

Лабораторная работа №3

По курсу "Нейроинформатика"

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Цель работы:

Исследование свойств многослойной нейронной сети прямого распространения и алгоритмов ее обучения, применение сети в задачах классификации и аппроксимации функции.

```
In [1]: import numpy as np
import pylab
import torch
import torch.nn as nn
import copy
import random
import sklearn as skl
import sklearn.metrics
```

1. Классификация точек

Области:

- Эллипс. $a = 0.4, b = 0.5, \alpha = \pi/3, x_0 = -0.2, y_0 = -0.18$
- Эллипс. $a = 0.4, b = 0.5, \alpha = -\pi/3, x_0 = -0.2, y_0 = -0.18$
- Эллипс. $a = 1, b = 1, \alpha = 0, x_0 = 0, y_0 = 0$

```
In [123]: # Уравнение эллипса в параметрическом виде.
ell ellipse(t, inp_arr):
    a, b, x0, y0 = copy.deepcopy(inp_arr)
```

```
    x = x0 + a * np.cos(t)
    y = y0 + b * np.sin(t)
    return x, y
# Уравнение параболы в параметрическом виде.
def parabola(t, p, x0, y0):
    x = x0 + t ** 2 / (2 * p)
    y = y0 + t
    return x, y
# Функция вращения фигуры на заданный угол.
def rotate(pt, alpha):
    x, y = pt
    xr = x * np.cos(alpha) - y * np.sin(alpha)
    yr = x * np.sin(alpha) + y * np.cos(alpha)
    return xr, yr
```

```
In [124]: ellipse1 = [0.4, 0.15, -0.2, -0.18]
ellipse2 = [0.4, 0.5, -0.2, -0.18]
ellipse3 = [1.1, 0, 0]
```

```
In [125]: ell_arr_1 = []
for t in range(0, 1000, 1):
    ell_arr_1.append(rotate(ellipse(t/100, ellipse1), np.pi/3))
ell_arr_1 = np.array(ell_arr_1)

ell_arr_2 = []
for t in range(0, 1000, 1):
    ell_arr_2.append(rotate(ellipse(t/100, ellipse2), -np.pi/3))
ell_arr_2 = np.array(ell_arr_2)

ell_arr_3 = []
for t in range(0, 1000, 1):
    ell_arr_3.append(ellipse(t/100, ellipse3))
ell_arr_3 = np.array(ell_arr_3)
```



Функции для построения датасета:

```
In [127]: def in_ellipse(ell_arr, pt, rot = 0):
a, b, x0, y0 = ell_arr
pt = (pt[0]-x0)*(pt[0]-x0)/(a*a) + ((pt[1]-y0)*(pt[1]-y0))/(b*b) < 1
```

```
In [128]: def make_dataset_on(sel_cnt = 1000, class_cnt = 500):
data_X = []
data_L = []
for i in range(sel_cnt):
    pt = random.random()*10
    choose = random.random()*3
    if(choose > 2):
        data_X.append(rotate(ellipse(pt, ellipse1), np.pi/3))
        data_L.append(0)
    elif(choose > 1):
        data_X.append(rotate(ellipse(pt, ellipse2), -np.pi/3))
        data_L.append(1)
    else:
        data_X.append(ellipse(pt, ellipse3))
        data_L.append(2)
return np.array(data_X), np.array(data_L)

def make_dataset_in(sel_cnt = 30000, class_cnt = 500):
class_cnt = [0, 0, 0]
data_X = []
for i in range(30000):
    pt = [(random.random()*2)-1, (random.random()*2)-1]

    if(in_ellipse(ellipse1, pt, np.pi/3) and class_cnt[0] < 1000):
        data_X.append(pt)
        data_L.append(0)
        class_cnt[0] += 1
        continue

    if(in_ellipse(ellipse2, pt, -np.pi/3) and class_cnt[1] < 1000):
        data_X.append(pt)
        data_L.append(1)
        class_cnt[1] += 1
        continue

    if(in_ellipse(ellipse3, pt) and class_cnt[2] < 1000):
        data_X.append(pt)
        data_L.append(2)
        class_cnt[2] += 1
        continue

data_X = np.array(data_X)
data_L = np.array(data_L)
return np.array(data_X), np.array(data_L)
```

```
In [129]: def calculate_wts(data_L):
class_wts = []
for i in range(np.max(data_L) + 1):
    class_wts.append(1 - (data_L == i).mean())
class_wts = torch.tensor(class_wts, dtype = torch.float32)
return class_wts
```

