Spatstat Quick Reference guide

February 8, 2017

spatstat-package

The Spatstat Package

Description

This is a summary of the features of **spatstat**, a package in R for the statistical analysis of spatial point patterns.

Details

spatstat is a package for the statistical analysis of spatial data. Its main focus is the analysis of spatial patterns of points in two-dimensional space. The points may carry auxiliary data ('marks'), and the spatial region in which the points were recorded may have arbitrary shape.

The package is designed to support a complete statistical analysis of spatial data. It supports

- creation, manipulation and plotting of point patterns;
- · exploratory data analysis;
- spatial random sampling;
- simulation of point process models;
- parametric model-fitting;
- non-parametric smoothing and regression;
- formal inference (hypothesis tests, confidence intervals);
- · model diagnostics.

Apart from two-dimensional point patterns and point processes, **spatstat** also supports point patterns in three dimensions, point patterns in multidimensional space-time, point patterns on a linear network, patterns of line segments in two dimensions, and spatial tessellations and random sets in two dimensions.

The package can fit several types of point process models to a point pattern dataset:

- Poisson point process models (by Berman-Turner approximate maximum likelihood or by spatial logistic regression)
- Gibbs/Markov point process models (by Baddeley-Turner approximate maximum pseudolikelihood, Coeurjolly-Rubak logistic likelihood, or Huang-Ogata approximate maximum likelihood)

Cox/cluster point process models (by Waagepetersen's two-step fitting procedure and minimum contrast, composite likelihood, or Palm likelihood)

• determinantal point process models (by Waagepetersen's two-step fitting procedure and minimum contrast, composite likelihood, or Palm likelihood)

The models may include spatial trend, dependence on covariates, and complicated interpoint interactions. Models are specified by a formula in the R language, and are fitted using a function analogous to 1m and g1m. Fitted models can be printed, plotted, predicted, simulated and so on.

Getting Started

For a quick introduction to **spatstat**, read the package vignette *Getting started with spatstat* installed with **spatstat**. To read that document, you can either

- visit cran.r-project.org/web/packages/spatstat and click on Getting Started with Spatstat
- start R, type library(spatstat) and vignette('getstart')
- start R, type help.start() to open the help browser, and navigate to Packages > spatstat > Vignettes.

Once you have installed **spatstat**, start R and type library(spatstat). Then type beginner for a beginner's introduction, or demo(spatstat) for a demonstration of the package's capabilities.

For a complete course on **spatstat**, and on statistical analysis of spatial point patterns, read the book by Baddeley, Rubak and Turner (2015). Other recommended books on spatial point process methods are Diggle (2014), Gelfand et al (2010) and Illian et al (2008).

The **spatstat** package includes over 50 datasets, which can be useful when learning the package. Type demo(data) to see plots of all datasets available in the package. Type vignette('datasets') for detailed background information on these datasets, and plots of each dataset.

For information on converting your data into **spatstat** format, read Chapter 3 of Baddeley, Rubak and Turner (2015). This chapter is available free online, as one of the sample chapters at the book companion website, **spatstat.github.io/book**.

For information about handling data in **shapefiles**, see Chapter 3, or the Vignette *Handling shapefiles in the spatstat package*, installed with **spatstat**, accessible as vignette('shapefiles').

Updates

New versions of **spatstat** are released every 8 weeks. Users are advised to update their installation of **spatstat** regularly.

Type latest.news to read the news documentation about changes to the current installed version of **spatstat**.

See the Vignette *Summary of recent updates*, installed with **spatstat**, which describes the main changes to **spatstat** since the book (Baddeley, Rubak and Turner, 2015) was published. It is accessible as vignette('updates').

Type news(package="spatstat") to read news documentation about all previous versions of the package.

FUNCTIONS AND DATASETS

Following is a summary of the main functions and datasets in the **spatstat** package. Alternatively an alphabetical list of all functions and datasets is available by typing library(help=spatstat).

For further information on any of these, type help(name) or ?name where name is the name of the function or dataset.

CONTENTS:

I. Creating and manipulating dataII. Exploratory Data Analysis

III. Model fitting (Cox and cluster models)
IV. Model fitting (Poisson and Gibbs models)
V. Model fitting (determinantal point processes)
VI. Model fitting (spatial logistic regression)

VII. Simulation

VIII. Tests and diagnosticsIX. Documentation

I. CREATING AND MANIPULATING DATA

Types of spatial data:

The main types of spatial data supported by **spatstat** are:

ppp point pattern
owin window (spatial region)
im pixel image
psp line segment pattern
tess tessellation
pp3 three-dimensional point pattern
ppx point pattern in any number of dimensions

ppx point pattern in any number of diffici

1pp point pattern on a linear network

To create a point pattern:

ppp create a point pattern from (x,y) and window information ppp(x, y, xlim, ylim) for rectangular window ppp(x, y, poly) for polygonal window ppp(x, y, mask) for binary image window convert other types of data to a ppp object clickppp interactively add points to a plot attach/reassign marks to a point pattern

