



# FruitPunch AI Bootcamp

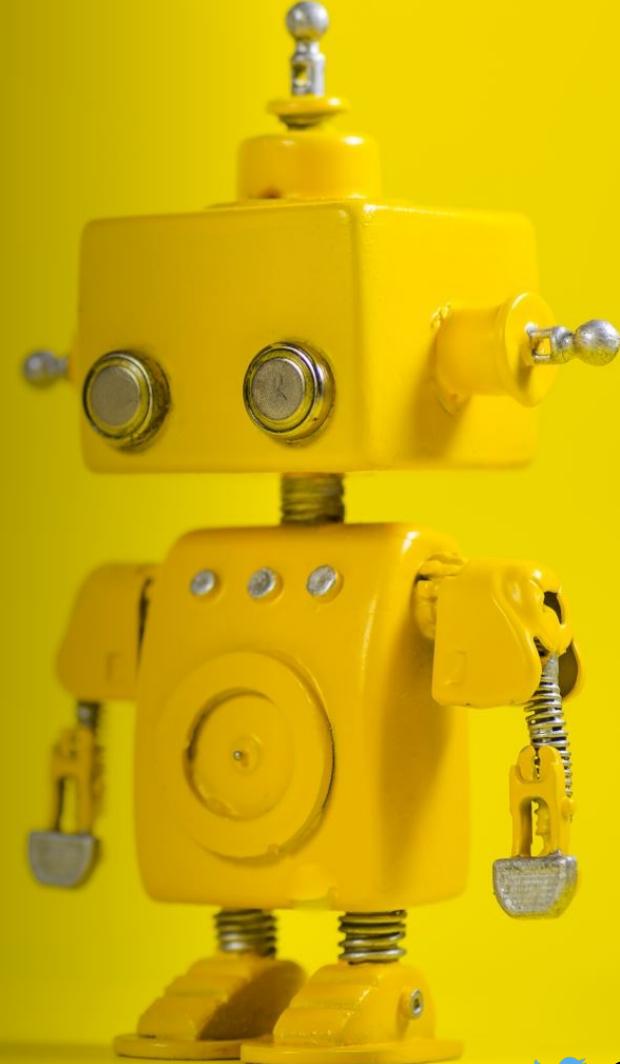
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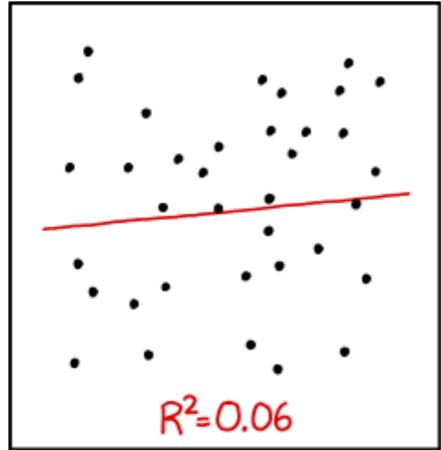
Session 1 – Linear Regression

15.11.2020

M. Alican Noyan

FruitPunch AI & Ipsumio





# What is Machine Learning?



## Challenge 1 Linear regression

scikit  
*learn*

Any ML experience?	50/50
Any ML course?	None/All of them
Stats?	Low/High
Software?	Low/High



45 min



3 hours

## Challenge 2

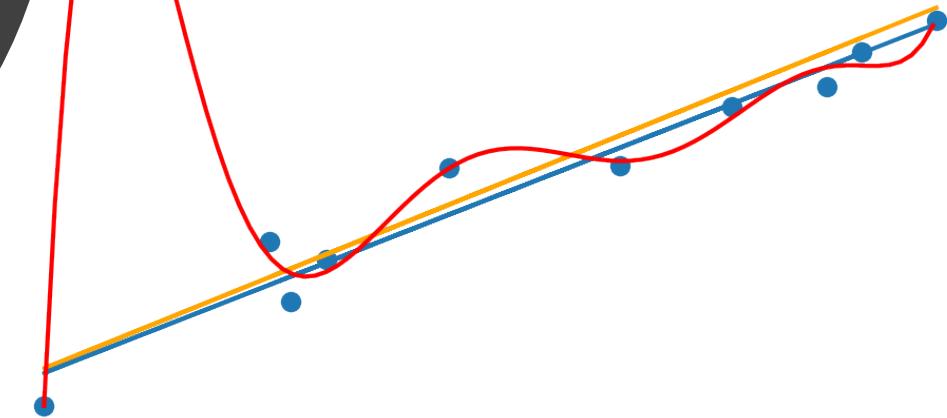
Aleatoric  
Epistemic

## Challenge 4

### Implement Linear regression

$$\theta_j = \theta_j - \alpha \frac{\partial J}{\partial \theta_j}$$

## Challenge 3 Overfitting



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M.Sc. Materials Science and Nanotechnology (Bilkent - Ankara)

Ph.D. Photonics (ICFO - Barcelona)

ipsumio

[www.ipsumio.com](http://www.ipsumio.com)

The screenshot shows the homepage of the journal "Light: Science & Applications". The header includes the journal logo, a search bar, and a login link. Below the header, there are two dropdown menus: "Explore our content" and "Journal information". The main content area displays a navigation path: "nature > light: science & applications > articles > article". A blue horizontal bar separates this from the article details. The article is identified as an "Article | Open Access | Published: 12 February 2020". The title of the article is "An ultra-compact particle size analyser using a CMOS image sensor and machine learning". The authors listed are Rubaiya Hussain, Mehmet Alican Noyan, Getinet Woyessa, Rodrigo R. Retamal Marín, Pedro Antonio Martinez, Faiz M. Mahdi, Vittoria Finazzi, Thomas A. Hazlehurst, Timothy N. Hunter, Tomeu Coll, Michael Stintz, Frans Muller, Georgios Chalkias & Valerio Pruneri. Below the article summary, there is a link to "Light: Science & Applications 9, Article number: 21 (2020)" and a "Cite this article" button. At the bottom, there are links for "5346 Accesses | 4 Citations | 25 Altmetric | Metrics".

The screenshot shows the homepage of the journal "scientific reports". The header includes the journal logo, a search bar, and a login link. Below the header, there are two dropdown menus: "Explore our content" and "Journal information". The main content area displays a navigation path: "nature > scientific reports > articles > article". A blue horizontal bar separates this from the article details. The article is identified as an "Article | Open Access | Published: 27 October 2020". The title of the article is "TzanckNet: a convolutional neural network to identify cells in the cytology of erosive-vesiculobullous diseases". The authors listed are Mehmet Alican Noyan, Murat Durdu & Ali Haydar Eskiocak. Below the article summary, there is a link to "Scientific Reports 10, Article number: 18314 (2020)" and a "Cite this article" button. At the bottom, there are links for "1065 Accesses | 23 Altmetric | Metrics".

# Machine Learning

*Symbolic AI*

Regression	Classification
Diabetes	Digits

• Neural Network  
**Deep Learning**

• Linear Regression

• Random Forest

**Supervised**

## Machine Learning

**Unsupervised**

*Symbolic AI*

ML Research

Applied ML

Data = Signal + Noise



## Challenge 1 Linear regression

scikit  
*learn*

Aleatoric  
Epistemic

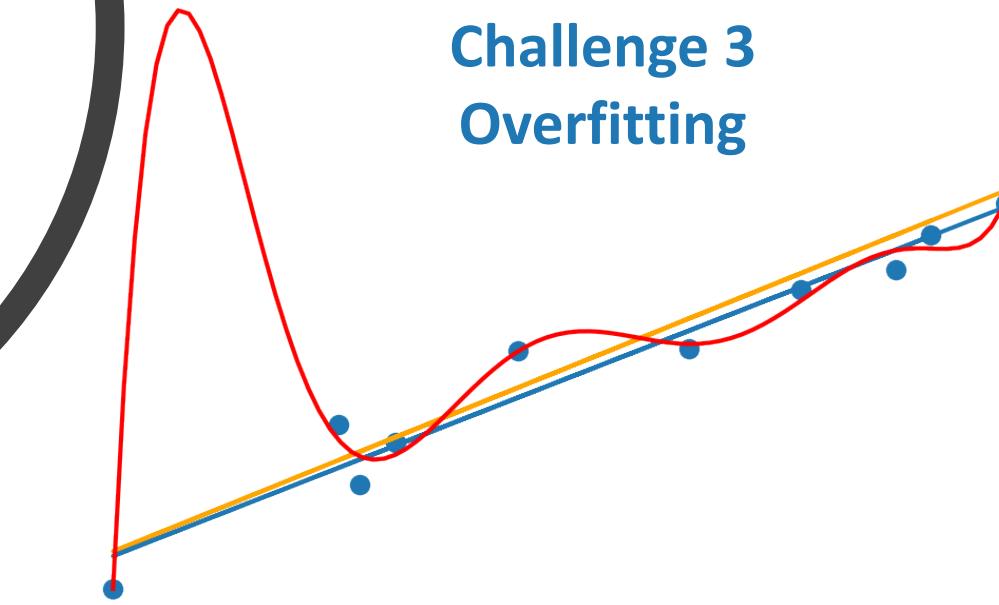
## Challenge 2

## Challenge 4

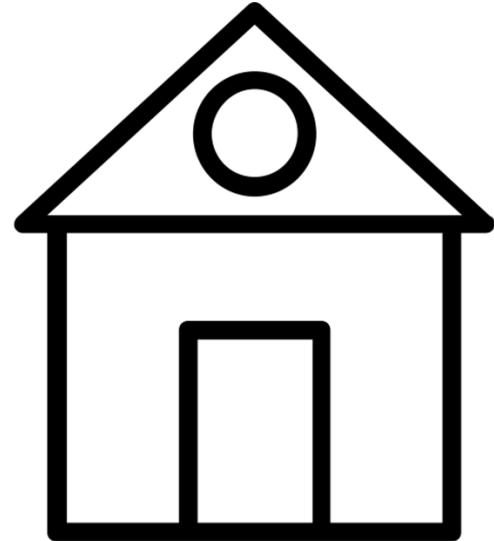
### Implement Linear regression

$$\theta_j = \theta_j - \alpha \frac{\partial J}{\partial \theta_j}$$

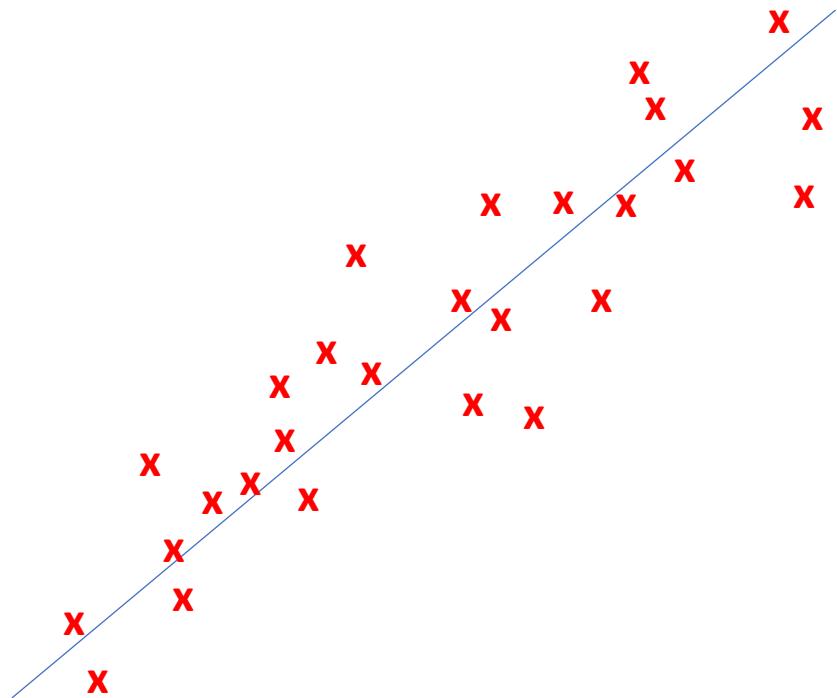
## Challenge 3 Overfitting



# House price prediction



# House price prediction



$m = 27$

Size (m <sup>2</sup> )	Price (€)
40	150,000
45 $x^{(2)}$	170,000 $y^{(2)}$
...	
100	310,000

