# An Introduction to Quantum Natural Language Processing (QNLP)

**Part 4:** 

**Quantum Natural Language Processing** 

Introducing Quantum Natural Language Processing

- Introducing Quantum Natural Language Processing
- Distributional Word Representation

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- Compositionality of Grammar

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- Future Directions for Research

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- Morphing into quantum circuit form

Introduction to QNLP Concludes

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- Meanings of words can be depicted by high-dimensional "meaning-space" where context words act as orthogonal basis vectors
- ❖ Inner product can be used to identify distances between different words which represents the closeness of meaning of the words

**Distributional Word Representation Concludes** 

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- Diagrammatically, the composition is denoted by Cups & Caps, meaning that grammar compositionality is entanglement of words together!

**Compositionality of Grammar Concludes** 

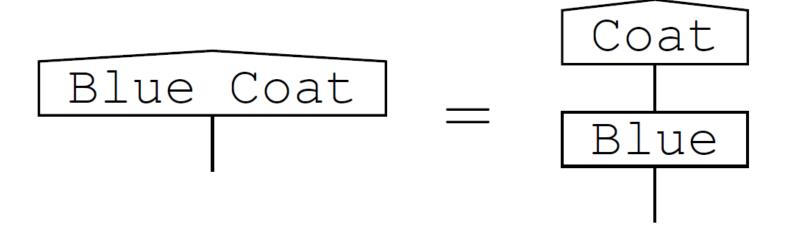
# QNLP Basics Adjective & Noun

# **Adjective & Noun**

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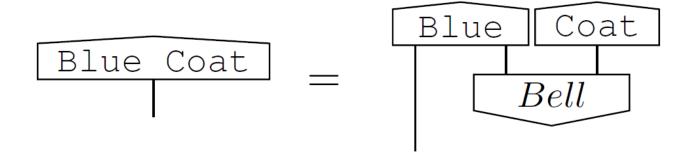
Applying an adjective 'Blue' to a noun 'Coat' is like applying a process to 'Coat'

# **Adjective & Noun**

Representing 'Blue' as a 2-qubit state, we get another way of getting the meaning of Blue Coat from the meaning of 'Blue' and 'Coat'

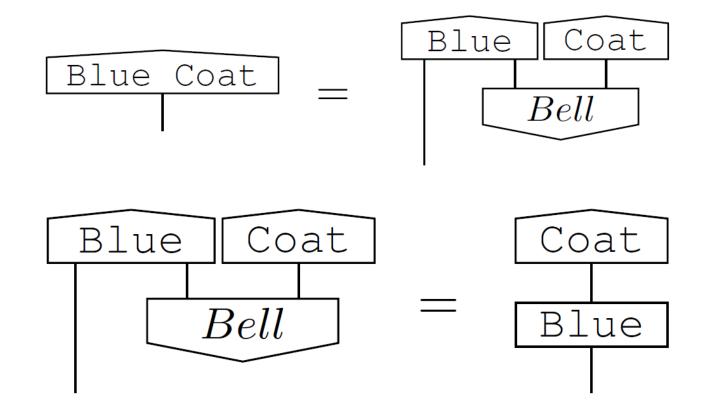
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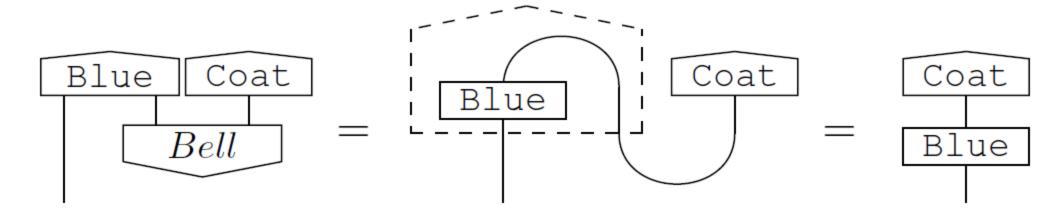
We obtain the following diagram of Blue Coat after yanking

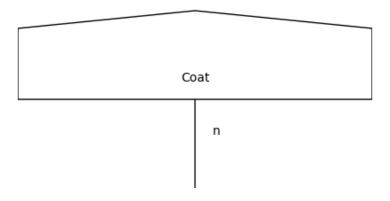
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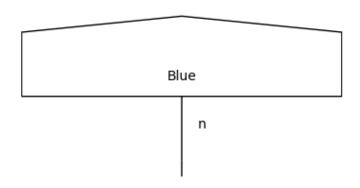
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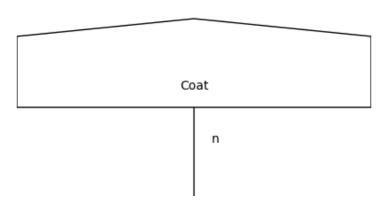
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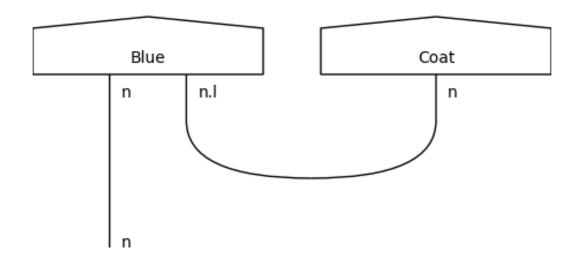
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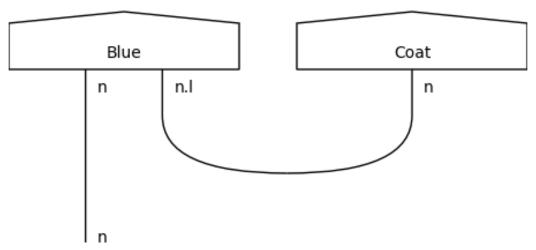




