

Deliverables

Loading the dataset. Note: The dataset starts from Jan22 .

```
options(scipen = 999) # turn off scientific notation
# Read the data
covid_data <- read_excel("C:/Users/meghs/Downloads/2020_Covid_Data.xlsx")

#Covid Data of Particular State
ct_data <- covid_data$CT # -----> #replace with your state

#The dataset contains values starting from Jan22 hence 345
ct_data <- ct_data[1:345]
length(ct_data)
```

```
## [1] 345
```

```
ct_data
```

```
## [1] 0 0 0 0 0 0 0 0 0 0
## [11] 0 0 0 0 0 0 0 0 0 0
## [21] 0 0 0 0 0 0 0 0 0 0
## [31] 0 0 0 0 0 0 0 0 0 0
## [41] 0 0 0 0 0 0 1 1 2 3
## [51] 7 7 7 26 41 68 96 159 194 223
## [61] 327 415 618 875 1012 1291 1524 1993 2571 3128
## [71] 3557 3824 4915 5276 5675 6906 7781 8781 9784 10131
## [81] 11510 12035 13381 13989 14755 15884 16809 17550 17962 19815
## [91] 20360 22469 23100 23921 24582 25269 25997 26312 26767 27700
## [101] 28764 29287 29312 29973 30621 30995 31784 32411 32984 33554
## [111] 33765 34333 34855 35464 36085 36703 37419 38116 38430 39017
## [121] 39208 39640 40022 40468 40873 41303 41288 41559 41762 42022
## [131] 42201 42740 42979 43091 43239 43460 43818 43968 44092 44179
## [141] 44347 44461 44689 44994 45088 45235 45349 45429 45440 45557
## [151] 45715 45755 45782 45899 45913 45994 46059 46206 46303 46362
## [161] 46514 46572 46646 46717 46717 46717 46976 47033 47108 47209
## [171] 47287 47287 47287 47510 47530 47636 47750 47893 47893 47893
## [181] 48055 48096 48223 48232 48776 48776 48776 48983 49077 49540
## [191] 49670 49810 49810 49810 50062 50110 50225 50245 50320 50320
## [201] 50320 50567 50684 50706 50782 50897 50897 50897 51267 51255
## [211] 51314 51432 51519 51519 51519 52011 52040 52220 52350 52495
## [221] 52495 52495 52879 53006 53108 53209 53365 53365 53365 53365
## [231] 53782 53871 54093 54326 54326 54326 54895 55031 55166 55386
## [241] 55527 55527 55527 56024 56160 56315 56472 56587 56587 56587
## [251] 57147 57329 57550 57742 58297 58297 58297 59120 59241 59364
## [261] 59748 60038 60038 60038 61377 61697 61861 62028 62830 62830
## [271] 62830 64021 64455 64871 65373 66052 66052 66052 68099 68637
## [281] 69127 70446 71207 71207 71207 73858 74843 75373 77060 78125
## [291] 78125 78125 81463 82987 84741 85899 88645 88645 88645 93284
## [301] 94986 97028 99381 101469 101469 101469 106740 107280 109152 109152
## [311] 112581 112581 112581 117295 118754 121426 126177 127715 127715 127715
## [321] 135844 138258 140548 142979 146761 146761 146761 153992 155462 157781
## [331] 160102 162782 162782 162782 167377 168960 170705 172743 172743 172743
## [341] 172743 181200 181967 183663 185708
```

1. Step-by-Step fit different ARIMA (p,d,q) x (P, D, Q) for the confirmed cases. Can you discover a better model than auto.arima?

Convert data to time series object and plot it

```
# Create a time series object using a simple numeric sequence as the time index
ct_ts <- ts(ct_data, start= c(2020,1,22), frequency=345)# Starts from the date Jan 22
ct_ts
```

