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## **ARN - Report - Labo04**

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## Learning algorithm

1. What is the learning algorithm being used to optimize the weights of the neural networks? What are the parameters (arguments) being used by that algorithm? What cost function is being used ? please, give the equation(s)

MLP\_from\_raw\_data.ipynb

The algorithm used is RMSprop.

The arguments used by this algorithm are: - Learning rate A Tensor, floating point value, or a schedule that is a `tf.keras.optimizers.schedules.LearningRateSchedule`, or a callable that takes no arguments and returns the actual value to use. The learning rate. Defaults to 0.001. - rho: Discounting factor for the history/coming gradient. Defaults to 0.9. - momentum: A scalar or a scalar Tensor. Defaults to 0.0. - epsilon: A small constant for numerical stability. This epsilon is “epsilon hat” in the Kingma and Ba paper (in the formula just before Section 2.1), not the epsilon in Algorithm 1 of the paper. Defaults to 1e-7. - centered: Boolean. If True, gradients are normalized by the estimated variance of the gradient; if False, by the uncentered second moment. Setting this to True may help with training, but is slightly more expensive in terms of computation and memory. Defaults to False. - name: Optional name prefix for the operations created when applying gradients. Defaults to “RMSprop”. - \*\*kwargs: keyword arguments. Allowed arguments are clipvalue, clipnorm, global\_clipnorm. If clipvalue (float) is set, the gradient of each weight is clipped to be no higher than this value. If clipnorm (float) is set, the gradient of each weight is individually clipped so that its norm is no higher than this value. If global\_clipnorm (float) is set the gradient of all weights is clipped so that their global norm is no higher than this value.

The used cost function is the categorical crossentropy function. It's equation is:

$$\text{Loss} = - \sum_{i=1}^{\text{output size}} y_i \cdot \log \hat{y}_i$$

**Figure 1:** ARN-Labo04-CrossEntrEquation

## Model Complexity

2. Model complexity: for each experiment (shallow network learning from raw data, shallow network learning from features, CNN, and Fashion MNIST), select a neural network topology and describe the inputs, indicate how many are they, and how many outputs. Compute

the number of weights of each model (e.g., how many weights between the input and the hidden layer, how many weights between each pair of layers, biases, etc..) and explain how do you get to the total number of weights.

MLP\_from\_raw\_data.ipynb Inputs: 784, which are each pixels in a picture Outputs: 10 classes (numbers between 0 and 9) Activation function: tanh Activation function for output layer: softmax Neurons in hidden layer: 250 Batch size: 4096 Dropout: 0.5 Number of epoch: 150 The model has 784 inputs, 1 hidden layer that contains 250 neurons and 10 outputs. The number of weights between the inputs and the hidden layer is  $784 \cdot 250 = 196000$ . The number of weights between the hidden layer and the outputs is  $250 \cdot 10 = 2500$ . The total number of weights is 198500.

MLP\_from\_HOG.ipynb Inputs: 392 Outputs: 10 classes (numbers between 0 and 9) Activation function: sigmoid Activation function for output layer: softmax Neurons in hidden layer: 200 Batch size: 1024 pixel per cell: 7 n\_orientation: 16 number of epoch: 250 (but we could see that 150 is enough) Dropout: 0.5 The model has 392 inputs, 1 hidden layer that contains 200 neurons and 10 outputs. The number of weights between the inputs and the hidden layer is  $392 \cdot 200 = 78400$ . The number of weights between the hidden layer and the outputs is  $200 \cdot 10 = 2000$ . The total number of weights is 80400.

CNN.ipynb

Fashion\_MNIST.ipynb

## Deep Neural Networks

3. Do the deep neural networks have much more “capacity” (i.e., do they have more weights?) than the shallow ones? explain with one example

The deep neural network have more hidden layer than the shallow ones, but it doesn't necessary mean that it has more neurons in it. For exemple, in this lab we use 300 neurons in the hidden layer for the shallows network (raw\_data and HOG), against only 25 neurons for the deep one (CNN). The deep neural networks have more capacity, because they usually need less components to achieve the same goal or better than a shallow neural network. If we compare the weights of each model, the shallow one will have more weight than the deep one. For exemple, a model with 2 entries, 6 neurons in one hidden layer and 2 output, we get  $2 \cdot 6 + 6 \cdot 2 = 24$  links that have each their weight. For the same model but with 3 hidden layers, we got  $2 \cdot 2 + 2 \cdot 2 + 2 \cdot 2 + 2 \cdot 2 = 16$  links, and so 16 weights.

## Tests

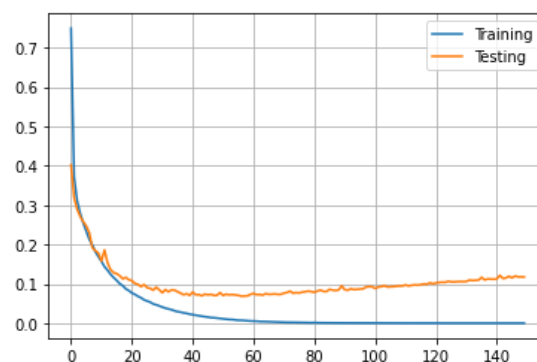
4. Test every notebook for at least three different meaningful cases (e.g., for the MLP exploiting raw data, test different models varying the number of hidden neurons, for the feature-based model, test pix\_p\_cell 4 and 7, and number of orientations or number of hidden neurons, for the CNN, try different number of neurons in the feed-forward part) describe the model and present the performance of the system (e.g., plot of the evolution of the error, final evaluation scores and confusion matrices). Comment the differences in results. Are there particular digits that are frequently confused?

MLP\_from\_raw\_data.ipynb

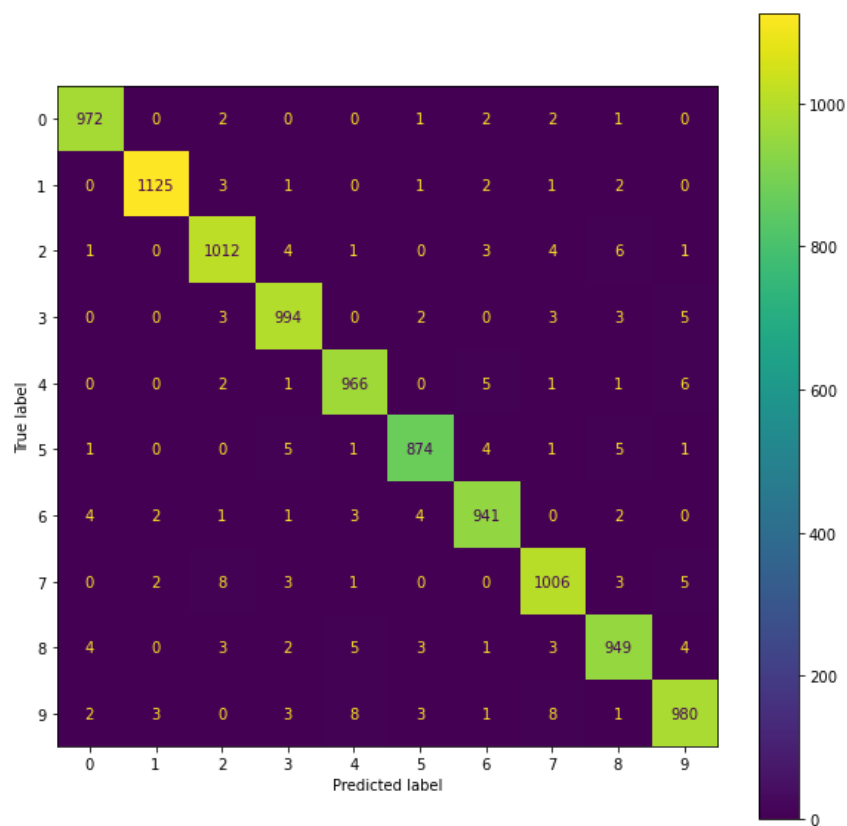
### Model:

- Activation function: tanh
- Neurons: 300
- Dropout: -
- Batch size: 2048
- Epochs: 150

Test score: 0.11751019209623337  
Test accuracy: 0.9818999767303467



**Figure 2:** ARN-RAW-Plot-tanh-softmax\_Batch2048\_NoDropout\_Epoch150



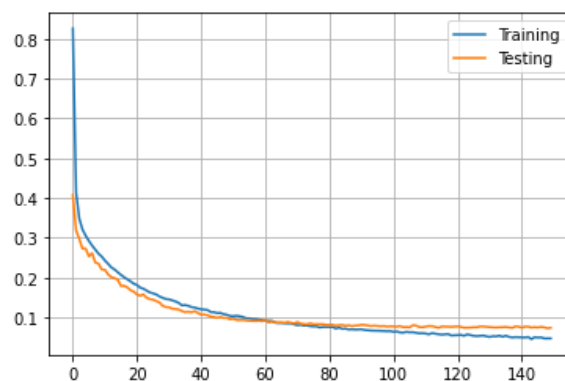
**Figure 3:** ARN-RAW-ConfMat-tanh-softmax\_Batch2048\_NoDropout\_Epoch150

We first tried to train a model without a dropout. As the graph shows there is a problem with overfitting. Surprisingly the confusion matrix is not so bad, the wrong classifications are low, but there are a lot.