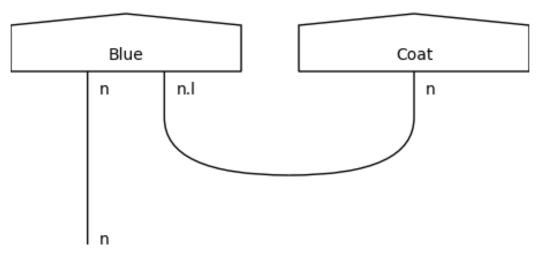




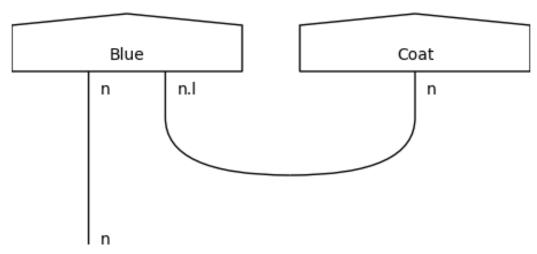
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 $\succ$  For the noun 'Coat', the adjective 'Blue' is on the left, therefore, the cup connects n to  $n^l$ 



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- ➤ Juxtaposition of types  $s \cdot n^l \cdot n \rightarrow s \cdot 1 \rightarrow s$

# QNLP Basics Adjective & Noun

**Adjective & Noun Concludes** 

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Individual diagrams for Eric, hates and Trev

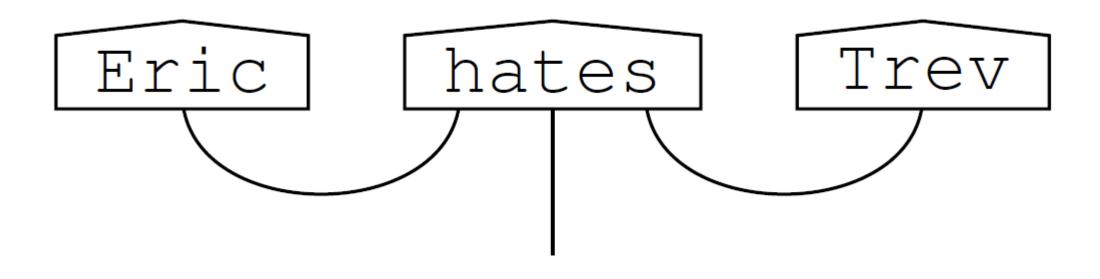
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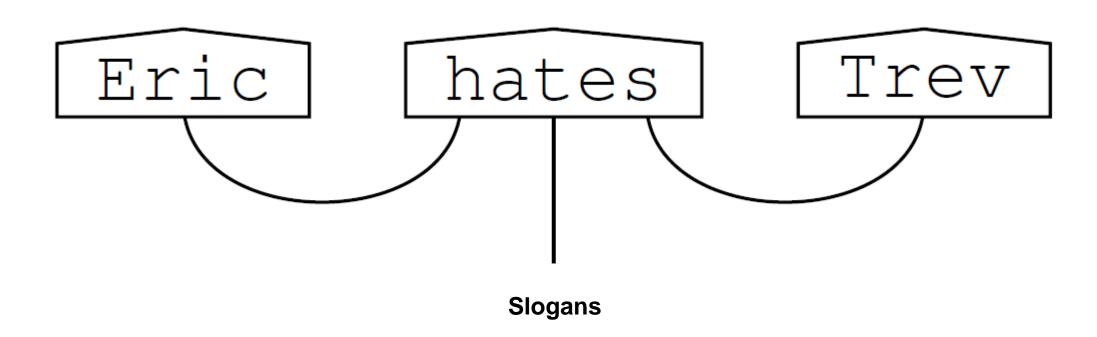


Meaning of the sentence is computed as follows (string diagram)

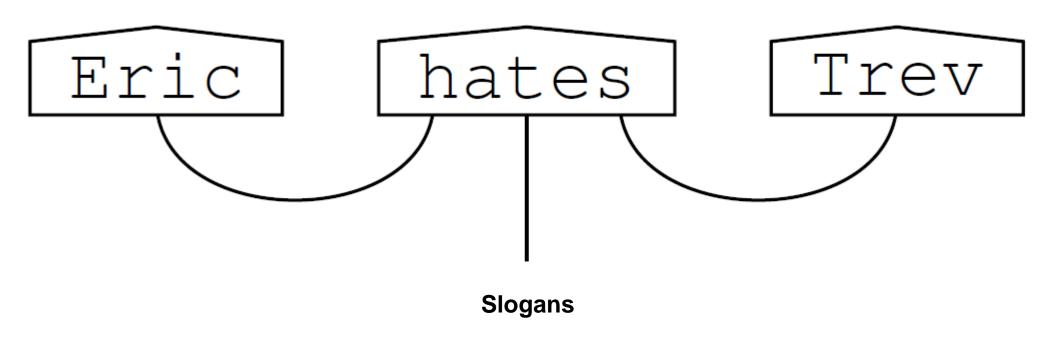
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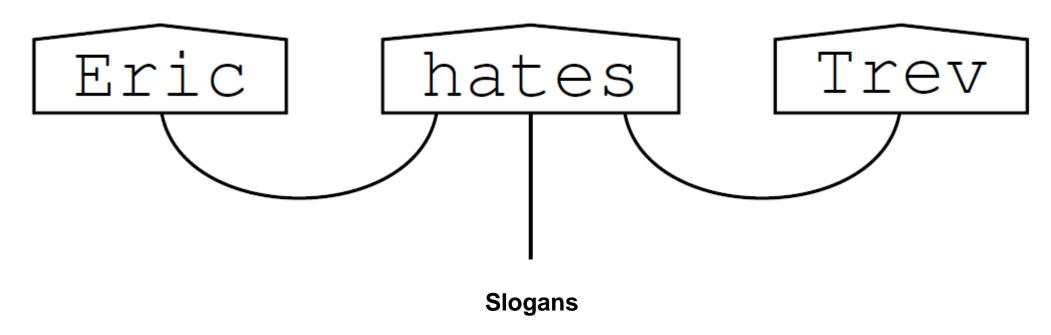