Обучающие функции

```
In [130]: def accuracy_mult(testRS, testLB):
return (np.argmax(testRS, axis = 1) == testLB).mean()

def train(net, trainXX, trainLB, n_epochs, batch_size, lr,
optimizer = torch.optim.SGD,
criterion = torch.nn.CrossEntropyLoss(weight = class_wts),
accuracy = accuracy_mult
):
#функция, производящая обучение сети
arr = []
optim = optimiser(model.parameters(), lr=lr)
num_batches = len(trainXX)/batch_size

for i in range(n_epochs):
    for j in range(int(num_batches)):
        batchXX = trainXX[j*batch_size : (j+1)*batch_size]
        batchLB = trainLB[j*batch_size : (j+1)*batch_size]

        optim.zero_grad()
        loss = criterion(model(batchXX), batchLB)
        loss.backward()
        optim.step()

#график обучения
arr.append([i, loss.detach().numpy(), #значение ф-и потерь
accuracy(model(trainXX).detach().numpy(), trainLB.detach().numpy())]) #среднее количество co

return np.array(arr)

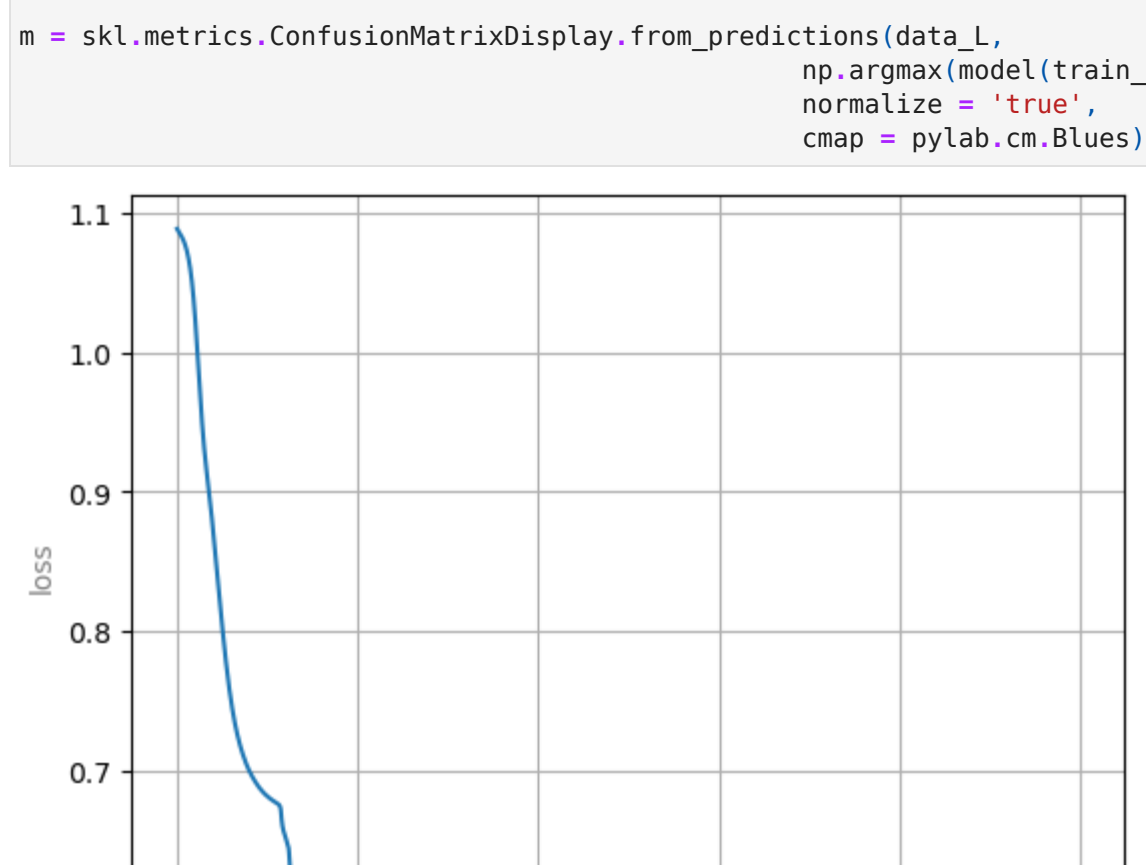
def plot_learning(arr):
pylab.xlabel("epochs", color = "grey")
pylab.ylabel("loss", color = "grey")
pylab.plot(arr[:, 0], arr[:, 1])
pylab.show()

pylab.grid()
pylab.axis([0, len(arr), 0, 1])
pylab.xlabel("epochs", color = "grey")
pylab.ylabel("accuracy", color = "grey")
pylab.plot(arr[:, 0], arr[:, 2])
pylab.show()
```