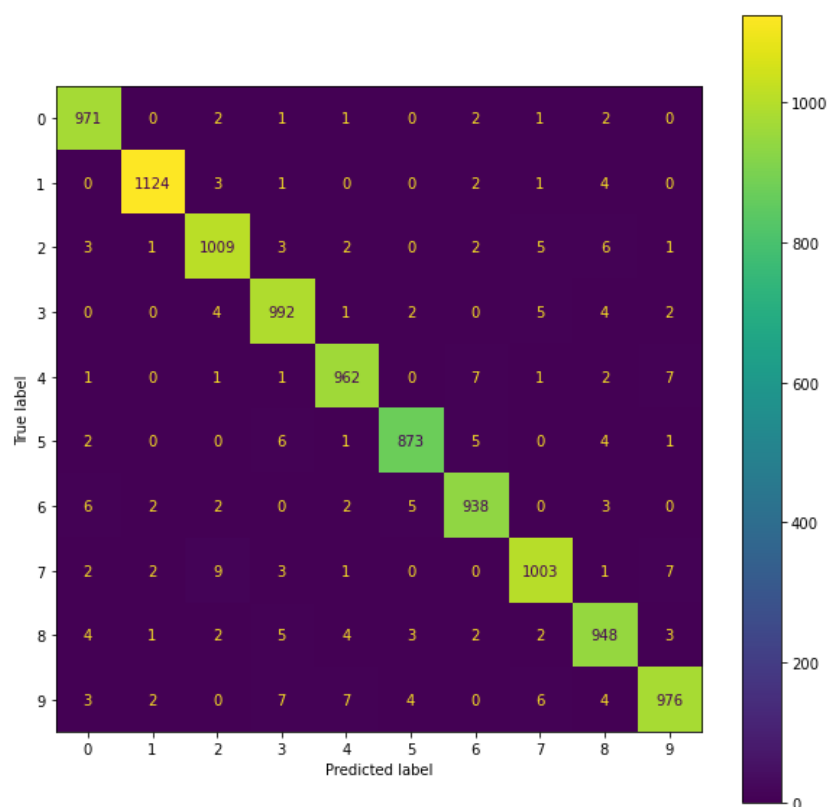
**Model:**

- Activation function: tanh
- Neurons: 300
- Dropout: 0.5
- Batch size: 2048
- Epochs: 150

Test score: 0.0734260305762291  
 Test accuracy: 0.9796000123023987



**Figure 4:** ARN-RAW-Plot-tanh-softmax\_Batch2048\_Dropout\_Epoch150



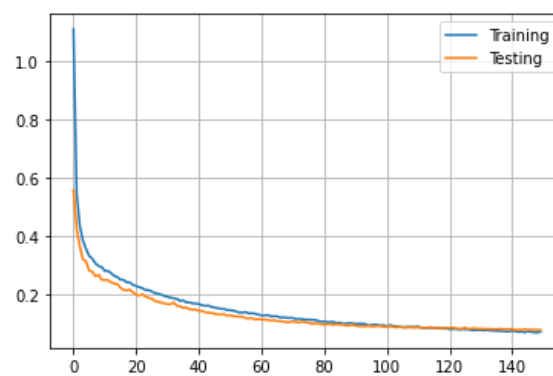
**Figure 5:** ARN-RAW-ConfMat-tanh-softmax\_Batch2048\_Dropout\_Epoch150

We added a dropout and the result already improved. The gap has decreased but at the beginning the test set looks too easy. The confusion matrix shows higher errors but no number really stands out.

**Model:**

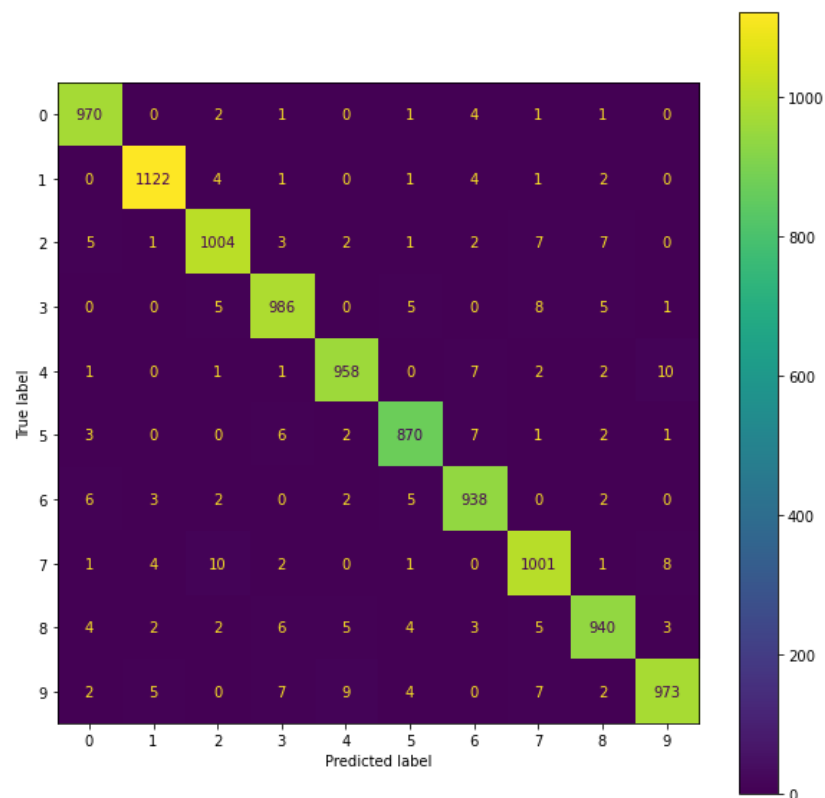
- Activation function: tanh
- Neurons: 250
- Dropout: 0.5
- Batch size: 4096
- Epochs: 150

Test score: 0.08130748569965363  
Test accuracy: 0.9761999845504761



**Figure 6:** ARN-RAW-Plot-tanh-softmax-Neur250\_Batch4096\_Dropout\_Epoch150





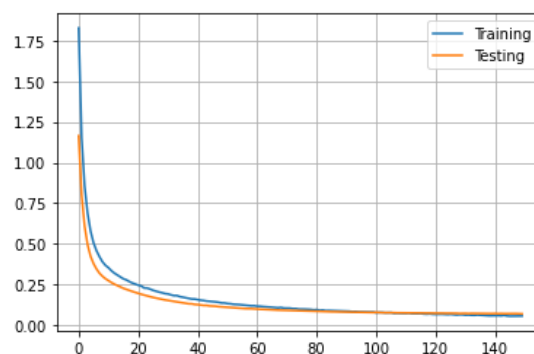
**Figure 7:** ARN-RAW-ConfMat-tanh-softmax-Neur250\_Batch4096\_Dropout\_Epoch150

With fewer neurons and a batch size of 4096, we get a nice result. The two curves are really close to each other. We begin to see numbers with two digits in the confusion matrix. Numbers 4 and 7 are the less good classified.

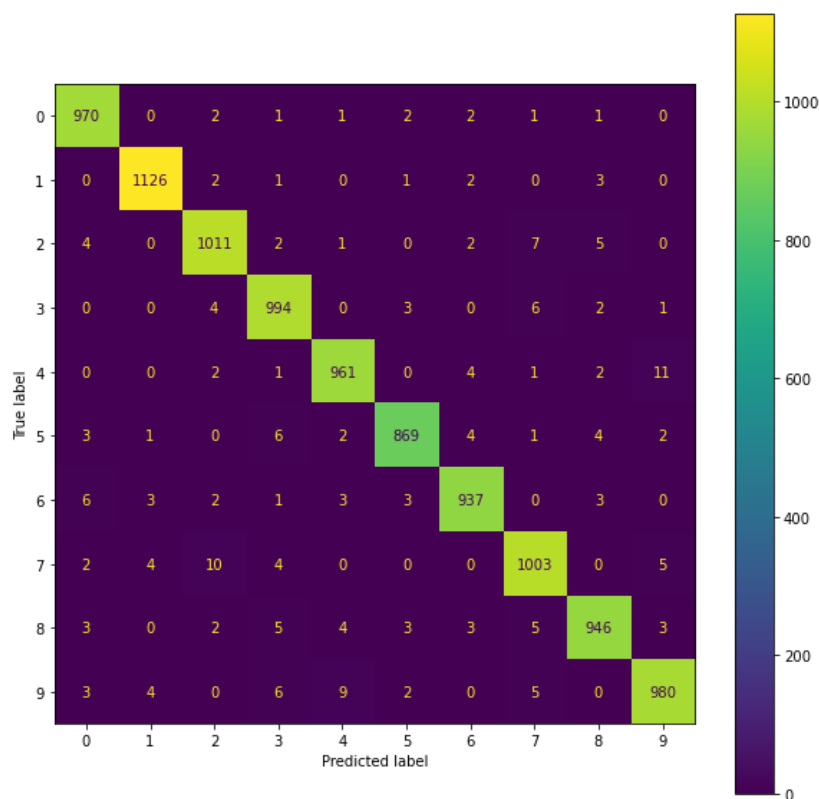
**Model:**

- Activation function: sigmoid
- Neurons: 250
- Dropout: 0.5
- Batch size: 4096
- Epochs: 150

Test score: 0.06945059448480606  
 Test accuracy: 0.9797000288963318



**Figure 8:** ARN-RAW-Plot-sigmoid-softmax-Neur250\_Batch4096\_Dropout\_Epoch150



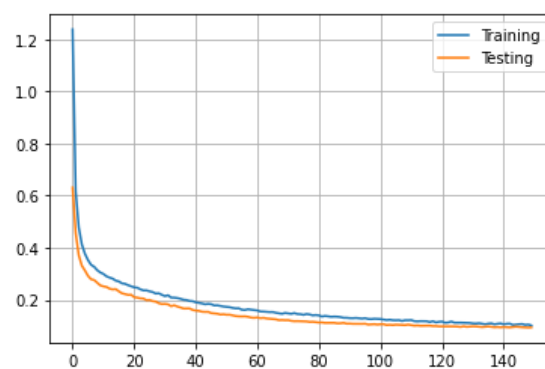
**Figure 9:** ARN-RAW-ConfMax-sigmoid-softmax-Neur250\_Batch4096\_Dropout\_Epoch150

When changing the activation function to sigmoid the errors drop faster, the meeting point is similar to the last graph. The same numbers (4 and 7) are less good classified with two digits boxes.