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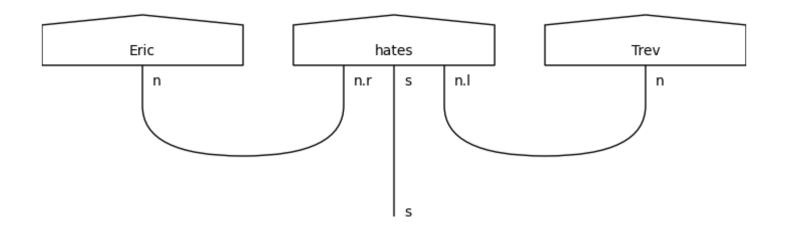
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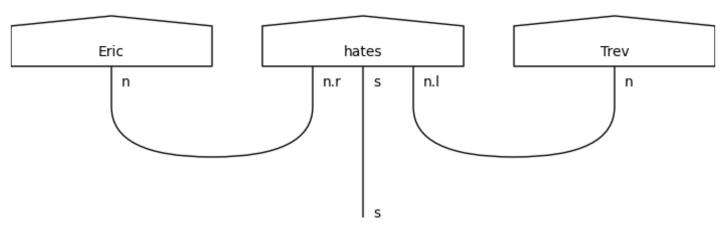
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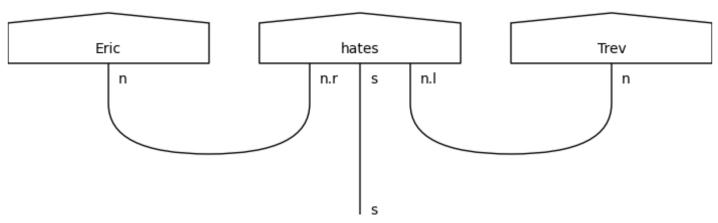
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Grammar is what mediates the flow of meanings between words

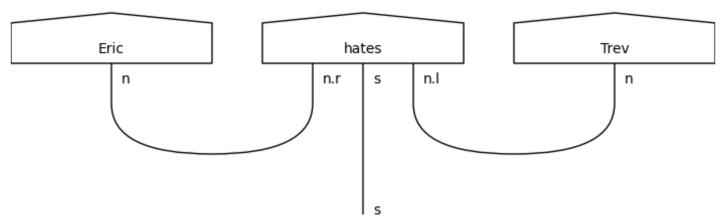




 $\succ$  For the noun 'Eric', the verb 'hates' is on the right, therefore, the cup connects n to  $n^r$ 

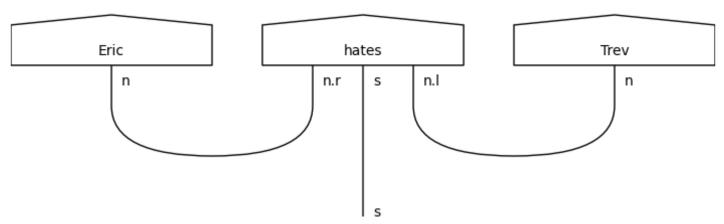


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#### Subject-Verb-Object Sentence



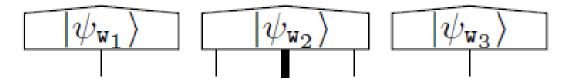
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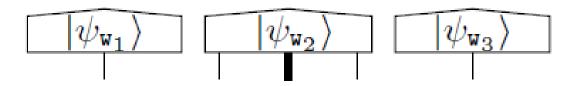
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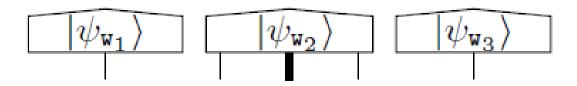


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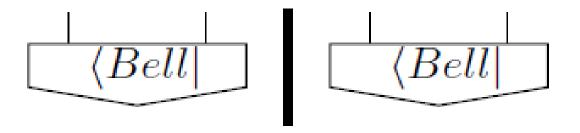


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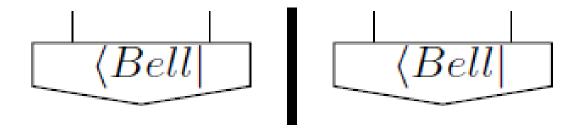


❖ Replace cups with bell states and all the straight wires with Identities

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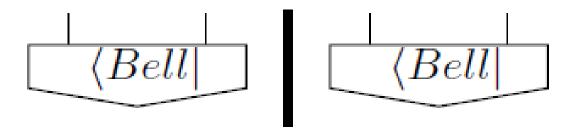


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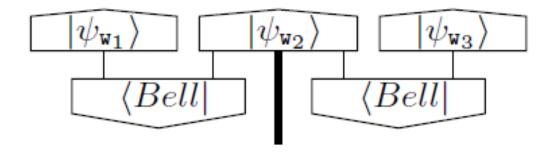


Apply this quantum process to the meaning of the parts

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Apply this quantum process to the meaning of the parts

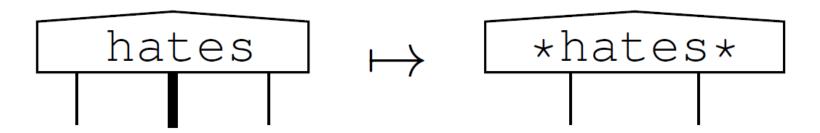


**DisCoCat Algorithm Concludes** 

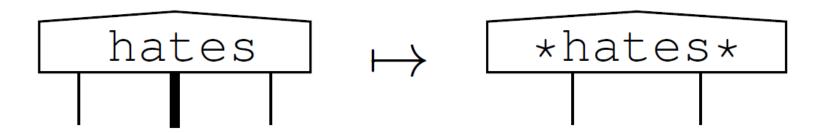
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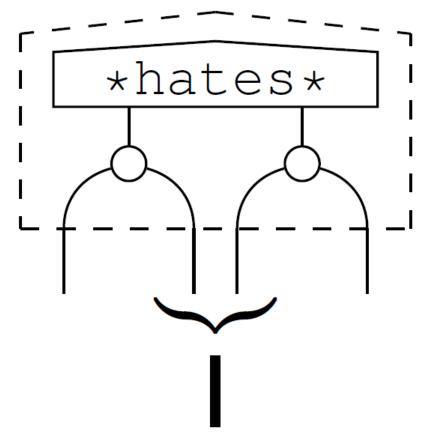
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> ZX calculus and Spiders is used to modify the internal wiring of the system.