$n = 1$

$(x^{(i)}, y^{(i)})$



## House price prediction



70

$$y = \theta_0 + \theta_1 \times x$$

m = 27

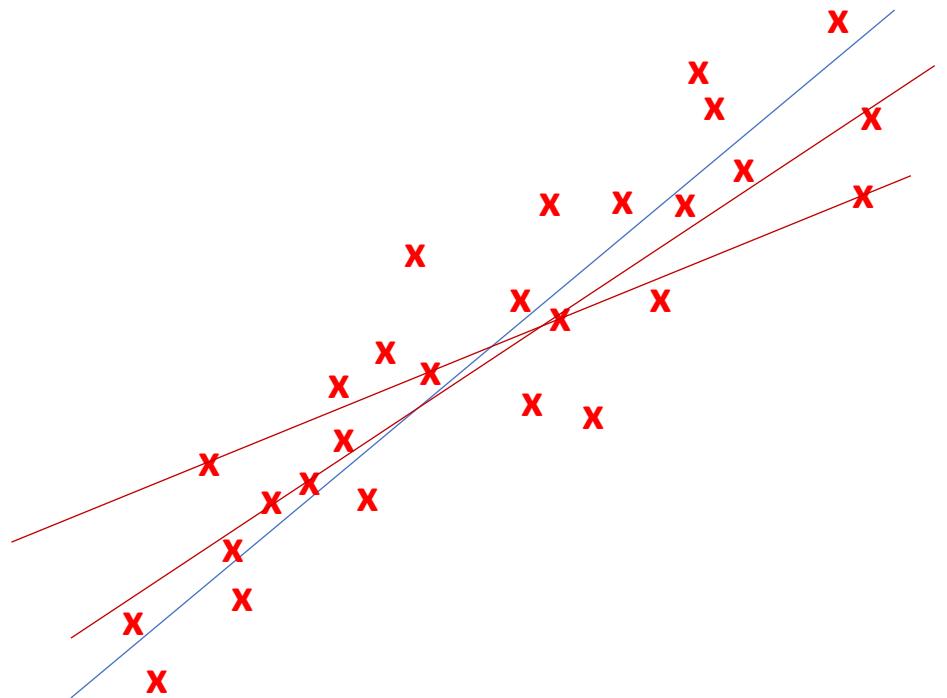


n = 1

Size (m <sup>2</sup> )	Price (€)
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45 <b>x<sup>(2)</sup></b>	170,000 <b>y<sup>(2)</sup></b>
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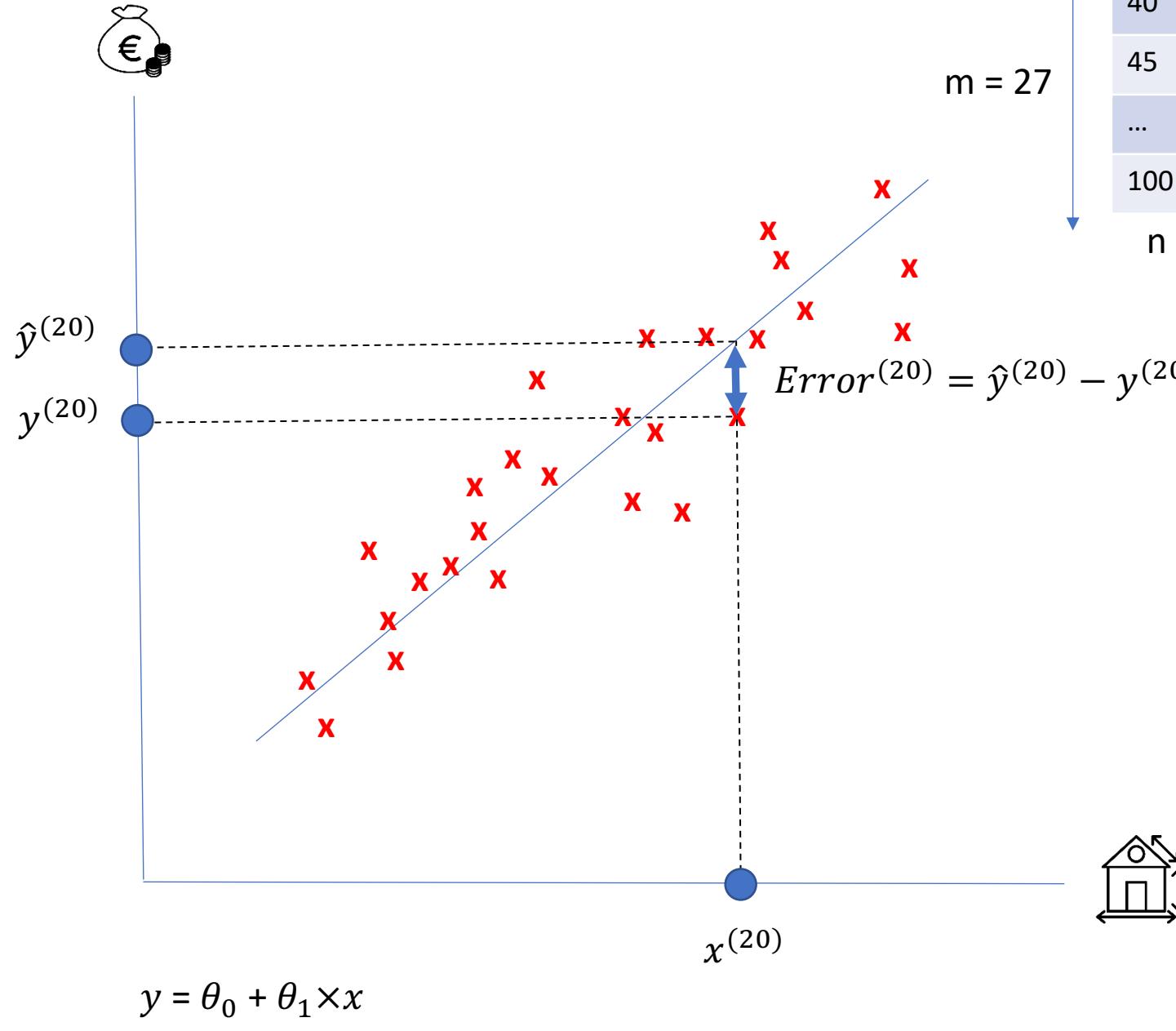
$n = 1$

$(x^{(i)}, y^{(i)})$



$$y = \theta_0 + \theta_1 \times x$$

# House price prediction



Size ( $m^2$ )	Price (€)
40	150,000
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...	
100	310,000

$(x^{(i)}, y^{(i)})$

$$\sum_{i=1}^m (\hat{y}^{(i)} - y^{(i)})$$

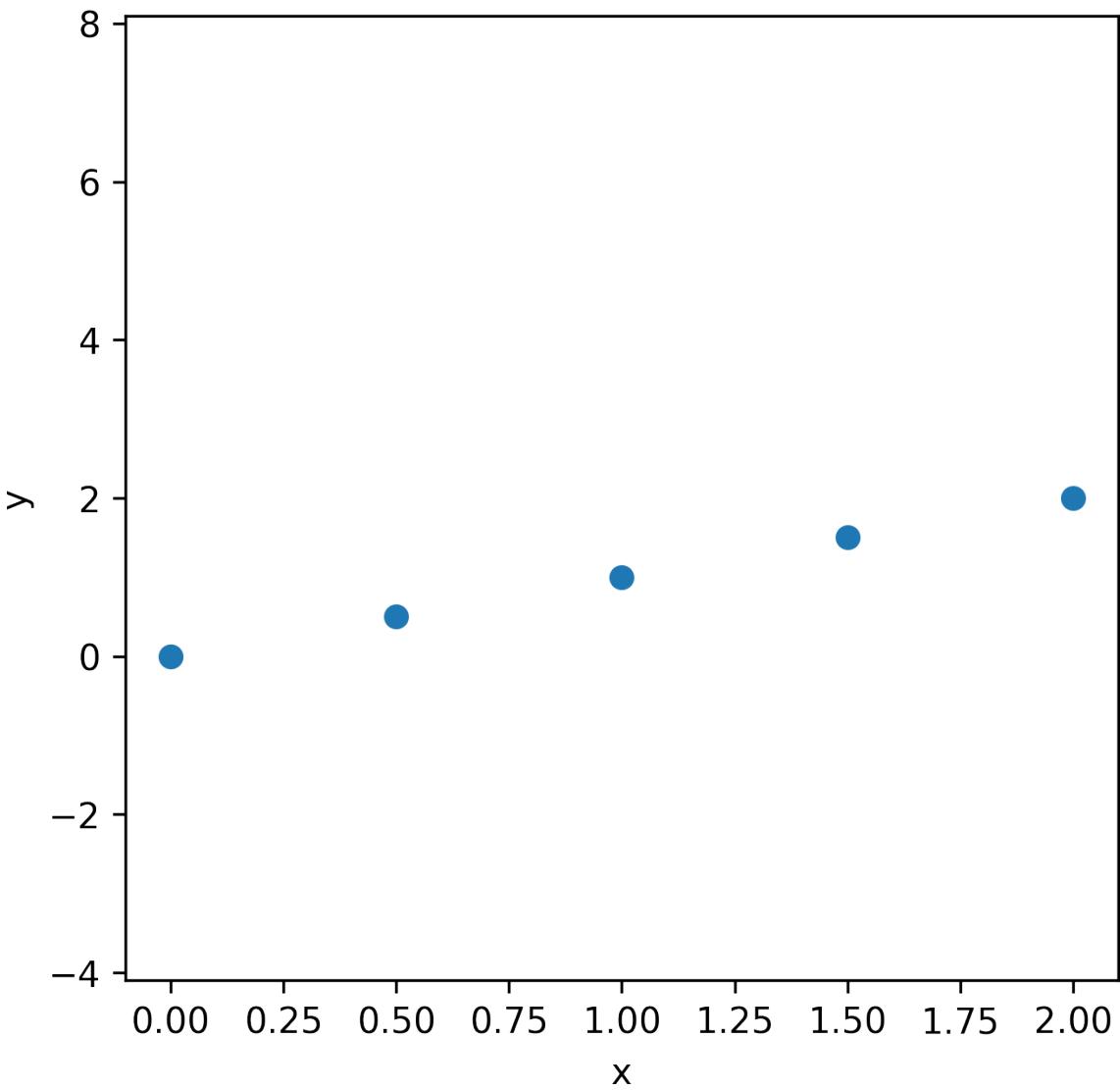
$$\sum_{i=1}^m (\hat{y}^{(i)} - y^{(i)})^2$$