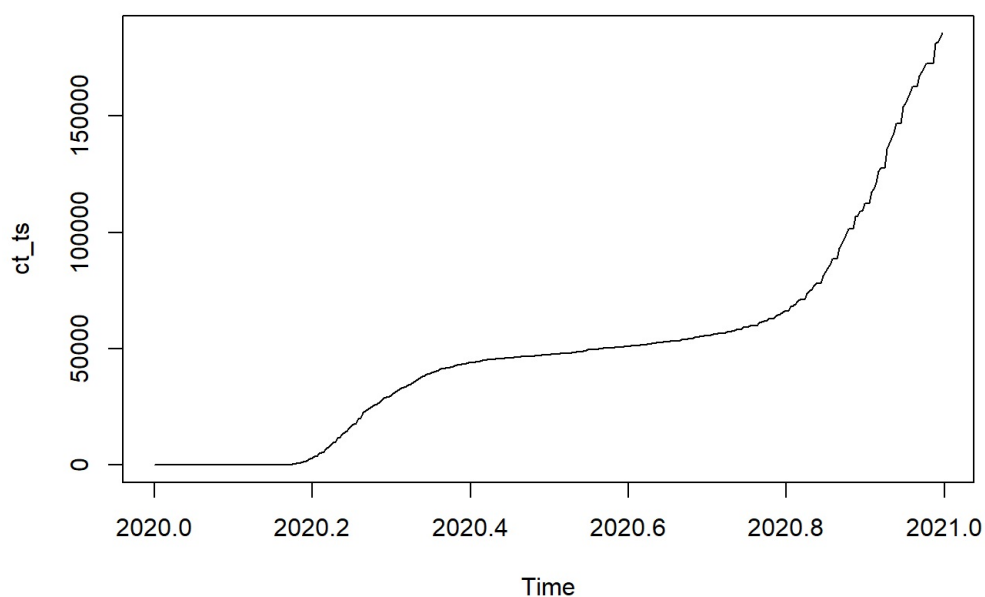
```
## Time Series:
## Start = c(2020, 1)
## End = c(2020, 345)
## Frequency = 345
## [1] 0 0 0 0 0 0 0 0 0 0
## [11] 0 0 0 0 0 0 0 0 0 0
## [21] 0 0 0 0 0 0 0 0 0 0
## [31] 0 0 0 0 0 0 0 0 0 0
## [41] 0 0 0 0 0 0 1 1 2 3
## [51] 7 7 7 26 41 68 96 159 194 223
## [61] 327 415 618 875 1012 1291 1524 1993 2571 3128
## [71] 3557 3824 4915 5276 5675 6906 7781 8781 9784 10131
## [81] 11510 12035 13381 13989 14755 15884 16809 17550 17962 19815
## [91] 20360 22469 23100 23921 24582 25269 25997 26312 26767 27700
## [101] 28764 29287 29312 29973 30621 30995 31784 32411 32984 33554
## [111] 33765 34333 34855 35464 36085 36703 37419 38116 38430 39017
## [121] 39208 39640 40022 40468 40873 41303 41288 41559 41762 42022
## [131] 42201 42740 42979 43091 43239 43460 43818 43968 44092 44179
## [141] 44347 44461 44689 44994 45088 45235 45349 45429 45440 45557
## [151] 45715 45755 45782 45899 45913 45994 46059 46206 46303 46362
## [161] 46514 46572 46646 46717 46717 46717 46976 47033 47108 47209
## [171] 47287 47287 47287 47510 47530 47636 47750 47893 47893 47893
## [181] 48055 48096 48223 48232 48776 48776 48776 48983 49077 49540
## [191] 49670 49810 49810 49810 50062 50110 50225 50245 50320 50320
## [201] 50320 50567 50684 50706 50782 50897 50897 50897 51267 51255
## [211] 51314 51432 51519 51519 51519 52011 52040 52220 52350 52495
## [221] 52495 52495 52879 53006 53108 53209 53365 53365 53365 53365
## [231] 53782 53871 54093 54326 54326 54326 54895 55031 55166 55386
## [241] 55527 55527 55527 56024 56160 56315 56472 56587 56587 56587
## [251] 57147 57329 57550 57742 58297 58297 58297 59120 59241 59364
## [261] 59748 60038 60038 60038 61377 61697 61861 62028 62830 62830
## [271] 62830 64021 64455 64871 65373 66052 66052 66052 68099 68637
## [281] 69127 70446 71207 71207 71207 73858 74843 75373 77060 78125
## [291] 78125 78125 81463 82987 84741 85899 88645 88645 88645 93284
## [301] 94986 97028 99381 101469 101469 101469 106740 107280 109152 109152
## [311] 112581 112581 112581 117295 118754 121426 126177 127715 127715 127715
## [321] 135844 138258 140548 142979 146761 146761 146761 153992 155462 157781
## [331] 160102 162782 162782 162782 167377 168960 170705 172743 172743 172743
## [341] 172743 181200 181967 183663 185708
```

see what would happen if we don't use the whole historical data? e.g. starts from 2020.8, 2023.8,...?

ct_ts

```
## Time Series:
## Start = c(2020, 1)
## End = c(2020, 345)
## Frequency = 345
## [1] 0 0 0 0 0 0 0 0 0 0
## [11] 0 0 0 0 0 0 0 0 0 0
## [21] 0 0 0 0 0 0 0 0 0 0
## [31] 0 0 0 0 0 0 0 0 0 0
## [41] 0 0 0 0 0 0 1 1 2 3
## [51] 7 7 7 26 41 68 96 159 194 223
## [61] 327 415 618 875 1012 1291 1524 1993 2571 3128
## [71] 3557 3824 4915 5276 5675 6906 7781 8781 9784 10131
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## [101] 28764 29287 29312 29973 30621 30995 31784 32411 32984 33554
## [111] 33765 34333 34855 35464 36085 36703 37419 38116 38430 39017
## [121] 39208 39640 40022 40468 40873 41303 41288 41559 41762 42022
## [131] 42201 42740 42979 43091 43239 43460 43818 43968 44092 44179
## [141] 44347 44461 44689 44994 45088 45235 45349 45429 45440 45557
## [151] 45715 45755 45782 45899 45913 45994 46059 46206 46303 46362
## [161] 46514 46572 46646 46717 46717 46717 46976 47033 47108 47209
## [171] 47287 47287 47287 47510 47530 47636 47750 47893 47893 47893
## [181] 48055 48096 48223 48232 48776 48776 48776 48983 49077 49540
## [191] 49670 49810 49810 49810 50062 50110 50225 50245 50320 50320
## [201] 50320 50567 50684 50706 50782 50897 50897 50897 51267 51255
## [211] 51314 51432 51519 51519 51519 52011 52040 52220 52350 52495
## [221] 52495 52495 52879 53006 53108 53209 53365 53365 53365 53365
## [231] 53782 53871 54093 54326 54326 54326 54895 55031 55166 55386
## [241] 55527 55527 55527 56024 56160 56315 56472 56587 56587 56587
## [251] 57147 57329 57550 57742 58297 58297 58297 59120 59241 59364
## [261] 59748 60038 60038 60038 61377 61697 61861 62028 62830 62830
## [271] 62830 64021 64455 64871 65373 66052 66052 66052 68099 68637
## [281] 69127 70446 71207 71207 71207 73858 74843 75373 77060 78125
## [291] 78125 78125 81463 82987 84741 85899 88645 88645 88645 93284
## [301] 94986 97028 99381 101469 101469 101469 106740 107280 109152 109152
## [311] 112581 112581 112581 117295 118754 121426 126177 127715 127715 127715
## [321] 135844 138258 140548 142979 146761 146761 146761 153992 155462 157781
## [331] 160102 162782 162782 162782 167377 168960 170705 172743 172743 172743
## [341] 172743 181200 181967 183663 185708
```

```
plot.ts(ct_ts) # plot time series first
```