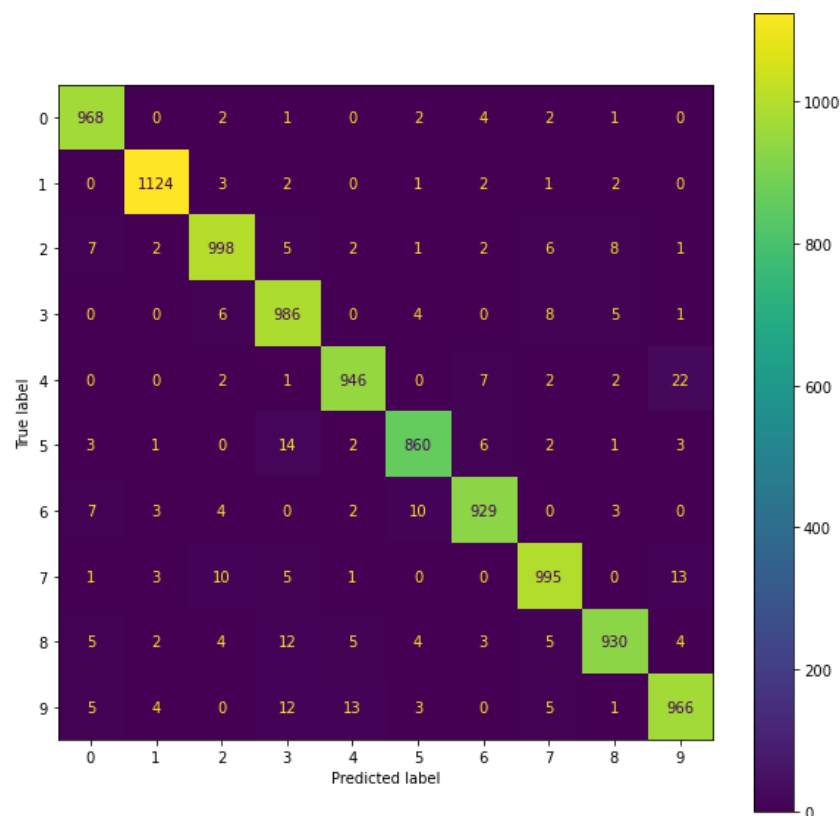
**Model:**

- Activation function: tanh
- Neurons: 150
- Dropout: 0.5
- Batch size: 4096
- Epochs: 150

Test score: 0.09491664171218872  
Test accuracy: 0.9702000021934509



**Figure 10:** ARN-RAW-Plot-tanh-softmax-Neur150\_Batch4096\_Dropout\_Epoch150



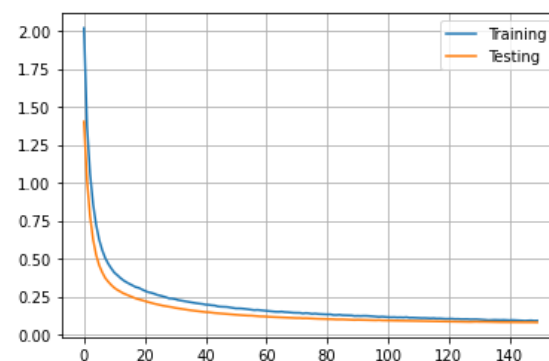
**Figure 11:** ARN-RAW-ConfMat-tanh-softmax-Neur150\_Batch4096\_Dropout\_Epoch150

Setting the number of neurons to 150 changes the moment when the two curves meet. With tanh we see that the testing set is too simple, the testing curve is always below the training one. More epochs are needed to find a stable ground. Too few neurons is not a good idea, it increases the amount of errors. We can see numbers up to 22. This model seems to have more difficulty to classify numbers from 4 to 9.

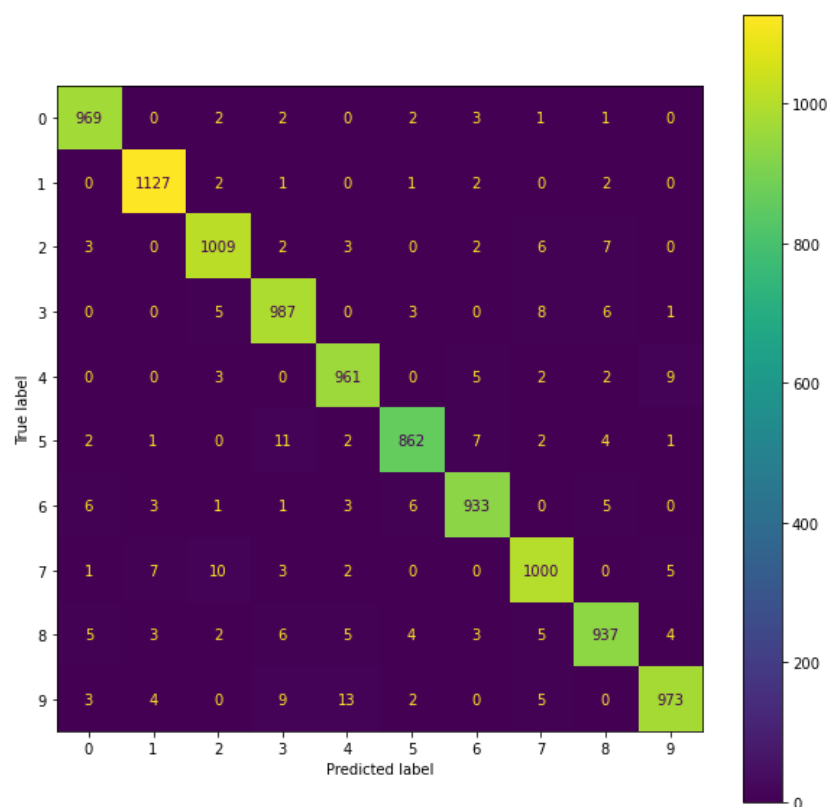
#### Model:

- Activation function: sigmoid
- Neurons: 150
- Dropout: 0.5
- Batch size: 4096
- Epochs: 150

Test score: 0.08042246848344803  
 Test accuracy: 0.9757999777793884



**Figure 12:** ARN-RAW-Plot-sigmoid-softmax-Neur150\_Batch4096\_Dropout\_Epoch150



**Figure 13:** ARN-RAW-ConfMat-sigmoid-softmax-Neur150\_Batch4096\_Dropout\_Epoch150

The result is similar with the sigmoid function, more epochs are needed to find the meeting point. The errors are however less significant than with tanh in the confusion matrix. 4, 5, 7 and 10 are the only numbers with two digits errors.

## Conclusion - RAW

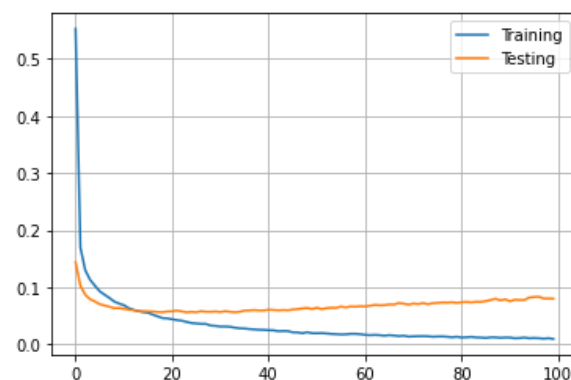
Removing neurons seems to delay the moment when the two curves meet. We didn't find a model that stands out. Some models have a good graph, but some numbers have a 1-2% error in the confusion matrix. When computing the f1\_score we obtained most of the time a score around 0.95 which is good. But this score doesn't really represent the model's behavior. Sometimes the graph clearly shows an overfitting but the f1\_score is 0.97. So when choosing a model we should take everything into account, the graph, the f1-score, the confusion matrix.