To simulate a random point pattern:

runifpoint generate n independent uniform random points rpoint generate n independent random points rmpoint generate n independent multitype random points rpoispp simulate the (in)homogeneous Poisson point process simulate the (in)homogeneous multitype Poisson point process rmpoispp generate n independent uniform random points in disc runifdisc rstrat stratified random sample of points systematic random sample of points rsyst rjitter apply random displacements to points in a pattern simulate the Matérn Model I inhibition process rMaternI simulate the Matérn Model II inhibition process rMaternII simulate Simple Sequential Inhibition process rSSI simulate Strauss process (perfect simulation) rStrauss simulate Hard Core process (perfect simulation) rHardcore

rStraussHard simulate Strauss-hard core process (perfect simulation)
rDiggleGratton simulate Diggle-Gratton process (perfect simulation)
rDGS simulate Diggle-Gates-Stibbard process (perfect simulation)

rPenttinen simulate Penttinen process (perfect simulation)
rNeymanScott simulate a general Neyman-Scott process
rPoissonCluster simulate a general Poisson cluster process
rMatClust simulate the Matérn Cluster process
rThomas simulate the Thomas process

rGaussPoisson simulate the Gauss-Poisson cluster process rCauchy simulate Neyman-Scott Cauchy cluster process

rVarGamma simulate Neyman-Scott Variance Gamma cluster process

rthin random thinning

rcell simulate the Baddeley-Silverman cell process

rmh simulate Gibbs point process using Metropolis-Hastings simulate.ppm simulate Gibbs point process using Metropolis-Hastings runifpointOnLines generate n random points along specified line segments generate Poisson random points along specified line segments

To randomly change an existing point pattern:

rshift random shifting of points

rjitter apply random displacements to points in a pattern

rthin random thinning

rlabel random (re)labelling of a multitype point pattern

quadratresample block resampling

Standard point pattern datasets:

Datasets in **spatstat** are lazy-loaded, so you can simply type the name of the dataset to use it; there is no need to type data(amacrine) etc.

Type demo(data) to see a display of all the datasets installed with the package.

Type vignette('datasets') for a document giving an overview of all datasets, including background information, and plots.

amacrine Austin Hughes' rabbit amacrine cells
anemones Upton-Fingleton sea anemones data
ants Harkness-Isham ant nests data
bdspots Breakdown spots in microelectrodes

bei Tropical rainforest trees

betacells Waessle et al. cat retinal ganglia data

bramblecanes Bramble Canes data
bronzefilter Bronze Filter Section data
cells Crick-Ripley biological cells data

chicagochorleychorley-Ribble cancer dataclmfiresCastilla-La Mancha forest fires

copper Berman-Huntington copper deposits data

dendrite Dendritic spines

demohyper
demopat
finpines
flu
Synthetic point patterns
Synthetic point pattern
Finnish Pines data
Influenza virus proteins

> gordon People in Gordon Square, London

gorillas Gorilla nest sites

hamster Aherne's hamster tumour data

humberside North Humberside childhood leukaemia data

hyytiala Mixed forest in Hyytiälä, Finland

Japanese Pines data japanesepines lansing Lansing Woods data Longleaf Pines data longleaf Cells in gastric mucosa mucosa murchison Murchison gold deposits New Brunswick fires data nbfires Mark-Esler-Ripley trees data nztrees osteo Osteocyte lacunae (3D, replicated) Kimboto trees in Paracou, French Guiana paracou ponderosa Getis-Franklin ponderosa pine trees data Pyramidal neurons from 31 brains pyramidal redwood Strauss-Ripley redwood saplings data Strauss redwood saplings data (full set) redwoodfull Data from Baddeley et al (2005) residualspaper Galaxies in an astronomical survey

simdat Simulated point pattern (inhomogeneous, with interaction)

spiders Spider webs on mortar lines of brick wall

Mycorrhizal fungi around a tree sporophores

Spruce trees in Saxonia spruces

swedishpines Strand-Ripley Swedish pines data

Urkiola Woods data urkiola

Trees in Waka national park waka waterstriders Insects on water surface

To manipulate a point pattern:

shapley

plot a point pattern (e.g. plot(X)) plot.ppp plot a point pattern interactively iplot

edit.ppp interactive text editor

[.ppp extract or replace a subset of a point pattern

pp[subset] or pp[subwindow]

extract subset of point pattern satisfying a condition subset.ppp

combine several point patterns superimpose

apply a function to sub-patterns of a point pattern by.ppp

classify the points in a point pattern cut.ppp divide pattern into sub-patterns split.ppp

unmark remove marks

count the number of points npoints

coords extract coordinates, change coordinates extract marks, change marks or attach marks marks

rotate pattern rotate translate pattern shift

swap x and y coordinates flipxy reflect in the origin reflect

periodify make several translated copies apply affine transformation affine apply scalar dilation scalardilate

kernel estimation of point pattern intensity density.ppp

kernel smoothing of marks of point pattern Smooth.ppp nnmark mark value of nearest data point sharpen.ppp data sharpening interactively identify points identify.ppp remove duplicate points unique.ppp determine which points are duplicates duplicated.ppp find clumps of points connected.ppp dirichlet compute Dirichlet-Voronoi tessellation compute Delaunay triangulation delaunay delaunayDistance graph distance in Delaunay triangulation convexhull compute convex hull discretise coordinates discretise approximate point pattern by pixel image pixellate.ppp approximate point pattern by pixel image as.im.ppp

See spatstat.options to control plotting behaviour.

To create a window:

An object of class "owin" describes a spatial region (a window of observation).