Классификация датасета с точками на эллипсах

```
In [131]: data_X, data_L = make_dataset_on(sel_cnt = 1000, class_cnt = 500)
train_X = torch.tensor(data_X, dtype = torch.float32)
train_L = torch.tensor(data_L)
```

Демонстрация точек датасета:



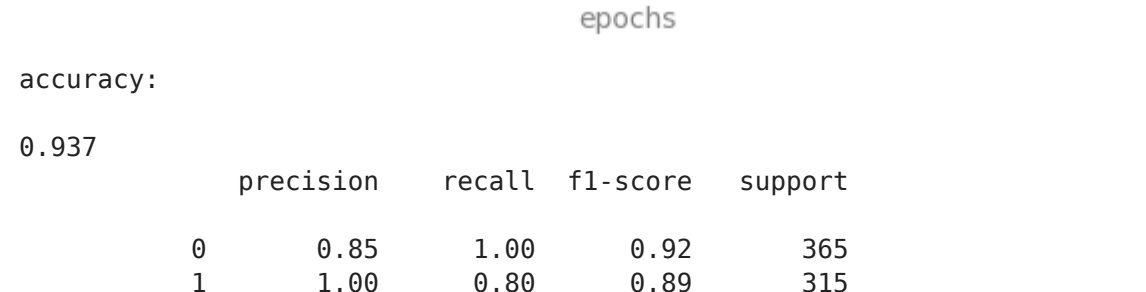
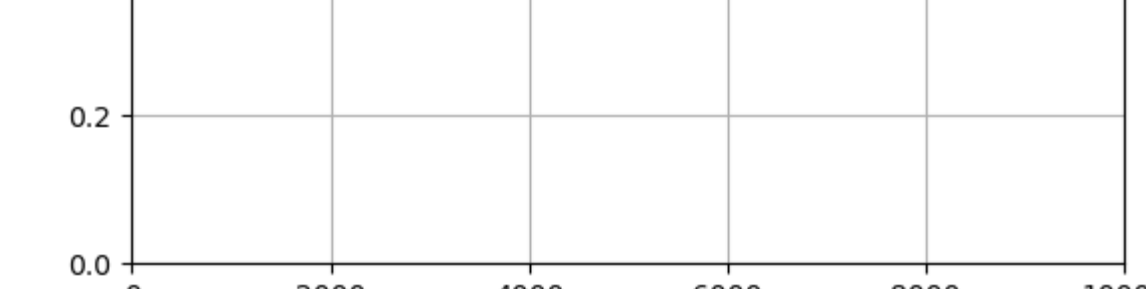
Обучение сети:

```
In [155]: class_wts = calculate_wts(data_L)
```

```
In [156]: model = torch.nn.Sequential(
nn.Linear(2, 50),
nn.Linear(50, 50),
nn.ReLU(),
nn.Linear(50, 20),
nn.ReLU(),
nn.Linear(20, 3),
nn.Softmax(dim = 1)
)
arr = train(model, train_X, train_L, 10000, 100, 0.01, criterion = torch.nn.CrossEntropyLoss(weight = class_wts))
```