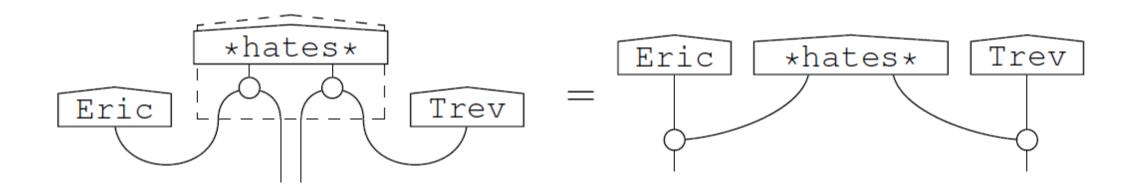
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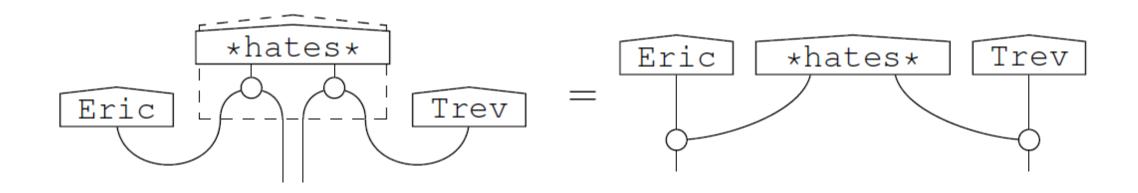


➤ With the help of the internal wiring, we can start converting the string diagram into a ZX quantum circuit

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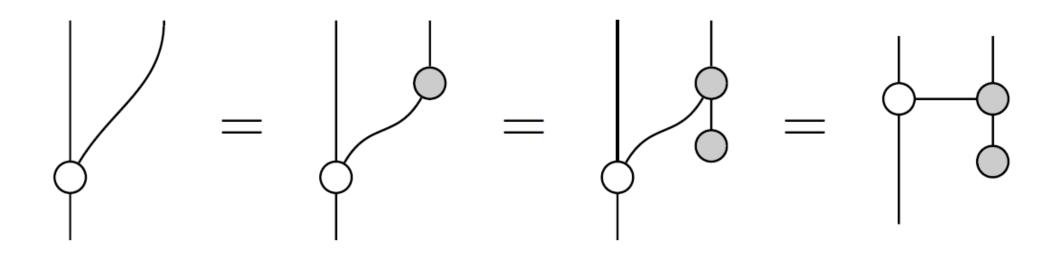
➤ With the help of the internal wiring, we can start converting the string diagram into a ZX quantum circuit



➤ The Z spiders are moved below the nouns – Eric & Trev and the extra wiring is removed

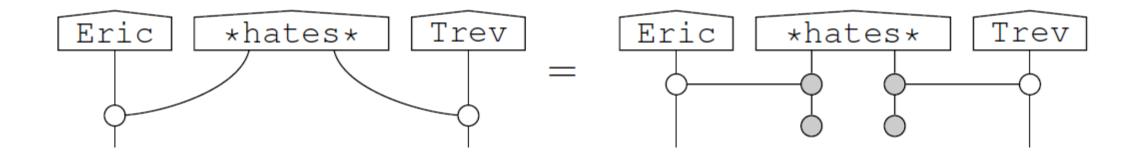
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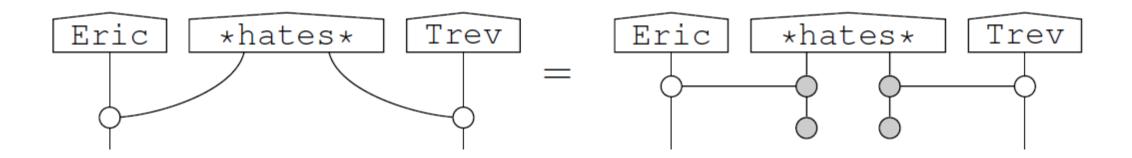


Two CNOT gates are being formed when the spiders are pulled out with ZX rules used and last two spiders (grey) are for post-selected measurement

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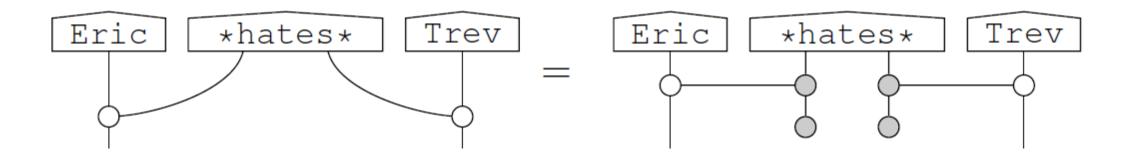


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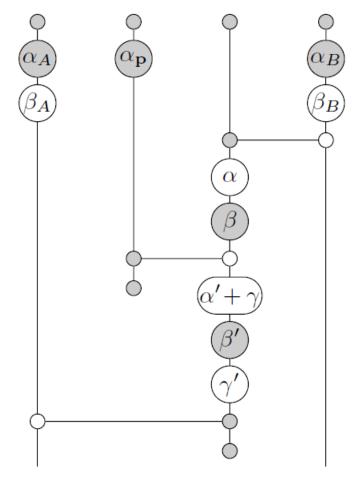