Create a window object owin owin(xlim, ylim) for rectangular window owin(poly) for polygonal window owin(mask) for binary image window Window Extract window of another object Frame Extract the containing rectangle ('frame') of another object Convert other data to a window object as.owin square make a square window make a circular window disc make an elliptical window ellipse Ripley-Rasson estimator of window, given only the points ripras convexhull compute convex hull of something polygonal window in the shape of the R logo letterR interactively draw a polygonal window clickpoly interactively draw a rectangle clickbox

To manipulate a window:

plot.owin	plot a window.
	plot(W)
boundingbox	Find a tight bounding box for the window
erosion	erode window by a distance r
dilation	dilate window by a distance r
closing	close window by a distance r
opening	open window by a distance r
border	difference between window and its erosion/dilation
complement.owin	invert (swap inside and outside)
simplify.owin	approximate a window by a simple polygon
rotate	rotate window
flipxy	swap x and y coordinates
shift	translate window
periodify	make several translated copies

```
affine apply affine transformation as.data.frame.owin convert window to data frame
```

Digital approximations:

Make a discrete pixel approximation of a given window as.mask convert window to pixel image as.im.owin pixellate.owin convert window to pixel image find common pixel grid for windows commonGrid nearest.raster.point map continuous coordinates to raster locations raster x coordinates raster.x raster y coordinates raster.y raster x and y coordinates raster.xy convert pixel mask to polygonal window as.polygonal

See spatstat.options to control the approximation

Geometrical computations with windows:

edges	extract boundary edges
intersect.owin	intersection of two windows
union.owin	union of two windows
setminus.owin	set subtraction of two windows
inside.owin	determine whether a point is inside a window
area.owin	compute area
perimeter	compute perimeter length
diameter.owin	compute diameter
incircle	find largest circle inside a window
inradius	radius of incircle
connected.owin	find connected components of window
eroded.areas	compute areas of eroded windows
dilated.areas	compute areas of dilated windows
bdist.points	compute distances from data points to window boundary
bdist.pixels	compute distances from all pixels to window boundary
bdist.tiles	boundary distance for each tile in tessellation
distmap.owin	distance transform image
distfun.owin	distance transform
centroid.owin	compute centroid (centre of mass) of window
is.subset.owin	determine whether one window contains another
is.convex	determine whether a window is convex
convexhull	compute convex hull
triangulate.owin	decompose into triangles
as.mask	pixel approximation of window
as.polygonal	polygonal approximation of window
is.rectangle	test whether window is a rectangle
is.polygonal	test whether window is polygonal
is.mask	test whether window is a mask
setcov	spatial covariance function of window
pixelcentres	extract centres of pixels in mask
clickdist	measure distance between two points clicked by user

Pixel images: An object of class "im" represents a pixel image. Such objects are returned by some

of the functions in **spatstat** including Kmeasure, setcov and density.ppp.

create a pixel image convert other data to a pixel image as.im pixellate convert other data to a pixel image as.matrix.im convert pixel image to matrix as.data.frame.im convert pixel image to data frame convert pixel image to function as.function.im plot a pixel image on screen as a digital image plot.im draw contours of a pixel image contour.im persp.im draw perspective plot of a pixel image rgbim create colour-valued pixel image create colour-valued pixel image hsvim extract a subset of a pixel image [.im Γ<-.im replace a subset of a pixel image rotate.im rotate pixel image shift.im apply vector shift to pixel image apply affine transformation to image affine.im print very basic information about image X summary(X) summary of image X histogram of image hist.im mean.im mean pixel value of image integral of pixel values integral.im quantile.im quantiles of image convert numeric image to factor image cut.im test whether an object is a pixel image is.im interp.im interpolate a pixel image apply Gaussian blur to image blur apply Gaussian blur to image Smooth.im connected.im find connected components compatible.im test whether two images have compatible dimensions make images compatible harmonise.im commonGrid find a common pixel grid for images eval.im evaluate any expression involving images scaletointerval rescale pixel values set very small pixel values to zero zapsmall.im levelset level set of an image solutionset region where an expression is true imcov spatial covariance function of image spatial convolution of images convolve.im transect.im line transect of image pixelcentres extract centres of pixels transmat convert matrix of pixel values to a different indexing convention random pixel noise rnoise

Line segment patterns

An object of class "psp" represents a pattern of straight line segments.

psp	create a line segment pattern
as.psp	convert other data into a line segment pattern
edges	extract edges of a window

is.psp	determine whether a dataset has class "psp"
plot.psp	plot a line segment pattern
print.psp	print basic information
summary.psp	print summary information
[.psp	extract a subset of a line segment pattern
as.data.frame.psp	convert line segment pattern to data frame
marks.psp	extract marks of line segments
marks <psp< td=""><td>assign new marks to line segments</td></psp<>	assign new marks to line segments
unmark.psp	delete marks from line segments
midpoints.psp	compute the midpoints of line segments
endpoints.psp	extract the endpoints of line segments
lengths.psp	compute the lengths of line segments
angles.psp	compute the orientation angles of line segments
superimpose	combine several line segment patterns
flipxy	swap x and y coordinates
rotate.psp	rotate a line segment pattern
shift.psp	shift a line segment pattern
periodify	make several shifted copies
affine.psp	apply an affine transformation
pixellate.psp	approximate line segment pattern by pixel image
as.mask.psp	approximate line segment pattern by binary mask
distmap.psp	compute the distance map of a line segment pattern
distfun.psp	compute the distance map of a line segment pattern
density.psp	kernel smoothing of line segments
selfcrossing.psp	find crossing points between line segments
selfcut.psp	cut segments where they cross
crossing.psp	find crossing points between two line segment patterns
nncross	find distance to nearest line segment from a given point
nearestsegment	find line segment closest to a given point
project2segment	find location along a line segment closest to a given point
pointsOnLines	generate points evenly spaced along line segment
rpoisline	generate a realisation of the Poisson line process inside a window
rlinegrid	generate a random array of parallel lines through a window