ARIMA models Auto ARIMA model

```
#Fit the auto.arima model

auto_fit <- auto.arima(ct_ts)
summary(auto_fit)
```

```
## Series: ct_ts
## ARIMA(2,2,2)
##
## Coefficients:
##          ar1          ar2          ma1          ma2
##          0.3824 -0.2181 -1.6356  0.7939
## s.e.  0.0693  0.0621  0.0506  0.0472
##
## sigma^2 = 673855: log likelihood = -2787.9
## AIC=5585.8 AICc=5585.98 BIC=5604.99
##
## Training set error measures:
##          ME          RMSE          MAE          MPE          MAPE MASE          ACF1
## Training set 40.15631 813.7172 388.816 2.684823 3.321913 NaN -0.01221406
```

```
# Series: ct_ts
# ARIMA(2,2,2)
#
# Coefficients:
#          ar1          ar2          ma1          ma2
#          0.3824 -0.2181 -1.6356  0.7939
# s.e.  0.0693  0.0621  0.0506  0.0472
#
# sigma^2 = 673855: log likelihood = -2787.9
# AIC=5585.8 AICc=5585.98 BIC=5604.99
#
# Training set error measures:
#          ME          RMSE          MAE          MPE          MAPE MASE          ACF1
# Training set 40.15631 813.7172 388.816 2.684823 3.321913 NaN -0.01221406
```

Step-by-Step

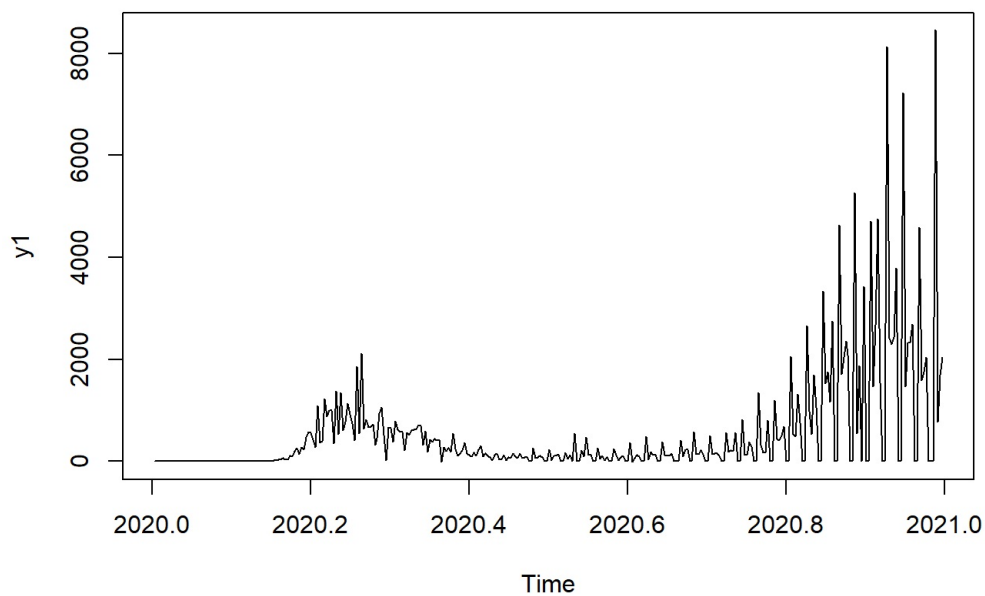
2. Select the best model using information criteria (AIC_c, BIC), and present out-of-sample forecasts with prediction intervals

```
## Step 1. Is the time series stationary?

# Use Augmented Dickey-Fuller Test to test stationary
adf.test(ct_ts)          # if p-value is large (> 0.10), then non stationary
```

```
##
## Augmented Dickey-Fuller Test
##
## data: ct_ts
## Dickey-Fuller = -1.8445, Lag order = 7, p-value = 0.6424
## alternative hypothesis: stationary
```

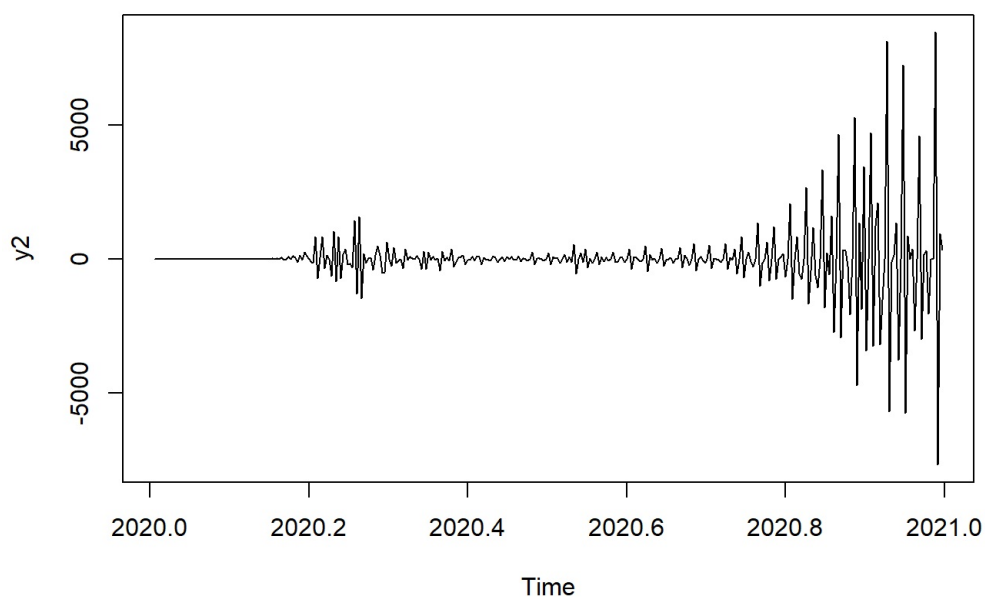
```
y1 <- diff(ct_ts, differences = 1)
plot.ts(y1)          # looks stationary visually
```



```
adf.test(y1)    # p-value is large
```

```
##
## Augmented Dickey-Fuller Test
##
## data: y1
## Dickey-Fuller = -1.0266, Lag order = 6, p-value = 0.9334
## alternative hypothesis: stationary
```

```
y2 <- diff(ct_ts, differences = 2)
plot.ts(y2)     # looks stationary visually
```