$$\frac{1}{m} \sum_{i=1}^m (\hat{y}^{(i)} - y^{(i)})^2$$

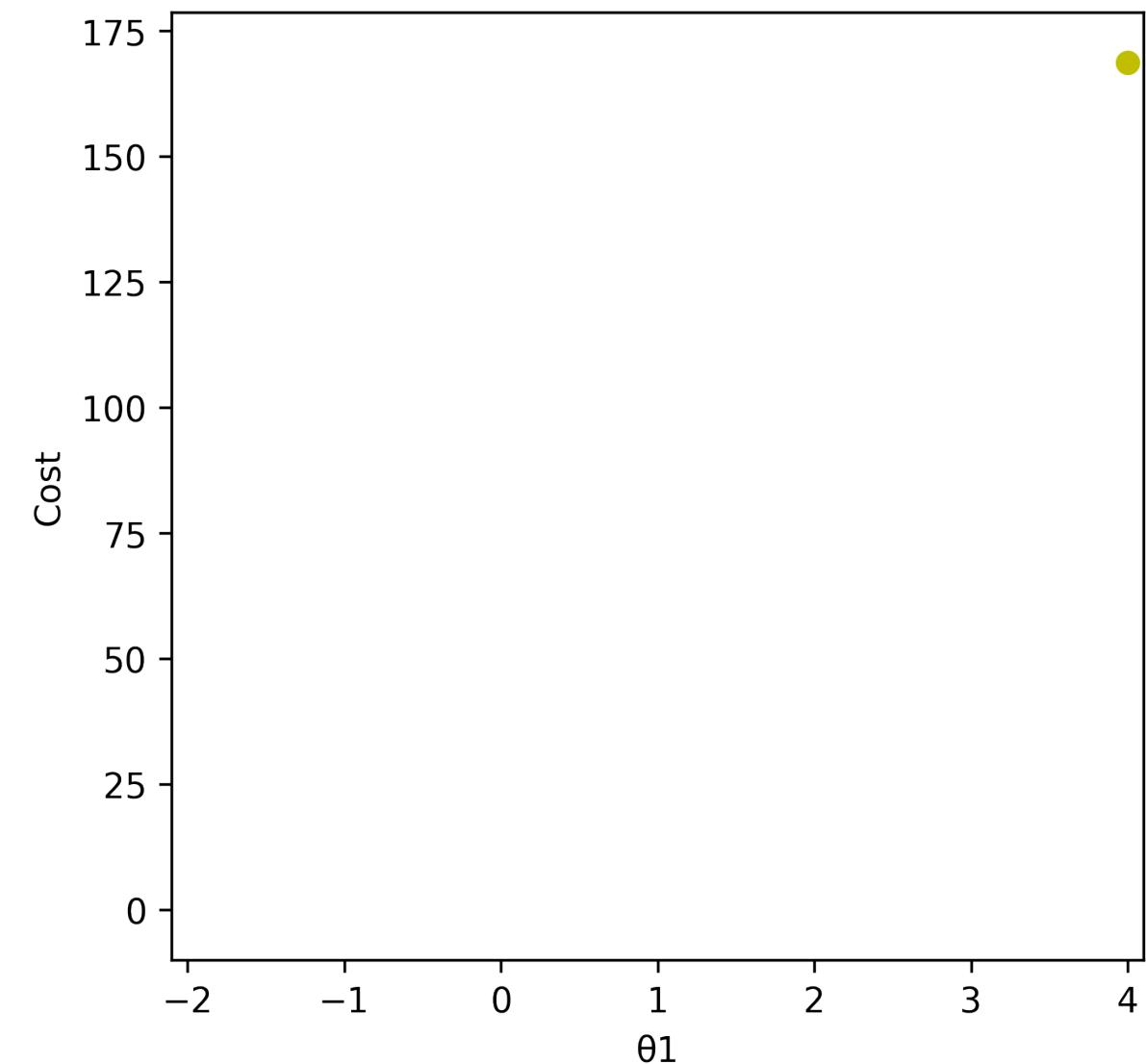
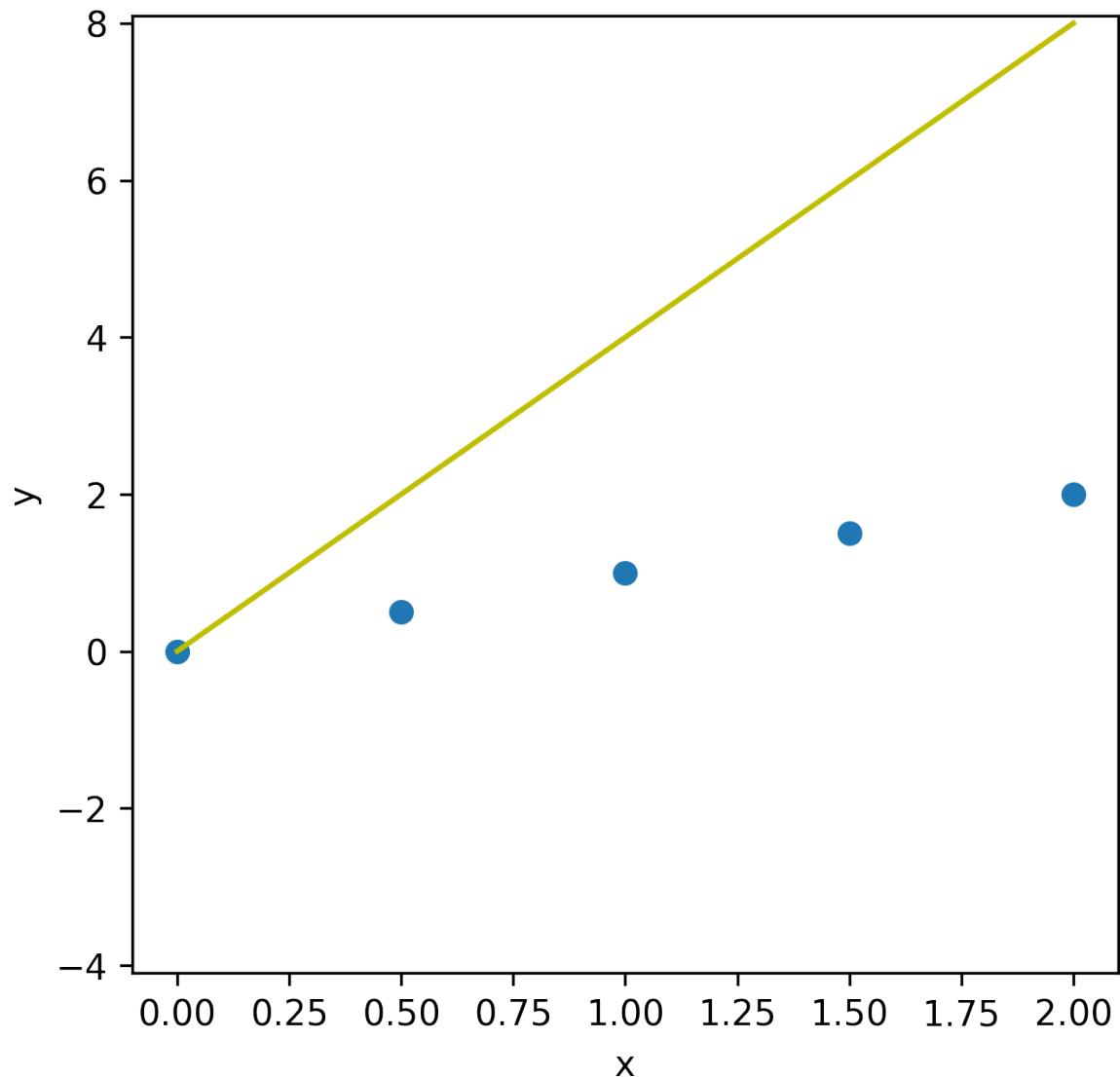
$$\frac{1}{2m} \sum_{i=1}^m (\hat{y}^{(i)} - y^{(i)})^2$$

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)})^2$$

## Minimize a simplified J

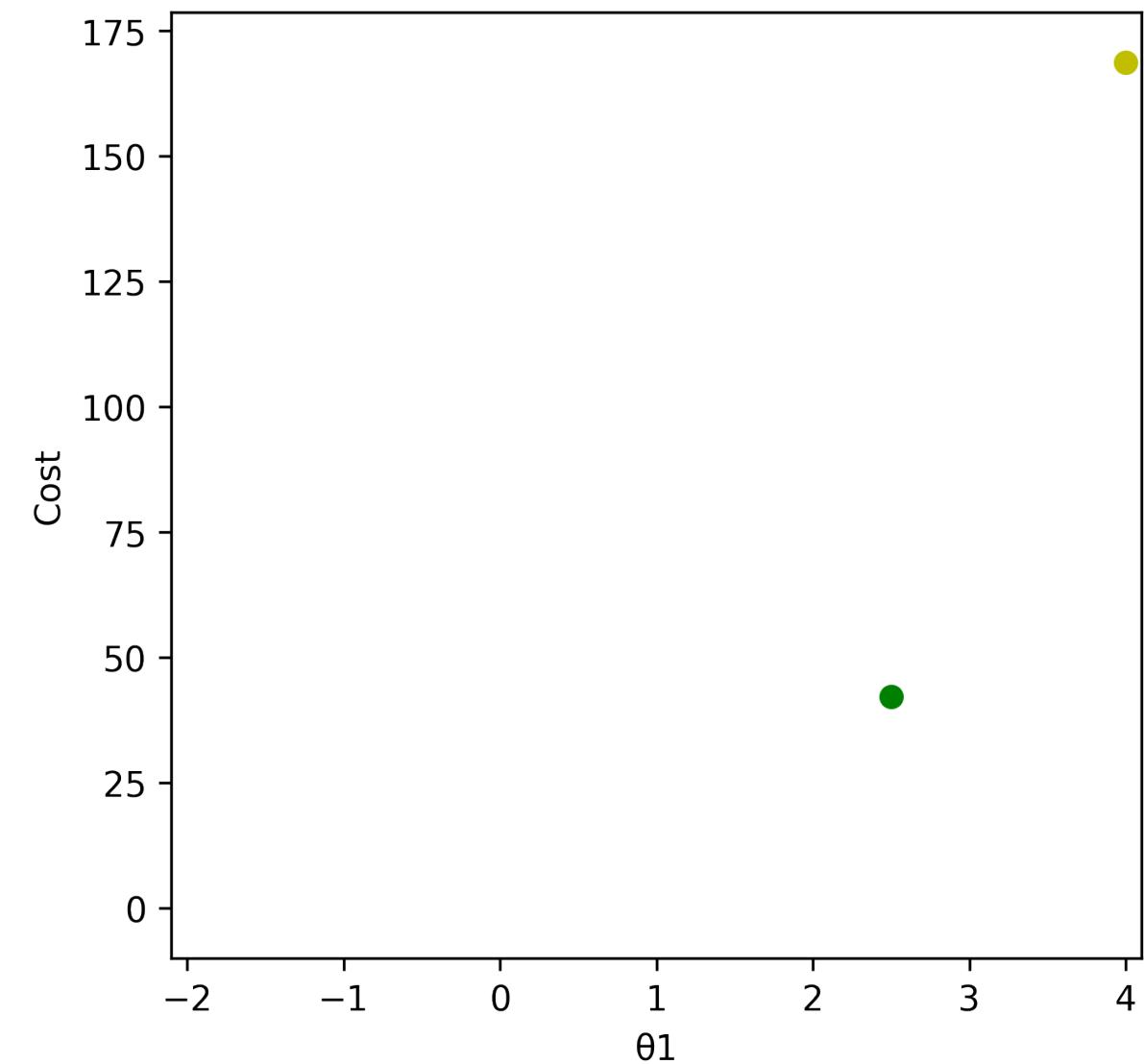
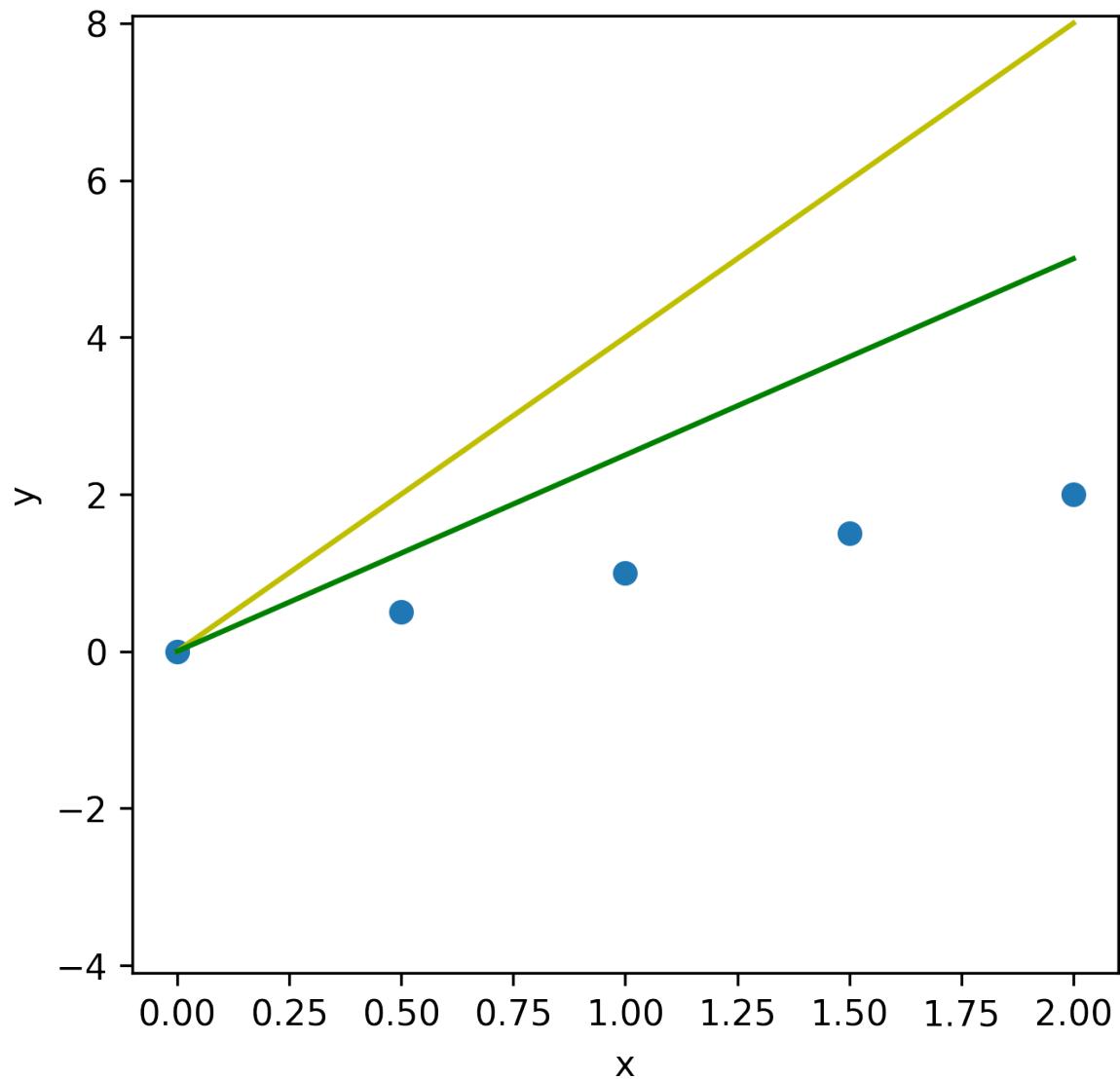


