# **Spatstat Quick Reference**

September 4, 2014

spatstat-package

The Spatstat Package

# **Description**

This is a summary of the features of **spatstat**, a package in R for the statistical analysis of spatial point patterns.

#### **Details**

**spatstat** is a package for the statistical analysis of spatial data. Currently, it deals mainly with the analysis of spatial patterns of points in two-dimensional space. The points may carry auxiliary data ('marks'), and the spatial region in which the points were recorded may have arbitrary shape.

The package supports

- creation, manipulation and plotting of point patterns
- exploratory data analysis
- simulation of point process models
- parametric model-fitting
- · hypothesis tests and model diagnostics

Apart from two-dimensional point patterns and point processes, **spatstat** also supports point patterns in three dimensions, point patterns in multidimensional space-time, point patterns on a linear network, patterns of line segments in two dimensions, and spatial tessellations and random sets in two dimensions.

The package can fit several types of point process models to a point pattern dataset:

- Poisson point process models (by Berman-Turner approximate maximum likelihood or by spatial logistic regression)
- Gibbs/Markov point process models (by Baddeley-Turner approximate maximum pseudolikelihood, Coeurjolly-Rubak logistic likelihood, or Huang-Ogata approximate maximum likelihood)

 Cox/cluster process models (by Waagepetersen's two-step fitting procedure and minimum contrast, or by composite likelihood)

The models may include spatial trend, dependence on covariates, and complicated interpoint interactions. Models are specified by a formula in the R language, and are fitted using a function analogous to lm and glm. Fitted models can be printed, plotted, predicted, simulated and so on.

# **Getting Started**

For a quick introduction to **spatstat**, see the package vignette *Getting started with spatstat* installed with **spatstat**. (To see this document online, start R, type help.start() to open the help browser, and navigate to Packages > spatstat > Vignettes).

For a complete 2-day course on using **spatstat**, see the workshop notes by Baddeley (2010), available on the internet. (This is now somewhat out-of-date but it will get you started.)

Type demo(spatstat) for a demonstration of the package's capabilities. Type demo(data) to see all the datasets available in the package.

For information about handling data in **shapefiles**, see the Vignette *Handling shapefiles in the spat-stat package* installed with **spatstat**.

To learn about spatial point process methods, see the short book by Diggle (2003) and the handbook Gelfand et al (2010).

# **Updates**

New versions of **spatstat** are produced about once a month. Users are advised to update their installation of **spatstat** regularly.

Type latest.news to read the news documentation about changes to the current installed version of **spatstat**.

See the Vignette *Summary of recent updates*, installed with **spatstat**, which describes the main changes to **spatstat** since the workshop notes were published in 2010,

Type news(package="spatstat") to read news documentation about all previous versions of the package.

#### FUNCTIONS AND DATASETS

Following is a summary of the main functions and datasets in the **spatstat** package. Alternatively an alphabetical list of all functions and datasets is available by typing library(help=spatstat).

For further information on any of these, type help(name) where name is the name of the function or dataset.

#### **CONTENTS:**

- I. Creating and manipulating data
- II. Exploratory Data Analysis
- III. Model fitting (cluster models)
- IV. Model fitting (Poisson and Gibbs models)
- V. Model fitting (spatial logistic regression)
- VI. Simulation

VII. Tests and diagnosticsVIII. Documentation

#### I. CREATING AND MANIPULATING DATA

# Types of spatial data:

The main types of spatial data supported by **spatstat** are:

ppp point pattern
owin window (spatial region)
im pixel image
psp line segment pattern
tess tessellation
pp3 three-dimensional point pattern
ppx point pattern in any number of dimensions
1pp point pattern on a linear network

# To create a point pattern:

ppp create a point pattern from (x,y) and window information ppp(x, y, xlim, ylim) for rectangular window ppp(x, y, poly) for polygonal window ppp(x, y, mask) for binary image window as.ppp convert other types of data to a ppp object clickppp interactively add points to a plot attach/reassign marks to a point pattern

# To simulate a random point pattern:

runifpoint	generate $n$ independent uniform random points
rpoint	generate $n$ independent random points
rmpoint	generate $n$ independent multitype random points
rpoispp	simulate the (in)homogeneous Poisson point process
rmpoispp	simulate the (in)homogeneous multitype Poisson point process
runifdisc	generate $n$ independent uniform random points in disc
rstrat	stratified random sample of points
rsyst	systematic random sample of points
rjitter	apply random displacements to points in a pattern
rMaternI	simulate the Matérn Model I inhibition process
rMaternII	simulate the Matérn Model II inhibition process
rSSI	simulate Simple Sequential Inhibition process
rStrauss	simulate Strauss process (perfect simulation)
rHardcore	simulate Hard Core process (perfect simulation)
rDiggleGratton	simulate Diggle-Gratton process (perfect simulation)
rDGS	simulate Diggle-Gates-Stibbard process (perfect simulation)
rNeymanScott	simulate a general Neyman-Scott process

rPoissonCluster simulate a general Neyman-Scott process
rNeymanScott simulate a general Neyman-Scott process
rMatClust simulate the Matérn Cluster process
rThomas simulate the Thomas process

rGaussPoisson simulate the Gauss-Poisson cluster process rCauchy simulate Neyman-Scott Cauchy cluster process

rVarGamma simulate Neyman-Scott Variance Gamma cluster process

rthin random thinning

rcell simulate the Baddeley-Silverman cell process

rmhsimulate Gibbs point process using Metropolis-Hastingssimulate.ppmsimulate Gibbs point process using Metropolis-HastingsrunifpointOnLinesgenerate n random points along specified line segmentsrpoisppOnLinesgenerate Poisson random points along specified line segments

#### To randomly change an existing point pattern:

rshift random shifting of points

rjitter apply random displacements to points in a pattern

rthin random thinning

rlabel random (re)labelling of a multitype point pattern

quadratresample block resampling

#### **Standard point pattern datasets:**

Datasets in **spatstat** are lazy-loaded, so you can simply type the name of the dataset to use it; there is no need to type data(amacrine) etc.

Type demo(data) to see a display of all the datasets installed with the package.

amacrine Austin Hughes' rabbit amacrine cells
anemones Upton-Fingleton sea anemones data
ants Harkness-Isham ant nests data

bei Tropical rainforest trees

betacells Waessle et al. cat retinal ganglia data

bramblecanes Bramble Canes data
bronzefilter Bronze Filter Section data

cells Crick-Ripley biological cells data

chicago Chicago street crimes
chorley Chorley-Ribble cancer data
clmfires Castilla-La Mancha forest fires

copper Berman-Huntington copper deposits data

demohyperSynthetic point patternsdemopatSynthetic point patternfinpinesFinnish Pines datafluInfluenza virus proteins

gordon People in Gordon Square, London

gorillas Gorilla nest sites

hamster Aherne's hamster tumour data

humberside North Humberside childhood leukaemia data

hyytiala Mixed forest in Hyytiälä, Finland

japanesepines Japanese Pines data Lansing Woods data lansing longleaf Longleaf Pines data mucosa Cells in gastric mucosa murchison Murchison gold deposits nbfires New Brunswick fires data Mark-Esler-Ripley trees data nztrees Osteocyte lacunae (3D, replicated) osteo paracou Kimboto trees in Paracou, French Guiana ponderosa Getis-Franklin ponderosa pine trees data Pyramidal neurons from 31 brains pyramidal redwood Strauss-Ripley redwood saplings data redwoodfull Strauss redwood saplings data (full set) Data from Baddeley et al (2005) residualspaper shapley Galaxies in an astronomical survey

simulated point pattern (inhomogeneous, with interaction)

sporophores Mycorrhizal fungi around a tree

spruces Spruce trees in Saxonia

swedishpines Strand-Ripley Swedish pines data

urkiola Urkiola Woods data

waka Trees in Waka national park waterstriders Insects on water surface

#### To manipulate a point pattern:

plot.ppp plot a point pattern (e.g. plot(X)) iplot plot a point pattern interactively

