargamma.estK
```

vargamma.estpcf fit a Neyman-Scott Variance Gamma process
mincontrast low-level algorithm for fitting models
by the method of minimum contrast

IV. MODEL FITTING (POISSON AND GIBBS MODELS)

Types of models

Poisson point processes are the simplest models for point patterns. A Poisson model assumes that the points are stochastically independent. It may allow the points to have a non-uniform spatial density. The special case of a Poisson process with a uniform spatial density is often called Complete Spatial Randomness.

Poisson point processes are included in the more general class of Gibbs point process models. In a Gibbs model, there is *interaction* or dependence between points. Many different types of interaction can be specified.

For a detailed explanation of how to fit Poisson or Gibbs point process models to point pattern data using **spatstat**, see Baddeley and Turner (2005b) or Baddeley (2008).

To fit a Poison or Gibbs point process model:

Model fitting in **spatstat** is performed mainly by the function ppm. Its result is an object of class "ppm".

Here are some examples, where X is a point pattern (class "ppp"):

command	model
ppm(X)	Complete Spatial Randomness
ppm(X ~ 1)	Complete Spatial Randomness
ppm(X ~ x)	Poisson process with
	intensity loglinear in x coordinate
$ppm(X \sim 1, Strauss(0.1))$	Stationary Strauss process
$ppm(X \sim x, Strauss(0.1))$	Strauss process with
	conditional intensity loglinear in x

It is also possible to fit models that depend on other covariates.

Manipulating the fitted model:

plot.ppm	Plot the fitted model
<pre>predict.ppm</pre>	Compute the spatial trend and conditional intensity
	of the fitted point process model
coef.ppm	Extract the fitted model coefficients
formula.ppm	Extract the trend formula
<pre>intensity.ppm</pre>	Compute fitted intensity
Kmodel.ppm	K function of fitted model
pcfmodel.ppm	pair correlation of fitted model
fitted.ppm	Compute fitted conditional intensity at quadrature points
residuals.ppm	Compute point process residuals at quadrature points
update.ppm	Update the fit
vcov.ppm	Variance-covariance matrix of estimates
rmh.ppm	Simulate from fitted model

Simulate from fitted model simulate.ppm Print basic information about a fitted model print.ppm Summarise a fitted model summary.ppm effectfun Compute the fitted effect of one covariate logLik.ppm log-likelihood or log-pseudolikelihood anova.ppm Analysis of deviance Extract data frame used to fit model model.frame.ppm Extract spatial data used to fit model model.images Identify variables in the model model.depends Interpoint interaction component of model as.interact fitin Extract fitted interpoint interaction is.hybrid Determine whether the model is a hybrid valid.ppm Check the model is a valid point process Ensure the model is a valid point process project.ppm

For model selection, you can also use the generic functions step, drop1 and AIC on fitted point process models.

See spatstat.options to control plotting of fitted model.

To specify a point process model:

The first order "trend" of the model is determined by an R language formula. The formula specifies the form of the *logarithm* of the trend.

X ~ 1	No trend (stationary)
X ~ X	Loglinear trend $\lambda(x,y) = \exp(\alpha + \beta x)$
	where x, y are Cartesian coordinates
$X \sim polynom(x,y,3)$	Log-cubic polynomial trend
$X \sim harmonic(x,y,2)$	Log-harmonic polynomial trend
X ~ Z	Loglinear function of covariate Z
	$\lambda(x,y) = \exp(\alpha + \beta Z(x,y))$

The higher order ("interaction") components are described by an object of class "interact". Such objects are created by:

Poisson()	the Poisson point process
AreaInter()	Area-interaction process
BadGey()	multiscale Geyer process
Concom()	connected component interaction
<pre>DiggleGratton()</pre>	Diggle-Gratton potential
<pre>DiggleGatesStibbard()</pre>	Diggle-Gates-Stibbard potential
Fiksel()	Fiksel pairwise interaction process
Geyer()	Geyer's saturation process
Hardcore()	Hard core process
Hybrid()	Hybrid of several interactions
LennardJones()	Lennard-Jones potential
MultiHard()	multitype hard core process
MultiStrauss()	multitype Strauss process
MultiStraussHard()	multitype Strauss/hard core process

OrdThresh()	Ord process, threshold potential
Ord()	Ord model, user-supplied potential
PairPiece()	pairwise interaction, piecewise constant
Pairwise()	pairwise interaction, user-supplied potential
SatPiece()	Saturated pair model, piecewise constant potential
Saturated()	Saturated pair model, user-supplied potential
Softcore()	pairwise interaction, soft core potential
Strauss()	Strauss process
StraussHard()	Strauss/hard core point process
Triplets()	Geyer triplets process

Note that it is also possible to combine several such interactions using Hybrid.

Finer control over model fitting:

A quadrature scheme is represented by an object of class "quad". To create a quadrature scheme, typically use quadscheme.

quadscheme default quadrature scheme using rectangular cells or Dirichlet cells pixelquad quadrature scheme based on image pixels create an object of class "quad"

To inspect a quadrature scheme:

```
plot(Q) plot quadrature scheme Q
print(Q) print basic information about quadrature scheme Q
summary(Q) summary of quadrature scheme Q
```

A quadrature scheme consists of data points, dummy points, and weights. To generate dummy points:

default.dummy default pattern of dummy points
gridcentres dummy points in a rectangular grid
stratified random dummy pattern
spokes radial pattern of dummy points
corners dummy points at corners of the window

To compute weights:

```
gridweights quadrature weights by the grid-counting rule dirichlet.weights quadrature weights are Dirichlet tile areas
```

Simulation and goodness-of-fit for fitted models:

```
rmh.ppm simulate realisations of a fitted model simulate.ppm simulate realisations of a fitted model compute simulation envelopes for a fitted model
```

Point process models on a linear network:

An object of class "1pp" represents a pattern of points on a linear network. Point process models can also be fitted to these objects. Currently only Poisson models can be fitted.

1ppm point process model on linear network anova.lppm analysis of deviance for point process model on linear network envelope.lppm simulation envelopes for point process model on linear network model prediction on linear network predict.lppm linim pixel image on linear network plot.linim plot a pixel image on linear network eval.linim evaluate expression involving images function defined on linear network linfun methods.linfun conversion facilities

V. MODEL FITTING (SPATIAL LOGISTIC REGRESSION)

Logistic regression

Pixel-based spatial logistic regression is an alternative technique for analysing spatial point patterns that is widely used in Geographical Information Systems. It is approximately equivalent to fitting a Poisson point process model.

In pixel-based logistic regression, the spatial domain is divided into small pixels, the presence or absence of a data point in each pixel is recorded, and logistic regression is used to model the presence/absence indicators as a function of any covariates.

Facilities for performing spatial logistic regression are provided in **spatstat** for comparison purposes.

Fitting a spatial logistic regression

Spatial logistic regression is performed by the function slrm. Its result is an object of class "slrm". There are many methods for this class, including methods for print, fitted, predict, simulate, anova, coef, logLik, terms, update, formula and vcov.

For example, if X is a point pattern (class "ppp"):

command model

slrm(X ~ 1) Complete Spatial Randomness

slrm(X ~ x) Poisson process with
intensity loglinear in x coordinate

slrm(X ~ Z) Poisson process with
intensity loglinear in covariate Z

Manipulating a fitted spatial logistic regression

anova.slrm	Analysis of deviance
coef.slrm	Extract fitted coefficients
vcov.slrm	Variance-covariance matrix of fitted coefficients
fitted.slrm	Compute fitted probabilities or intensity

logLik.slrm	Evaluate loglikelihood of fitted model
plot.slrm	Plot fitted probabilities or intensity
predict.slrm	Compute predicted probabilities or intensity with new data
simulate.slrm	Simulate model

There are many other undocumented methods for this class, including methods for print, update, formula and terms. Stepwise model selection is possible using step or stepAIC.

VI. SIMULATION

There are many ways to generate a random point pattern, line segment pattern, pixel image or tessellation in **spatstat**.

Random point patterns:

runifpoint	generate n independent uniform random points
rpoint	generate n independent random points
rmpoint	generate n independent multitype random points
rpoispp	simulate the (in)homogeneous Poisson point process
rmpoispp	simulate the (in)homogeneous multitype Poisson point process
runifdisc	generate n independent uniform random points in disc
rstrat	stratified random sample of points
rsyst	systematic random sample (grid) of points
rMaternI	simulate the Matérn Model I inhibition process
rMaternII	simulate the Matérn Model II inhibition process
rSSI	simulate Simple Sequential Inhibition process
rStrauss	simulate Strauss process (perfect simulation)
rNeymanScott	simulate a general Neyman-Scott process
rMatClust	simulate the Matérn Cluster process
rThomas	simulate the Thomas process
rLGCP	simulate the log-Gaussian Cox process
rGaussPoisson	simulate the Gauss-Poisson cluster process
rCauchy	simulate Neyman-Scott process with Cauchy clusters
rVarGamma	simulate Neyman-Scott process with Variance Gamma clusters
rcell	simulate the Baddeley-Silverman cell process
runifpointOnLines	generate n random points along specified line segments
rpoisppOnLines	generate Poisson random points along specified line segments

Resampling a point pattern:

quadratresample	block resampling
rjitter	apply random displacements to points in a pattern
rshift	random shifting of (subsets of) points
rthin	random thinning

See also varblock for estimating the variance of a summary statistic by block resampling, and lohboot for another bootstrap technique.

Fitted point process models:

If you have fitted a point process model to a point pattern dataset, the fitted model can be simulated.

Cluster process models are fitted by the function kppm yielding an object of class "kppm". To generate one or more simulated realisations of this fitted model, use simulate.kppm.

Gibbs point process models are fitted by the function ppm yielding an object of class "ppm". To generate a simulated realisation of this fitted model, use rmh. To generate one or more simulated realisations of the fitted model, use simulate.ppm.

Other random patterns:

```
rlinegrid generate a random array of parallel lines through a window simulate the Poisson line process within a window generate random tessellation using Poisson line process generate random set by selecting some tiles of a tessellation generate random pixel image by assigning random values in each tile of a tessellation
```

Simulation-based inference

```
envelope critical envelope for Monte Carlo test of goodness-of-fit diagnostic plot for interpoint interaction spatial scan statistic/test
```

VII. TESTS AND DIAGNOSTICS

Classical hypothesis tests:

```
\chi^2 goodness-of-fit test on quadrat counts
quadrat.test
clarkevans.test
                     Clark and Evans test
                     Spatial distribution goodness-of-fit test
cdf.test
                     Berman's goodness-of-fit tests
berman.test
                     critical envelope for Monte Carlo test of goodness-of-fit
envelope
                     spatial scan statistic/test
scan.test
dclf.test
                     Diggle-Cressie-Loosmore-Ford test
                     Mean Absolute Deviation test
mad.test
dclf.progress
                     Progress plot for DCLF test
mad.progress
                     Progress plot for MAD test
anova.ppm
                     Analysis of Deviance for point process models
```

Sensitivity diagnostics:

Classical measures of model sensitivity such as leverage and influence have been adapted to point process models.

```
leverage.ppm Leverage for point process model influence.ppm Influence for point process model dfbetas.ppm Parameter influence
```

Diagnostics for covariate effect:

Classical diagnostics for covariate effects have been adapted to point process models.

parres Partial residual plot addvar Added variable plot

rhohat Kernel estimate of covariate effect

rho2hat Kernel estimate of covariate effect (bivariate)

Residual diagnostics:

Residuals for a fitted point process model, and diagnostic plots based on the residuals, were introduced in Baddeley et al (2005) and Baddeley, Rubak and Møller (2011).

Type demo(diagnose) for a demonstration of the diagnostics features.

diagnostic plots for spatial trend diagnose.ppm diagnostic Q-Q plot for interpoint interaction qqplot.ppm examples from Baddeley et al (2005) residualspaper model compensator of K function **Kcom** Gcom model compensator of G function score residual of K function Kres score residual of G function Gres pseudoscore residual of summary function psst pseudoscore residual of empty space function psstA psstG pseudoscore residual of G function

Resampling and randomisation procedures

compareFit

You can build your own tests based on randomisation and resampling using the following capabilities:

compare compensators of several fitted models

VIII. DOCUMENTATION

The online manual entries are quite detailed and should be consulted first for information about a particular function.

The paper by Baddeley and Turner (2005a) is a brief overview of the package. Baddeley and Turner (2005b) is a more detailed explanation of how to fit point process models to data. Baddeley (2010) is a complete set of notes from a 2-day workshop on the use of **spatstat**.

Type citation("spatstat") to get these references.

Licence

This library and its documentation are usable under the terms of the "GNU General Public License", a copy of which is distributed with the package.

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