Tessellations

An object of class "tess" represents a tessellation.

tess	create a tessellation
quadrats	create a tessellation of rectangles
hextess	create a tessellation of hexagons
quantess	quantile tessellation
as.tess	convert other data to a tessellation
plot.tess	plot a tessellation
tiles	extract all the tiles of a tessellation
[.tess	extract some tiles of a tessellation
[<tess< td=""><td>change some tiles of a tessellation</td></tess<>	change some tiles of a tessellation
intersect.tess	intersect two tessellations
	or restrict a tessellation to a window
chop.tess	subdivide a tessellation by a line
dirichlet	compute Dirichlet-Voronoi tessellation of points
delaunay	compute Delaunay triangulation of points
rpoislinetess	generate tessellation using Poisson line process

> tile.areas area of each tile in tessellation bdist.tiles boundary distance for each tile in tessellation

Three-dimensional point patterns

An object of class "pp3" represents a three-dimensional point pattern in a rectangular box. The box is represented by an object of class "box3".

> pp3 create a 3-D point pattern plot a 3-D point pattern plot.pp3 coords extract coordinates as.hyperframe extract coordinates extract subset of 3-D point pattern subset.pp3 name of unit of length unitname.pp3 npoints count the number of points runifpoint3 generate uniform random points in 3-D generate Poisson random points in 3-D rpoispp3 generate simulation envelopes for 3-D pattern envelope.pp3 box3 create a 3-D rectangular box as.box3 convert data to 3-D rectangular box name of unit of length unitname.box3 diameter of box diameter.box3 volume.box3 volume of box shortest side of box shortside.box3 eroded.volumes volumes of erosions of box

Multi-dimensional space-time point patterns

An object of class "ppx" represents a point pattern in multi-dimensional space and/or time.

ррх create a multidimensional space-time point pattern coords extract coordinates as.hyperframe extract coordinates subset.ppx extract subset name of unit of length unitname.ppx npoints count the number of points generate uniform random points runifpointx generate Poisson random points rpoisppx define multidimensional box boxx diameter.boxx diameter of box volume.boxx volume of box shortest side of box shortside.boxx volumes of erosions of box

Point patterns on a linear network

eroded.volumes.boxx

An object of class "linnet" represents a linear network (for example, a road network).

create a linear network linnet clickjoin interactively join vertices in network interactively plot network iplot.linnet simplenet simple example of network lineardisc disc in a linear network delaunayNetwork network of Delaunay triangulation

```
dirichletNetwork methods.linnet methods for linnet objects methods of network methods for linnet objects nodes of network approximate by pixel image
```

An object of class "lpp" represents a point pattern on a linear network (for example, road accidents on a road network).

lpp	create a point pattern on a linear network
methods.lpp	methods for 1pp objects
subset.lpp	method for subset
rpoislpp	simulate Poisson points on linear network
runiflpp	simulate random points on a linear network
chicago	Chicago street crime data
dendrite	Dendritic spines data
spiders	Spider webs on mortar lines of brick wall

Hyperframes

A hyperframe is like a data frame, except that the entries may be objects of any kind.

hyperframe	create a hyperframe
as.hyperframe	convert data to hyperframe
plot.hyperframe	plot hyperframe
with.hyperframe	evaluate expression using each row of hyperframe
cbind.hyperframe	combine hyperframes by columns
rbind.hyperframe	combine hyperframes by rows
as.data.frame.hyperframe	convert hyperframe to data frame
subset.hyperframe	method for subset
head.hyperframe	first few rows of hyperframe
tail.hyperframe	last few rows of hyperframe

Layered objects

A layered object represents data that should be plotted in successive layers, for example, a background and a foreground.

```
layered create layered object
plot.layered plot layered object
[.layered extract subset of layered object
```

Colour maps

A colour map is a mechanism for associating colours with data. It can be regarded as a function, mapping data to colours. Using a colourmap object in a plot command ensures that the mapping from numbers to colours is the same in different plots.

colourmap	create a colour map
plot.colourmap	plot the colour map only
tweak.colourmap	alter individual colour values
<pre>interp.colourmap</pre>	make a smooth transition between colours
beachcolourmap	one special colour map

II. EXPLORATORY DATA ANALYSIS

Inspection of data:

Classical exploratory tools:

clarkevans Clark and Evans aggregation index

fryplot Fry plot

miplot Morisita Index plot

Smoothing:

density.ppp kernel smoothed density/intensity kernel estimate of relative risk relrisk spatial interpolation of marks Smooth.ppp cross-validated bandwidth selection for density.ppp bw.diggle likelihood cross-validated bandwidth selection for density.ppp bw.ppl bw.scott Scott's rule of thumb for density estimation bw.relrisk cross-validated bandwidth selection for relrisk bw.smoothppp cross-validated bandwidth selection for Smooth.ppp bw.frac bandwidth selection using window geometry

Stoyan's rule of thumb for bandwidth for pcf

Modern exploratory tools:

bw.stoyan

clusterset
nnclean
sharpen.ppp
rhohat
spatialcdf
roc

Allard-Fraley feature detection
Byers-Raftery feature detection
Choi-Hall data sharpening
Kernel estimate of covariate effect
Kernel estimate of effect of two covariates
Spatialcdf
roc
Receiver operating characteristic curve

Summary statistics for a point pattern: Type demo(sumfun) for a demonstration of many of the summary statistics.