[.ppp extract or replace a subset of a point pattern

pp[subset] or pp[subwindow]

subset.ppp extract subset of point pattern satisfying a condition

superimpose combine several point patterns

by .ppp apply a function to sub-patterns of a point pattern

cut.ppp classify the points in a point pattern split.ppp divide pattern into sub-patterns

unmark remove marks

npoints count the number of points

coords extract coordinates, change coordinates
marks extract marks, change marks or attach marks

rotate rotate pattern shift translate pattern

flipxy swap x and y coordinates reflect reflect in the origin

periodify make several translated copies affine apply affine transformation

scalardilate apply scalar dilation

density.ppp kernel estimation of point pattern intensity
Smooth.ppp kernel smoothing of marks of point pattern

nnmark mark value of nearest data point

data sharpening sharpen.ppp identify.ppp interactively identify points remove duplicate points unique.ppp duplicated.ppp determine which points are duplicates connected.ppp find clumps of points dirichlet compute Dirichlet-Voronoi tessellation compute Delaunay triangulation delaunay graph distance in Delaunay triangulation delaunay.distance convexhull compute convex hull discretise discretise coordinates pixellate.ppp approximate point pattern by pixel image approximate point pattern by pixel image as.im.ppp

See spatstat.options to control plotting behaviour.

#### To create a window:

An object of class "owin" describes a spatial region (a window of observation).

Create a window object owin owin(xlim, ylim) for rectangular window owin(poly) for polygonal window owin(mask) for binary image window Extract window of another object Window Frame Extract the containing rectangle ('frame') of another object Convert other data to a window object as.owin square make a square window make a circular window disc Ripley-Rasson estimator of window, given only the points ripras compute convex hull of something convexhull polygonal window in the shape of the R logo letterR clickpoly interactively draw a polygonal window clickbox interactively draw a rectangle

# To manipulate a window:

plot.owin	plot a window.
	plot(W)
boundingbox	Find a tight bounding box for the window
erosion	erode window by a distance r
dilation	dilate window by a distance r
closing	close window by a distance r
opening	open window by a distance r
border	difference between window and its erosion/dilation
complement.owin	invert (swap inside and outside)
simplify.owin	approximate a window by a simple polygon
rotate	rotate window
flipxy	swap $x$ and $y$ coordinates
shift	translate window

periodify make several translated copies affine apply affine transformation

# **Digital approximations:**

Make a discrete pixel approximation of a given window as.mask as.im.owin convert window to pixel image pixellate.owin convert window to pixel image find common pixel grid for windows commonGrid map continuous coordinates to raster locations nearest.raster.point raster x coordinates raster.x raster.y raster y coordinates convert pixel mask to polygonal window as.polygonal

See spatstat.options to control the approximation

# Geometrical computations with windows:

edges	extract boundary edges
intersect.owin	intersection of two windows
union.owin	union of two windows
setminus.owin	set subtraction of two windows
inside.owin	determine whether a point is inside a window
area.owin	compute area
perimeter	compute perimeter length
diameter.owin	compute diameter
incircle	find largest circle inside a window
connected.owin	find connected components of window
eroded.areas	compute areas of eroded windows
dilated.areas	compute areas of dilated windows
bdist.points	compute distances from data points to window boundary
bdist.pixels	compute distances from all pixels to window boundary
bdist.tiles	boundary distance for each tile in tessellation
distmap.owin	distance transform image
distfun.owin	distance transform
centroid.owin	compute centroid (centre of mass) of window
is.subset.owin	determine whether one window contains another
is.convex	determine whether a window is convex
convexhull	compute convex hull
as.mask	pixel approximation of window
as.polygonal	polygonal approximation of window
is.rectangle	test whether window is a rectangle
is.polygonal	test whether window is polygonal
is.mask	test whether window is a mask
setcov	spatial covariance function of window
pixelcentres	extract centres of pixels in mask

Pixel images: An object of class "im" represents a pixel image. Such objects are returned by some

of the functions in **spatstat** including Kmeasure, setcov and density.ppp.

im	create a pixel image
as.im	convert other data to a pixel image
pixellate	convert other data to a pixel image
as.matrix.im	convert pixel image to matrix
as.data.frame.im	convert pixel image to data frame
plot.im	plot a pixel image on screen as a digital image
contour.im	draw contours of a pixel image
persp.im	draw perspective plot of a pixel image
rgbim	create colour-valued pixel image
hsvim	create colour-valued pixel image
[.im	extract a subset of a pixel image
[ <im< td=""><td>replace a subset of a pixel image</td></im<>	replace a subset of a pixel image
rotate.im	rotate pixel image
shift.im	apply vector shift to pixel image
affine.im	apply affine transformation to image
Χ	print very basic information about image X
<pre>summary(X)</pre>	summary of image X
hist.im	histogram of image
mean.im	mean pixel value of image
integral.im	integral of pixel values
quantile.im	quantiles of image
cut.im	convert numeric image to factor image
is.im	test whether an object is a pixel image
interp.im	interpolate a pixel image
blur	apply Gaussian blur to image
Smooth.im	apply Gaussian blur to image
connected.im	find connected components
compatible.im	test whether two images have compatible dimensions
harmonise.im	make images compatible
commonGrid	find a common pixel grid for images
eval.im	evaluate any expression involving images
scaletointerval	rescale pixel values
zapsmall.im	set very small pixel values to zero
levelset	level set of an image
solutionset	region where an expression is true
imcov	spatial covariance function of image
convolve.im	spatial convolution of images
transect.im	line transect of image
pixelcentres	extract centres of pixels

# Line segment patterns

An object of class "psp" represents a pattern of straight line segments.

```
psp create a line segment pattern
as.psp convert other data into a line segment pattern
edges extract edges of a window
```

is.psp	determine whether a dataset has class "psp"
plot.psp	plot a line segment pattern
print.psp	print basic information
summary.psp	print summary information
[.psp	extract a subset of a line segment pattern
as.data.frame.psp	convert line segment pattern to data frame
marks.psp	extract marks of line segments
marks <psp< td=""><td>assign new marks to line segments</td></psp<>	assign new marks to line segments
unmark.psp	delete marks from line segments
midpoints.psp	compute the midpoints of line segments
endpoints.psp	extract the endpoints of line segments
lengths.psp	compute the lengths of line segments
angles.psp	compute the orientation angles of line segments
superimpose	combine several line segment patterns
flipxy	swap $x$ and $y$ coordinates
rotate.psp	rotate a line segment pattern
shift.psp	shift a line segment pattern
periodify	make several shifted copies
affine.psp	apply an affine transformation
pixellate.psp	approximate line segment pattern by pixel image
as.mask.psp	approximate line segment pattern by binary mask
distmap.psp	compute the distance map of a line segment pattern
distfun.psp	compute the distance map of a line segment pattern
density.psp	kernel smoothing of line segments
selfcrossing.psp	find crossing points between line segments
crossing.psp	find crossing points between two line segment patterns
nncross	find distance to nearest line segment from a given point
nearestsegment	find line segment closest to a given point
project2segment	find location along a line segment closest to a given point
pointsOnLines	generate points evenly spaced along line segment
rpoisline	generate a realisation of the Poisson line process inside a window
rlinegrid	generate a random array of parallel lines through a window

# **Tessellations**

An object of class "tess" represents a tessellation.

tess	create a tessellation
quadrats	create a tessellation of rectangles
hextess	create a tessellation of hexagons
as.tess	convert other data to a tessellation
plot.tess	plot a tessellation
tiles	extract all the tiles of a tessellation
[.tess	extract some tiles of a tessellation
[ <tess< td=""><td>change some tiles of a tessellation</td></tess<>	change some tiles of a tessellation
intersect.tess	intersect two tessellations
	or restrict a tessellation to a window
chop.tess	subdivide a tessellation by a line
dirichlet	compute Dirichlet-Voronoi tessellation of points

delaunay	compute Delaunay triangulation of points
rpoislinetess	generate tessellation using Poisson line process
tile.areas	area of each tile in tessellation
hdist tiles	boundary distance for each tile in tessellation