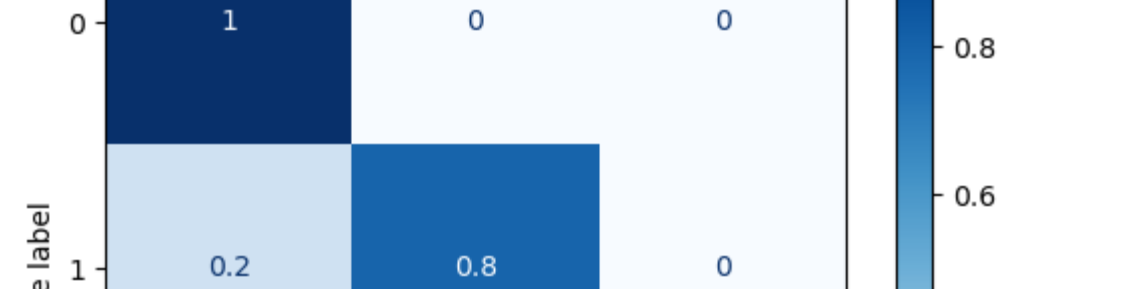
Подсчет метрик

```
In [157]: plot_learning(arr)
print("accuracy: %n")
print((np.argmax(model(train_X).detach().numpy(), axis = 1) == np.array(train_L)).mean())
print(skl.metrics.classification_report(data_L, np.argmax(model(train_X).detach().numpy(), axis = 1)))
m = skl.metrics.ConfusionMatrixDisplay.from_predictions(data_L,
np.argmax(model(train_X).detach().numpy(), axis = 1),
normalize = "true",
cmap = pylab.cm.Blues)
```



accuracy:

	precision	recall	f1-score	support
0	0.85	1.00	0.92	365
1	0.80	0.80	0.80	315
2	1.00	1.00	1.00	320
accuracy				1000
macro avg	0.95	0.93	0.94	1000
weighted avg	0.95	0.94	0.94	1000