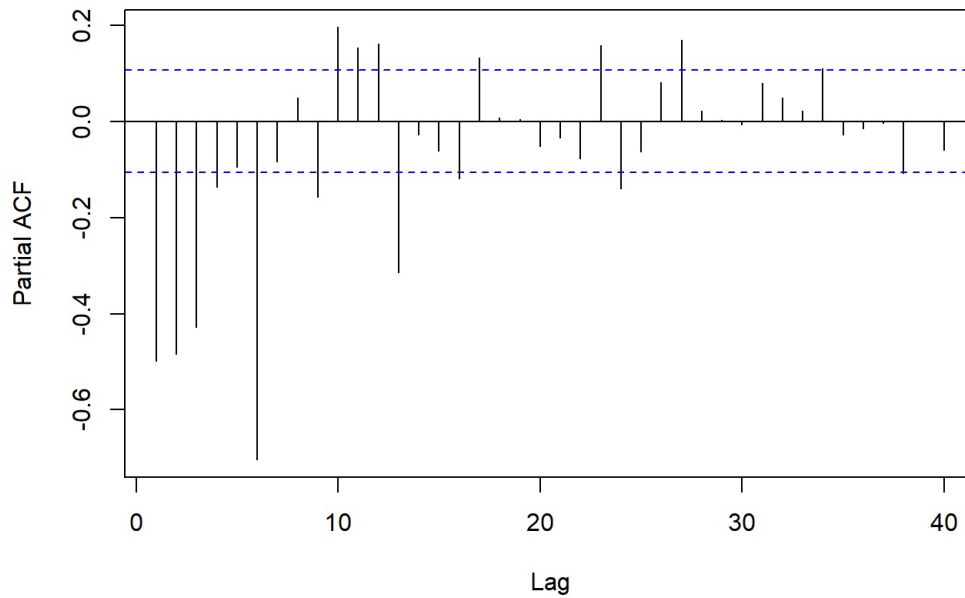
```
adf.test(y2)    # estimated p = 0.01 => small p-value (< 0.10) => so yd is stationary ==> fix d = 2 in ARIMA mode
ls to be fitted -----> here my p value is 0.01
```

```
## Warning in adf.test(y2): p-value smaller than printed p-value
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: y2  
## Dickey-Fuller = -15.936, Lag order = 6, p-value = 0.01  
## alternative hypothesis: stationary
```

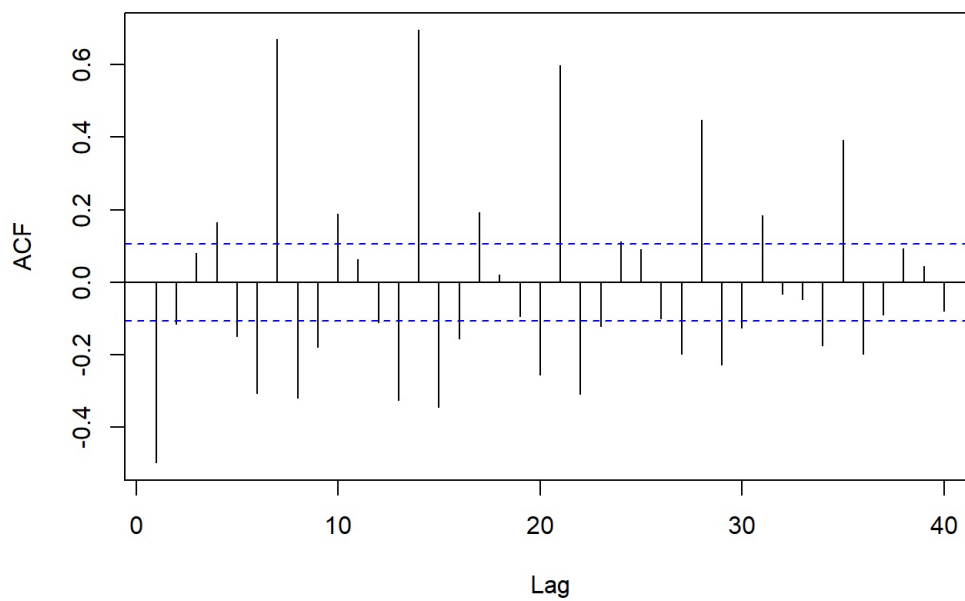
```
## Step 2. Decide AR(p) or MA(q) or both ARMA(p,q).  
Pacf(y2, lag.max = 40) # PACF suggest p=4
```

Series y2



```
Acf(y2, lag.max = 40) #ACF suggest q=6
```

Series y2



```

# # nearby models Arima, d = 2;p->1,2,3 d-->2 q-->1,2,3
# Create a list to store models and their BIC values
models <- list()
bic_values <- numeric()

# Define the range of p, d, and q
p_values <- 1:3
d_value <- 2
q_values <- 1:3

# Iterate over all combinations of p, d, q
for (p in p_values) {
  for (q in q_values) {
    model <- Arima(ct_ts, order = c(p, d_value, q))
    model_name <- paste("ARIMA(", p, ",", d_value, ",", q, ")", sep = "")
    models[[model_name]] <- model
    bic_values[model_name] <- BIC(model)
  }
}

# Print the summaries and BIC of all models
for (model_name in names(models)) {
  cat("Model:", model_name, "\n")
  print(summary(models[[model_name]]))
  cat("BIC:", bic_values[model_name], "\n\n")
}