intensity Mean intensity quadratcount Quadrat counts

 $\begin{array}{ll} {\rm intensity.quadratcount} & {\rm Mean\ intensity\ in\ quadrats} \\ {\rm Fest} & {\rm empty\ space\ function\ } F \end{array}$

Gest nearest neighbour distribution function G Jest J-function J=(1-G)/(1-F)

pcfpair correlation functionKinhomK for inhomogeneous point patternsLinhomL for inhomogeneous point patternspcfinhompair correlation for inhomogeneous patternsFinhomF for inhomogeneous point patternsGinhomG for inhomogeneous point patternsJinhomJ for inhomogeneous point patterns

localL Getis-Franklin neighbourhood density function

localK neighbourhood K-function localpcf local pair correlation function

Kest.fft fast K-function using FFT for large datasets

Kmeasure reduced second moment measure

envelope simulation envelopes for a summary function

variances and confidence intervals

for a summary function

lohboot bootstrap for a summary function

Related facilities:

plot.fv plot a summary function eval.fv evaluate any expression involving summary functions make functions compatible harmonise.fv eval.fasp evaluate any expression involving an array of functions with.fv evaluate an expression for a summary function Smooth.fv apply smoothing to a summary function deriv.fv calculate derivative of a summary function pool.fv pool several estimates of a summary function nndist nearest neighbour distances find nearest neighbours nnwhich distances between all pairs of points pairdist distances between points in two patterns crossdist nearest neighbours between two point patterns nncross exactdt distance from any location to nearest data point distance map image distmap distance map function distfun nearest point image nnmap nearest point function nnfun kernel smoothed density density.ppp Smooth.ppp spatial interpolation of marks relrisk kernel estimate of relative risk sharpen.ppp data sharpening theoretical distribution of nearest neighbour distance rknn

Summary statistics for a multitype point pattern: A multitype point pattern is represented by an object X of class "ppp" such that marks (X) is a factor.

relrisk

kernel estimation of relative risk

```
scan.test
                                     spatial scan test of elevated risk
Gcross, Gdot, Gmulti
                                     multitype nearest neighbour distributions G_{ij}, G_{i\bullet}
Kcross,Kdot, Kmulti
                                     multitype K-functions K_{ij}, K_{i\bullet}
Lcross, Ldot
                                     multitype L-functions L_{ij}, L_{i\bullet}
                                     multitype J-functions J_{ij}, J_{i\bullet}
Jcross, Jdot, Jmulti
                                     multitype pair correlation function g_{ij}
pcfcross
                                     multitype pair correlation function g_{i\bullet}
pcfdot
pcfmulti
                                     general pair correlation function
markconnect
                                     marked connection function p_{ij}
alltypes
                                     estimates of the above for all i, j pairs
                                     multitype I-function
Iest
                                     inhomogeneous counterparts of Kcross, Kdot
Kcross.inhom, Kdot.inhom
Lcross.inhom,Ldot.inhom
                                     inhomogeneous counterparts of Lcross, Ldot
pcfcross.inhom,pcfdot.inhom
                                     inhomogeneous counterparts of pcfcross, pcfdot
```

Summary statistics for a marked point pattern: A marked point pattern is represented by an object X of class "ppp" with a component X\$marks. The entries in the vector X\$marks may be numeric, complex, string or any other atomic type. For numeric marks, there are the following functions:

markmean	smoothed local average of marks
markvar	smoothed local variance of marks
markcorr	mark correlation function
markcrosscorr	mark cross-correlation function
markvario	mark variogram
Kmark	mark-weighted K function
Emark	mark independence diagnostic $E(r)$
Vmark	mark independence diagnostic $V(r)$
nnmean	nearest neighbour mean index
nnvario	nearest neighbour mark variance index

For marks of any type, there are the following:

Alternatively use cut.ppp to convert a marked point pattern to a multitype point pattern.

Programming tools:

```
applynbd apply function to every neighbourhood in a point pattern apply function to the marks of neighbours in a point pattern tabulate the marks of neighbours in a point pattern find the optimal match between two point patterns
```

Summary statistics for a point pattern on a linear network:

These are for point patterns on a linear network (class 1pp). For unmarked patterns:

linearK	K function on linear network
linearKinhom	inhomogeneous K function on linear network
linearpcf	pair correlation function on linear network

linearpcfinhom inhomogeneous pair correlation on linear network

For multitype patterns:

linearKcross	K function between two types of points
linearKdot	K function from one type to any type
linearKcross.inhom	Inhomogeneous version of linearKcross
linearKdot.inhom	Inhomogeneous version of linearKdot
linearmarkconnect	Mark connection function on linear network
linearmarkequal	Mark equality function on linear network
linearpcfcross	Pair correlation between two types of points
linearpcfdot	Pair correlation from one type to any type
linearpcfcross.inhom	Inhomogeneous version of linearpcfcross
linearpcfdot.inhom	Inhomogeneous version of linearpcfdot

Related facilities:

pairdist.lpp	distances between pairs
crossdist.lpp	distances between pairs
nndist.lpp	nearest neighbour distances
nncross.lpp	nearest neighbour distances
nnwhich.lpp	find nearest neighbours
nnfun.lpp	find nearest data point
density.lpp	kernel smoothing estimator of intensity
distfun.lpp	distance transform
envelope.lpp	simulation envelopes
rpoislpp	simulate Poisson points on linear network
runiflpp	simulate random points on a linear network

It is also possible to fit point process models to 1pp objects. See Section IV.

Summary statistics for a three-dimensional point pattern:

These are for 3-dimensional point pattern objects (class pp3).