MLP\_from\_HOG.ipynb

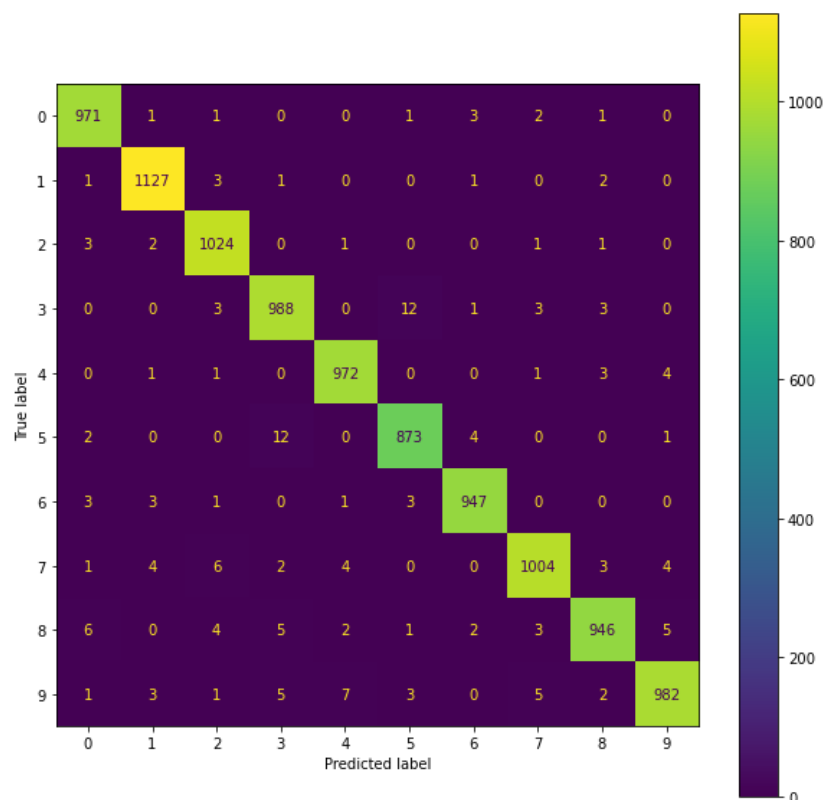
### Model:

- Activation function: relu
- Neurons: 200
- Batch size: 512
- Dropout: 0.5
- Epochs: 100
- Pixels: 4
- Orientations: 8

Test score: 0.08003607392311096  
Test accuracy: 0.9833999872207642



**Figure 14:** ARN-HOG-Plot-relu-softmax-Neur200\_Batch512\_Dropout\_Epoch100



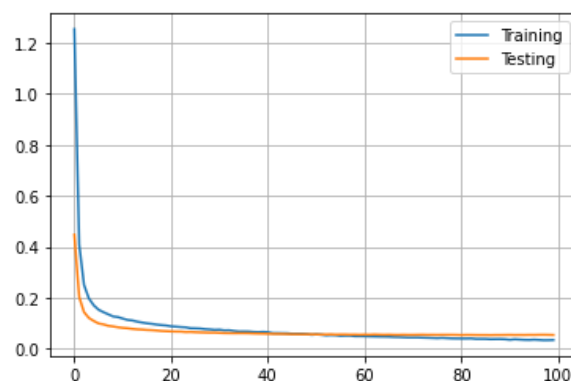
**Figure 15:** ARN-HOG-ConfMat-relu-softmax-Neur200\_Batch512\_Dropout\_Epoch100

We tried to use the preconfigured model but with a batch size of 512 so it could go faster. The scores are not so bad, but the graph shows some overfitting starting from 10 epochs. The confusion matrix shows that number 3 is often assimilated as a 5 and number 5 as a 3. Those are the only values that strike out.

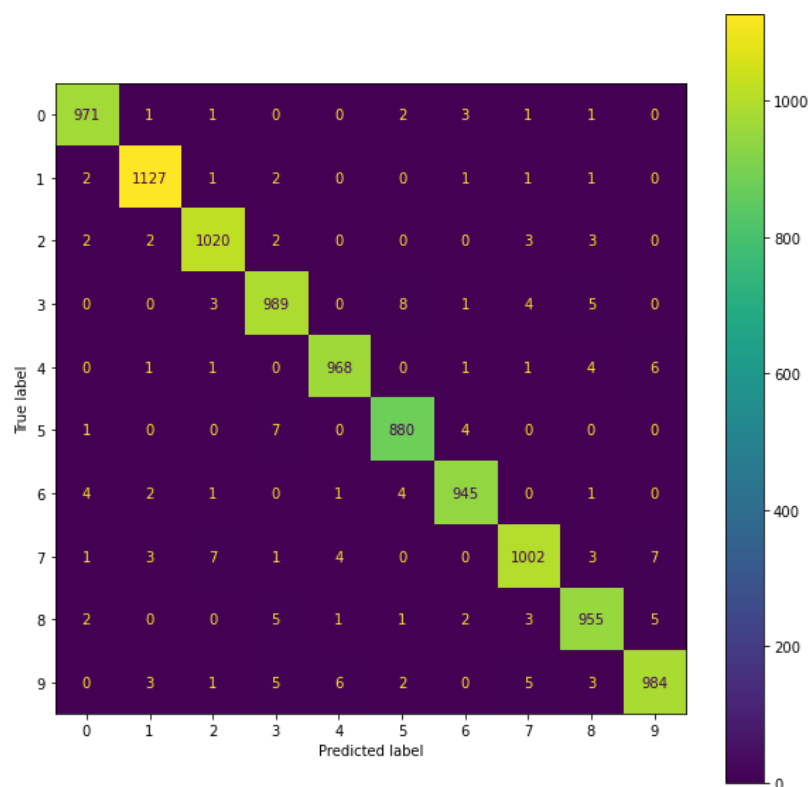
#### Model:

- Activation function: sigmoid
- Neurons: 200
- Batch size: 512
- Dropout: 0.5
- Epochs: 100
- Pixels: 4
- Orientations: 8

Test score: 0.05404368415474892  
 Test accuracy: 0.9840999841690063



**Figure 16:** ARN-HOG-Plot-sigmoid-softmax-Neur200\_Batch512\_Dropout\_Epoch100



**Figure 17:** ARN-HOG-ConfMat-sigmoid-softmax-Neur200\_Batch512\_Dropout\_Epoch100

We decided to try different activation functions with the preconfigured model. This one shows the sigmoid function. As we can see this one behaves better than the previous and there's almost no overfitting. However we can see that the testing error is below the testing error until around 50 epochs

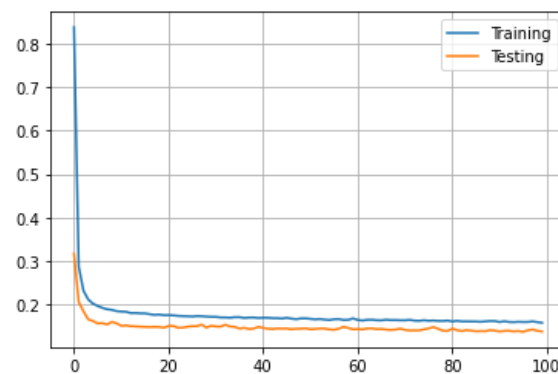


which might signify that the test set is a little bit too easy. The confusion matrix doesn't indicate any abnormalities.

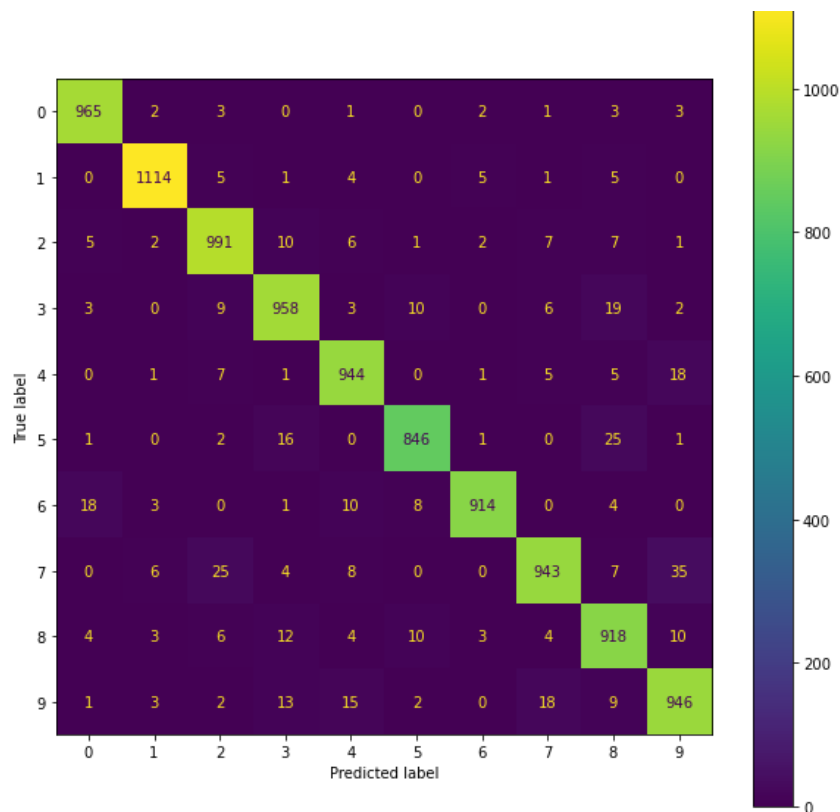
**Model:**

- Activation function: tanh
- Neurons: 200
- Batch size: 512
- Dropout: 0.5
- Epochs: 100
- Pixels: 7
- Orientations: 8