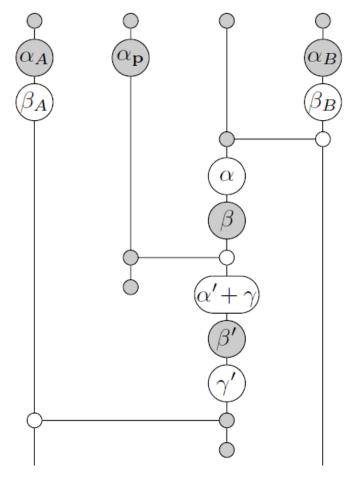
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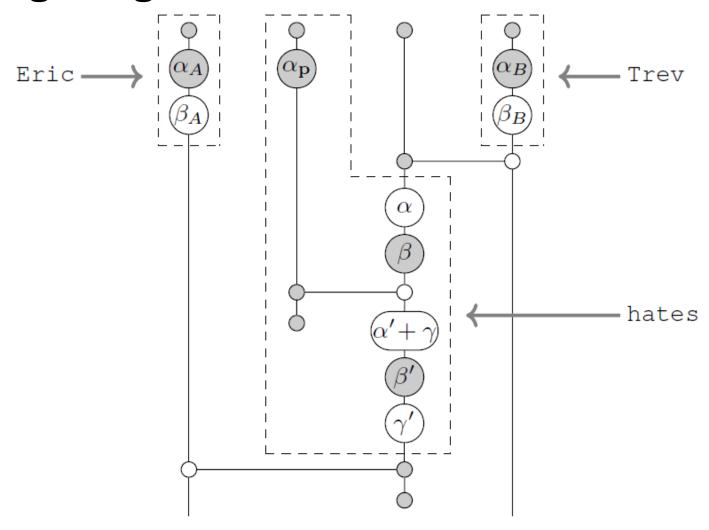


- For the complete quantum circuit between the subject and objects Eric and Trev, the nouns are also converted into parameterized gates
- We represent verbs like 'hates' with ZX unitary gates and large space consisting of different verbs can be encoded by  $\alpha$ ,  $\beta$ ,  $\gamma$





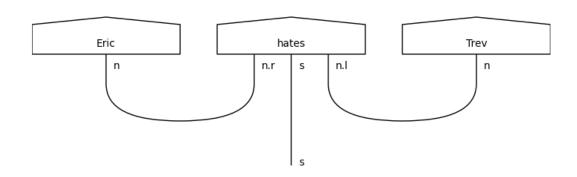
 $\triangleright$  We can depict different verbs by changing the values of  $\alpha$ ,  $\beta$ ,  $\gamma$ 



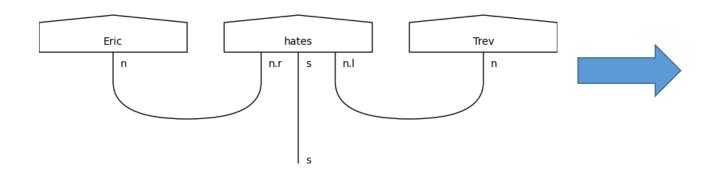
String Diagrams into ZX Quantum Circuits Concludes

❖ Released by Cambridge Quantum on October 13<sup>th</sup>, 2021

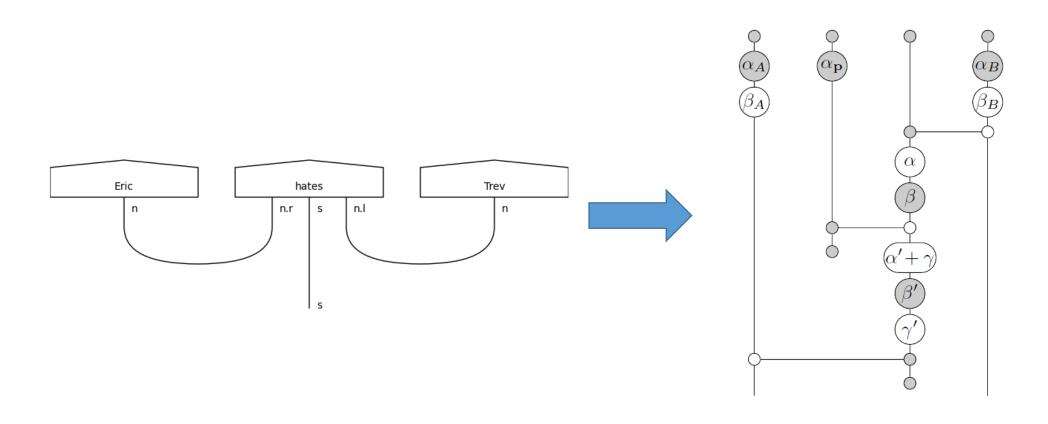
❖ Released by Cambridge Quantum on October 13th, 2021



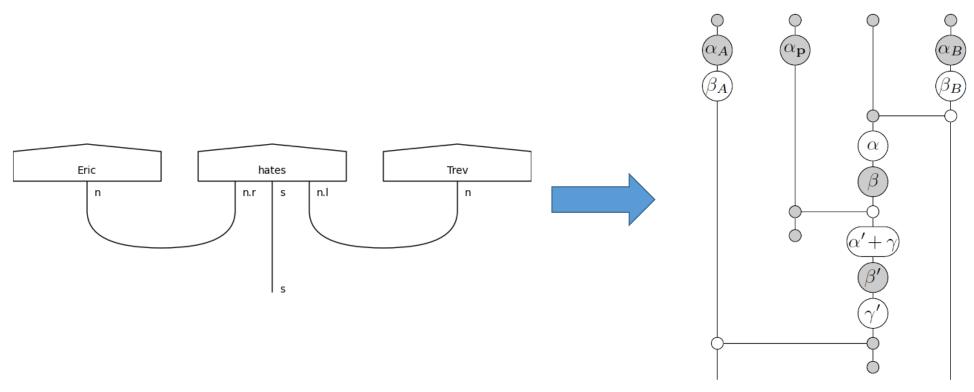
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Converts any sentence into quantum circuit based on compositional model (DisCoCat, Bag of Words & Word Sequence) and choices of ansatz (SpiderAnsatz, TensorAnsatz, IQPAnsatz)