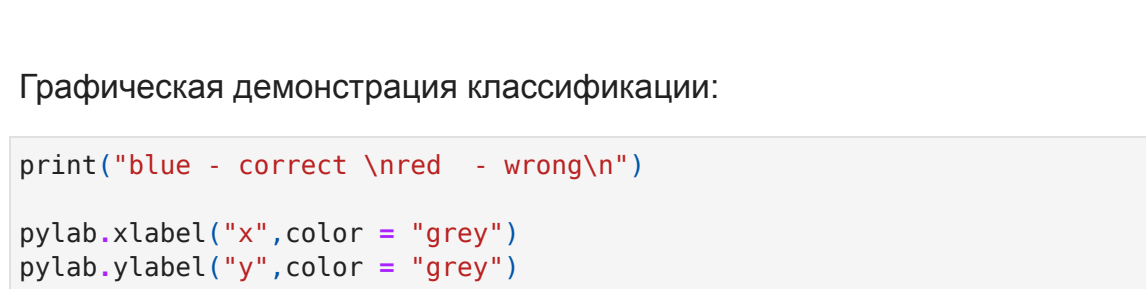


Графическая демонстрация классификации:

```
In [158]: print("blue - correct \nred - wrong\n")
pylab.xlabel("x", color = "grey")
pylab.ylabel("y", color = "grey")
pylab.grid()
pylab.plot(ell_arr_1[:, 0], ell_arr_1[:, 1])
pylab.plot(ell_arr_2[:, 0], ell_arr_2[:, 1])
pylab.plot(ell_arr_3[:, 0], ell_arr_3[:, 1])

for i in range(len(data_X)):
    if(data_L[i] == torch.argmax(model(train_X[i].reshape(1,2))),
pylab.plot(data_X[i, 0], data_X[i, 1], 'bo')
    else:
        pylab.plot(data_X[i, 0], data_X[i, 1], 'ro')

pylab.show()
blue - correct
red - wrong
```



```
In [159]: print("Correct Labels")
pylab.xlabel("x", color = "grey")
pylab.ylabel("y", color = "grey")
pylab.grid()
pylab.plot(ell_arr_1[:, 0], ell_arr_1[:, 1])
pylab.plot(ell_arr_2[:, 0], ell_arr_2[:, 1])
pylab.plot(ell_arr_3[:, 0], ell_arr_3[:, 1])

for i in range(len(data_X)):
    if(data_L[i] == 0):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'bo')
    elif(data_L[i] == 1):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'ro')
    elif(data_L[i] == 2):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'go')

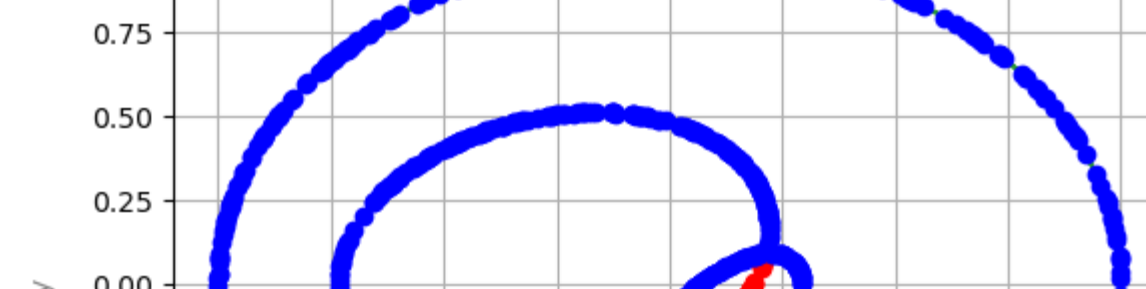
pylab.show()

print("Predicted Labels")
pylab.plot(ell_arr_1[:, 0], ell_arr_1[:, 1])
pylab.plot(ell_arr_2[:, 0], ell_arr_2[:, 1])
pylab.plot(ell_arr_3[:, 0], ell_arr_3[:, 1])

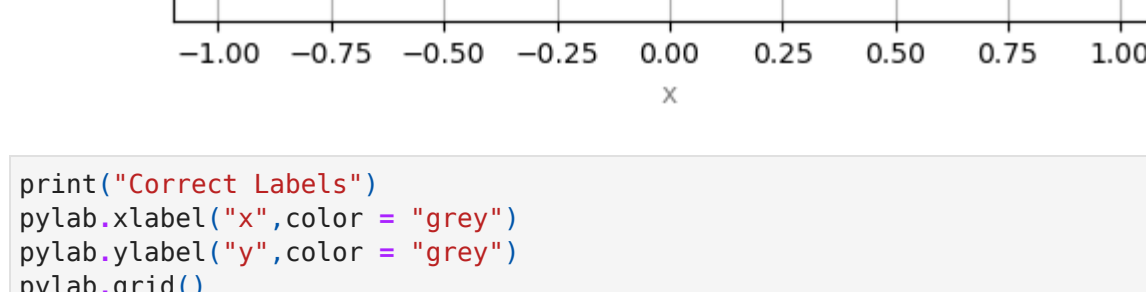
pylab.xlabel("x", color = "grey")
pylab.ylabel("y", color = "grey")
pylab.grid()
for i in range(len(data_X)):
    if(torch.argmax(model(train_X[i].reshape(1,2))) == 0):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'bo')
    elif(torch.argmax(model(train_X[i].reshape(1,2))) == 1):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'ro')
    elif(torch.argmax(model(train_X[i].reshape(1,2))) == 2):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'go')

pylab.show()
```