## Minimize a simplified J



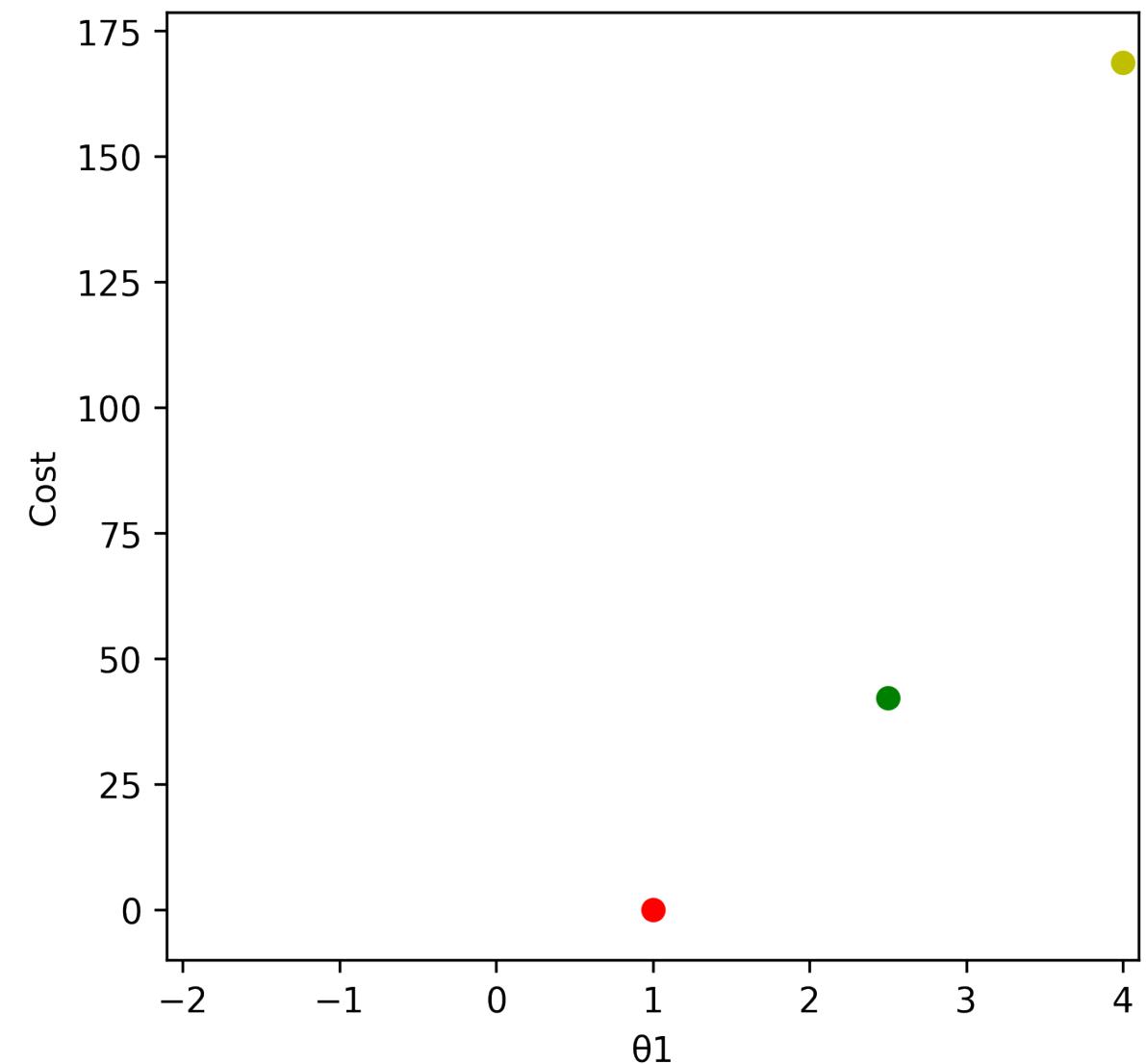
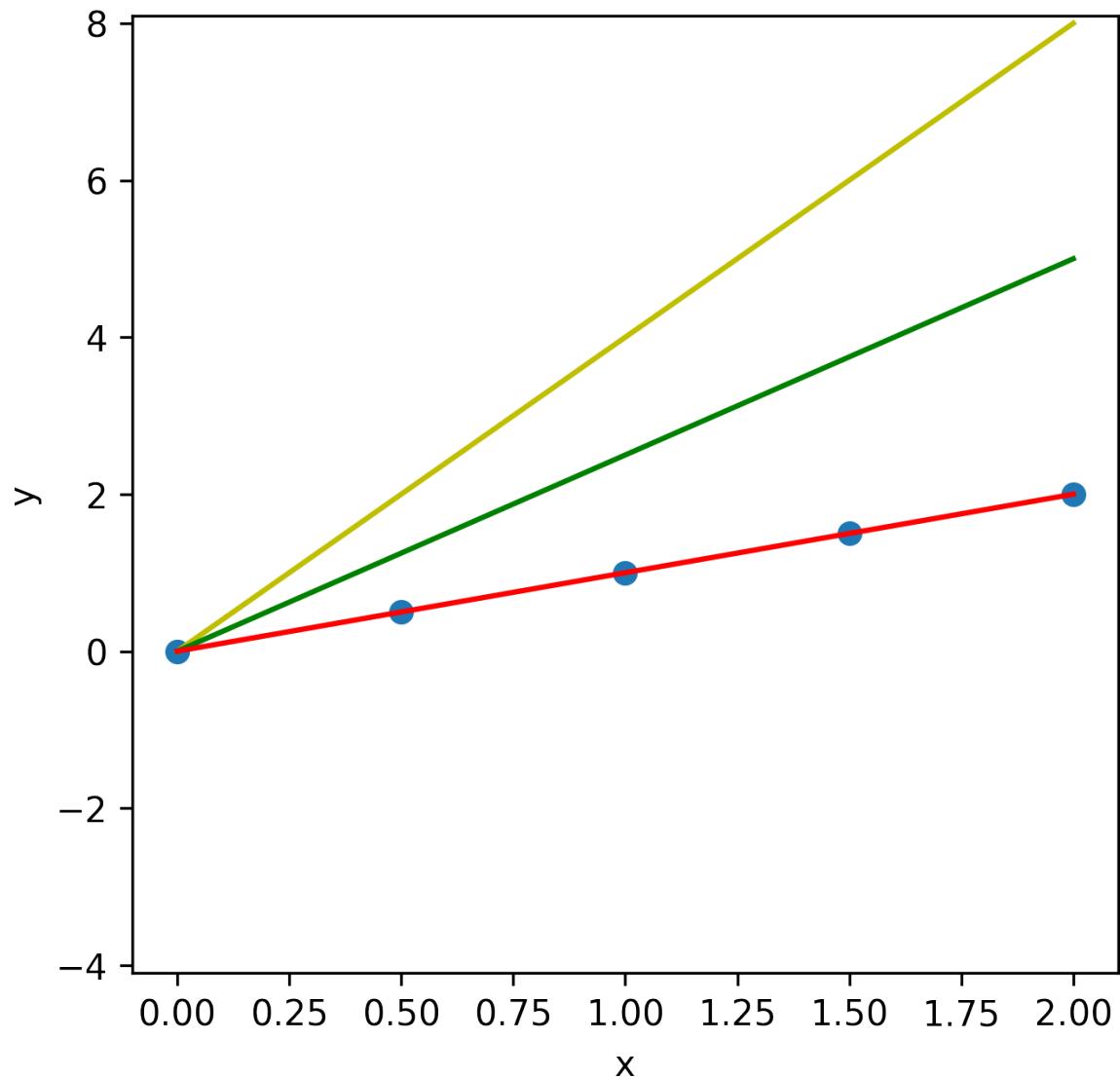
$$J(0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (0 + \theta_1 x^{(i)} - y^{(i)})^2$$