#### Three-dimensional point patterns

An object of class "pp3" represents a three-dimensional point pattern in a rectangular box. The box is represented by an object of class "box3".

```
pp3
                   create a 3-D point pattern
plot.pp3
                   plot a 3-D point pattern
                   extract coordinates
coords
                   extract coordinates
as.hyperframe
subset.pp3
                   extract subset of 3-D point pattern
                   name of unit of length
unitname.pp3
npoints
                   count the number of points
                   generate uniform random points in 3-D
runifpoint3
                   generate Poisson random points in 3-D
rpoispp3
                   generate simulation envelopes for 3-D pattern
envelope.pp3
                   create a 3-D rectangular box
box3
as.box3
                   convert data to 3-D rectangular box
                   name of unit of length
unitname.box3
                   diameter of box
diameter.box3
volume.box3
                   volume of box
                   shortest side of box
shortside.box3
eroded.volumes
                   volumes of erosions of box
```

# Multi-dimensional space-time point patterns

An object of class "ppx" represents a point pattern in multi-dimensional space and/or time.

```
create a multidimensional space-time point pattern
ррх
coords
                         extract coordinates
                         extract coordinates
as.hyperframe
subset.ppx
                         extract subset
unitname.ppx
                         name of unit of length
npoints
                         count the number of points
                         generate uniform random points
runifpointx
                         generate Poisson random points
rpoisppx
                         define multidimensional box
boxx
diameter.boxx
                         diameter of box
volume.boxx
                         volume of box
shortside.boxx
                         shortest side of box
eroded.volumes.boxx
                         volumes of erosions of box
```

#### Point patterns on a linear network

An object of class "linnet" represents a linear network (for example, a road network).

linnet create a linear network

clickjoin interactively join vertices in network

simplenet simple example of network lineardisc disc in a linear network methods.linnet methods for linnet objects

An object of class "lpp" represents a point pattern on a linear network (for example, road accidents on a road network).

lpp create a point pattern on a linear network

methods.lpp methods for lpp objects subset.lpp method for subset

rpoislpp simulate Poisson points on linear network runiflpp simulate random points on a linear network

chicago Chicago street crime data

# Hyperframes

A hyperframe is like a data frame, except that the entries may be objects of any kind.

hyperframe create a hyperframe as.hyperframe convert data to hyperframe

plot.hyperframe plot hyperframe

with.hyperframe evaluate expression using each row of hyperframe

cbind.hyperframe combine hyperframes by columns rbind.hyperframe combine hyperframes by rows as.data.frame.hyperframe convert hyperframe to data frame

# Layered objects

A layered object represents data that should be plotted in successive layers, for example, a background and a foreground.

layered create layered object plot.layered plot layered object

[.layered extract subset of layered object

# Colour maps

A colour map is a mechanism for associating colours with data. It can be regarded as a function, mapping data to colours. Using a colourmap object in a plot command ensures that the mapping from numbers to colours is the same in different plots.

colourmap create a colour map
plot.colourmap plot the colour map only
tweak.colourmap alter individual colour values

interp.colourmap make a smooth transition between colours

beachcolourmap one special colour map

#### II. EXPLORATORY DATA ANALYSIS

#### **Inspection of data:**

# Classical exploratory tools:

clarkevans Clark and Evans aggregation index

fryplot Fry plot

miplot Morisita Index plot

#### **Smoothing:**

density.ppp kernel smoothed density/intensity relrisk kernel estimate of relative risk Smooth.ppp spatial interpolation of marks cross-validated bandwidth selection for density.ppp bw.diggle likelihood cross-validated bandwidth selection for density.ppp bw.ppl Scott's rule of thumb for density estimation bw.scott bw.relrisk cross-validated bandwidth selection for relrisk bw.smoothppp cross-validated bandwidth selection for Smooth.ppp bandwidth selection using window geometry bw.frac bw.stoyan Stoyan's rule of thumb for bandwidth for pcf

#### Modern exploratory tools:

clusterset
nnclean
Sharpen.ppp
rhohat
rho2hat
spatialcdf
Spatialcdf
Allard-Fraley feature detection
Byers-Raftery feature detection
Choi-Hall data sharpening
Kernel estimate of covariate effect
Spatial cumulative distribution function

**Summary statistics for a point pattern:** Type demo(sumfun) for a demonstration of many of the summary statistics.

intensity Mean intensity quadratcount Quadrat counts Mean intensity in quadrats intensity.quadratcount Fest empty space function Fnearest neighbour distribution function GGest J-function J = (1 - G)/(1 - F)Jest Ripley's K-function Kest Besag L-function Lest

Tstat Third order T-function all stats all four functions F, G, J, K pcf pair correlation function K for inhomogeneous point patterns

LinhomL for inhomogeneous point patternspcfinhompair correlation for inhomogeneous patternsFinhomF for inhomogeneous point patternsGinhomG for inhomogeneous point patterns

Finhom F for inhomogeneous point patterns Ginhom G for inhomogeneous point patterns J inhom J for inhomogeneous point patterns

localL Getis-Franklin neighbourhood density function

localK neighbourhood K-function localpcf local pair correlation function

Ksector Directional K-function

Kscaled locally scaled K-function

Kest.fft fast K-function using FFT for large datasets

Kmeasure reduced second moment measure

envelope simulation envelopes for a summary function

variances and confidence intervals

for a summary function

lohboot bootstrap for a summary function

#### Related facilities:

plot.fv plot a summary function

eval. fv evaluate any expression involving summary functions

harmonise.fv make functions compatible

eval.fasp evaluate any expression involving an array of functions

with.fv evaluate an expression for a summary function Smooth.fv apply smoothing to a summary function deriv.fv calculate derivative of a summary function

nndist nearest neighbour distances nnwhich find nearest neighbours

pairdist distances between all pairs of points
crossdist distances between points in two patterns
nncross nearest neighbours between two point patterns
exactdt distance from any location to nearest data point

distmap distance map image
distfun distance map function
nnmap nearest point image
nnfun nearest point function
density.ppp kernel smoothed density
Smooth.ppp spatial interpolation of marks
relrisk kernel estimate of relative risk

sharpen.ppp data sharpening

rknn theoretical distribution of nearest neighbour distance

**Summary statistics for a multitype point pattern:** A multitype point pattern is represented by an object X of class "ppp" such that marks(X) is a factor.

```
relrisk
                                      kernel estimation of relative risk
scan.test
                                      spatial scan test of elevated risk
Gcross,Gdot,Gmulti
                                      multitype nearest neighbour distributions G_{ij}, G_{i\bullet}
Kcross, Kdot, Kmulti
                                      multitype K-functions K_{ij}, K_{i\bullet}
Lcross, Ldot
                                      multitype L-functions L_{ij}, L_{i\bullet}
                                      multitype J-functions J_{ij}, J_{i\bullet}
Jcross, Jdot, Jmulti
pcfcross
                                      multitype pair correlation function g_{ij}
pcfdot
                                      multitype pair correlation function g_{i\bullet}
pcfmulti
                                      general pair correlation function
markconnect
                                      marked connection function p_{ij}
                                      estimates of the above for all i, j pairs
alltypes
Iest
                                      multitype I-function
                                      inhomogeneous counterparts of Kcross, Kdot
Kcross.inhom,Kdot.inhom
Lcross.inhom,Ldot.inhom
                                      inhomogeneous counterparts of Lcross, Ldot
pcfcross.inhom,pcfdot.inhom
                                      inhomogeneous counterparts of pcfcross, pcfdot
```

**Summary statistics for a marked point pattern:** A marked point pattern is represented by an object X of class "ppp" with a component X\$marks. The entries in the vector X\$marks may be numeric, complex, string or any other atomic type. For numeric marks, there are the following functions:

```
markmean
                smoothed local average of marks
markvar
                smoothed local variance of marks
markcorr
                mark correlation function
markvario
                mark variogram
                mark correlation integral
markcorrint
Emark
                mark independence diagnostic E(r)
Vmark
                mark independence diagnostic V(r)
                nearest neighbour mean index
nnmean
nnvario
                nearest neighbour mark variance index
```

For marks of any type, there are the following:

Alternatively use cut. ppp to convert a marked point pattern to a multitype point pattern.