Correct Labels



Predicted Labels



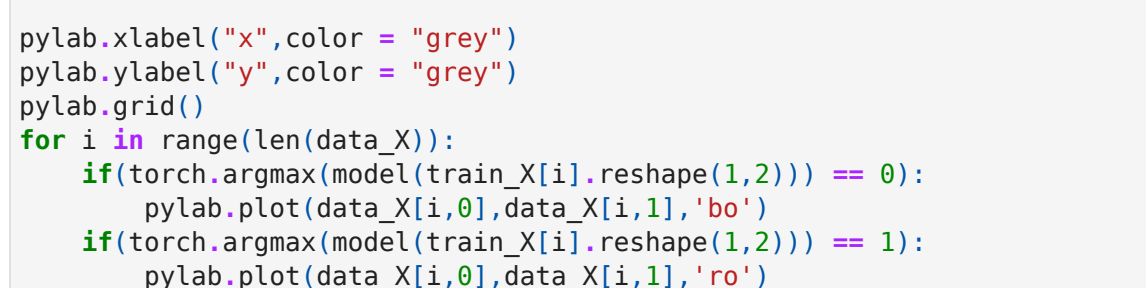
Классификация пространственного датасета той же сетью:

```
In [188]: data_X, data_L = make_dataset_in(sel_cnt = 1000, class_cnt = 500)
train_X = torch.tensor(data_X, dtype = torch.float32)
train_L = torch.tensor(data_L)
```

```
In [189]: print("blue - correct \nred - wrong\n")
pylab.xlabel("x", color = "grey")
pylab.ylabel("y", color = "grey")
pylab.grid()
pylab.plot(ell_arr_1[:, 0], ell_arr_1[:, 1])
pylab.plot(ell_arr_2[:, 0], ell_arr_2[:, 1])
pylab.plot(ell_arr_3[:, 0], ell_arr_3[:, 1])

for i in range(len(data_X)):
    if(data_L[i] == torch.argmax(model(train_X[i].reshape(1,2))),
pylab.plot(data_X[i, 0], data_X[i, 1], 'bo')
    else:
        pylab.plot(data_X[i, 0], data_X[i, 1], 'ro')

pylab.show()
blue - correct
red - wrong
```



```
In [190]: print("Correct Labels")
pylab.xlabel("x", color = "grey")
pylab.ylabel("y", color = "grey")
pylab.grid()
pylab.plot(ell_arr_1[:, 0], ell_arr_1[:, 1])
pylab.plot(ell_arr_2[:, 0], ell_arr_2[:, 1])
pylab.plot(ell_arr_3[:, 0], ell_arr_3[:, 1])

for i in range(len(data_X)):
    if(data_L[i] == 0):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'bo')
    elif(data_L[i] == 1):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'ro')
    elif(data_L[i] == 2):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'go')

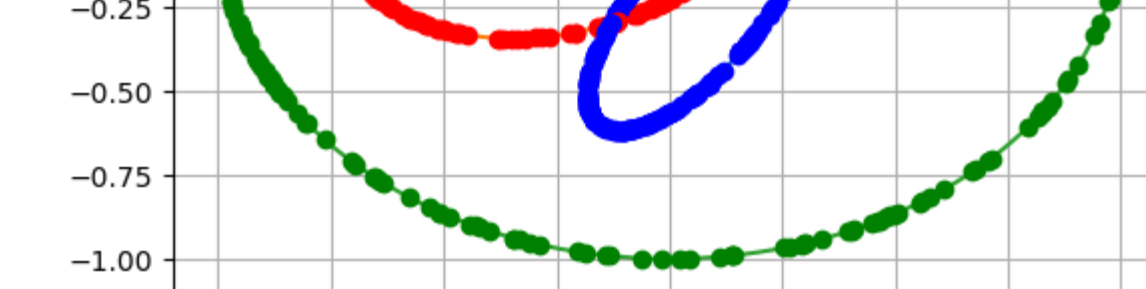
pylab.show()

print("Predicted Labels")
pylab.plot(ell_arr_1[:, 0], ell_arr_1[:, 1])
pylab.plot(ell_arr_2[:, 0], ell_arr_2[:, 1])
pylab.plot(ell_arr_3[:, 0], ell_arr_3[:, 1])

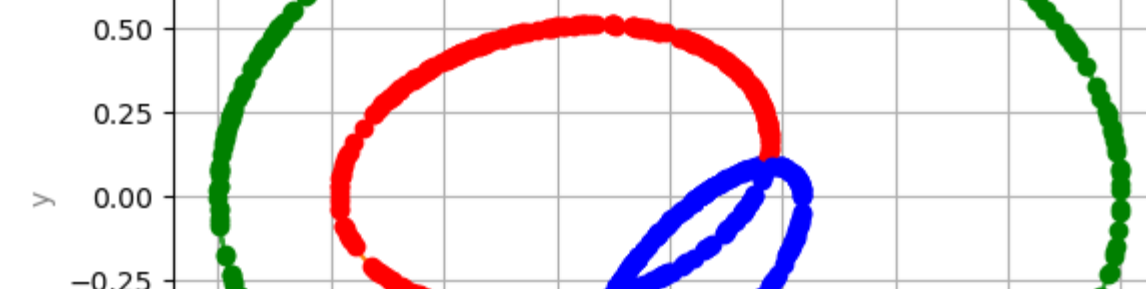
pylab.xlabel("x", color = "grey")
pylab.ylabel("y", color = "grey")
pylab.grid()
for i in range(len(data_X)):
    if(torch.argmax(model(train_X[i].reshape(1,2))) == 0):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'bo')
    elif(torch.argmax(model(train_X[i].reshape(1,2))) == 1):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'ro')
    elif(torch.argmax(model(train_X[i].reshape(1,2))) == 2):
        pylab.plot(data_X[i, 0], data_X[i, 1], 'go')

pylab.show()
```