## Minimize a simplified $J$



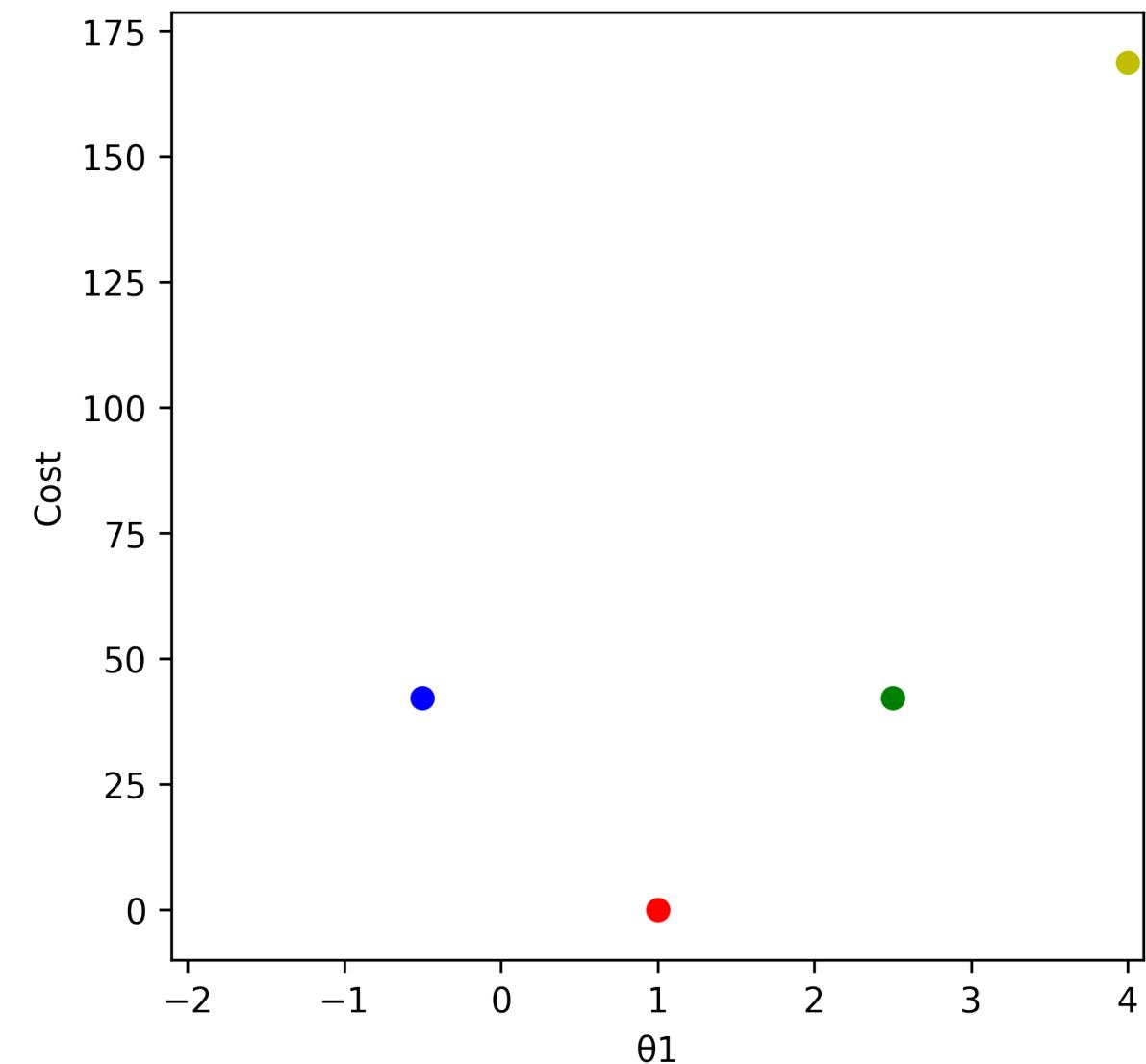
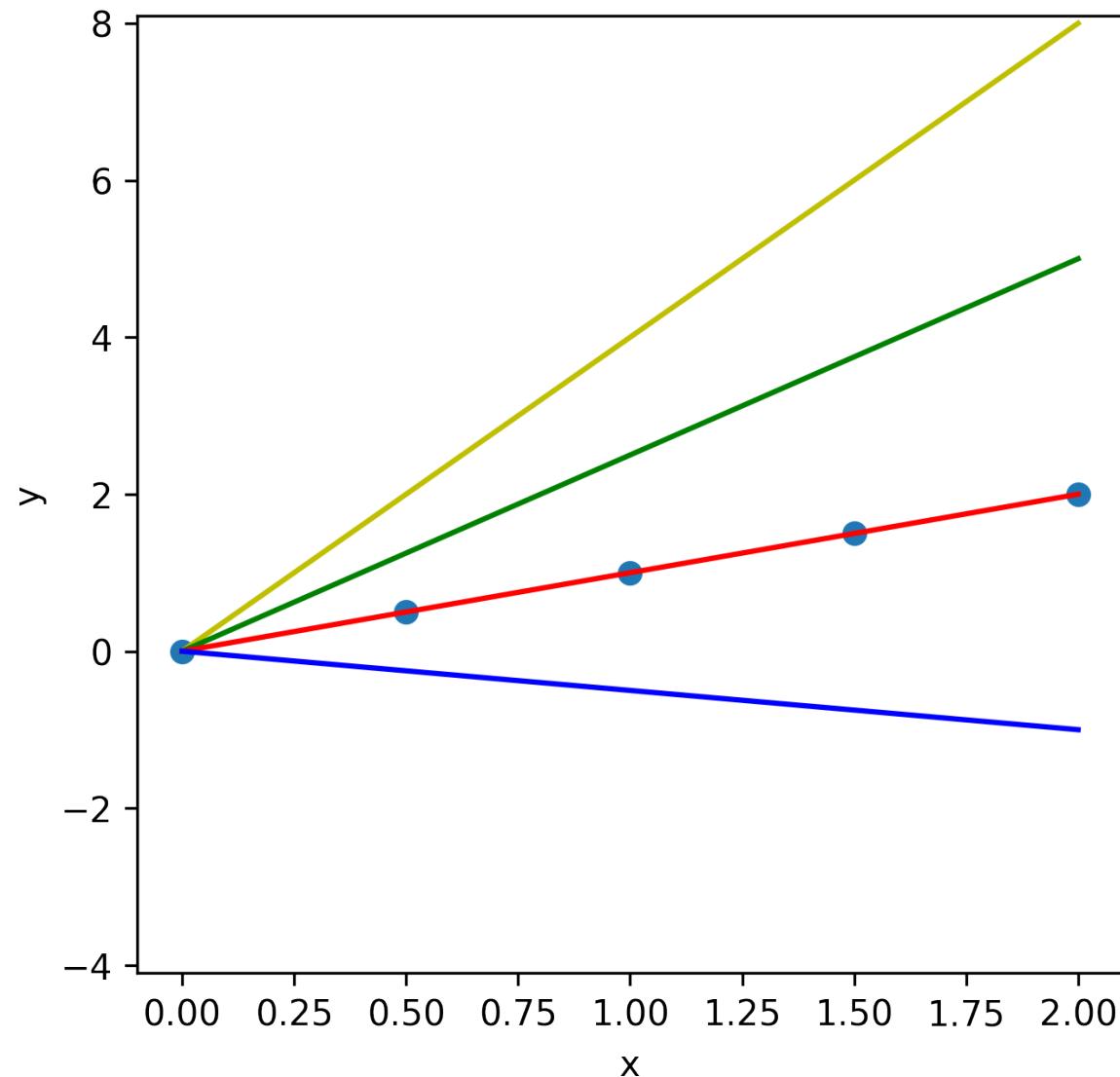
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## Minimize a simplified $J$



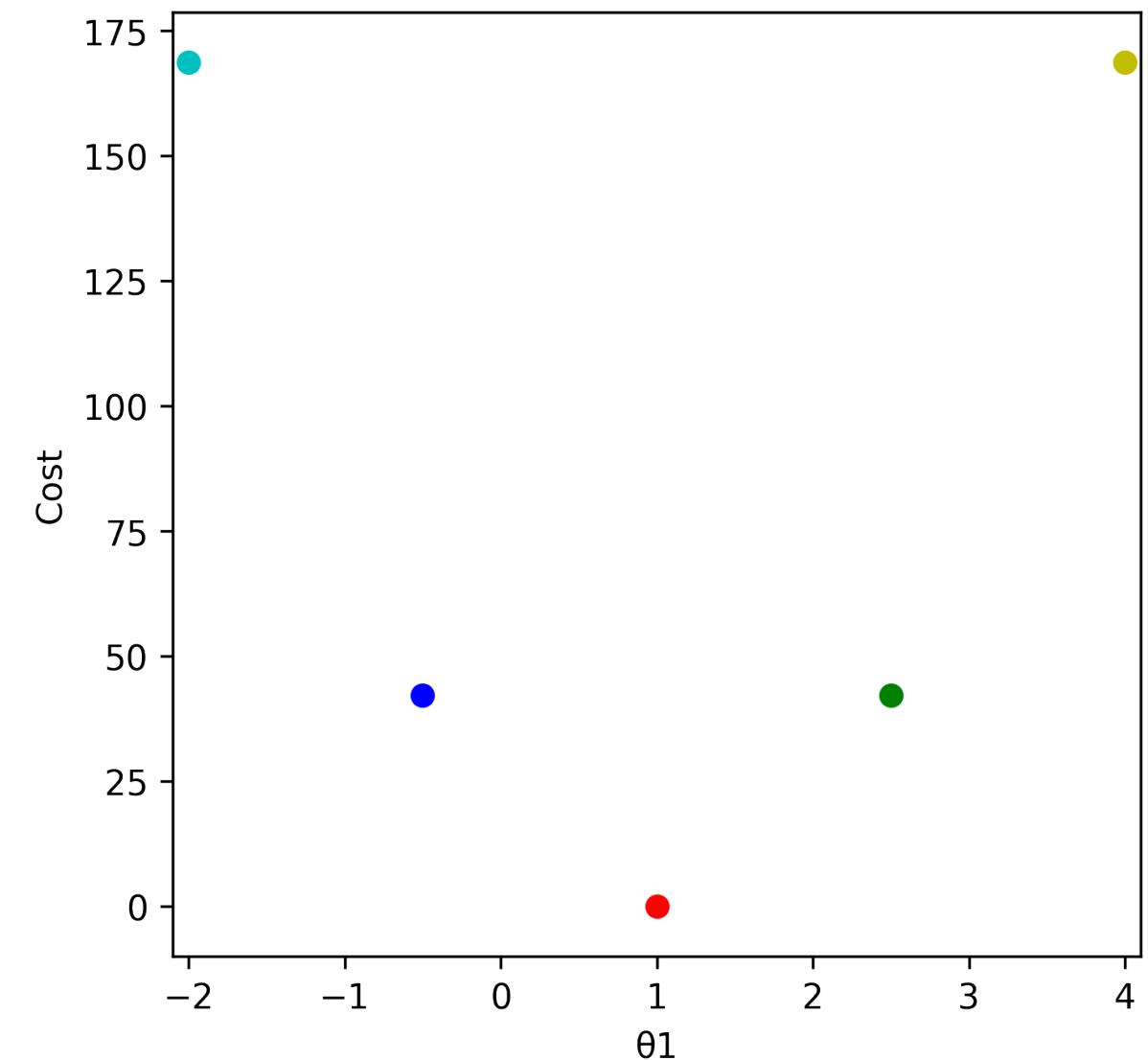
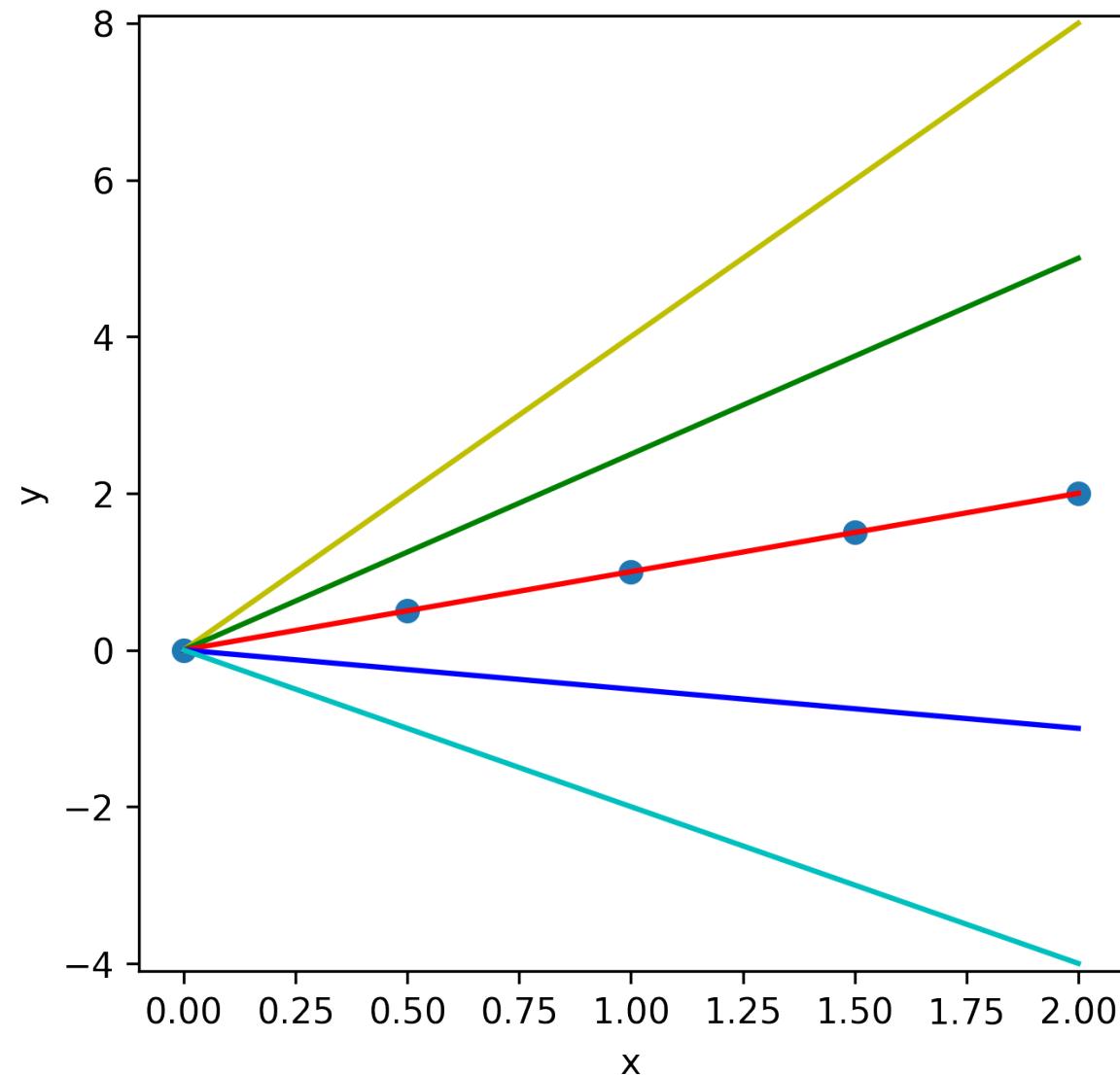
$$J(0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (0 + \theta_1 x^{(i)} - y^{(i)})^2$$