Test score: 0.13775815069675446  
Test accuracy: 0.9538999795913696



**Figure 18:** ARN-HOG-Plot-tanh-Pixel7\_Neur200\_Batch512\_Dropout\_Epoch100



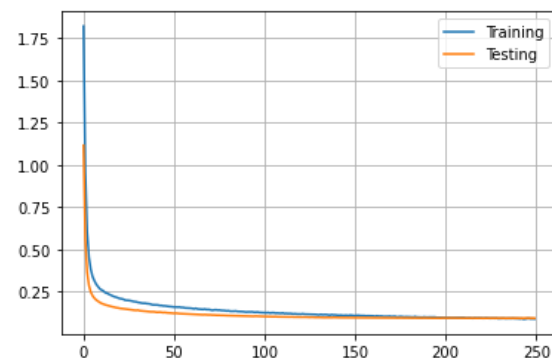
**Figure 19:** ARN-HOG-ConfMat-tanh-Pixel7\_Neur200\_Batch512\_Dropout\_Epoch100

Those previous attempts were done with 4 pixels, we also tried 7 pixels. This example with the tanh function clearly depicts a test set that is too easy. The testing curves never overlaps the training one. We notice that the test score is really bad compared to the previous models. Of course the confusion matrix shows a similar result. This model doesn't seem to recognize the numbers between 2 and 9. In some cases we can see up to 35 wrong classification in one box.

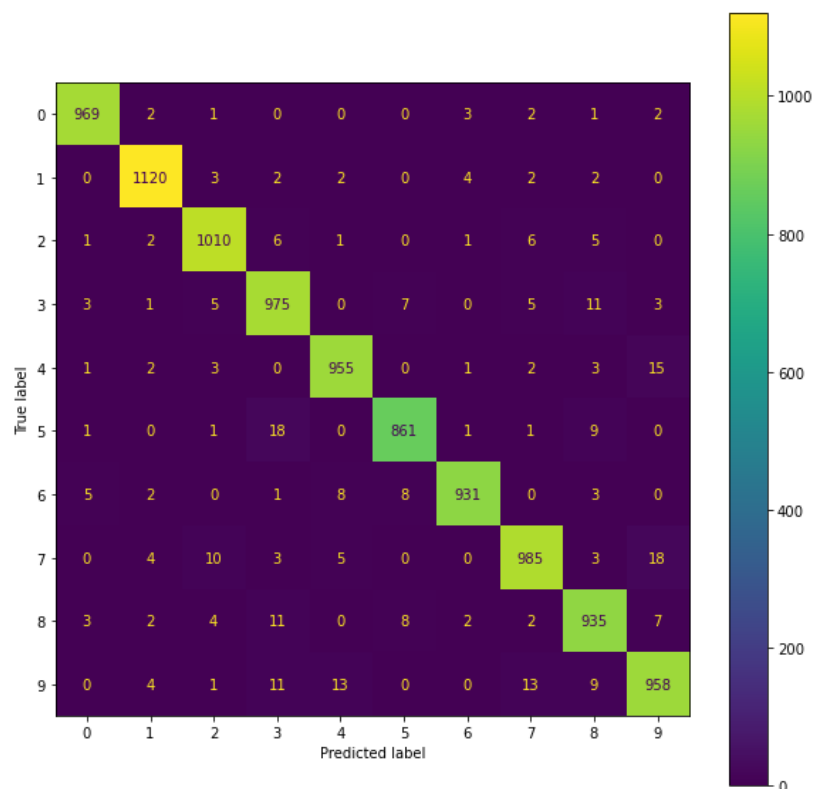
**Model:**

- Activation function: sigmoid
- Neurons: 200
- Batch size: 512
- Dropout: 0.5
- Epochs: 250
- Pixels: 7
- Orientations: 8

Test score: 0.09379129111766815  
 Test accuracy: 0.9699000120162964



**Figure 20:** ARN-HOG-Plot-sigmoid-Pixel7\_Neur200\_Batch512\_Dropout\_Epoch250



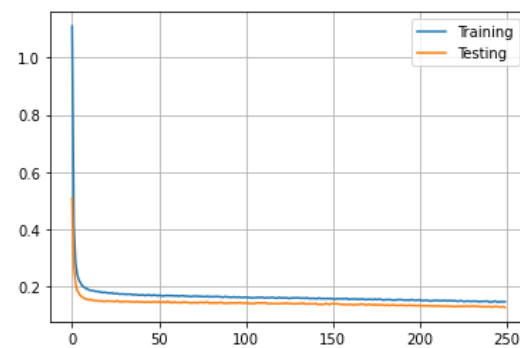
**Figure 21:** ARN-HOG-ConfMat-sigmoid-Pixel7\_Neur200\_Batch512\_Dropout\_Epoch250

By changing the activation function to sigmoid we see a clear improvement with a slightly lower score. The confusion matrix also improved, but those numbers are still too high. We can actually see a value of 30 which is not good.

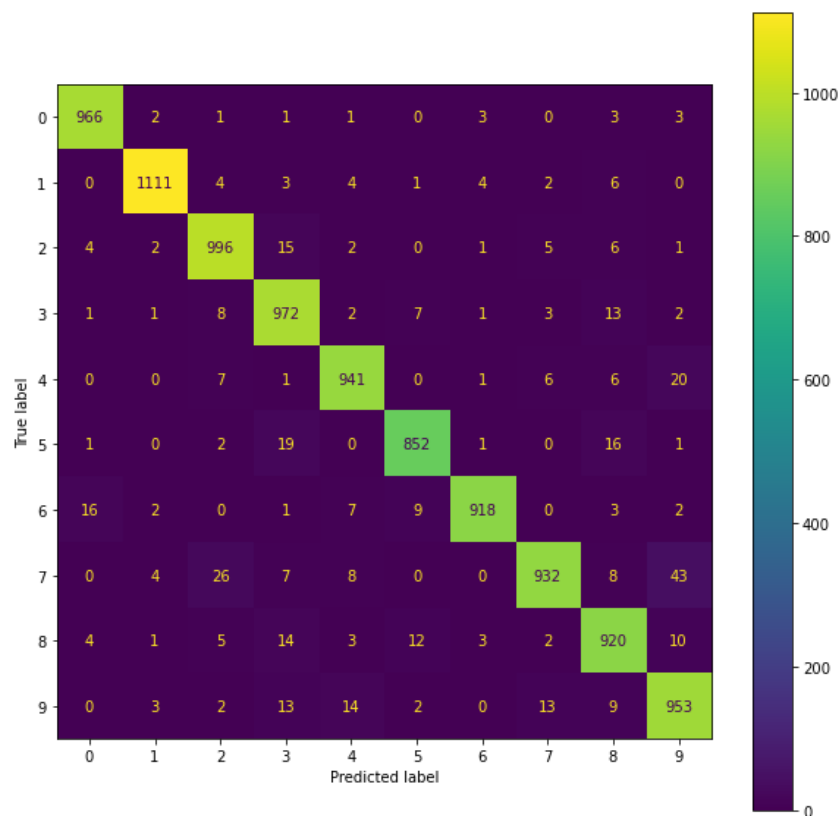
**Model:**

- Activation function: tanh
- Neurons: 200
- Batch size: 1024
- Dropout: 0.5
- Epochs: 250
- Pixels: 7
- Orientations: 8