Related facilities:

simulation envelopes
distances between all pairs of points
distances between points in two patterns
nearest neighbour distances
find nearest neighbours
find nearest neighbours in another pattern

Computations for multi-dimensional point pattern:

These are for multi-dimensional space-time point pattern objects (class ppx).

```
pairdist.ppx distances between all pairs of points
```

```
crossdist.ppx distances between points in two patterns
nndist.ppx nearest neighbour distances
nnwhich.ppx find nearest neighbours
```

Summary statistics for random sets:

These work for point patterns (class ppp), line segment patterns (class psp) or windows (class owin).

 $\begin{array}{ll} {\sf Hest} & {\sf spherical\ contact\ distribution\ } H \\ {\sf Gfox} & {\sf Foxall\ } G\text{-function} \\ {\sf Jfox} & {\sf Foxall\ } J\text{-function} \\ \end{array}$

III. MODEL FITTING (COX AND CLUSTER MODELS)

Cluster process models (with homogeneous or inhomogeneous intensity) and Cox processes can be fitted by the function kppm. Its result is an object of class "kppm". The fitted model can be printed, plotted, predicted, simulated and updated.

kppm plot.kppm	Fit model Plot the fitted model
summary.kppm	Summarise the fitted model
fitted.kppm	Compute fitted intensity
predict.kppm	Compute fitted intensity
update.kppm	Update the model
<pre>improve.kppm</pre>	Refine the estimate of trend
simulate.kppm	Generate simulated realisations
vcov.kppm	Variance-covariance matrix of coefficients
coef.kppm	Extract trend coefficients
formula.kppm	Extract trend formula
parameters	Extract all model parameters
clusterfield	Compute offspring density
clusterradius	Radius of support of offspring density
Kmodel.kppm	K function of fitted model
<pre>pcfmodel.kppm</pre>	Pair correlation of fitted model

For model selection, you can also use the generic functions step, drop1 and AIC on fitted point process models.

The theoretical models can also be simulated, for any choice of parameter values, using rThomas, rMatClust, rCauchy, rVarGamma, and rLGCP.

Lower-level fitting functions include:

```
lgcp.estK
                    fit a log-Gaussian Cox process model
                    fit a log-Gaussian Cox process model
lgcp.estpcf
                    fit the Thomas process model
thomas.estK
                    fit the Thomas process model
thomas.estpcf
                    fit the Matern Cluster process model
matclust.estK
                    fit the Matern Cluster process model
matclust.estpcf
cauchy.estK
                    fit a Neyman-Scott Cauchy cluster process
                    fit a Neyman-Scott Cauchy cluster process
cauchy.estpcf
vargamma.estK
                    fit a Neyman-Scott Variance Gamma process
                    fit a Neyman-Scott Variance Gamma process
vargamma.estpcf
                    low-level algorithm for fitting models
mincontrast
                    by the method of minimum contrast
```

IV. MODEL FITTING (POISSON AND GIBBS MODELS)

Types of models

Poisson point processes are the simplest models for point patterns. A Poisson model assumes that the points are stochastically independent. It may allow the points to have a non-uniform spatial density. The special case of a Poisson process with a uniform spatial density is often called Complete Spatial Randomness.

Poisson point processes are included in the more general class of Gibbs point process models. In a Gibbs model, there is *interaction* or dependence between points. Many different types of interaction can be specified.

For a detailed explanation of how to fit Poisson or Gibbs point process models to point pattern data using **spatstat**, see Baddeley and Turner (2005b) or Baddeley (2008).

To fit a Poisson or Gibbs point process model:

Model fitting in **spatstat** is performed mainly by the function ppm. Its result is an object of class "ppm".

Here are some examples, where X is a point pattern (class "ppp"):

command	model
ppm(X)	Complete Spatial Randomness
ppm(X ~ 1)	Complete Spatial Randomness
ppm(X ~ x)	Poisson process with
	intensity loglinear in x coordinate
$ppm(X \sim 1, Strauss(0.1))$	Stationary Strauss process
$ppm(X \sim x, Strauss(0.1))$	Strauss process with
	conditional intensity loglinear in x

It is also possible to fit models that depend on other covariates.

Manipulating the fitted model:

plot.ppm	Plot the fitted model
<pre>predict.ppm</pre>	Compute the spatial trend and conditional intensity
	of the fitted point process model
coef.ppm	Extract the fitted model coefficients
parameters	Extract all model parameters
formula.ppm	Extract the trend formula
intensity.ppm	Compute fitted intensity
Kmodel.ppm	K function of fitted model
pcfmodel.ppm	pair correlation of fitted model
fitted.ppm	Compute fitted conditional intensity at quadrature points
residuals.ppm	Compute point process residuals at quadrature points
update.ppm	Update the fit
vcov.ppm	Variance-covariance matrix of estimates
rmh.ppm	Simulate from fitted model
simulate.ppm	Simulate from fitted model
print.ppm	Print basic information about a fitted model
summary.ppm	Summarise a fitted model
effectfun	Compute the fitted effect of one covariate
logLik.ppm	log-likelihood or log-pseudolikelihood
anova.ppm	Analysis of deviance
model.frame.ppm	Extract data frame used to fit model
model.images	Extract spatial data used to fit model

model.depends	Identify variables in the model
as.interact	Interpoint interaction component of model
fitin	Extract fitted interpoint interaction
is.hybrid	Determine whether the model is a hybrid
valid.ppm	Check the model is a valid point process
<pre>project.ppm</pre>	Ensure the model is a valid point process

For model selection, you can also use the generic functions step, drop1 and AIC on fitted point process models.