## Minimize a simplified $J$



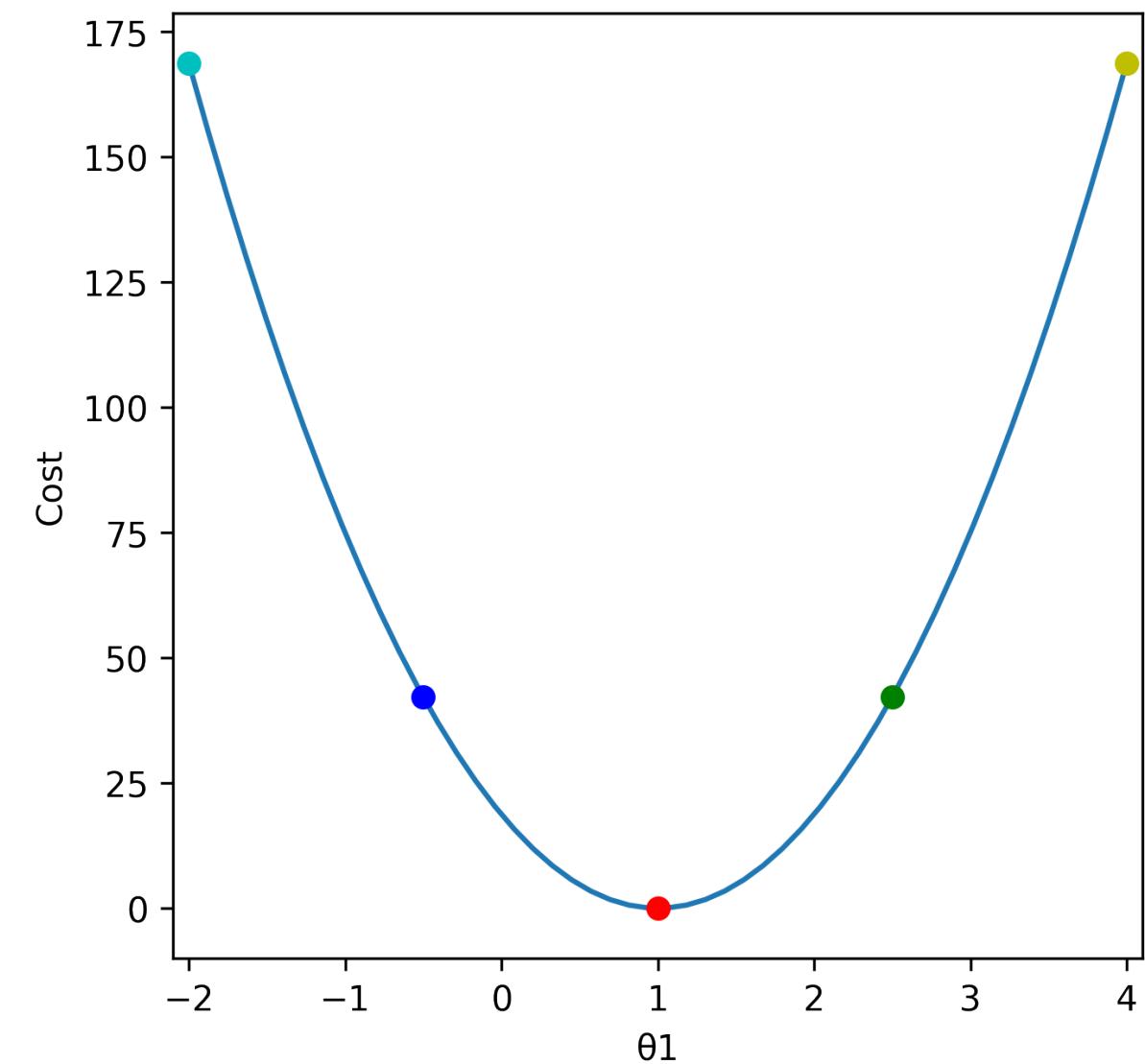
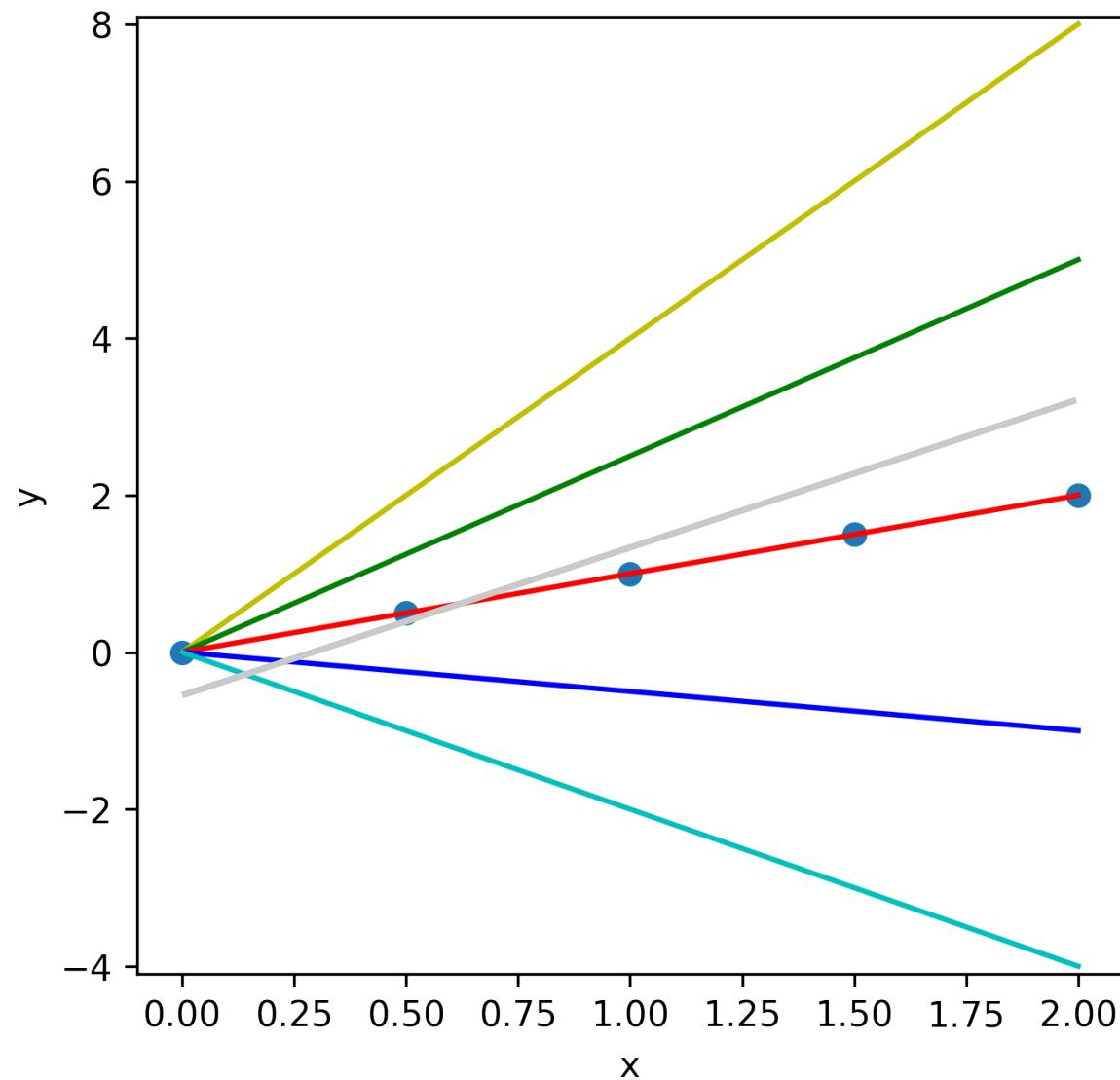
$$J(0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (0 + \theta_1 x^{(i)} - y^{(i)})^2$$