# **Programming tools:**

```
applynbd apply function to every neighbourhood in a point pattern
markstat apply function to the marks of neighbours in a point pattern
tabulate the marks of neighbours in a point pattern
pppdist find the optimal match between two point patterns
```

#### Summary statistics for a point pattern on a linear network:

These are for point patterns on a linear network (class 1pp). For unmarked patterns:

 $\begin{array}{lll} \textbf{linearK} & K \text{ function on linear network} \\ \textbf{linearKinhom} & \text{inhomogeneous } K \text{ function on linear network} \\ \textbf{linearpcf} & \text{pair correlation function on linear network} \\ \textbf{linearpcfinhom} & \text{inhomogeneous pair correlation on linear network} \\ \end{array}$ 

# For multitype patterns:

linearKcross	K function between two types of points
linearKdot	K function from one type to any type
linearKcross.inhom	Inhomogeneous version of linearKcross
linearKdot.inhom	Inhomogeneous version of linearKdot
linearmarkconnect	Mark connection function on linear network
linearmarkequal	Mark equality function on linear network
linearpcfcross	Pair correlation between two types of points
linearpcfdot	Pair correlation from one type to any type
linearpcfcross.inhom	Inhomogeneous version of linearpcfcross
linearpcfdot.inhom	Inhomogeneous version of linearpcfdot

# Related facilities:

paindist lpp	distances between noire
pairdist.lpp	distances between pairs
crossdist.lpp	distances between pairs
nndist.lpp	nearest neighbour distances
nncross.lpp	nearest neighbour distances
nnwhich.lpp	find nearest neighbours
nnfun.lpp	find nearest data point
distfun.lpp	distance transform
envelope.lpp	simulation envelopes
rpoislpp	simulate Poisson points on linear network
runiflpp	simulate random points on a linear network

It is also possible to fit point process models to 1pp objects. See Section IV.

# Summary statistics for a three-dimensional point pattern:

These are for 3-dimensional point pattern objects (class pp3).

F3est empty space function FG3est nearest neighbour function GK3est K-function
pcf3est pair correlation function

Related facilities:

envelope.pp3 simulation envelopes pairdist.pp3 distances between all pairs of points

crossdist.pp3	distances between points in two patterns
nndist.pp3	nearest neighbour distances
nnwhich.pp3	find nearest neighbours
nncross.pp3	find nearest neighbours in another pattern

# Computations for multi-dimensional point pattern:

These are for multi-dimensional space-time point pattern objects (class ppx).

```
pairdist.ppx distances between all pairs of points crossdist.ppx distances between points in two patterns nndist.ppx nnwhich.ppx find nearest neighbours
```

# Summary statistics for random sets:

These work for point patterns (class ppp), line segment patterns (class psp) or windows (class owin).

```
Hest spherical contact distribution H Gfox Foxall G-function Jfox Foxall J-function
```

# III. MODEL FITTING (CLUSTER MODELS)

Cluster process models (with homogeneous or inhomogeneous intensity) and Cox processes can be fitted by the function kppm. Its result is an object of class "kppm". The fitted model can be printed, plotted, predicted, simulated and updated.

kppm	Fit model
plot.kppm	Plot the fitted model
fitted.kppm	Compute fitted intensity
predict.kppm	Compute fitted intensity
update.kppm	Update the model
improve.kppm	Refine the estimate of trend
simulate.kppm	Generate simulated realisations
vcov.kppm	Variance-covariance matrix of coefficients
Kmodel.kppm	K function of fitted model
pcfmodel.kppm	Pair correlation of fitted model

The theoretical models can also be simulated, for any choice of parameter values, using rThomas, rMatClust, rCauchy, rVarGamma, and rLGCP.

Lower-level fitting functions include:

```
lgcp.estK fit a log-Gaussian Cox process model fit a log-Gaussian Cox process model thomas.estK fit the Thomas process model fit the Thomas process model fit the Matern Cluster process model fit the Matern Cluster process model fit the Matern Cluster process model
```

cauchy.estK	fit a Neyman-Scott Cauchy cluster process
cauchy.estpcf	fit a Neyman-Scott Cauchy cluster process
vargamma.estK	fit a Neyman-Scott Variance Gamma process
vargamma.estpcf	fit a Neyman-Scott Variance Gamma process
mincontrast	low-level algorithm for fitting models
	by the method of minimum contrast

# IV. MODEL FITTING (POISSON AND GIBBS MODELS)

#### Types of models

Poisson point processes are the simplest models for point patterns. A Poisson model assumes that the points are stochastically independent. It may allow the points to have a non-uniform spatial density. The special case of a Poisson process with a uniform spatial density is often called Complete Spatial Randomness.

Poisson point processes are included in the more general class of Gibbs point process models. In a Gibbs model, there is *interaction* or dependence between points. Many different types of interaction can be specified.

For a detailed explanation of how to fit Poisson or Gibbs point process models to point pattern data using **spatstat**, see Baddeley and Turner (2005b) or Baddeley (2008).

#### To fit a Poison or Gibbs point process model:

Model fitting in **spatstat** is performed mainly by the function ppm. Its result is an object of class "ppm".

Here are some examples, where X is a point pattern (class "ppp"):

command	model
ppm(X)	Complete Spatial Randomness
ppm(X ~ 1)	Complete Spatial Randomness
ppm(X ~ x)	Poisson process with
	intensity loglinear in $x$ coordinate
$ppm(X \sim 1, Strauss(0.1))$	Stationary Strauss process
$ppm(X \sim x, Strauss(0.1))$	Strauss process with
	conditional intensity loglinear in $x$

It is also possible to fit models that depend on other covariates.

# Manipulating the fitted model:

plot.ppm	Plot the fitted model
<pre>predict.ppm</pre>	Compute the spatial trend and conditional intensity
	of the fitted point process model
coef.ppm	Extract the fitted model coefficients
formula.ppm	Extract the trend formula
intensity.ppm	Compute fitted intensity
Kmodel.ppm	K function of fitted model
pcfmodel.ppm	pair correlation of fitted model
fitted.ppm	Compute fitted conditional intensity at quadrature points
residuals.ppm	Compute point process residuals at quadrature points

Update the fit update.ppm Variance-covariance matrix of estimates vcov.ppm Simulate from fitted model rmh.ppm Simulate from fitted model simulate.ppm print.ppm Print basic information about a fitted model summary.ppm Summarise a fitted model effectfun Compute the fitted effect of one covariate log-likelihood or log-pseudolikelihood logLik.ppm Analysis of deviance anova.ppm Extract data frame used to fit model model.frame.ppm model.images Extract spatial data used to fit model Identify variables in the model model.depends as.interact Interpoint interaction component of model Extract fitted interpoint interaction fitin is.hybrid Determine whether the model is a hybrid valid.ppm Check the model is a valid point process project.ppm Ensure the model is a valid point process

For model selection, you can also use the generic functions step, drop1 and AIC on fitted point process models.

See spatstat.options to control plotting of fitted model.

## To specify a point process model:

The first order "trend" of the model is determined by an R language formula. The formula specifies the form of the *logarithm* of the trend.

