3 Assume mRNA is at QSS:  

$$0 = \dot{m} = k_m g - d_m m = 0$$
  
 $\Rightarrow m = \frac{k_m g}{dm} = constant$ 

$$\begin{array}{ll}
\text{P. New SDE:} \\
\dot{\rho} = \left[ k_{p} \frac{k_{m} g}{\alpha m} - d_{p} P \right] + \sqrt{k_{p} \frac{k_{m} g}{\alpha m}} + d_{p} P \left[ 7_{p}(t) \right]
\end{array}$$

Approximate 
$$p$$
 as being not too for from equilibrium:

 $P = \overline{P} + \Delta P$  with  $\frac{\Delta P}{\overline{P}} \ll 1$ 

The mean/ss is where  $\hat{p} = 0$ ,

The mean/ss is where 
$$p = 0$$
,  
i.e.  $0 = \dot{p} = k_p \frac{k_m g}{dm} - dp P$   
 $\Rightarrow Pss = \bar{p} = \frac{k_p k_m g}{dp dm}$ 

(b) Use Taylor series:  

$$\sqrt{1+x} \approx 1+\frac{1}{2}x - \frac{1}{8}x^2 + \cdots$$

hoise 
$$\approx 6a$$
  $8a \approx \frac{3}{4}\sqrt{2dpPss} + \sqrt{2dpPss} = \sqrt{2dpPss}$ 

noise 
$$\approx 5 \text{mP}$$

noise  $\approx \frac{3}{4} \frac{\sqrt{20pPss}}{Pss} P + \frac{\sqrt{20pPss}}{4Pss} P$