Correct Labels



Predicted Labels



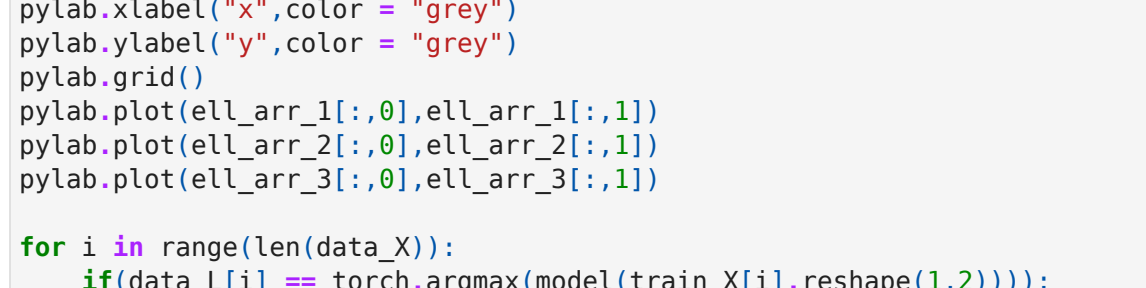
2. Аппроксимация функции

lin[0,4], h=0.02

```
In [2]: def func(t):
return np.cos(t**2)
```

```
In [3]: line = np.array([f(i/1000, func(i/1000)) for i in range(0, 4000)])
```