X ~ 1	No trend (stationary)
X ~ X	Loglinear trend $\lambda(x,y) = \exp(\alpha + \beta x)$
	where $x, y$ are Cartesian coordinates
$X \sim polynom(x,y,3)$	Log-cubic polynomial trend
$X \sim harmonic(x,y,2)$	Log-harmonic polynomial trend
X ~ Z	Loglinear function of covariate Z
	$\lambda(x,y) = \exp(\alpha + \beta Z(x,y))$

The higher order ("interaction") components are described by an object of class "interact". Such objects are created by:

Poisson()	the Poisson point process
AreaInter()	Area-interaction process
BadGey()	multiscale Geyer process
Concom()	connected component interaction
<pre>DiggleGratton()</pre>	Diggle-Gratton potential
<pre>DiggleGatesStibbard()</pre>	Diggle-Gates-Stibbard potential
Fiksel()	Fiksel pairwise interaction process
Geyer()	Geyer's saturation process
Hardcore()	Hard core process
Hybrid()	Hybrid of several interactions
LennardJones()	Lennard-Jones potential

multitype hard core process MultiHard() multitype Strauss process MultiStrauss() multitype Strauss/hard core process MultiStraussHard() Ord process, threshold potential OrdThresh() 0rd() Ord model, user-supplied potential PairPiece() pairwise interaction, piecewise constant pairwise interaction, user-supplied potential Pairwise() Saturated pair model, piecewise constant potential SatPiece() Saturated() Saturated pair model, user-supplied potential Softcore() pairwise interaction, soft core potential Strauss() Strauss process Strauss/hard core point process StraussHard() Triplets() Geyer triplets process

Note that it is also possible to combine several such interactions using Hybrid.

#### Finer control over model fitting:

A quadrature scheme is represented by an object of class "quad". To create a quadrature scheme, typically use quadscheme.

quadscheme default quadrature scheme
using rectangular cells or Dirichlet cells
pixelquad quadrature scheme based on image pixels
quad create an object of class "quad"

To inspect a quadrature scheme:

plot(Q) plot quadrature scheme Q print(Q) print basic information about quadrature scheme Q summary(Q) summary of quadrature scheme Q

A quadrature scheme consists of data points, dummy points, and weights. To generate dummy points:

default.dummy default pattern of dummy points
gridcentres dummy points in a rectangular grid
stratified random dummy pattern
spokes radial pattern of dummy points
corners dummy points at corners of the window

To compute weights:

gridweights quadrature weights by the grid-counting rule dirichlet.weights quadrature weights are Dirichlet tile areas

# Simulation and goodness-of-fit for fitted models:

rmh.ppm simulate realisations of a fitted model

```
simulate.ppm simulate realisations of a fitted model compute simulation envelopes for a fitted model
```

#### Point process models on a linear network:

An object of class "1pp" represents a pattern of points on a linear network. Point process models can also be fitted to these objects. Currently only Poisson models can be fitted.

1ppm	point process model on linear network
anova.lppm	analysis of deviance for
	point process model on linear network
envelope.lppm	simulation envelopes for
	point process model on linear network
<pre>predict.lppm</pre>	model prediction on linear network
linim	pixel image on linear network
plot.linim	plot a pixel image on linear network
eval.linim	evaluate expression involving images
linfun	function defined on linear network
methods.linfun	conversion facilities

#### V. MODEL FITTING (SPATIAL LOGISTIC REGRESSION)

# Logistic regression

Pixel-based spatial logistic regression is an alternative technique for analysing spatial point patterns that is widely used in Geographical Information Systems. It is approximately equivalent to fitting a Poisson point process model.

In pixel-based logistic regression, the spatial domain is divided into small pixels, the presence or absence of a data point in each pixel is recorded, and logistic regression is used to model the presence/absence indicators as a function of any covariates.

Facilities for performing spatial logistic regression are provided in **spatstat** for comparison purposes.

#### Fitting a spatial logistic regression

Spatial logistic regression is performed by the function slrm. Its result is an object of class "slrm". There are many methods for this class, including methods for print, fitted, predict, simulate, anova, coef, logLik, terms, update, formula and vcov.

For example, if X is a point pattern (class "ppp"):

command	model
$slrm(X \sim 1)$	Complete Spatial Randomness
$slrm(X \sim x)$	Poisson process with
	intensity loglinear in $x$ coordinate
$slrm(X \sim Z)$	Poisson process with
	intensity loglinear in covariate Z

# Manipulating a fitted spatial logistic regression

```
anova.slrm Analysis of deviance
```

coef.slrm	Extract fitted coefficients
vcov.slrm	Variance-covariance matrix of fitted coefficients
fitted.slrm	Compute fitted probabilities or intensity
logLik.slrm	Evaluate loglikelihood of fitted model
plot.slrm	Plot fitted probabilities or intensity
<pre>predict.slrm</pre>	Compute predicted probabilities or intensity with new data
simulate.slrm	Simulate model

There are many other undocumented methods for this class, including methods for print, update, formula and terms. Stepwise model selection is possible using step or stepAIC.

# VI. SIMULATION

There are many ways to generate a random point pattern, line segment pattern, pixel image or tessellation in **spatstat**.

# **Random point patterns:**

runifooint	ganarata m indapandant uniform random points
runifpoint	generate <i>n</i> independent uniform random points
rpoint	generate $n$ independent random points
rmpoint	generate $n$ independent multitype random points
rpoispp	simulate the (in)homogeneous Poisson point process
rmpoispp	simulate the (in)homogeneous multitype Poisson point process
runifdisc	generate $n$ independent uniform random points in disc
rstrat	stratified random sample of points
rsyst	systematic random sample (grid) of points
rMaternI	simulate the Matérn Model I inhibition process
rMaternII	simulate the Matérn Model II inhibition process
rSSI	simulate Simple Sequential Inhibition process
rStrauss	simulate Strauss process (perfect simulation)
rNeymanScott	simulate a general Neyman-Scott process
rMatClust	simulate the Matérn Cluster process
rThomas	simulate the Thomas process
rLGCP	simulate the log-Gaussian Cox process
rGaussPoisson	simulate the Gauss-Poisson cluster process
rCauchy	simulate Neyman-Scott process with Cauchy clusters
rVarGamma	simulate Neyman-Scott process with Variance Gamma clusters
rcell	simulate the Baddeley-Silverman cell process
runifpointOnLines	generate $n$ random points along specified line segments
rpoisppOnLines	generate Poisson random points along specified line segments

# Resampling a point pattern:

quadratresample	block resampling
rjitter	apply random displacements to points in a pattern
rshift	random shifting of (subsets of) points
rthin	random thinning

See also varblock for estimating the variance of a summary statistic by block resampling, and

lohboot for another bootstrap technique.

#### Fitted point process models:

If you have fitted a point process model to a point pattern dataset, the fitted model can be simulated.

Cluster process models are fitted by the function kppm yielding an object of class "kppm". To generate one or more simulated realisations of this fitted model, use simulate.kppm.

Gibbs point process models are fitted by the function ppm yielding an object of class "ppm". To generate a simulated realisation of this fitted model, use rmh. To generate one or more simulated realisations of the fitted model, use simulate.ppm.