Test score: 0.1260688304901123  
Test accuracy: 0.9575999975204468



**Figure 22:** ARN-HOG-Plot-tanh-Pixel7\_Neur200\_Batch1024\_Dropout\_Epoch250

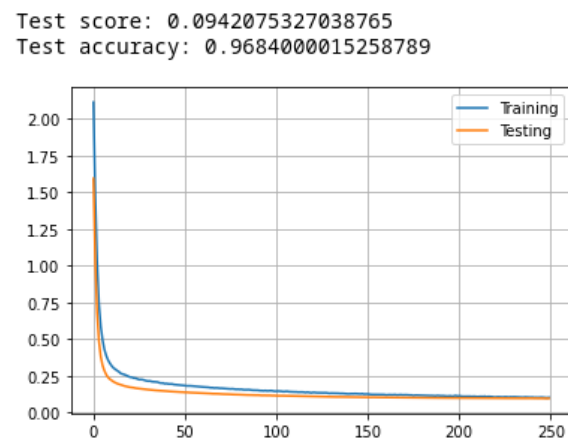


**Figure 23:** ARN-HOG-ConfMat-tanh-Pixel7\_Neur200\_Batch1024\_Dropout\_Epoch250

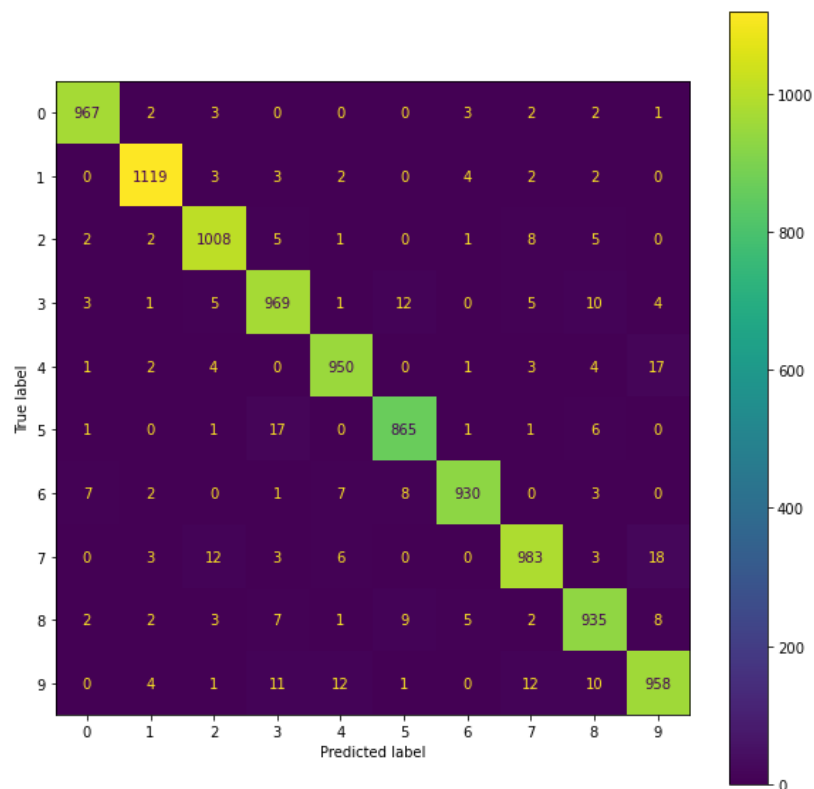
We tried to increase the batch size which improved the curve for tanh activation function and lowered the gap between the two curves. The test set looks still too easy for the model. The confusion matrix shows really bad results. Numbers from 2 to 9 classification generates many errors.

**Model:**

- Activation function: sigmoid
- Neurons: 200
- Batch size: 1024
- Dropout: 0.5
- Epochs: 250
- Pixels: 7
- Orientations: 8



**Figure 24:** ARN-HOG-Plot-sigmoid-Pixel7\_Neur200\_Batch1024\_Dropout\_Epoch250



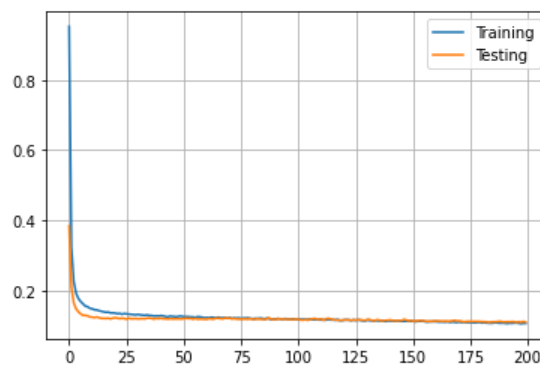
**Figure 25:** ARN-HOG-ConfMat-sigmoid-Pixel7\_Neur200\_Batch1024\_Dropout\_Epoch250

With the sigmoid function the results are the same.

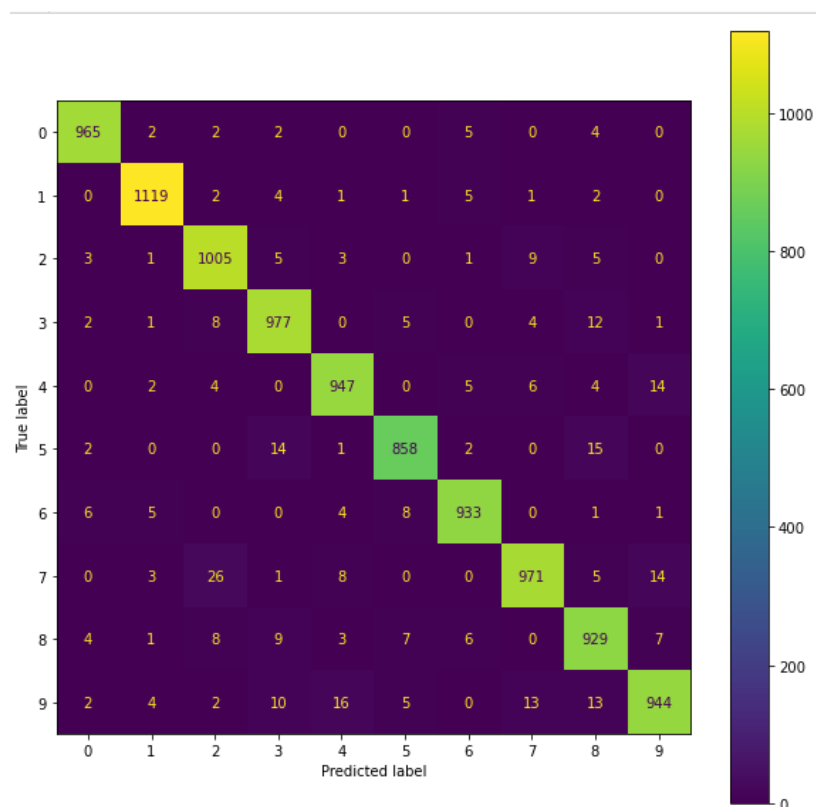
**Model:**

- Activation function: tanh
- Neurons: 200
- Batch size: 1024
- Dropout: 0.5
- Epochs: 200
- Pixels: 7
- Orientations: 16

Test score: 0.10891010612249374  
Test accuracy: 0.9648000001907349



**Figure 26:** ARN-HOG-Plot-tanh-Pixel7\_Or16\_Neur200\_Batch1024\_Dropout\_Epoch200



**Figure 27:** ARN-HOG-ConfMat-tanh-Pixel7\_Or16\_Neur200\_Batch1024\_Dropout\_Epoch200

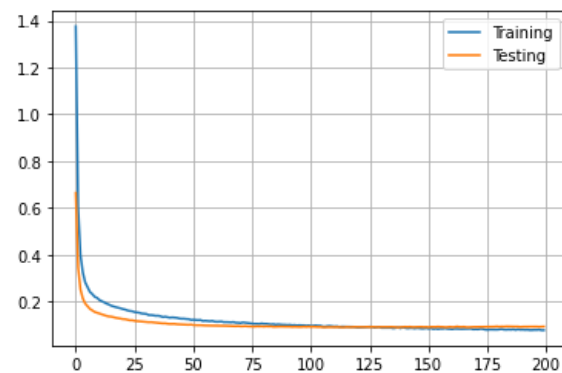
Changing the number of orientations to 16 changed the curves with tanh function. It looks like a really good model because the curves are overlapping the entire time. Again, the confusion matrix shows something we couldn't see with the graph. This model is not really good at predicting what number it sees.

**Model:**

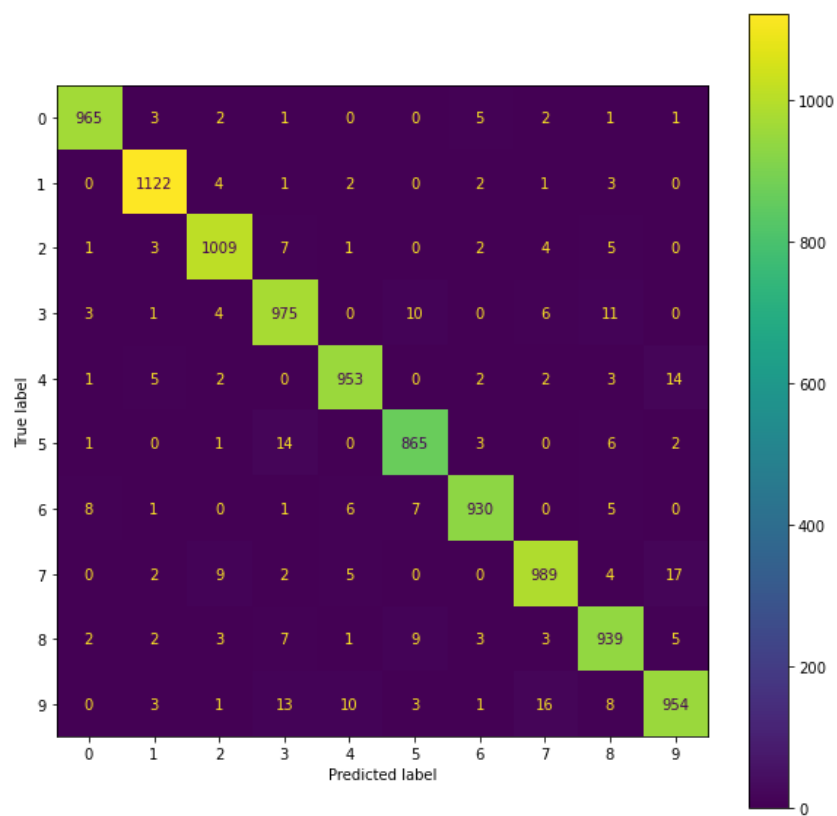
- Activation function: relu
- Neurons: 150
- Batch size: 1024
- Dropout: 0.5
- Epochs: 200
- Pixels: 7
- Orientations: 8