Features of  $\lambda$ ambeq

#### Features of λambeq

❖ Modular – Independent modules providing flexibility

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- ❖ Modular Independent modules providing flexibility
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- Extensive Object-oriented design

#### Features of λambeq

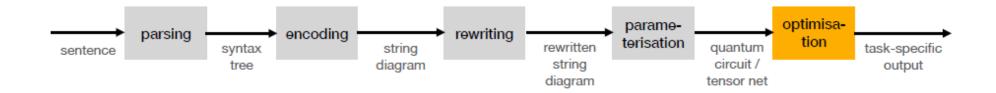
- ❖ Modular Independent modules providing flexibility
- Open source
- Extensive Object-oriented design
- High level

#### Features of λambeq

- ❖ Modular Independent modules providing flexibility
- Open source
- Extensive Object-oriented design
- High level
- ❖ Interoperability Simple communication with other packages

**λambeq Architecture** 

#### **λambeq Architecture**



#### Working of lambeq:

Based on selected compositional model, a sentence is parsed using a parser. Currently the parser is DepCCGParser. This parser creates a syntax tree.

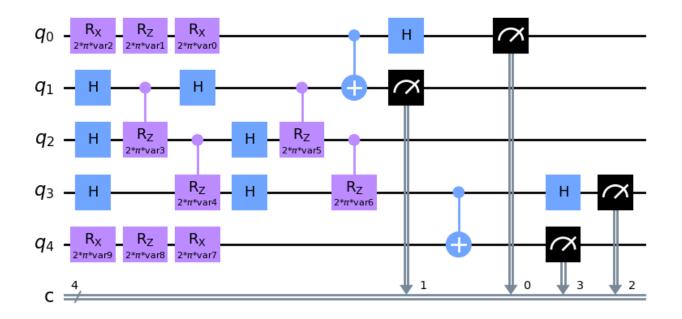
The parsed tree is converted into a string diagram dependent on the compositional model chosen

The string diagram is simplified by using rewrite rules to remove any redundancies making it compatible for quantum computation

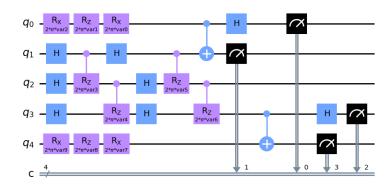
The final simplified string diagram is converted into a quantum circuit or tensor network based on choice of ansatz and parameterization scheme

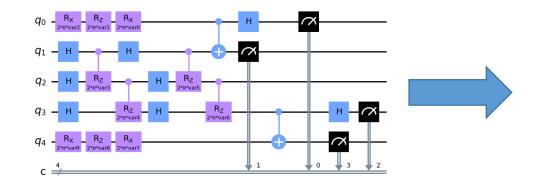
Qiskit Circuit of 'Eric hates Trev'

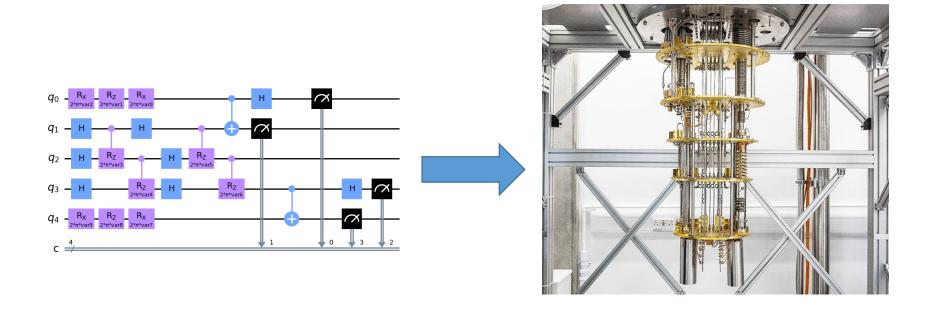
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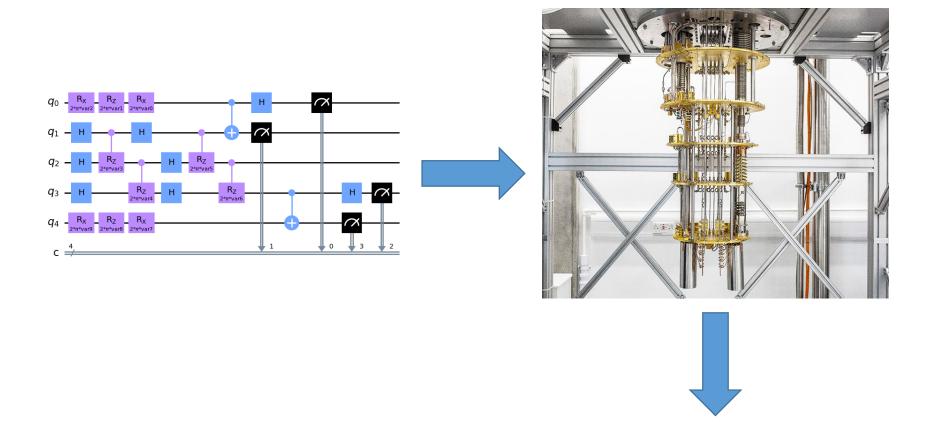