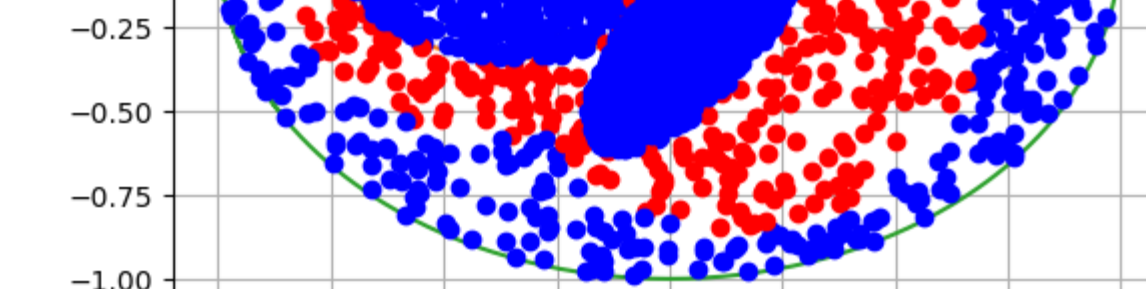
```
In [4]: pylab.xlabel("x", color = "grey")
pylab.ylabel("sin(x)", color = "grey")
pylab.grid()
pylab.plot(line[:], 0, line[:], 1)
pylab.show()
```



```
In [5]: def make_dataset(line, ln = 200):
train_X = []
train_Y = []
for j in range(ln):
    i = int(random.random()*len(line))
    train_X.append((line[i]/1))
    train_Y.append((line[i]))
train_X = torch.tensor(train_X, dtype = torch.float32)
train_Y = torch.tensor(train_Y, dtype = torch.float)
return train_X, train_Y
```

```
In [6]: train_X, train_Y = make_dataset(line)
test_X, test_Y = make_dataset(line, ln = 1000)
```

```
In [7]: pylab.xlabel("x", color = "grey")
pylab.ylabel("y", color = "grey")
pylab.grid()
pylab.plot(train_X, train_Y, 'yo')
pylab.show()
```



```
In [9]: def accuracy_line(testRS, testLB):
return (np.sum(abs(testRS - testLB)))

def train(net, trainXX, trainLB, n_epochs, batch_size, lr,
optimizer = torch.optim.SGD,
criterion = torch.nn.MSELoss(),
accuracy = accuracy_line
):
#функция, производящая обучение сети
arr = []
optim = optimiser(model.parameters(), lr=lr)
num_batches = len(trainXX)/batch_size

for i in range(n_epochs):
    for j in range(int(num_batches)):
        batchXX = trainXX[j*batch_size : (j+1)*batch_size]
        batchLB = trainLB[j*batch_size : (j+1)*batch_size]

        optim.zero_grad()
        loss = criterion(model(batchXX), batchLB)
        loss.backward()
        optim.step()

#график обучения
arr.append([i, loss.detach().numpy(), #значение ф-и потерь
accuracy(model(trainXX).detach().numpy(), trainLB.detach().numpy())]) #среднее количество co

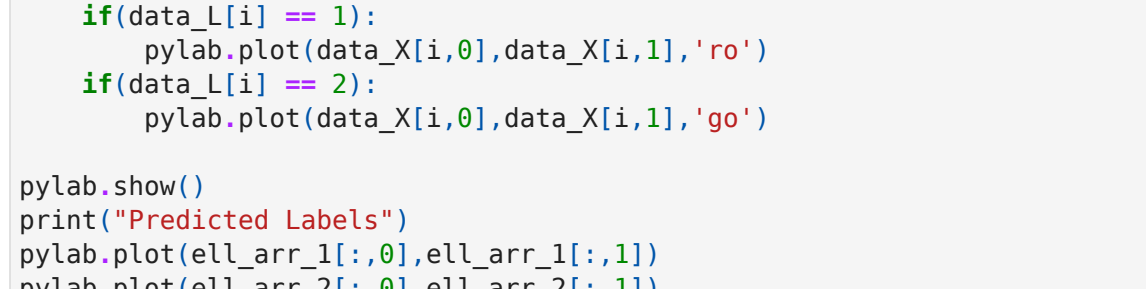
return np.array(arr)
```

```
In [10]: def plot_learning(arr):
pylab.xlabel("epochs", color = "grey")
pylab.ylabel("loss", color = "grey")
pylab.plot(arr[:, 0], arr[:, 1])
pylab.show()

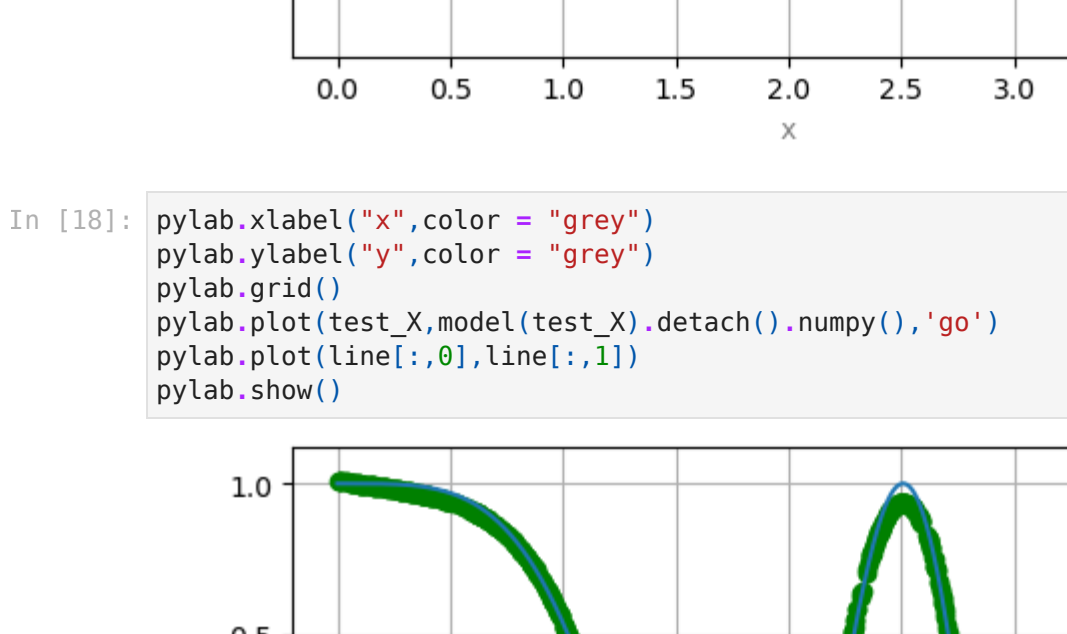
def plot_both(pts_exmpl, pts_res, additional_plot = None):
arr_res = np.array([(i/1000, pts_res[i]) for i in range(len(pts_res))])
pts_exm = np.array([(i/1000, pts_exmpl[i]) for i in range(len(pts_exmpl))])

if(not np.array(additional_plot) == None).all():
    pylab.plot(additional_plot[:], 0, additional_plot[:], 1, color = "red")

print("blue - target line")
print("orange - predicted line")
pylab.xlabel("x", color = "grey")
pylab.ylabel("f(x)", color = "grey")
pylab.grid()
pylab.plot(arr_res[:], 0, arr_res[:], 1, 'bo', color = "blue", linewidth = 3)
pylab.plot(pts_exmpl[:], 0, pts_exmpl[:], 1, 'ro', color = "orange", linewidth = 1.5)
pylab.show()
```



0.4



The plot shows two classes of data points: blue circles and green circles. The x-axis ranges from 0.0 to 4.0, and the y-axis ranges from -1.0 to -0.5. A green curve represents the decision boundary, which is non-linear and separates the two classes. The blue points are generally located to the left of the curve, and the green points are generally located to the right of the curve.