# Other random patterns:

```
rlinegrid generate a random array of parallel lines through a window simulate the Poisson line process within a window generate random tessellation using Poisson line process generate random set by selecting some tiles of a tessellation generate random pixel image by assigning random values in each tile of a tessellation
```

#### Simulation-based inference

```
envelope critical envelope for Monte Carlo test of goodness-of-fit diagnostic plot for interpoint interaction spatial scan statistic/test
```

#### VII. TESTS AND DIAGNOSTICS

#### **Classical hypothesis tests:**

```
\chi^2 goodness-of-fit test on quadrat counts
quadrat.test
clarkevans.test
                     Clark and Evans test
cdf.test
                     Spatial distribution goodness-of-fit test
                     Berman's goodness-of-fit tests
berman.test
                     critical envelope for Monte Carlo test of goodness-of-fit
envelope
                     spatial scan statistic/test
scan.test
dclf.test
                     Diggle-Cressie-Loosmore-Ford test
mad.test
                     Mean Absolute Deviation test
                     Progress plot for DCLF test
dclf.progress
                     Progress plot for MAD test
mad.progress
anova.ppm
                     Analysis of Deviance for point process models
```

#### Sensitivity diagnostics:

Classical measures of model sensitivity such as leverage and influence have been adapted to point process models.

```
leverage.ppm Leverage for point process model influence.ppm Influence for point process model dfbetas.ppm Parameter influence
```

#### Diagnostics for covariate effect:

Classical diagnostics for covariate effects have been adapted to point process models.

parres Partial residual plot addvar Added variable plot

rhohat Kernel estimate of covariate effect

rho2hat Kernel estimate of covariate effect (bivariate)

# Residual diagnostics:

Residuals for a fitted point process model, and diagnostic plots based on the residuals, were introduced in Baddeley et al (2005) and Baddeley, Rubak and Møller (2011).

Type demo(diagnose) for a demonstration of the diagnostics features.

diagnose.ppm diagnostic plots for spatial trend diagnostic Q-Q plot for interpoint interaction qqplot.ppm examples from Baddeley et al (2005) residualspaper model compensator of K function **Kcom** Gcom model compensator of G function score residual of K function Kres score residual of G function Gres pseudoscore residual of summary function psst pseudoscore residual of empty space function psstA pseudoscore residual of G function psstG compare compensators of several fitted models compareFit

#### Resampling and randomisation procedures

You can build your own tests based on randomisation and resampling using the following capabilities:

quadratresampleblock resamplingrjitterapply random displacements to points in a patternrshiftrandom shifting of (subsets of) pointsrthinrandom thinning

#### VIII. DOCUMENTATION

The online manual entries are quite detailed and should be consulted first for information about a particular function.

The paper by Baddeley and Turner (2005a) is a brief overview of the package. Baddeley and Turner (2005b) is a more detailed explanation of how to fit point process models to data. Baddeley (2010) is a complete set of notes from a 2-day workshop on the use of **spatstat**.

Type citation("spatstat") to get these references.

#### Licence

This library and its documentation are usable under the terms of the "GNU General Public License", a copy of which is distributed with the package.

#### Acknowledgements

Kasper Klitgaard Berthelsen, Abdollah Jalilian, Marie-Colette van Lieshout, Dominic Schuhmacher and Rasmus Waagepetersen made substantial contributions of code.

Additional contributions by Ang Qi Wei, Sandro Azaele, Malissa Baddeley, Colin Beale, Melanie Bell, Thomas Bendtsen, Ricardo Bernhardt, Andrew Bevan, Brad Biggerstaff, Leanne Bischof, Roger Bivand, Jose M. Blanco Moreno, Florent Bonneu, Julian Burgos, Simon Byers, Ya-Mei Chang, Jianbao Chen, Igor Chernayavsky, Y.C. Chin, Bjarke Christensen, Jean-Francois Coeurjolly, Robin Corria Ainslie, Marcelino de la Cruz, Peter Dalgaard, Sourav Das, Peter Diggle, Patrick Donnelly, Ian Dryden, Stephen Eglen, Olivier Flores, David Ford, Peter Forbes, Janet Franklin, Funwi-Gabga Neba, Oscar Garcia, Agnes Gault, Marc Genton, Julian Gilbey, Jason Goldstick, Pavel Grabarnik, C. Graf, Ute Hahn, Andrew Hardegen, Mandy Hering, Martin Bøgsted Hansen, Martin Hazelton, Juha Heikkinen, Kurt Hornik, Philipp Hunziker, Ross Ihaka, Aruna Jammalamadaka, Robert John-Chandran, Devin Johnson, Mike Kuhn, Jeff Laake, Frederic Lavancier, Tom Lawrence, Robert Lamb, Jonathan Lee, George Leser, Li Haitao, George Limitsios, Ben Madin, Kiran Marchikanti, Jeff Marcus, Robert Mark, Peter McCullagh, Monia Mahling, Jorge Mateu Mahiques, Ulf Mehlig, Sebastian Wastl Meyer, Mi Xiangcheng, Lore De Middeleer, Robin Milne, Jesper Møller, Erika Mudrak, Gopalan Nair, Linda Stougaard Nielsen, Felipe Nunes, Jens Oehlschlägel, Thierry Onkelinx, Sean O'Riordan, Evgeni Parilov, Jeff Picka, Nicolas Picard, Mike Porter, Sergiy Protsiv, Adrian Raftery, Suman Rakshit, Pablo Ramon, Xavier Raynaud, Matt Reiter, Tom Richardson, Brian Ripley, Ted Rosenbaum, Barry Rowlingson, Jason Rudokas, John Rudge, Christopher Ryan, Farzaneh Safavimanesh, Aila Särkkä, Katja Schladitz, Bryan Scott, Vadim Shcherbakov, Shen Guochun, Ida-Maria Sintorn, Yong Song, Malte Spiess, Mark Stevenson, Kaspar Stucki, Michael Sumner, P. Surovy, Ben Taylor, Thordis Linda Thorarinsdottir, Berwin Turlach, Kevin Ummer, Medha Uppala, Andrew van Burgel, Tobias Verbeke, Mikko Vihtakari, Alexendre Villers, Fabrice Vinatier, Hao Wang, H. Wendrock, Jan Wild, Selene Wong, Mike Zamboni and Achim Zeileis.

#### Author(s)

Adrian Baddeley <Adrian.Baddeley@uwa.edu.au> http://www.maths.uwa.edu.au/~adrian/, Rolf Turner <r.turner@auckland.ac.nz> and Ege Rubak <rubak@math.aau.dk>.

#### References

Baddeley, A. (2010) *Analysing spatial point patterns in R.* Workshop notes. Version 4.1. CSIRO online technical publication. URL: www.uwa.edu.au/resources/pf16h.html

Baddeley, A. and Turner, R. (2005a) Spatstat: an R package for analyzing spatial point patterns. *Journal of Statistical Software* **12**:6, 1–42. URL: www.jstatsoft.org, ISSN: 1548-7660.

Baddeley, A. and Turner, R. (2005b) Modelling spatial point patterns in R. In: A. Baddeley, P. Gregori, J. Mateu, R. Stoica, and D. Stoyan, editors, *Case Studies in Spatial Point Pattern Modelling*, Lecture Notes in Statistics number 185. Pages 23–74. Springer-Verlag, New York, 2006. ISBN: 0-387-28311-0.

Baddeley, A., Turner, R., Møller, J. and Hazelton, M. (2005) Residual analysis for spatial point processes. *Journal of the Royal Statistical Society, Series B* **67**, 617–666.

Baddeley, A., Rubak, E. and Møller, J. (2011) Score, pseudo-score and residual diagnostics for spatial point process models. *Statistical Science* **26**, 613–646.

Baddeley, A., Turner, R., Mateu, J. and Bevan, A. (2013) Hybrids of Gibbs point process models and their implementation. *Journal of Statistical Software* **55**:11, 1–43. http://www.jstatsoft.org/v55/i11/

Diggle, P.J. (2003) Statistical analysis of spatial point patterns, Second edition. Arnold.

Gelfand, A.E., Diggle, P.J., Fuentes, M. and Guttorp, P., editors (2010) *Handbook of Spatial Statistics*. CRC Press.

Huang, F. and Ogata, Y. (1999) Improvements of the maximum pseudo-likelihood estimators in various spatial statistical models. *Journal of Computational and Graphical Statistics* **8**, 510–530.

Waagepetersen, R. An estimating function approach to inference for inhomogeneous Neyman-Scott processes. *Biometrics* **63** (2007) 252–258.