## Minimize a simplified $J$



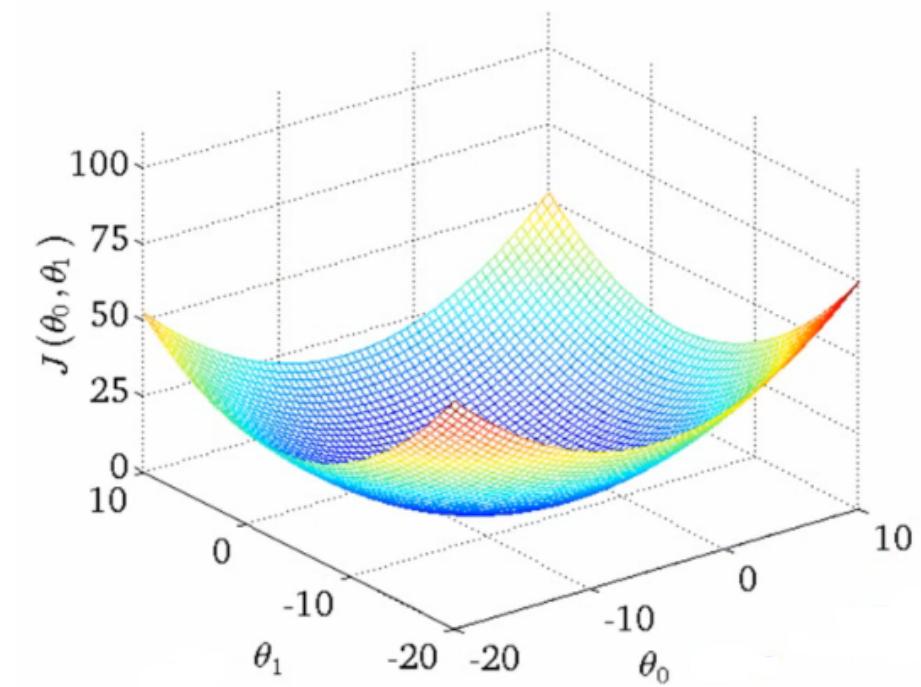
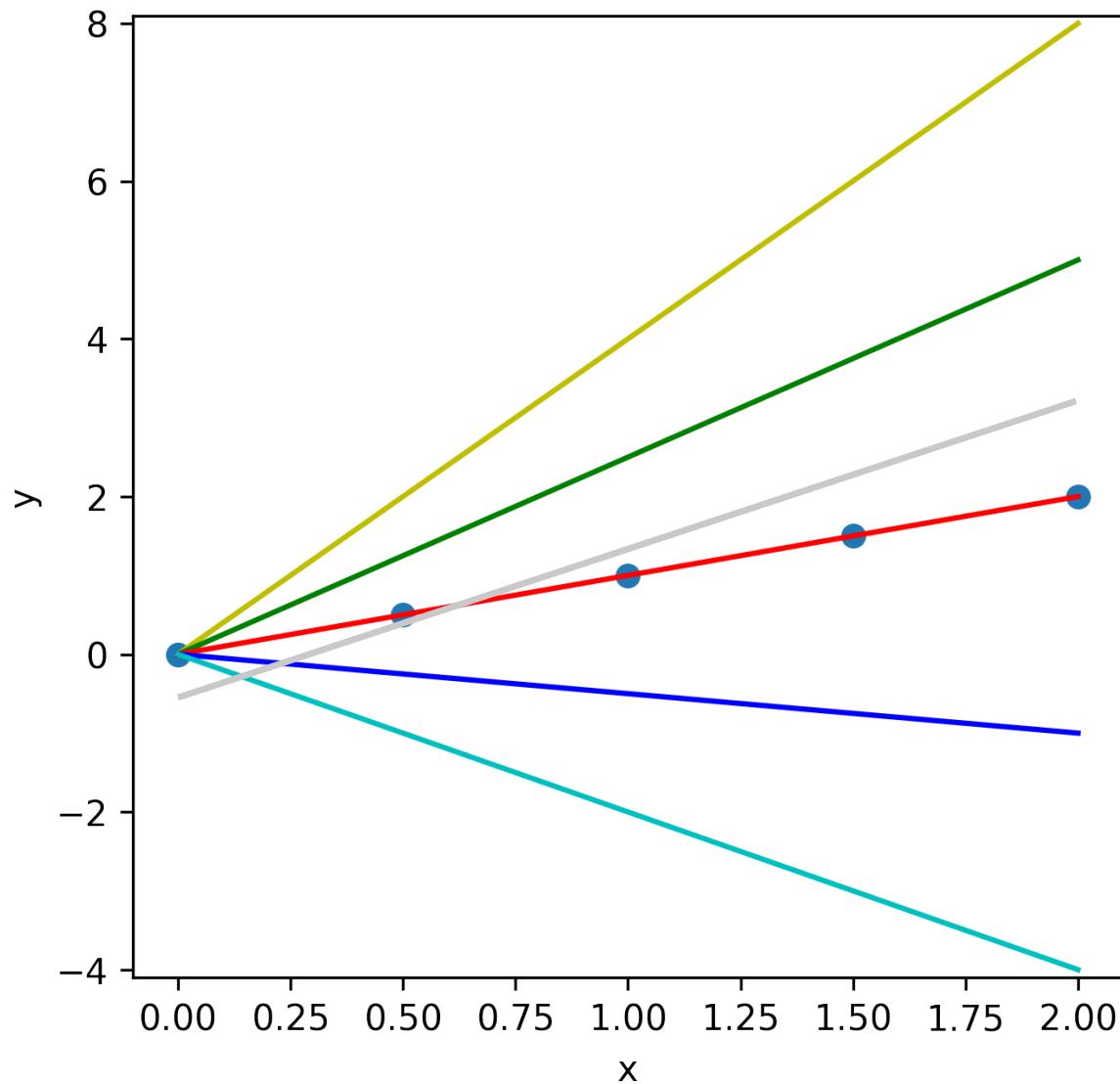
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## Minimize a simplified $J$

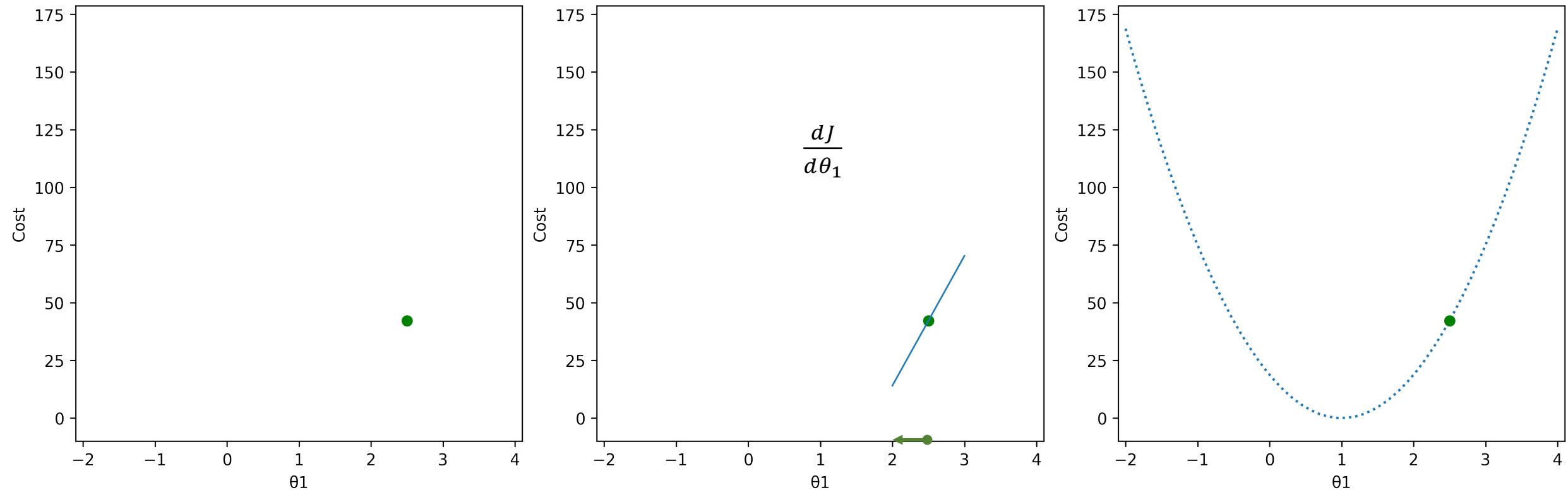


$$J(0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (0 + \theta_1 x^{(i)} - y^{(i)})^2$$

## Minimize a simplified $J$

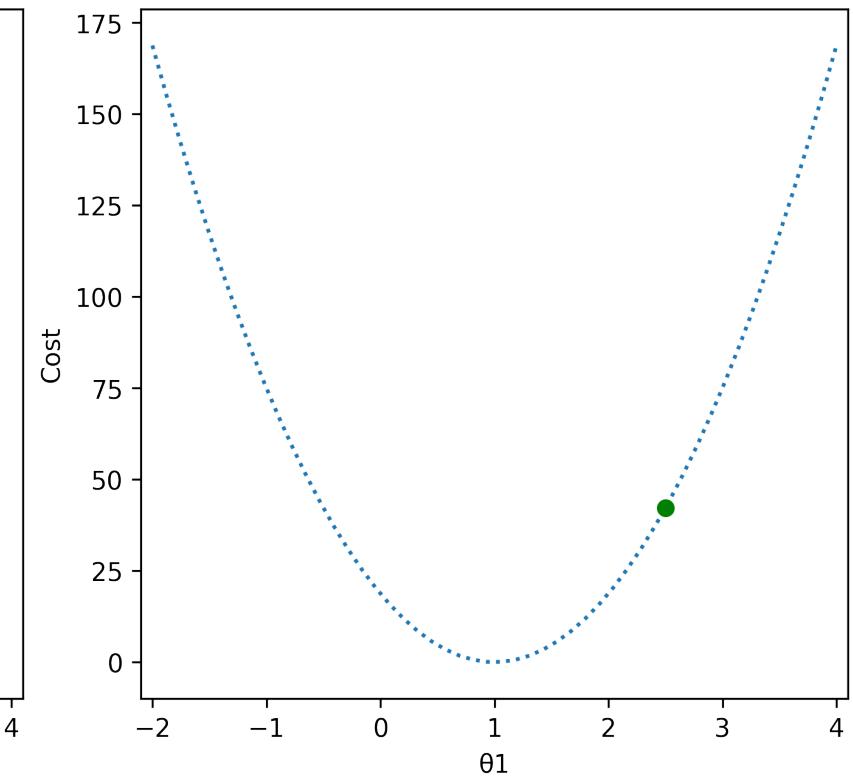
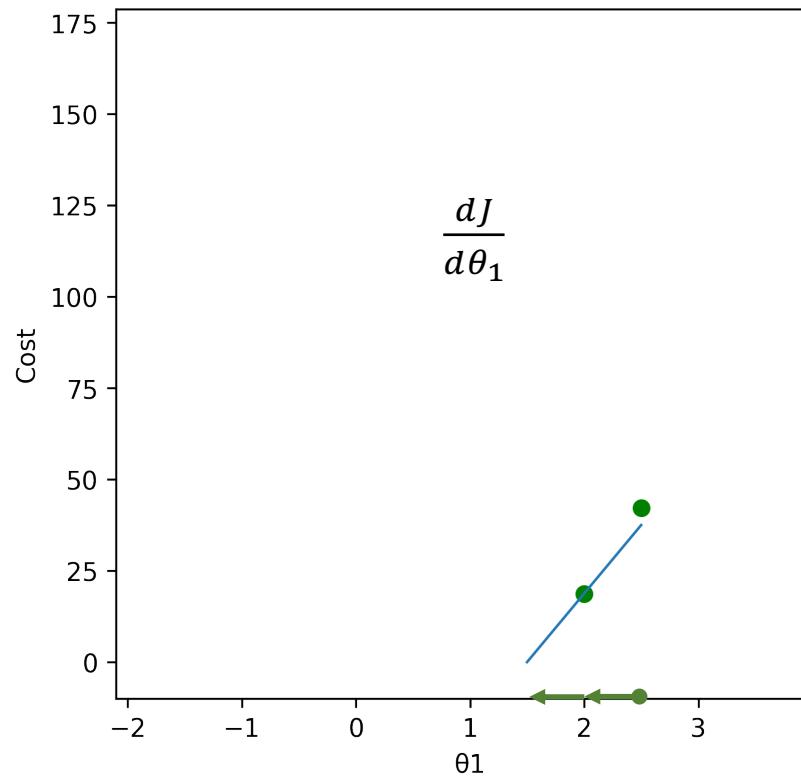
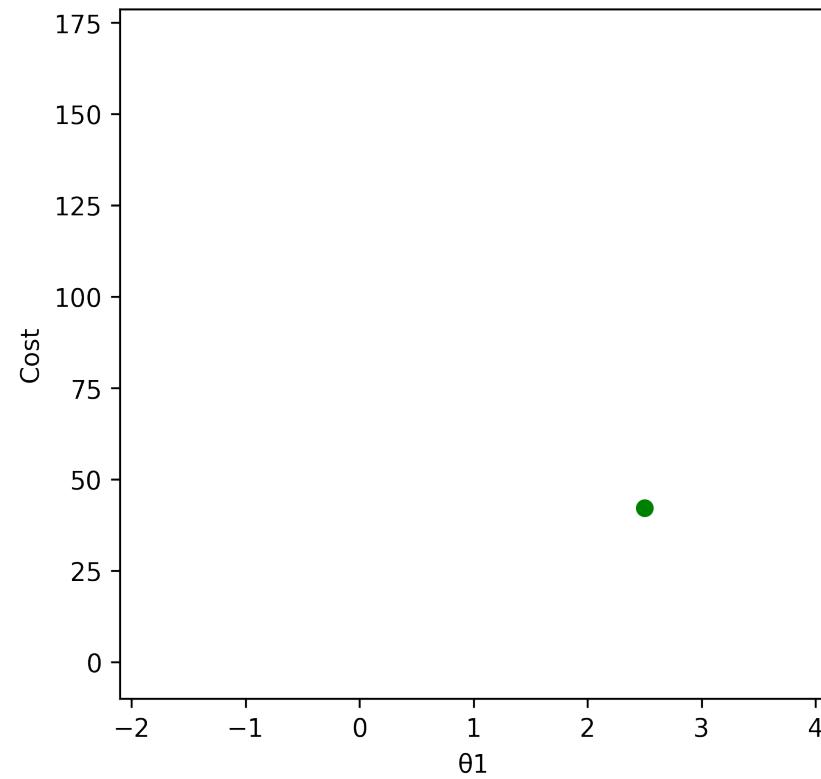