See spatstat.options to control plotting of fitted model.

To specify a point process model:

Strauss()

The first order "trend" of the model is determined by an R language formula. The formula specifies the form of the *logarithm* of the trend.

```
X ~ 1 No trend (stationary)

X ~ x Loglinear trend \lambda(x,y) = \exp(\alpha + \beta x) where x,y are Cartesian coordinates

X ~ polynom(x,y,3) Log-cubic polynomial trend

X ~ harmonic(x,y,2) Log-harmonic polynomial trend

X ~ Z Loglinear function of covariate Z

\lambda(x,y) = \exp(\alpha + \beta Z(x,y))
```

The higher order ("interaction") components are described by an object of class "interact". Such objects are created by:

Poisson()	the Poisson point process
AreaInter()	Area-interaction process
	•
BadGey()	multiscale Geyer process
Concom()	connected component interaction
DiggleGratton()	Diggle-Gratton potential
<pre>DiggleGatesStibbard()</pre>	Diggle-Gates-Stibbard potential
Fiksel()	Fiksel pairwise interaction process
Geyer()	Geyer's saturation process
Hardcore()	Hard core process
HierHard()	Hierarchical multiype hard core process
HierStrauss()	Hierarchical multiype Strauss process
HierStraussHard()	Hierarchical multiype Strauss-hard core process
Hybrid()	Hybrid of several interactions
LennardJones()	Lennard-Jones potential
MultiHard()	multitype hard core process
MultiStrauss()	multitype Strauss process
MultiStraussHard()	multitype Strauss/hard core process
OrdThresh()	Ord process, threshold potential
Ord()	Ord model, user-supplied potential
PairPiece()	pairwise interaction, piecewise constant
Pairwise()	pairwise interaction, user-supplied potential
Penttinen()	Penttinen pairwise interaction
SatPiece()	Saturated pair model, piecewise constant potential
Saturated()	Saturated pair model, user-supplied potential
Softcore()	pairwise interaction, soft core potential

Strauss process

StraussHard()	Strauss/hard core point process
<pre>Triplets()</pre>	Geyer triplets process

Note that it is also possible to combine several such interactions using Hybrid.

Finer control over model fitting:

A quadrature scheme is represented by an object of class "quad". To create a quadrature scheme, typically use quadscheme.

quadscheme default quadrature scheme
using rectangular cells or Dirichlet cells
pixelquad quadrature scheme based on image pixels
quad create an object of class "quad"

To inspect a quadrature scheme:

plot(Q) plot quadrature scheme Q print(Q) print basic information about quadrature scheme Q summary(Q) summary of quadrature scheme Q

A quadrature scheme consists of data points, dummy points, and weights. To generate dummy points:

default.dummy default pattern of dummy points
gridcentres dummy points in a rectangular grid
stratified random dummy pattern
spokes radial pattern of dummy points
corners dummy points at corners of the window

To compute weights:

gridweights quadrature weights by the grid-counting rule dirichletWeights quadrature weights are Dirichlet tile areas

Simulation and goodness-of-fit for fitted models:

rmh.ppm simulate realisations of a fitted model simulate.ppm simulate realisations of a fitted model compute simulation envelopes for a fitted model

Point process models on a linear network:

An object of class "1pp" represents a pattern of points on a linear network. Point process models can also be fitted to these objects. Currently only Poisson models can be fitted.

linim	pixel image on linear network
plot.linim	plot a pixel image on linear network
eval.linim	evaluate expression involving images
linfun	function defined on linear network
methods.linfun	conversion facilities

V. MODEL FITTING (DETERMINANTAL POINT PROCESS MODELS)

Code for fitting determinantal point process models has recently been added to spatstat.

For information, see the help file for dppm.

VI. MODEL FITTING (SPATIAL LOGISTIC REGRESSION)

Logistic regression

Pixel-based spatial logistic regression is an alternative technique for analysing spatial point patterns that is widely used in Geographical Information Systems. It is approximately equivalent to fitting a Poisson point process model.

In pixel-based logistic regression, the spatial domain is divided into small pixels, the presence or absence of a data point in each pixel is recorded, and logistic regression is used to model the presence/absence indicators as a function of any covariates.

Facilities for performing spatial logistic regression are provided in **spatstat** for comparison purposes.

Fitting a spatial logistic regression

Spatial logistic regression is performed by the function slrm. Its result is an object of class "slrm". There are many methods for this class, including methods for print, fitted, predict, simulate, anova, coef, logLik, terms, update, formula and vcov.

For example, if X is a point pattern (class "ppp"):

command	model
$slrm(X \sim 1)$	Complete Spatial Randomness
$slrm(X \sim x)$	Poisson process with
	intensity loglinear in x coordinate
$slrm(X \sim Z)$	Poisson process with
	intensity loglinear in covariate Z

Manipulating a fitted spatial logistic regression

anova.slrm	Analysis of deviance
coef.slrm	Extract fitted coefficients
vcov.slrm	Variance-covariance matrix of fitted coefficients
fitted.slrm	Compute fitted probabilities or intensity
logLik.slrm	Evaluate loglikelihood of fitted model
plot.slrm	Plot fitted probabilities or intensity
predict.slrm	Compute predicted probabilities or intensity with new data
simulate.slrm	Simulate model

There are many other undocumented methods for this class, including methods for print, update, formula and terms. Stepwise model selection is possible using step or stepAIC.