# **Index**

*Topic <b>package</b>	as.matrix.im,8
spatstat-package, 1	as.owin, 6
*Topic <b>spatial</b>	as.polygonal, 7
spatstat-package, 1	as.ppp, $3$
[.im, 8	as.psp, 8
[.layered, 11	as.tess, 9
[.ppp, 5	a3. te33, /
[.psp, 9	BadGey, <i>18</i>
[.tess, 9	bdist.pixels, 7
[ <im, 8<="" th=""><td>bdist.points, 7</td></im,>	bdist.points, 7
[ <tess, 9<="" th=""><td>bdist.tiles, 7, 10</td></tess,>	bdist.tiles, 7, 10
[	beachcolourmap, <i>11</i>
addvar, <i>23</i>	bei, <i>4</i>
affine, 5, 7	berman.test, 22
affine.im, 8	betacells, 4
affine.psp,9	blur, 8
AIC, 18	border, 6
allstats, 13	boundingbox, 6
alltypes, 14	box3, <i>10</i>
amacrine, 4	boxx, <i>10</i>
anemones, 4	bramblecanes, 4
angles.psp,9	bronzefilter, 4
anova.lppm, 20	bw.diggle, 12
anova.ppm, 18, 22	bw.frac, <i>12</i>
anova.slrm, $20$	bw.ppl, <i>12</i>
ants, 4	bw.relrisk, <i>12</i>
applynbd, <i>14</i>	bw.scott, 12
area.owin, $7$	bw.smoothppp, 12
AreaInter, 18	bw.stoyan, 12
as.box3, <i>10</i>	by.ppp, <i>5</i>
as.data.frame.hyperframe, 11	
as.data.frame.im, $8$	cauchy.estK, 17
as.data.frame.psp, $9$	cauchy.estpcf, 17
as.hyperframe, 10, 11	cbind.hyperframe, 11
as.im, $8$	cdf.test,22
as.im.owin, 7	cells, 4
as.im.ppp, 6	centroid.owin, 7
as.interact, 18	chicago, <i>4</i> , <i>11</i>
as.mask,7	chop.tess,9
as.mask.psp,9	chorley,4

clarkevans, 12	diameter.owin, 7
clarkevans.test, 22	DiggleGatesStibbard, 18
clickbox, 6	DiggleGratton, 18
clickjoin, 11	dilated.areas, 7
clickpoly, 6	dilation, $6$
clickppp, 3	dirichlet, $6, 9$
clmfires, 4	dirichlet.weights, 19
closing, $6$	disc, <i>6</i>
clusterset, 12	discretise, 6
coef.ppm, <i>17</i>	distfun, <i>13</i>
coef.slrm, 21	distfun.lpp, 15
colourmap, 11	distfun.owin, 7
commonGrid, 7, 8	distfun.psp,9
compareFit, 23	distmap, <i>13</i>
compatible.im, $8$	distmap.owin, 7
complement.owin, $6$	distmap.psp,9
Concom, 18	drop1, <i>18</i>
connected.im, 8	duplicated.ppp, $6$
connected.owin, 7	
connected.ppp, 6	edges, <i>7</i> , <i>8</i>
contour.im, 8	effectfun, 18
convexhull, 6, 7	Emark, <i>14</i>
convolve.im, 8	endpoints.psp, 9
coords, 5, 10	envelope, <i>13</i> , <i>20</i> , <i>22</i>
copper, 4	envelope.lpp, 15
corners, 19	envelope.lppm, 20
crossdist, 13	envelope.pp3, <i>10</i> , <i>15</i>
crossdist.lpp, 15	eroded.areas, 7
crossdist.pp3, 16	eroded.volumes, 10
crossdist.ppx, 16	eroded.volumes.boxx, <i>10</i>
crossing.psp,9	erosion, $6$
cut.im, 8	eval.fasp, <i>13</i>
cut.ppp, 5, 14	eval.fv, <i>13</i>
	eval.im,8
data, 4	eval.linim, 20
dclf.progress, 22	exactdt, 13
dclf.test, 22	
default.dummy, 19	F3est, <i>15</i>
delaunay, 6, 10	Fest, <i>12</i>
delaunay.distance, 6	Fiksel, <i>18</i>
demohyper, 4	Finhom, 13
demopat, 4	finpines, 4
density.ppp, 5, 8, 12, 13	fitin, <i>18</i>
density.psp,9	fitted.kppm, 16
deriv.fv, <i>13</i>	fitted.ppm, 17
dfbetas.ppm, 22	fitted.slrm, 21
diagnose.ppm, 23	flipxy, 5, 6, 9
diameter.box3, 10	flu, 4
diameter.boxx, 10	formula.ppm, 17

Frame, 6 fryplot, 12	is.convex, 7 is.hybrid, 18
G3est, <i>15</i>	is.im, 8 is.mask, 7
Gcom, 23	is.polygonal, 7
Gcross, 14	is.psp, 9
Gdot, 14	is.rectangle, 7
Gest, <i>12</i>	is.subset.owin, 7
Geyer, 18	istat, <i>12</i>
Gfox, 16	15tat, 12
Ginhom, <i>13</i>	japanesepines, 5
glm, 2	Jcross, 14
Gmulti, 14	Jdot, <i>14</i>
gordon, 4	Jest, <i>12</i>
gorillas, 4	Jfox, <i>16</i>
Gres, 23	Jinhom, 13
gridcentres, 19	Jmulti, <i>14</i>
gridweights, 19	
	K3est, <i>15</i>
hamster, 4	Kcom, 23
Hardcore, 18	Kcross, <i>14</i>
harmonise.fv, 13	Kcross.inhom, <i>14</i>
harmonise.im, $8$	Kdot, <i>14</i>
Hest, <i>16</i>	Kdot.inhom, <i>14</i>
hextess, 9	Kest, <i>12</i>
hist.im, 8	Kest.fft, <i>13</i>
hsvim, 8	Kinhom, 13
humberside, 4	Kmeasure, <i>8</i> , <i>13</i>
Hybrid, 18, 19	Kmodel.kppm, 16
hyperframe, 11	Kmodel.ppm, 17
hyytiala, 5	Kmulti, <i>14</i>
identify non 6	kppm, 16, 22
identify.ppp, 6	Kres, 23
Iest, 14	Kscaled, 13
im, 3, 8 $imcov, 8$	Ksector, 13
	lansing, 5
<pre>improve.kppm, 16 incircle, 7</pre>	layered, 11
influence.ppm, 22	Lcross, 14
inside.owin, 7	Lcross.inhom, 14
integral.im, 8	Ldot, <i>14</i>
intensity, 12	Ldot.inhom, 14
intensity, 12	lengths.psp, 9
intensity.quadratcount, 12	LennardJones, 18
interp.colourmap, 11	Lest, <i>12</i>
interp.im, 8	letterR, 6
intersect.owin, 7	levelset, 8
intersect.tess, 9	leverage.ppm, 22
iplot, 5	lgcp.estK, 16
L	5-1