```

```

## Model: ARIMA(1,2,1)
## Series: ct_ts
## ARIMA(1,2,1)
##
## Coefficients:
##          ar1          ma1
##        -0.2108    -0.8942
## s.e.    0.0547    0.0187
##
## sigma^2 = 789555: log likelihood = -2815.53
## AIC=5637.06 AICc=5637.13 BIC=5648.57
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE MASE      ACF1
## Training set 67.83507 883.4029 386.5834 2.521119 3.099501 NaN -0.06660272
## BIC: 5648.572
##
## Model: ARIMA(1,2,2)
## Series: ct_ts
## ARIMA(1,2,2)
##
## Coefficients:
##          ar1          ma1          ma2
##        0.3966    -1.7108    0.8433
## s.e.    0.0692    0.0423    0.0427
##
## sigma^2 = 695126: log likelihood = -2793.71
## AIC=5595.42 AICc=5595.53 BIC=5610.77
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE MASE      ACF1
## Training set 35.73504 827.6787 386.1961 2.591942 3.279466 NaN 0.05447678
## BIC: 5610.766
##
## Model: ARIMA(1,2,3)
## Series: ct_ts
## ARIMA(1,2,3)
##
## Coefficients:
##          ar1          ma1          ma2          ma3
##        0.0258    -1.2796    0.1492    0.3297
## s.e.    0.1547    0.1458    0.2186    0.0993
##
## sigma^2 = 678429: log likelihood = -2789.05
## AIC=5588.1 AICc=5588.27 BIC=5607.28
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE MASE      ACF1
## Training set 37.46222 816.4742 387.481 2.626935 3.271208 NaN -0.005104951
## BIC: 5607.284

```

```

##
## Model: ARIMA(2,2,1)
## Series: ct_ts
## ARIMA(2,2,1)
##
## Coefficients:
##          ar1          ar2          ma1
##        -0.3126  -0.3105  -0.8479
## s.e.    0.0544   0.0538   0.0255
##
## sigma^2 = 723382:  log likelihood = -2800.18
## AIC=5608.36  AICc=5608.47  BIC=5623.71
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 63.78378 844.3331 399.0209 2.765527 3.310667 NaN -0.04685579
## BIC: 5623.706
##
## Model: ARIMA(2,2,2)
## Series: ct_ts
## ARIMA(2,2,2)
##
## Coefficients:
##          ar1          ar2          ma1          ma2
##        0.3824  -0.2181  -1.6356   0.7939
## s.e.   0.0693   0.0621   0.0506   0.0472
##
## sigma^2 = 673855:  log likelihood = -2787.9
## AIC=5585.8  AICc=5585.98  BIC=5604.99
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 40.15631 813.7172 388.816 2.684823 3.321913 NaN -0.01221406
## BIC: 5604.989
##
## Model: ARIMA(2,2,3)
## Series: ct_ts
## ARIMA(2,2,3)
##
## Coefficients:
##          ar1          ar2          ma1          ma2          ma3
##        -0.4075   0.1993  -0.8494  -0.5973   0.7005
## s.e.    0.1119   0.0904   0.0934   0.1498   0.0847
##
## sigma^2 = 677708:  log likelihood = -2788.4
## AIC=5588.81  AICc=5589.06  BIC=5611.83
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 36.02659 814.8358 386.9043 2.611586 3.25787 NaN 0.01067431
## BIC: 5611.832
##
## Model: ARIMA(3,2,1)
## Series: ct_ts
## ARIMA(3,2,1)
##
## Coefficients:
##          ar1          ar2          ar3          ma1
##        -0.3871  -0.3830  -0.1531  -0.8115
## s.e.    0.0613   0.0602   0.0595   0.0341
##
## sigma^2 = 711788:  log likelihood = -2796.96
## AIC=5603.92  AICc=5604.1  BIC=5623.11
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 62.5553 836.3067 397.3354 2.859249 3.405724 NaN -0.004775868
## BIC: 5623.109
##
## Model: ARIMA(3,2,2)
## Series: ct_ts
## ARIMA(3,2,2)
##
## Coefficients:
##          ar1          ar2          ar3          ma1          ma2
##        -0.6446  -0.4667  -0.2402  -0.5503  -0.2194
## s.e.    0.1727   0.0814   0.0744   0.1703   0.1435
##
## sigma^2 = 711829:  log likelihood = -2796.46

```



```
## AIC=5604.93   AICc=5605.18   BIC=5627.95
##
## Training set error measures:
##           ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 62.86999 835.0964 395.6497 2.840162 3.384065  NaN -0.00453057
## BIC: 5627.952
##
## Model: ARIMA(3,2,3)
## Series: ct_ts
## ARIMA(3,2,3)
##
## Coefficients:
##           ar1      ar2      ar3      ma1      ma2      ma3
##           -0.5967  0.1589 -0.1986 -0.6387 -0.8431  0.7956
## s.e.      0.0700  0.0940  0.0627  0.0533  0.0327  0.0490
##
## sigma^2 = 667485: log likelihood = -2786.15
## AIC=5586.3   AICc=5586.63   BIC=5613.16
##
## Training set error measures:
##           ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 39.72626 807.4693 390.4017 2.661136 3.300773  NaN -0.01373434
## BIC: 5613.16
```

```
# Identify the model with the lowest BIC
best_model_name <- names(which.min(bic_values))
best_model <- models[[best_model_name]]
cat("Model with the lowest BIC:\n")
```

```
## Model with the lowest BIC:
```

```
cat(best_model_name, "\n")
```

```
## ARIMA(2,2,2)
```

```
print(summary(best_model))
```

```
## Series: ct_ts
## ARIMA(2,2,2)
##
## Coefficients:
##           ar1      ar2      ma1      ma2
##           0.3824 -0.2181 -1.6356  0.7939
## s.e.      0.0693  0.0621  0.0506  0.0472
##
## sigma^2 = 673855: log likelihood = -2787.9
## AIC=5585.8   AICc=5585.98   BIC=5604.99
##
## Training set error measures:
##           ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 40.15631 813.7172 388.816 2.684823 3.321913  NaN -0.01221406
```