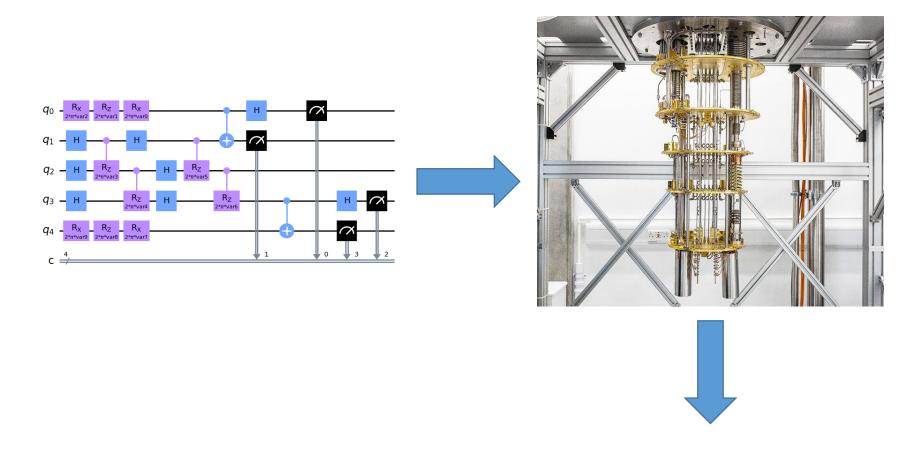
Introducing *it's Features Concludes* 



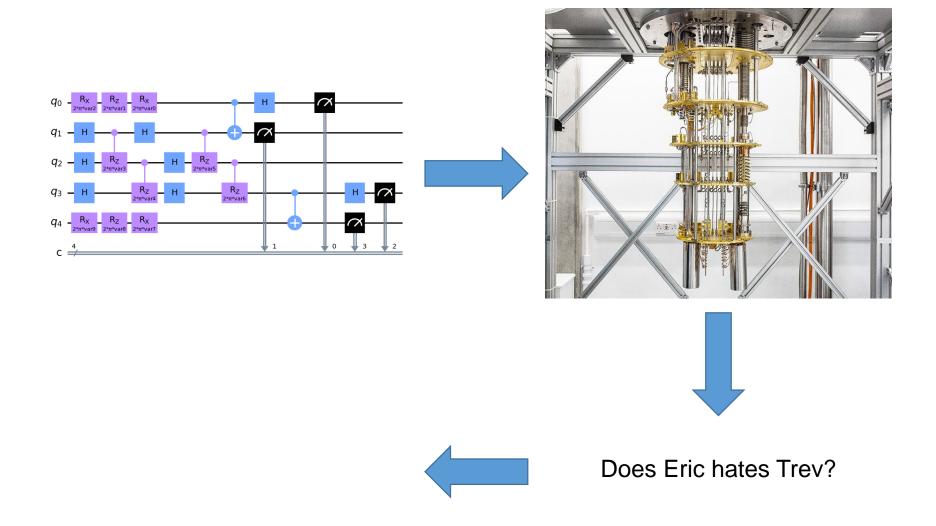


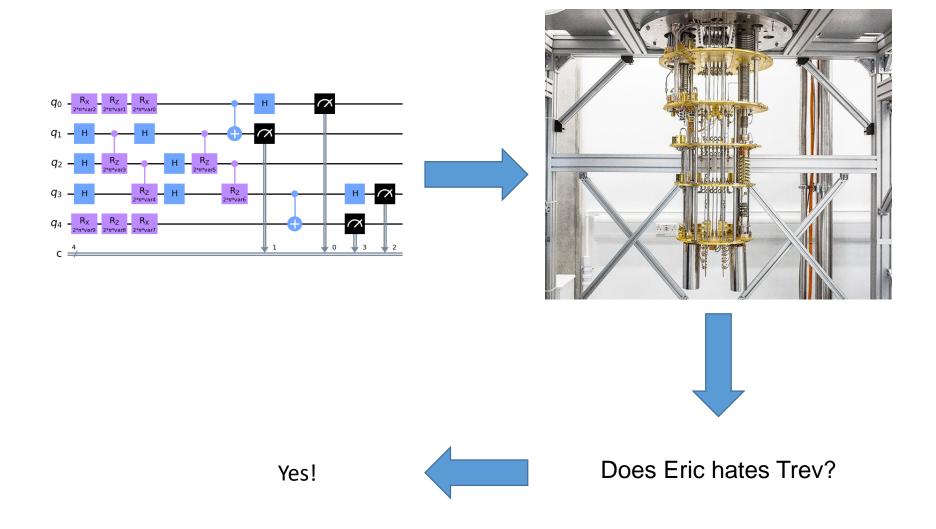






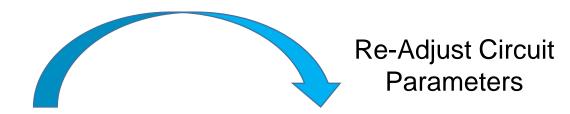
Does Eric hates Trev?