VII. SIMULATION

There are many ways to generate a random point pattern, line segment pattern, pixel image or tessellation in spatstat.

Random point patterns:

runifpoint generate n independent uniform random points generate n independent random points rpoint rmpoint generate n independent multitype random points simulate the (in)homogeneous Poisson point process rpoispp simulate the (in)homogeneous multitype Poisson point process rmpoispp generate n independent uniform random points in disc runifdisc rstrat stratified random sample of points systematic random sample (grid) of points rsyst simulate the Matérn Model I inhibition process rMaternI simulate the Matérn Model II inhibition process rMaternII simulate Simple Sequential Inhibition process rSST simulate hard core process (perfect simulation) rHardcore simulate Strauss process (perfect simulation) rStrauss simulate Strauss-hard core process (perfect simulation) rStraussHard simulate Diggle-Gratton process (perfect simulation) rDiggleGratton rDGS simulate Diggle-Gates-Stibbard process (perfect simulation) simulate Penttinen process (perfect simulation) rPenttinen rNeymanScott simulate a general Neyman-Scott process simulate the Matérn Cluster process rMatClust simulate the Thomas process rThomas simulate the log-Gaussian Cox process rLGCP rGaussPoisson simulate the Gauss-Poisson cluster process simulate Neyman-Scott process with Cauchy clusters

rCauchy

simulate Neyman-Scott process with Variance Gamma clusters rVarGamma

simulate the Baddeley-Silverman cell process rcell

runifpointOnLines generate n random points along specified line segments rpoisppOnLines generate Poisson random points along specified line segments

Resampling a point pattern:

quadratresample block resampling

rjitter apply random displacements to points in a pattern

random shifting of (subsets of) points rshift

rthin random thinning

See also varblock for estimating the variance of a summary statistic by block resampling, and lohboot for another bootstrap technique.

Fitted point process models:

If you have fitted a point process model to a point pattern dataset, the fitted model can be simulated.

Cluster process models are fitted by the function kppm yielding an object of class "kppm". To generate one or more simulated realisations of this fitted model, use simulate.kppm.

Gibbs point process models are fitted by the function ppm yielding an object of class "ppm". To generate a simulated realisation of this fitted model, use rmh. To generate one or more simulated realisations of the fitted model, use simulate.ppm.

Other random patterns:

rlinegrid	generate a random array of parallel lines through a window
rpoisline	simulate the Poisson line process within a window
rpoislinetess	generate random tessellation using Poisson line process
rMosaicSet	generate random set by selecting some tiles of a tessellation
rMosaicField	generate random pixel image by assigning random values in each tile of a tessellation

Simulation-based inference

```
envelope critical envelope for Monte Carlo test of goodness-of-fit diagnostic plot for interpoint interaction spatial scan statistic/test studentised permutation test segregation.test test of segregation of types
```

VIII. TESTS AND DIAGNOSTICS

Classical hypothesis tests:

quadrat.test	χ^2 goodness-of-fit test on quadrat counts
clarkevans.test	Clark and Evans test
cdf.test	Spatial distribution goodness-of-fit test
berman.test	Berman's goodness-of-fit tests
envelope	critical envelope for Monte Carlo test of goodness-of-fit
scan.test	spatial scan statistic/test
dclf.test	Diggle-Cressie-Loosmore-Ford test
mad.test	Mean Absolute Deviation test
dclf.progress	Progress plot for DCLF test
mad.progress	Progress plot for MAD test
anova.ppm	Analysis of Deviance for point process models

Sensitivity diagnostics:

Classical measures of model sensitivity such as leverage and influence have been adapted to point process models.

```
leverage.ppm Leverage for point process model influence.ppm Influence for point process model dfbetas.ppm Parameter influence
```

Diagnostics for covariate effect:

Classical diagnostics for covariate effects have been adapted to point process models.

```
parres Partial residual plot
addvar Added variable plot
rhohat Kernel estimate of covariate effect
rho2hat Kernel estimate of covariate effect (bivariate)
```

Residual diagnostics:

Residuals for a fitted point process model, and diagnostic plots based on the residuals, were introduced in Baddeley et al (2005) and Baddeley, Rubak and Møller (2011).

Type demo(diagnose) for a demonstration of the diagnostics features.

diagnose.ppm diagnostic plots for spatial trend diagnostic Q-Q plot for interpoint interaction qqplot.ppm residualspaper examples from Baddeley et al (2005) model compensator of K function **Kcom** Gcom model compensator of G function score residual of K function Kres score residual of G function Gres pseudoscore residual of summary function psst psstA pseudoscore residual of empty space function pseudoscore residual of G function psstG compareFit compare compensators of several fitted models

Resampling and randomisation procedures

You can build your own tests based on randomisation and resampling using the following capabilities:

quadratresampleblock resamplingrjitterapply random displacements to points in a patternrshiftrandom shifting of (subsets of) pointsrthinrandom thinning

IX. DOCUMENTATION

The online manual entries are quite detailed and should be consulted first for information about a particular function.

The book Baddeley, Rubak and Turner (2015) is a complete course on analysing spatial point patterns, with full details about **spatstat**.

Older material (which is now out-of-date but is freely available) includes Baddeley and Turner (2005a), a brief overview of the package in its early development; Baddeley and Turner (2005b), a more detailed explanation of how to fit point process models to data; and Baddeley (2010), a complete set of notes from a 2-day workshop on the use of **spatstat**.

Type citation("spatstat") to get a list of these references.

Licence

This library and its documentation are usable under the terms of the "GNU General Public License", a copy of which is distributed with the package.

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