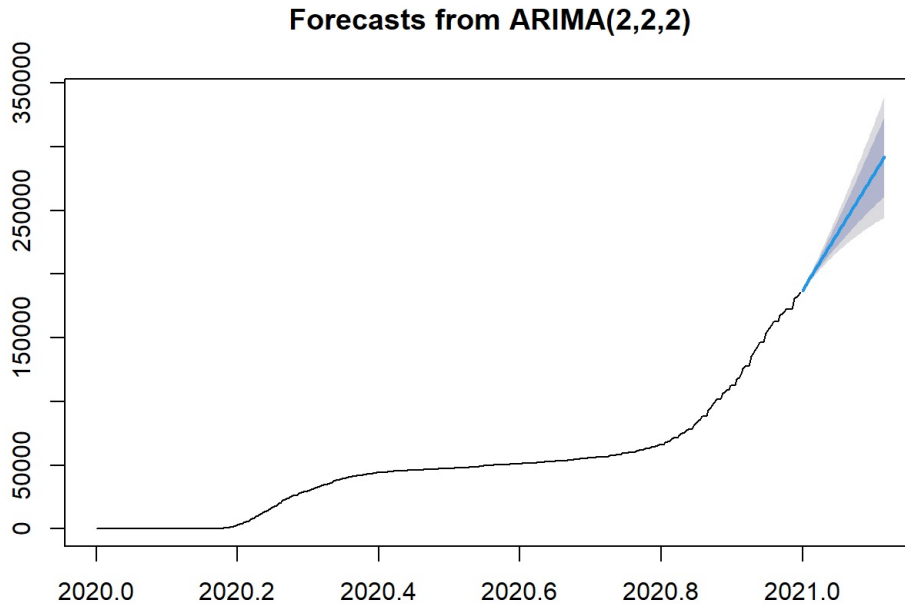
```
# predict best_model
y_hat <- predict(best_model)
y_hat
```

```
## $pred
## Time Series:
## Start = c(2021, 1)
## End = c(2021, 1)
## Frequency = 345
## [1] 187207.9
##
## $se
## Time Series:
## Start = c(2021, 1)
## End = c(2021, 1)
## Frequency = 345
## [1] 820.8867
```

3. Discover a set of good models in the neighborhood of the

best model. Then present the “Consensus Forecast” for COVID cases over the next week (from Sunday to Saturday after the submission date).

```
# Forecasting for a specified period (e.g., 41 days from the end of the series)
forecasted_values <- forecast(best_model, h=41)
# Plot the forecast
plot(forecasted_values)
```



```
print(forecasted_values)
```

##	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## 2021.0000	187207.9	186155.9	188259.9	185599.0	188816.8
## 2021.0029	189528.0	188215.0	190840.9	187520.0	191536.0
## 2021.0058	192280.5	190828.2	193732.8	190059.4	194501.6
## 2021.0087	195019.5	193369.9	196669.1	192496.7	197542.3
## 2021.0116	197659.0	195705.4	199612.6	194671.3	200646.7
## 2021.0145	200263.4	197928.5	202598.3	196692.4	203834.4
## 2021.0174	202876.1	200113.5	205638.7	198651.1	207101.1
## 2021.0203	205499.6	202272.5	208726.7	200564.2	210435.0
## 2021.0232	208125.4	204398.5	211852.4	202425.5	213825.3
## 2021.0261	210749.8	206489.3	215010.3	204233.9	217265.7
## 2021.0290	213373.1	208548.2	218198.0	205994.0	220752.2
## 2021.0319	215996.3	210578.7	221413.9	207710.8	224281.8
## 2021.0348	218619.7	212583.0	224656.4	209387.4	227852.1
## 2021.0377	221243.2	214562.4	227924.0	211025.8	231460.6
## 2021.0406	223866.7	216518.0	231215.5	212627.8	235105.7
## 2021.0435	226490.2	218450.6	234529.8	214194.7	238785.8
## 2021.0464	229113.7	220361.2	237866.1	215728.0	242499.4
## 2021.0493	231737.2	222250.7	241223.6	217228.8	246245.5
## 2021.0522	234360.6	224119.6	244601.7	218698.3	250022.9
## 2021.0551	236984.1	225968.6	247999.6	220137.4	253830.8
## 2021.0580	239607.6	227798.3	251416.9	221546.8	257668.4
## 2021.0609	242231.1	229609.1	254853.0	222927.4	261534.7
## 2021.0638	244854.5	231401.5	258307.5	224279.9	265429.1
## 2021.0667	247478.0	233176.0	261780.0	225605.0	269351.0
## 2021.0696	250101.5	234932.9	265270.0	226903.2	273299.8
## 2021.0725	252725.0	236672.7	268777.2	228175.1	277274.8
## 2021.0754	255348.4	238395.6	272301.2	229421.3	281275.5
## 2021.0783	257971.9	240102.0	275841.8	230642.3	285301.5
## 2021.0812	260595.4	241792.2	279398.6	231838.4	289352.4
## 2021.0841	263218.8	243466.5	282971.2	233010.2	293427.5
## 2021.0870	265842.3	245125.1	286559.5	234158.1	297526.6
## 2021.0899	268465.8	246768.3	290163.3	235282.4	301649.2
## 2021.0928	271089.3	248396.4	293782.1	236383.6	305795.0
## 2021.0957	273712.7	250009.6	297415.9	237462.0	309963.5
## 2021.0986	276336.2	251608.1	301064.3	238517.9	314154.6
## 2021.1014	278959.7	253192.2	304727.2	239551.6	318367.7
## 2021.1043	281583.2	254761.9	308404.4	240563.6	322602.7
## 2021.1072	284206.6	256317.6	312095.7	241554.0	326859.3
## 2021.1101	286830.1	257859.4	315800.9	242523.2	331137.0
## 2021.1130	289453.6	259387.5	319519.7	243471.4	335435.8
## 2021.1159	292077.1	260902.0	323252.1	244398.9	339755.2