Test score: 0.09441999346017838  
Test accuracy: 0.9700999855995178



**Figure 28:** ARN-HOG-Plot-relu-Pixel7\_Or8\_Neur150\_Batch1024\_Dropout\_Epoch200



**Figure 29:** ARN-HOG-ConfMat-relu-Pixel7\_Or8\_Neur150\_Batch1024\_Dropout\_Epoch200

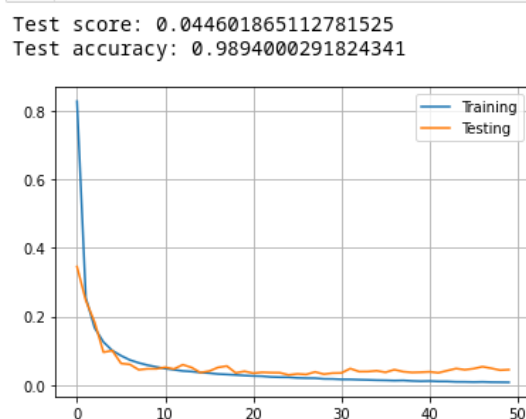
## Conclusion - HOG

We performed various tests and modified every parameter, we didn't find the perfect model. As we can see in most confusion matrices, the models tend to have difficulties with classifying numbers between 2 and 9. We see some values that stick out, such as 10, 22, 30, etc. The model {sigmoid, 200 neurons, 512 batch size, 0.5 dropout, 4 pixels, 9 orientations, 100 epochs} is quite good and it has the lowest amount of wrong classifications. The two curves meet at around 50 epochs which is pretty early compared to the other ones. In every graph we can see that the test curve is always below the training one. This shows that the test set might be too easy. The f1\_scores we computed were good and around 0.95. As stated in the RAW part, we think the f1\_score is not sufficient to determine if a model is good.

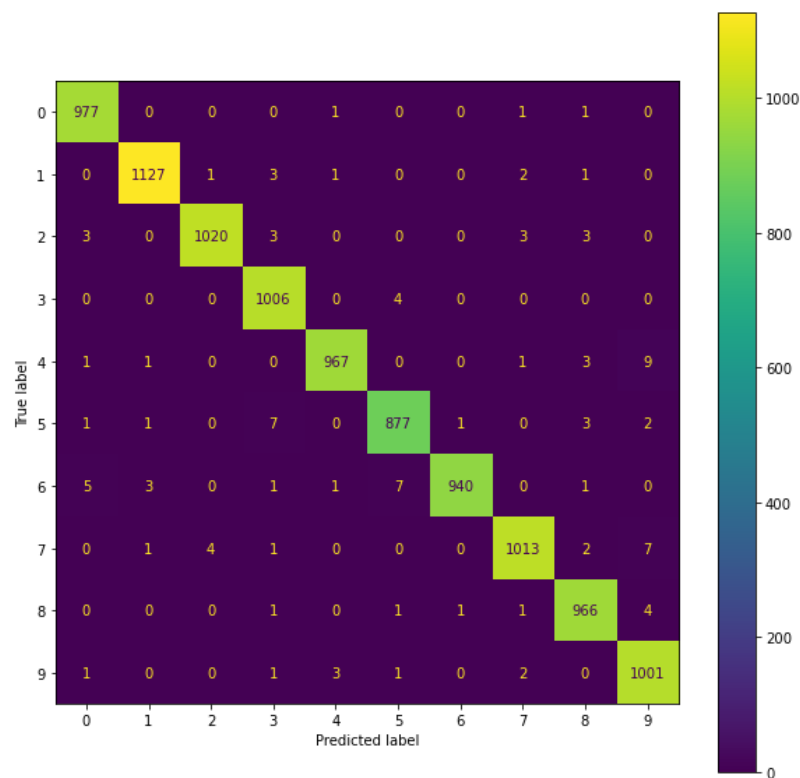
CNN.ipynb

### Model:

- L4 neurons: 25
- L4 activation function: Relu
- Batch size: 2048
- Epochs: 50



**Figure 30:** ARN-CNN-Plot-relu-Batch256\_25L4\_Epoch50

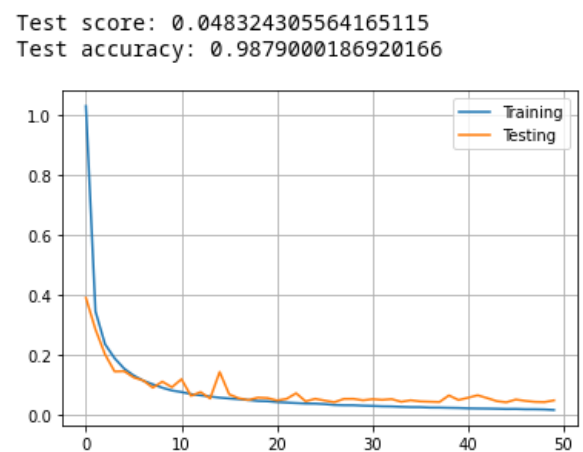


**Figure 31:** ARN-CNN-ConfMat-relu-Batch256\_25L4\_Epoch50

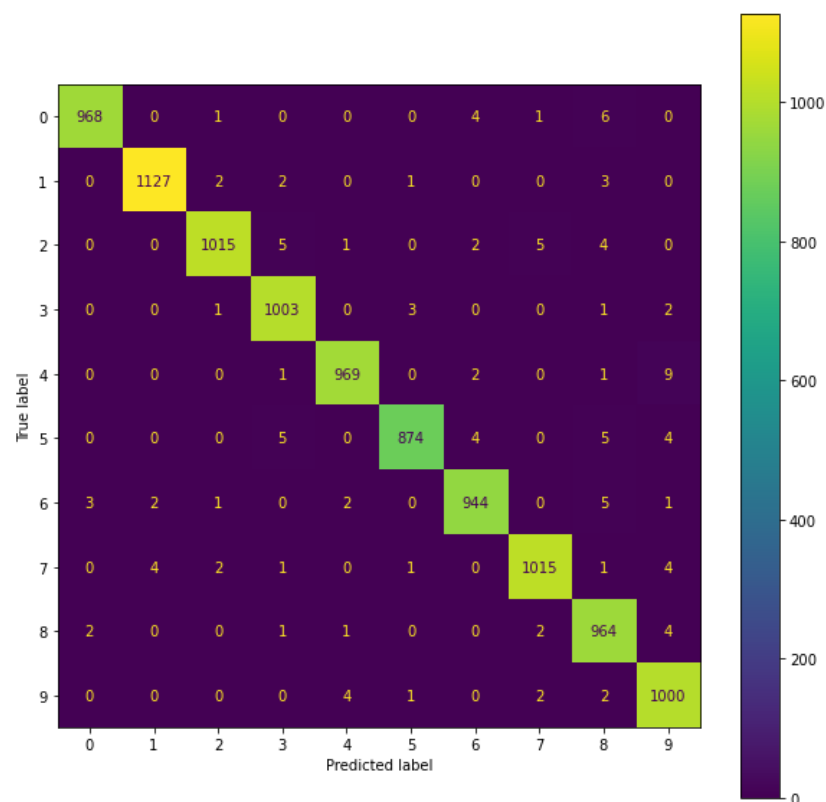
As we can see, the results with this preconfigured model are not that bad. The score is low and the accuracy is close to 1.0. However, from 10 epochs this model slowly starts to overfit. We can clearly see the gap between the training error and the testing error increases as we continue to iterate through the epochs.

**Model:**

- L4 neurons: 10
- L4 activation function: Relu
- Batch size: 2048
- Epochs: 50



**Figure 32:** ARN-CNN-Plot-relu-Batch256\_10L4\_Epoch50



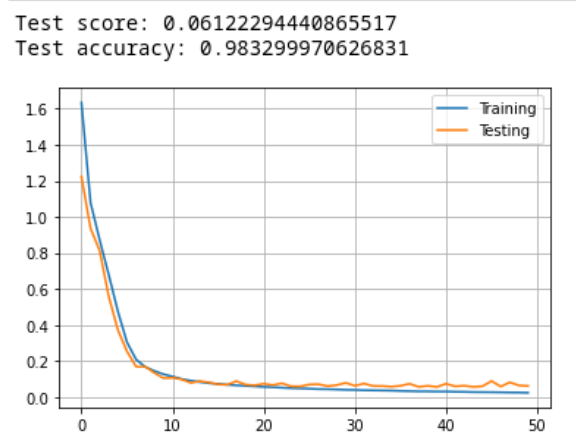
**Figure 33:** ARN-CNN-ConfMat-relu-Batch256\_10L4\_Epoch50

We tried to decrease the number of neurons in the L4 layer. The scores are quiet similar to the previous model, but the testing error fluctuates more especially from the start to around 25 epochs. There's still