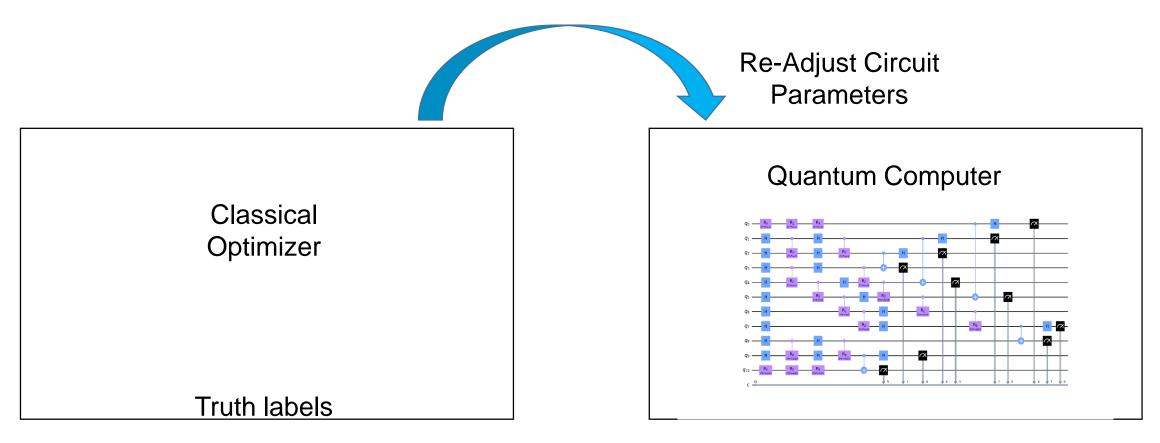
Classical Optimizer

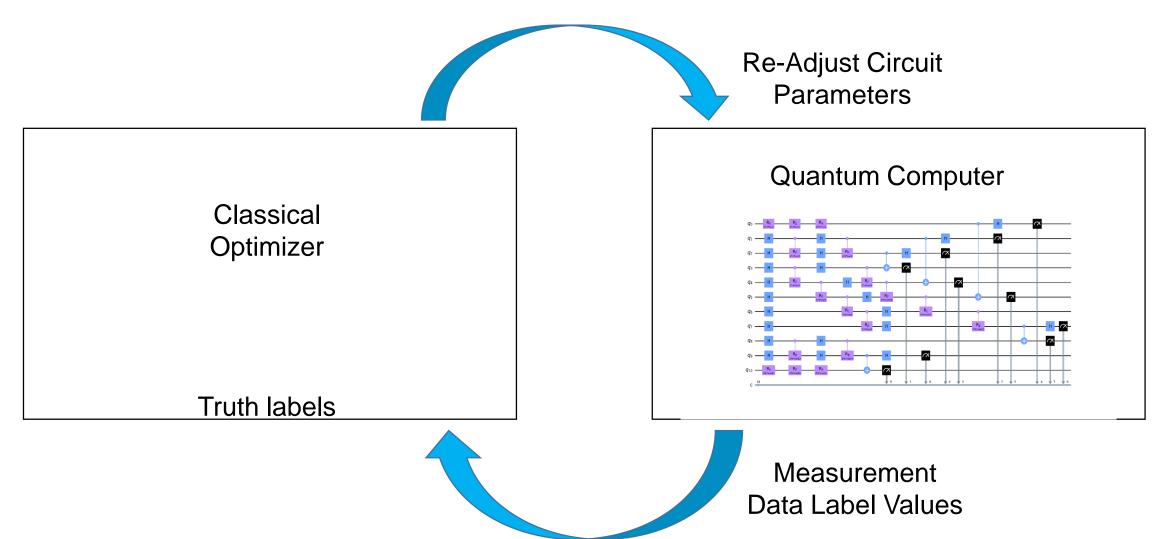
Truth labels

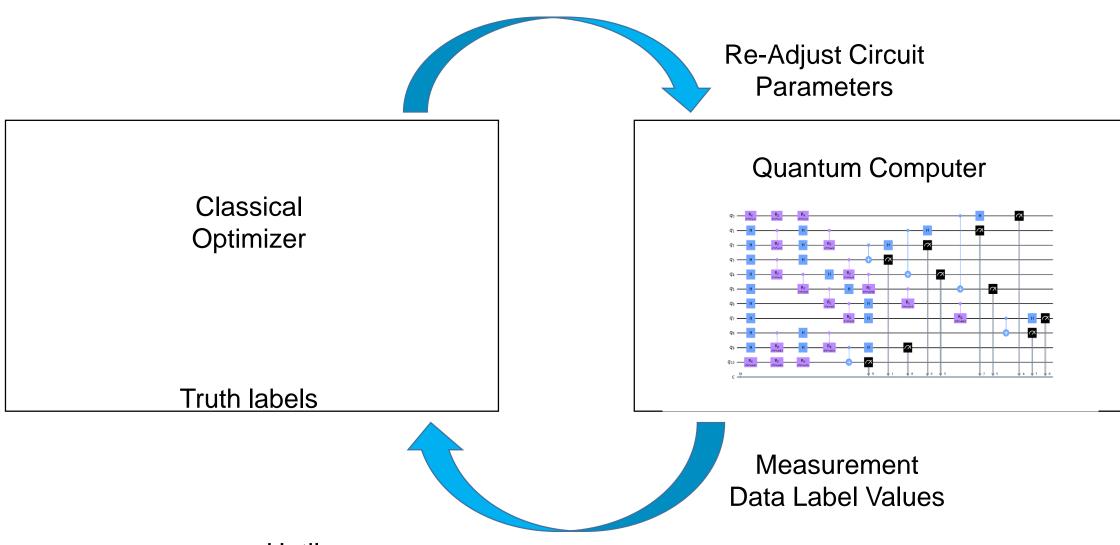


Classical Optimizer

Truth labels







Until Convergence!

**QNLP Training Process Concludes** 

Sentiment Classification

- Sentiment Classification
- Quantum Language Translation

- Sentiment Classification
- Quantum Language Translation
- Quantum Speech Recognition Systems

- Sentiment Classification
- Quantum Language Translation
- Quantum Speech Recognition Systems
- QNLP for Music Research

# Potential Use Cases/Applications of QNLP Concludes

Developing the lambeq QNLP toolkit further to have more functionalities such as more compositional models and ansatz

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- Support for quantum friendly optimization and training modules through more research on quantum machine learning and QNLP
- Implementation of diagrammatic differentiation for automated machine learning using lambeq
- Focusing on DisCoCirc algorithm to accommodate sentence to sentence grammatical structure
- Longer term goal is to scale up and productionization of QNLP models with the help of Quantum DevOps

**Future Directions for Research Concludes** 

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Thank you so much!