4. Your HW score will be based on MAPE (Mean Absolute Percentage Errors) based on actual cases and your forecasts. The smaller the MAPE, the better the model.

```
# Define the range of p, d, and q
p_values <- 1:3
d_value <- 2
q_values <- 1:3

# Store models
models <- list()

# Iterate over all combinations of p, d, q
for (p in p_values) {
  for (q in q_values) {
    model <- Arima(ct_ts, order = c(p, d_value, q))
    model_name <- paste("ARIMA(", p, ",", d_value, ",", q, ")", sep = "")
    models[[model_name]] <- model
  }
}

# Print the summary of all models
for (model_name in names(models)) {
  cat("Model:", model_name, "\n")
  print(summary(models[[model_name]]))
  cat("\n")
}
```

```
## Model: ARIMA(1,2,1)
## Series: ct_ts
```

```

## ARIMA(1,2,1)
##
## Coefficients:
##          ar1          ma1
##      -0.2108  -0.8942
## s.e.   0.0547   0.0187
##
## sigma^2 = 789555: log likelihood = -2815.53
## AIC=5637.06  AICc=5637.13  BIC=5648.57
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 67.83507 883.4029 386.5834 2.521119 3.099501  NaN -0.06660272
##
## Model: ARIMA(1,2,2)
## Series: ct_ts
## ARIMA(1,2,2)
##
## Coefficients:
##          ar1          ma1          ma2
##      0.3966  -1.7108   0.8433
## s.e.  0.0692   0.0423   0.0427
##
## sigma^2 = 695126: log likelihood = -2793.71
## AIC=5595.42  AICc=5595.53  BIC=5610.77
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 35.73504 827.6787 386.1961 2.591942 3.279466  NaN 0.05447678
##
## Model: ARIMA(1,2,3)
## Series: ct_ts
## ARIMA(1,2,3)
##
## Coefficients:
##          ar1          ma1          ma2          ma3
##      0.0258  -1.2796   0.1492   0.3297
## s.e.  0.1547   0.1458   0.2186   0.0993
##
## sigma^2 = 678429: log likelihood = -2789.05
## AIC=5588.1  AICc=5588.27  BIC=5607.28
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 37.46222 816.4742 387.481 2.626935 3.271208  NaN -0.005104951
##
## Model: ARIMA(2,2,1)
## Series: ct_ts
## ARIMA(2,2,1)
##
## Coefficients:
##          ar1          ar2          ma1
##      -0.3126  -0.3105  -0.8479
## s.e.   0.0544   0.0538   0.0255
##
## sigma^2 = 723382: log likelihood = -2800.18
## AIC=5608.36  AICc=5608.47  BIC=5623.71
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 63.78378 844.3331 399.0209 2.765527 3.310667  NaN -0.04685579
##
## Model: ARIMA(2,2,2)
## Series: ct_ts
## ARIMA(2,2,2)
##
## Coefficients:
##          ar1          ar2          ma1          ma2
##      0.3824  -0.2181  -1.6356   0.7939
## s.e.  0.0693   0.0621   0.0506   0.0472
##
## sigma^2 = 673855: log likelihood = -2787.9
## AIC=5585.8  AICc=5585.98  BIC=5604.99
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 40.15631 813.7172 388.816 2.684823 3.321913  NaN -0.01221406
##
## Model: ARIMA(2,2,3)

```

```

## Series: ct_ts
## ARIMA(2,2,3)
##
## Coefficients:
##          ar1      ar2      ma1      ma2      ma3
##      -0.4075  0.1993 -0.8494 -0.5973  0.7005
## s.e.   0.1119  0.0904  0.0934  0.1498  0.0847
##
## sigma^2 = 677708: log likelihood = -2788.4
## AIC=5588.81  AICc=5589.06  BIC=5611.83
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 36.02659 814.8358 386.9043 2.611586 3.25787  NaN  0.01067431
##
## Model: ARIMA(3,2,1)
## Series: ct_ts
## ARIMA(3,2,1)
##
## Coefficients:
##          ar1      ar2      ar3      ma1
##      -0.3871 -0.3830 -0.1531 -0.8115
## s.e.   0.0613  0.0602  0.0595  0.0341
##
## sigma^2 = 711788: log likelihood = -2796.96
## AIC=5603.92  AICc=5604.1  BIC=5623.11
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 62.5553 836.3067 397.3354 2.859249 3.405724  NaN -0.004775868
##
## Model: ARIMA(3,2,2)
## Series: ct_ts
## ARIMA(3,2,2)
##
## Coefficients:
##          ar1      ar2      ar3      ma1      ma2
##      -0.6446 -0.4667 -0.2402 -0.5503 -0.2194
## s.e.   0.1727  0.0814  0.0744  0.1703  0.1435
##
## sigma^2 = 711829: log likelihood = -2796.46
## AIC=5604.93  AICc=5605.18  BIC=5627.95
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 62.86999 835.0964 395.6497 2.840162 3.384065  NaN -0.00453057
##
## Model: ARIMA(3,2,3)
## Series: ct_ts
## ARIMA(3,2,3)
##
## Coefficients:
##          ar1      ar2      ar3      ma1      ma2      ma3
##      -0.5967  0.1589 -0.1986 -0.6387 -0.8431  0.7956
## s.e.   0.0700  0.0940  0.0627  0.0533  0.0327  0.0490
##
## sigma^2 = 667485: log likelihood = -2786.15
## AIC=5586.3  AICc=5586.63  BIC=5613.16
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE  MASE      ACF1
## Training set 39.72626 807.4693 390.4017 2.661136 3.300773  NaN -0.01373434

