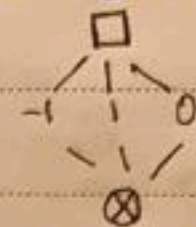


رای آلتیما: برای شروع، $C(s, x, in) = \square$ state $C(n, x, in) = C(n, x, out)$ بقید \otimes اینجا مقداردهی آلتیما \rightarrow اینو میبینیم برای حلقه \otimes loop اینجا

Orderings We can simplify the presentation of the analysis by ordering the values. $\otimes < C < \square \rightarrow$ stands for any possible run time value.

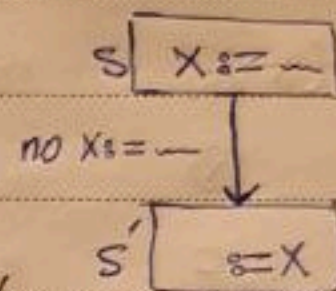


lub: least-upper-bound $lub(1, 2) = \square$ و $lub(\square, \otimes) = \square$, $lub(1, \otimes) = 1$

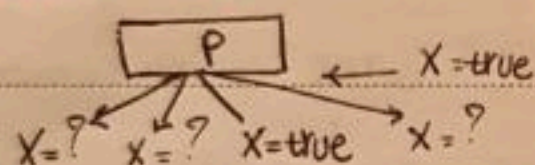
$$C(s, x, in) = lub \{ C(p, x, out) \mid p \text{ is a predecessor of } s \}$$

Live ness A variable x is live at statement s if

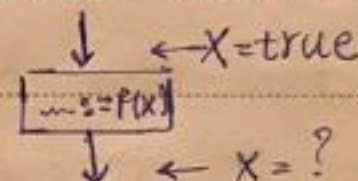
- There exists a statement s' that uses x .
- There is a path from s to s' .
- That path has no intervening assignment to x .



Liveness rule 1



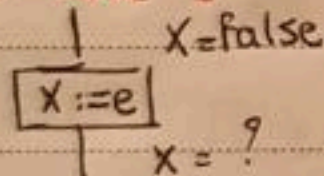
live ness Rule 2



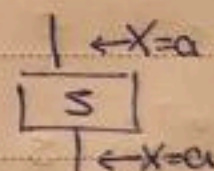
$$L(p, x, out) = \vee \{ L(s, x, in) \mid s \text{ a successor of } p \}$$

$L(s, x, in) = \text{true}$ if s refers to x on the rhs

Liveness Rule 3



Liveness Rule 4



$$L(x := e, x, in) = \text{false} \text{ if } e \text{ does not refer to } x \quad L(s, x, in) = L(s, x, out) \text{ if } s \text{ does not refer to } x.$$

آلتیما: در false باز بعد برین کجا زنده شده از جون جا rule نزن

* liveness is backward analysis.

* if $w = \text{rhs}$ appears in a basic block, w does not appear anywhere else in $\text{prog}^{\text{term}}$.
Then the statement $w = \text{rhs}$ is dead and can be eliminated.

$$\begin{array}{ccccccc} x = z+y & & b = z+y & & b = z+y & & b = z+y \\ a = x & \Rightarrow & a = b & \Rightarrow & a = b & \Rightarrow & x = 2*b \\ x = 2*a & & x = 2*a & & x = 2*b & & \end{array}$$

turn To single assignment form Copy Propagation dead code elimination

Global Data Flow analysis

Global constant Propagation \rightarrow it can be performed at any point where $**$ holds

$(**)$ On every path to the use of x , the last assignment to x is $x = k$

⊗ This statement never executes

c $x = \text{constant } c$

□ x is not a constant

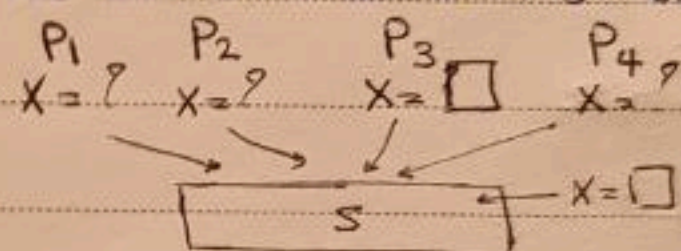
* For each statement S , we compute information about the value of x immediately before and after S . $C(S, x, \text{in}) = \text{value of } x \text{ before } S \text{ is executed.}$

stands for 'constant information' $C(S, x, \text{out}) = \text{value of } x \text{ after } S \text{ is executed.}$

فرض کنیم P_1, \dots, P_n

برهای S باشند

Rule 1



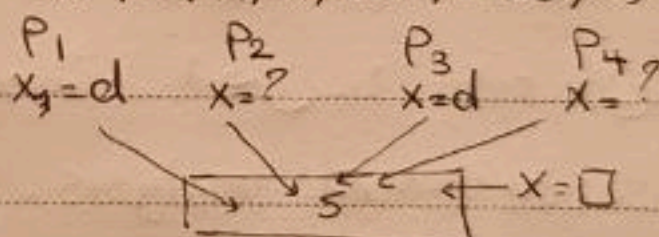
OUT \rightarrow IN

if $\exists i (C(P_i, x, \text{out}) = \square)$, then $C(S, x, \text{in}) = \square$

Rule 3 if $\forall i (C(P_i, x, \text{out}) = c \text{ or } \otimes)$

then $C(S, x, \text{in}) = c$

Rule 2



Rule 4 if $\forall i (C(P_i, x, \text{out}) = \otimes)$

then $C(S, x, \text{in}) = \otimes$

if $\exists i, j (C(P_i, x, \text{out}) = c \ \& \ C(P_j, x, \text{out}) = d \ \& \ c \neq d)$

then $C(S, x, \text{in}) = \square$

IN \rightarrow OUT

Rule 5 if $C(S, x, \text{in}) = \otimes \Rightarrow C(S, x, \text{out}) = \otimes$

Rule 6 if c is constant $\Rightarrow C(x := c, x, \text{out}) = c$

Rule 7 if $f(\dots)$ is anything except a constant $C(x := f(\dots), x, \text{out}) = \square$

Rule 8 if $x \lt y \Rightarrow C(y := \dots, x, \text{out}) = C(y := \dots, x, \text{in})$

PAPCO