lgcp.estpcf, 16	matclust.estpcf, <i>16</i>
lineardisc, 11	mean.im, $8$
linearK, <i>15</i>	methods.linfun, 20
linearKcross, 15	methods.linnet, 11
linearKcross.inhom, 15	methods.lpp, 11
linearKdot, <i>15</i>	midpoints.psp,9
linearKdot.inhom, 15	mincontrast, 17
linearKinhom, 15	miplot, 12
linearmarkconnect, 15	model.depends, 18
linearmarkequal, 15	model.frame.ppm, 18
linearpcf, 15	model.images, 18
linearpcfcross, 15	mucosa, 5
linearpcfcross.inhom, 15	MultiHard, <i>19</i>
linearpcfdot, 15	MultiStrauss, 19
linearpcfdot.inhom, 15	MultiStraussHard, 19
linearpcfinhom, 15	murchison, 5
linfun, 20	mar crison, 5
Linhom, 13	nbfires, 5
linim, 20	nearest.raster.point, 7
linnet, 11	nearestsegment, 9
lm, 2	nnclean, 12
localK, <i>13</i>	nncross, 9, 13
localKinhom, 13	nncross.1pp, <i>15</i>
localL, 13	nncross.pp3, 16
localLinhom, 13	nndist, <i>13</i>
localpof, 13	nndist.lpp, 15
	nndist.pp3, 16
localpcfinhom, 13	
logLik.ppm, 18	nndist.ppx, <i>16</i> nnfun, <i>13</i>
logLik.slrm, 21	
lohboot, 13, 22	nnfun.lpp, 15
longleaf, 5	nnmap, <i>13</i>
lpp, 3, 11	nnmark, 5
1ppm, 20	nnmean, 14
mad programs 22	nnvario, <i>14</i>
mad.progress, 22	nnwhich, 13
mad.test, 22	nnwhich.lpp, <i>15</i>
markconnect, 14	nnwhich.pp3, 16
markcorr, 14	nnwhich.ppx, 16
markcorrint, 14	npoints, <i>5</i> , <i>10</i>
markmean, 14	nztrees, 5
marks, 5	
marks.psp, 9	opening, 6
marks<-, 3	Ord, 19
marks <psp,9< td=""><td>OrdThresh, 19</td></psp,9<>	OrdThresh, 19
markstat, 14	osteo, 5
marktable, 14	owin, $3, 6$
markvar, 14	
markvario, 14	pairdist, 13
matclust.estK, <i>16</i>	pairdist.lpp, <i>15</i>

pairdist.pp3, 15	predict.lppm, 20
pairdist.ppx, 16	predict.ppm, 17
PairPiece, 19	predict.slrm, 21
Pairwise, 19	print.ppm, 18
paracou, 5	print.psp,9
parres, 23	project.ppm, 18
pcf, 12, 13	project2segment, 9
pcf3est, <i>15</i>	psp, 3, 8
pcfcross, 14	psst, <i>23</i>
pcfcross.inhom, 14	psstA, <i>23</i>
pcfdot, 14	psstG, <i>23</i>
pcfdot.inhom, <i>14</i>	pyramidal, 5
pcfinhom, 13	
pcfmodel.kppm, 16	qqplot.ppm, 22, 23
pcfmodel.ppm, 17	quad, <i>19</i>
pcfmulti, 14	quadrat.test, 22
perimeter, 7	quadratcount, 12
periodify, 5, 7, 9	quadratresample, 4, 21, 23
persp.im, 8	quadrats, $9$
pixelcentres, 7, 8	quadscheme, 19
pixellate, 8	quantile.im, $8$
pixellate.owin, 7	_
pixellate.ppp, 6	raster.x, 7
pixellate.psp, 9	raster.y,7
pixelquad, 19	rbind.hyperframe, 11
	rCauchy, 4, 16, 21
plot.colourmap, 11	rcell, 4, 21
plot.fv, 13	rDGS, 3
plot.hyperframe, 11	rDiggleGratton, $3$
plot.im, 8	redwood, 5
plot.kppm, 16	redwoodfull, 5
plot.layered, 11	reflect, 5
plot.linim, 20	relrisk, <i>12–14</i>
plot.owin, 6	residuals.ppm, 17
plot.pp3, 10	residualspaper, 5, 23
plot.ppm, 17	rGaussPoisson, 4, 21
plot.ppp, 5	rgbim, 8
plot.psp, 9	rHardcore, 3
plot.slrm, 21	rho2hat, <i>12</i> , <i>23</i>
plot.tess,9	rhohat, <i>12</i> , <i>23</i>
pointsOnLines, 9	ripras, 6
Poisson, 18	rjitter, <i>3</i> , <i>4</i> , <i>21</i> , <i>23</i>
ponderosa, 5	rknn, <i>13</i>
pp3, <i>3</i> , <i>10</i>	rlabel, 4
ppm, 17, 22	rLGCP, 16, 21
ppp, <i>3</i>	rlinegrid, $9,22$
pppdist, 14	rMatClust, 4, 16, 21
ppx, 3, 10	rMaternI, <i>3</i> , <i>21</i>
predict.kppm, 16	rMaternII, 3, 21

rmh, 4, 22	simdat, 5
rmh.ppm, 18, 19	simplenet, <i>11</i>
rMosaicField, 22	simplify.owin, 6
rMosaicSet, 22	simulate.kppm, <i>16</i> , <i>22</i>
rmpoint, 3, 21	simulate.ppm, 4, 18, 20, 22
rmpoispp, <i>3</i> , <i>21</i>	simulate.slrm,21
rNeymanScott, 3, 4, 21	slrm, 20
rotate, <i>5</i> , <i>6</i>	Smooth.fv, 13
${\tt rotate.im}, 8$	Smooth.im, 8
rotate.psp, 9	Smooth.ppp, <i>5</i> , <i>12</i> , <i>13</i>
rpoint, 3, 21	Softcore, 19
rpoisline, 9, 22	solutionset, $8$
rpoislinetess, 10, 22	spatialcdf, <i>12</i>
rpoislpp, <i>11</i> , <i>15</i>	<pre>spatstat (spatstat-package), 1</pre>
rpoispp, <i>3</i> , <i>21</i>	spatstat-package, 1
rpoispp3, <i>10</i>	spatstat.options, 6, 7, 18
rpoisppOnLines, 4, 21	split.ppp, 5
rpoisppx, 10	spokes, 19
rPoissonCluster,4	sporophores, 5
rshift, 4, 21, 23	spruces, 5
rSSI, <i>3</i> , <i>21</i>	square, 6
rstrat, 3, 19, 21	step, <i>18</i>
rStrauss, <i>3</i> , <i>21</i>	Strauss, 19
rsyst, <i>3</i> , <i>21</i>	StraussHard, 19
rthin, 4, 21, 23	subset.lpp, <i>11</i>
rThomas, 4, 16, 21	subset.pp3, <i>10</i>
runifdisc, 3, 21	subset.ppp, 5
runiflpp, <i>11</i> , <i>15</i>	subset.ppx, 10
runifpoint, $3, 21$	summary, <i>8</i> , <i>12</i> , <i>19</i>
runifpoint3, 10	summary.ppm, 18
runifpointOnLines, 4, 21	summary.psp,9
runifpointx, 10	superimpose, $5, 9$
rVarGamma, 4, 16, 21	swedishpines, 5
SatPiece, 19	tess, 3, 9
Saturated, 19	thomas.estK, <i>16</i>
scalardilate, 5	thomas.estpcf, <i>16</i>
scaletointerval, 8	tile.areas, <i>10</i>
scan.test, <i>14</i> , <i>22</i>	tiles, 9
selfcrossing.psp, 9	transect.im, 8
setcov, 7, 8	Triplets, 19
setminus.owin, 7	Tstat, <i>13</i>
shapley, 5	tweak.colourmap, <i>11</i>
sharpen.ppp, 6, 12, 13	
shift, 5, 6	union.owin, 7
shift.im, 8	unique.ppp, 6
shift.psp,9	unitname.box3, <i>10</i>
shortside.box3, <i>10</i>	unitname.pp3, 10
shortside.boxx, <i>10</i>	unitname.ppx, 10

```
unmark, 5
unmark.psp, 9
update.kppm, 16
update.ppm, 18
urkiola, 5
valid.ppm, 18
varblock, 13, 21
vargamma.estK, 17
vargamma.estpcf, 17
vcov.kppm, 16
vcov.ppm, 18
vcov.slrm, 21
Vmark, 14
volume.box3, 10
volume.boxx, 10
waka, 5
waterstriders, 5
Window, 6
with.fv, 13
with.hyperframe, 11
{\tt zapsmall.im}, {\color{red} 8}
```