```

```

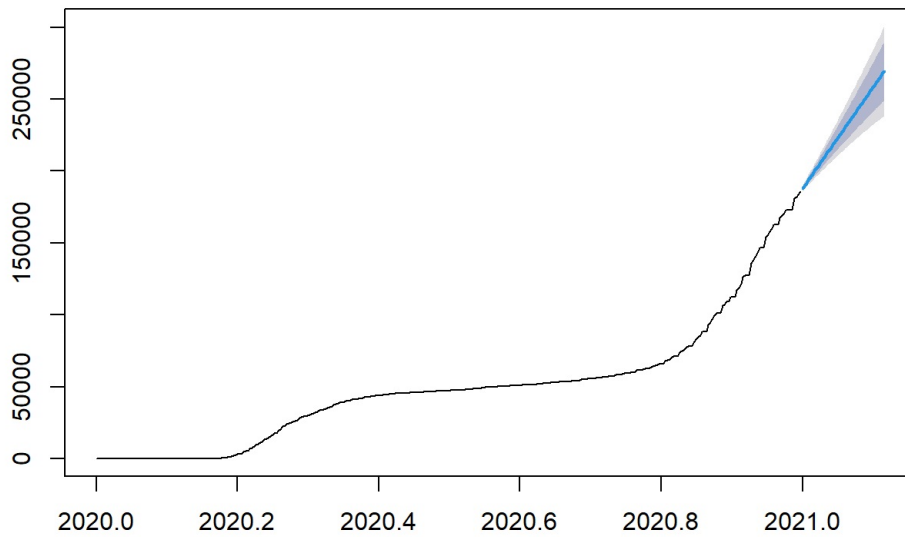
# ARIMA(1,2,1): MAPE = 3.099501
# ARIMA(1,2,2): MAPE = 3.279466
# ARIMA(1,2,3): MAPE = 3.271208
# ARIMA(2,2,1): MAPE = 3.310667
# ARIMA(2,2,2): MAPE = 3.321913
# ARIMA(2,2,3): MAPE = 3.25787
# ARIMA(3,2,1): MAPE = 3.405724
# ARIMA(3,2,2): MAPE = 3.384065
# ARIMA(3,2,3): MAPE = 3.300773
# Based on these values, the model with the lowest MAPE is:
#
# ARIMA(1,2,1) with a MAPE of 3.099501
# Therefore, the ARIMA(1,2,1) model is the best in terms of forecasting accuracy according to the MAPE criterion
among the models listed. Remember, a lower MAPE value indicates a better fit of the model to the data

```

```
# Fit the best ARIMA model based on lowest MAPE -substitute order which the combination that gave the lowest MAPE

best_model_MAPE <- Arima(ct_ts, order = c(1,2,1))
# Forecasting for a specified period (e.g., 41 days from the end of the series)
forecasted_values <- forecast(best_model_MAPE, h=41)
# Plot the forecast
plot(forecasted_values)
```

Forecasts from ARIMA(1,2,1)



```
print(forecasted_values)
```

##	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## 2021.0000	187752.7	186614.0	188891.4	186011.1	189494.3
## 2021.0029	189797.5	188269.3	191325.6	187460.3	192134.6
## 2021.0058	191842.2	189920.7	193763.7	188903.5	194780.9
## 2021.0087	193887.0	191592.2	196181.8	190377.4	197396.5
## 2021.0116	195931.7	193266.2	198597.3	191855.1	200008.3
## 2021.0145	197976.5	194939.6	201013.3	193332.0	202621.0
## 2021.0174	200021.2	196609.5	203432.9	194803.4	205239.0
## 2021.0203	202066.0	198274.3	205857.6	196267.2	207864.7
## 2021.0232	204110.7	199933.2	208288.3	197721.7	210499.7
## 2021.0261	206155.5	201585.3	210725.6	199166.0	213144.9
## 2021.0290	208200.2	203230.4	213170.1	200599.5	215801.0
## 2021.0319	210245.0	204868.1	215621.9	202021.7	218468.2
## 2021.0348	212289.7	206498.3	218081.2	203432.5	221147.0
## 2021.0377	214334.5	208120.9	220548.1	204831.6	223837.3
## 2021.0406	216379.2	209735.8	223022.6	206219.1	226539.4
## 2021.0435	218424.0	211343.2	225504.8	207594.8	229253.1
## 2021.0464	220468.7	212942.9	227994.6	208958.9	231978.5
## 2021.0493	222513.5	214535.0	230492.0	210311.4	234715.6
## 2021.0522	224558.2	216119.5	232996.9	211652.3	237464.1
## 2021.0551	226603.0	217696.6	235509.4	212981.8	240224.1
## 2021.0580	228647.7	219266.2	238029.2	214300.0	242995.5
## 2021.0609	230692.5	220828.5	240556.4	215606.9	245778.1
## 2021.0638	232737.2	222383.5	243090.9	216902.6	248571.8
## 2021.0667	234782.0	223931.3	245632.6	218187.4	251376.6
## 2021.0696	236826.7	225472.0	248181.4	219461.2	254192.3
## 2021.0725	238871.5	227005.6	250737.3	220724.2	257018.7
## 2021.0754	240916.2	228532.3	253300.2	221976.6	259855.9
## 2021.0783	242961.0	230052.0	255870.0	223218.4	262703.6
## 2021.0812	245005.7	231564.9	258446.6	224449.7	265561.7
## 2021.0841	247050.5	233071.0	261030.0	225670.7	268430.2
## 2021.0870	249095.2	234570.4	263620.0	226881.5	271309.0
## 2021.0899	251140.0	236063.2	266216.7	228082.1	274197.9
## 2021.0928	253184.7	237549.5	268820.0	229272.7	277096.8
## 2021.0957	255229.5	239029.3	271429.7	230453.4	280005.6
## 2021.0986	257274.2	240502.6	274045.9	231624.2	282924.2
## 2021.1014	259319.0	241969.6	276668.4	232785.4	285852.6
## 2021.1043	261363.7	243430.3	279297.2	233936.9	288790.6
## 2021.1072	263408.5	244884.7	281932.3	235078.8	291738.1
## 2021.1101	265453.2	246333.0	284573.5	236211.4	294695.1
## 2021.1130	267498.0	247775.2	287220.8	237334.5	297661.5
## 2021.1159	269542.7	249211.3	289874.2	238448.4	300637.1