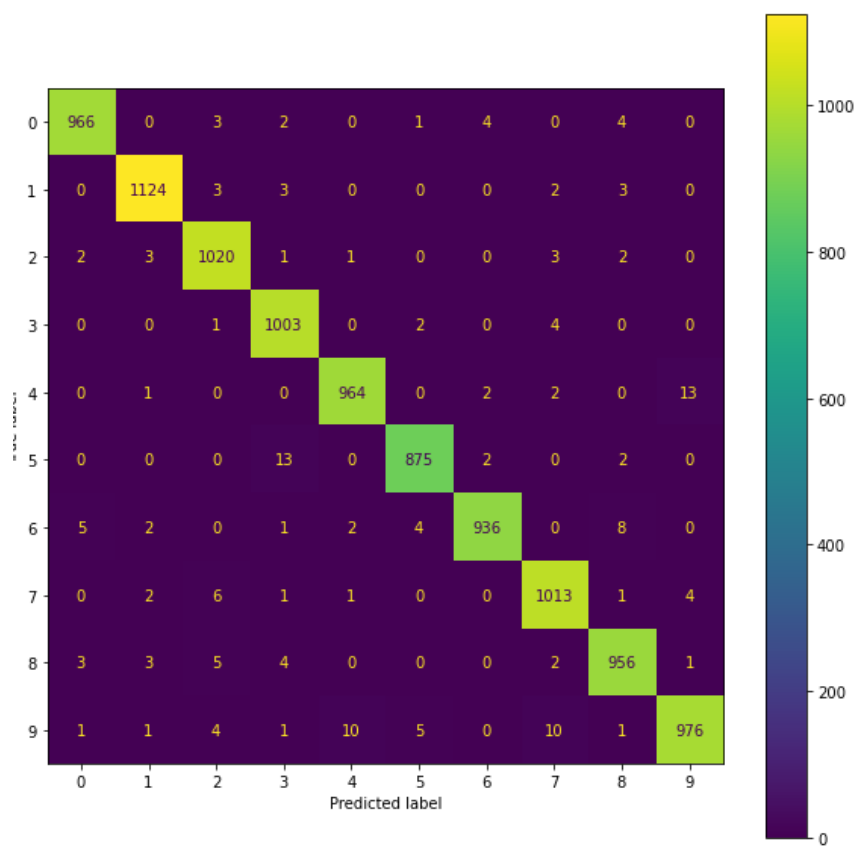
a small overfitting but the curves seem to be stable.

**Model:**

- L4 neurons: 5
- L4 activation function: Relu
- Batch size: 2048
- Epochs: 50



**Figure 34:** ARN-CNN-Plot-relu-Batch256\_5L4\_Epoch50

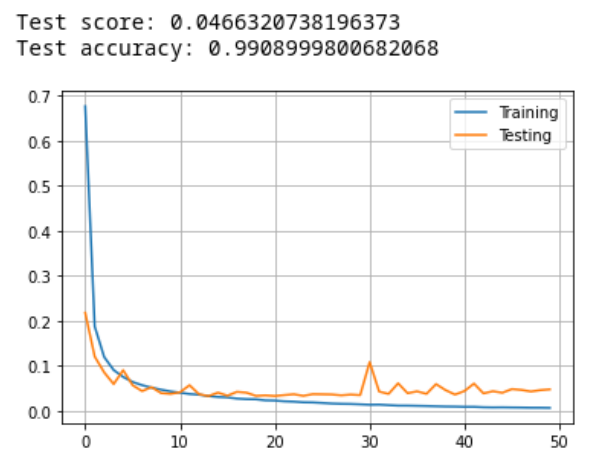
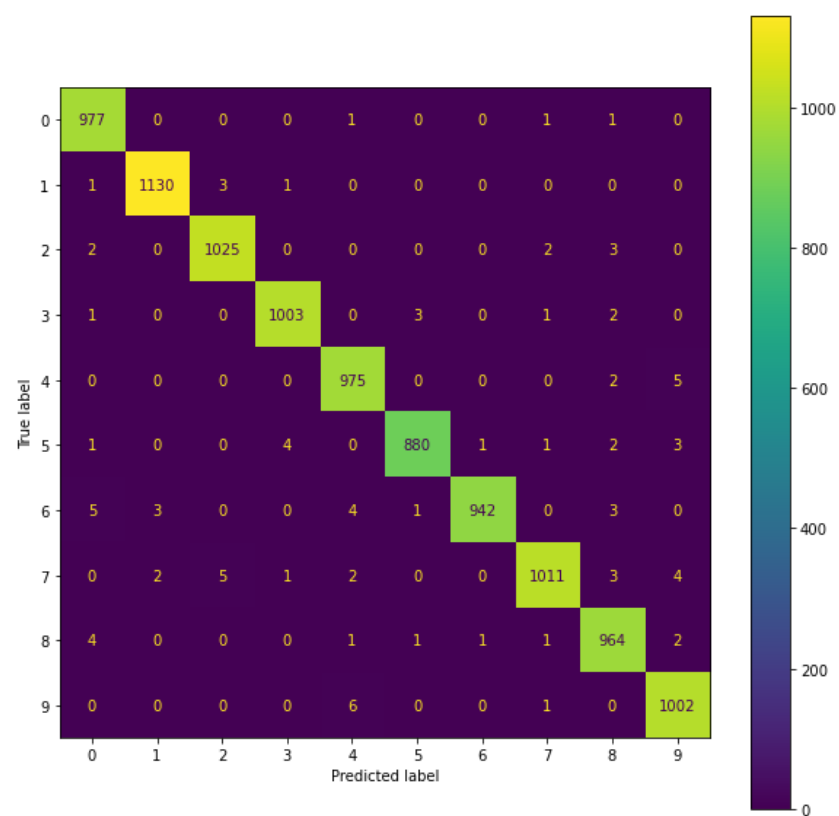


**Figure 35:** ARN-CNN-ConfMat-relu-Batch256\_5L4\_Epoch50

Here we tried an extremely low number of neurons in the L4 layer. The result is pretty good. The score is a little bit higher than the first model tested, but the two curves are almost overlapping the entire time. It looks like a good model. The confusion matrix shows that the number 4, 5 and 9 are quiet often wrongly classified.

**Model:**

- L4 neurons: 35
- L4 activation function: Relu
- Batch size: 2048
- Epochs: 50

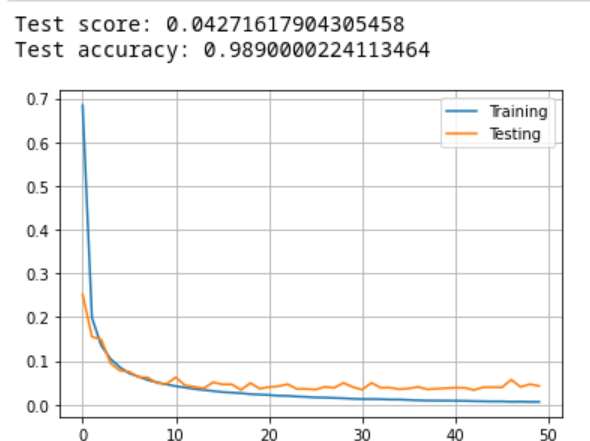
**Figure 36:** ARN-CNN-Plot-relu-Batch256\_35L4\_Epoch50**Figure 37:** ARN-CNN-ConfMat-relu-Batch256\_35L4\_Epoch50

We then chose a high number of neurons to see how the model reacts. It's definitely not a good model

and 35 neurons is probably a bit too much for this task. There's an overfitting starting at 20 epochs. Surprisingly (or not), despite our bad curves the accuracy is the best we've had. The confusion matrix doesn't show a lot, the classification is not so bad.

**Model:**

- L4 neurons: 25
- L4 activation function: tanh
- Batch size: 2048
- Epochs: 50



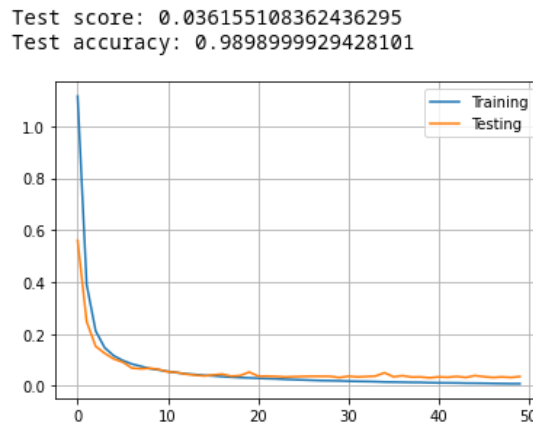
**Figure 38:** ARN-CNN-Plot-tanh-Batch256\_25L4\_Epoch50

We also wanted to see how the preconfigured model would behave when changing the activation function in layer 4. This one uses tanh and we can clearly see it overfits directly at 10 epochs, maybe it's just bad luck and after tweaking some parameters it will probably show something good, but we didn't try since we were told just to change the number of neurons in the feed-forward part.

**Model:**

- L4 neurons: 25
- L4 activation function: sigmoid
- Batch size: 2048
- Epochs: 50





**Figure 39:** ARN-CNN-Plot-sigmoid-Batch256\_25L4\_Epoch50

With sigmoid the score is really low, the accuracy close to 1.0 and the curves are overlapping. After 20 epochs the testing error looks like it is going away a bit, but the gap is still really small after 50 epochs. The confusion matrix doesn't show abnormalities, there are few errors here and there, but nothing out of the ordinary.

**##Conclusion - CNN** As we can see lowering the number of neurons in L4 helped us reduce the gap between the testing and training curves with relu activation function. However, when reaching really low numbers like 5, the really low numbers of neurons, the confusion matrix shows something pretty different than the plot. Some numbers are not classified properly such as 4,5 and 9. Sometimes it represents 1-2% of the predictions for one particular numbers. It's not a big deal, but if we need to be really precise, this result is not enough. Other than that the digits are globally correctly classified even when changing the activation function. The f1\_score we computed were around 0.95 with sometimes values up to 0.99.