## Gradient Descent



$$2 = 2.5 - 0.5$$

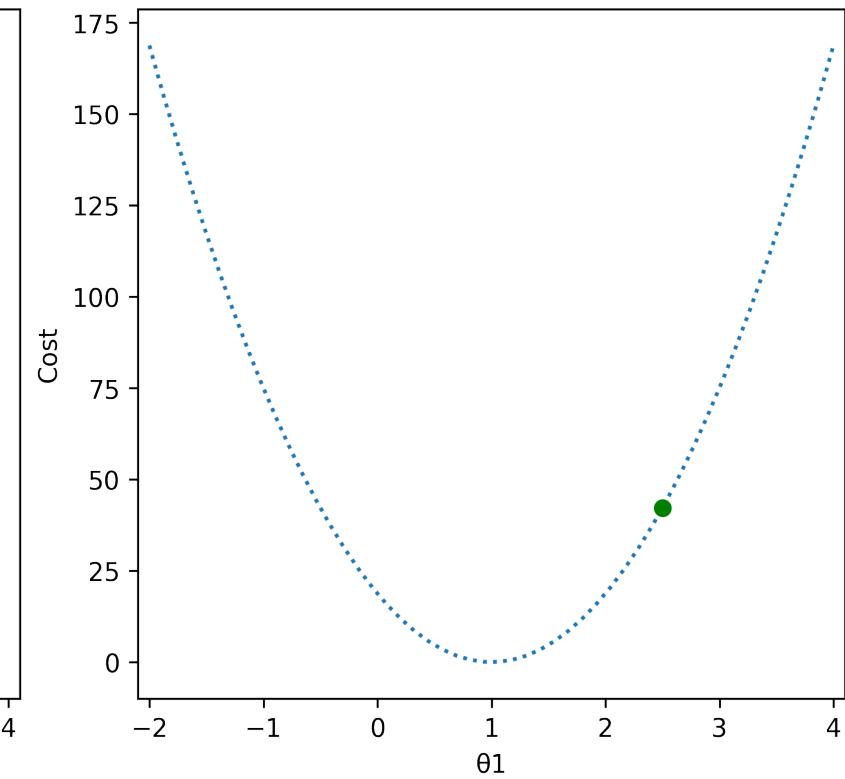
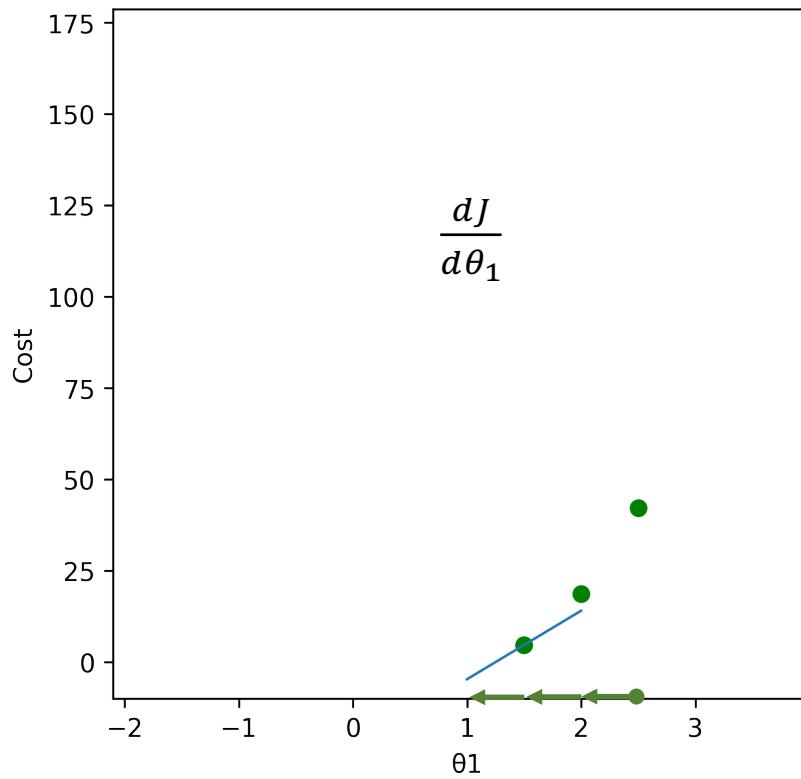
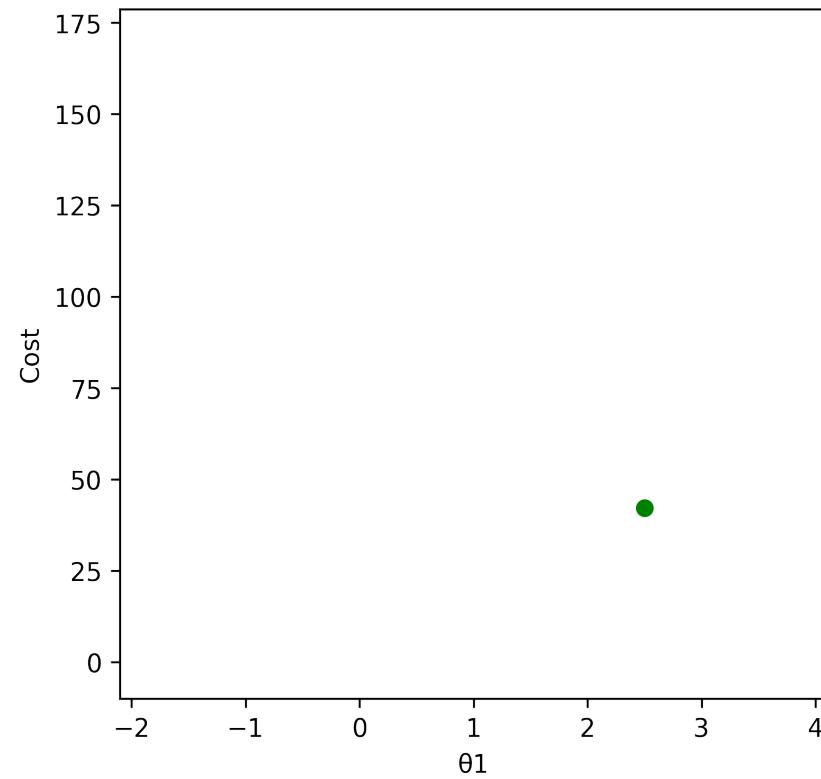
## Gradient Descent



$$2 = 2.5 - 0.5$$

$$1.5 = 2 - 0.5$$

## Gradient Descent

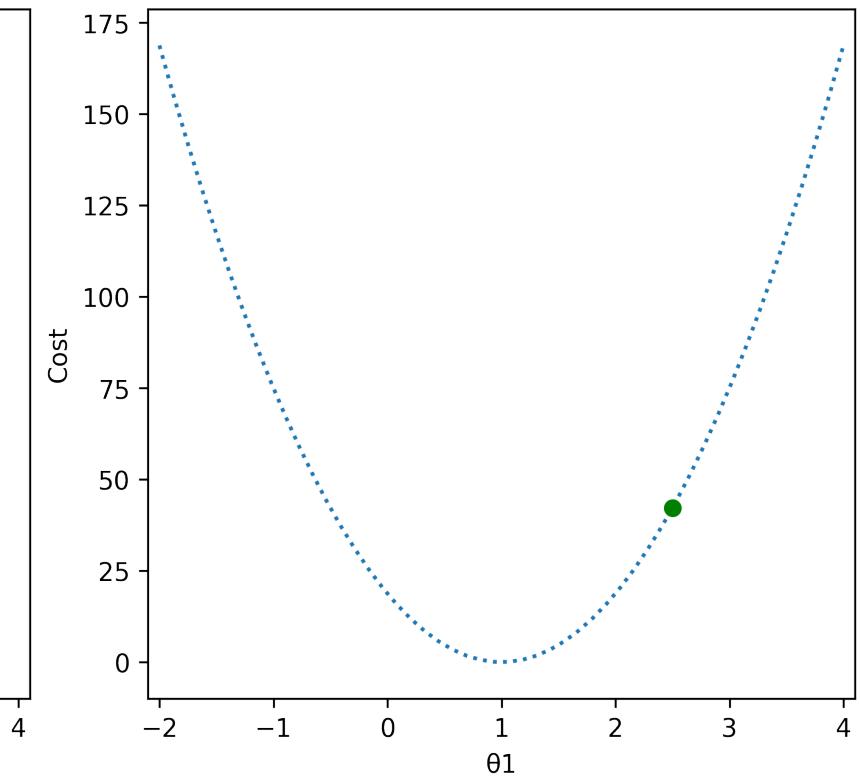
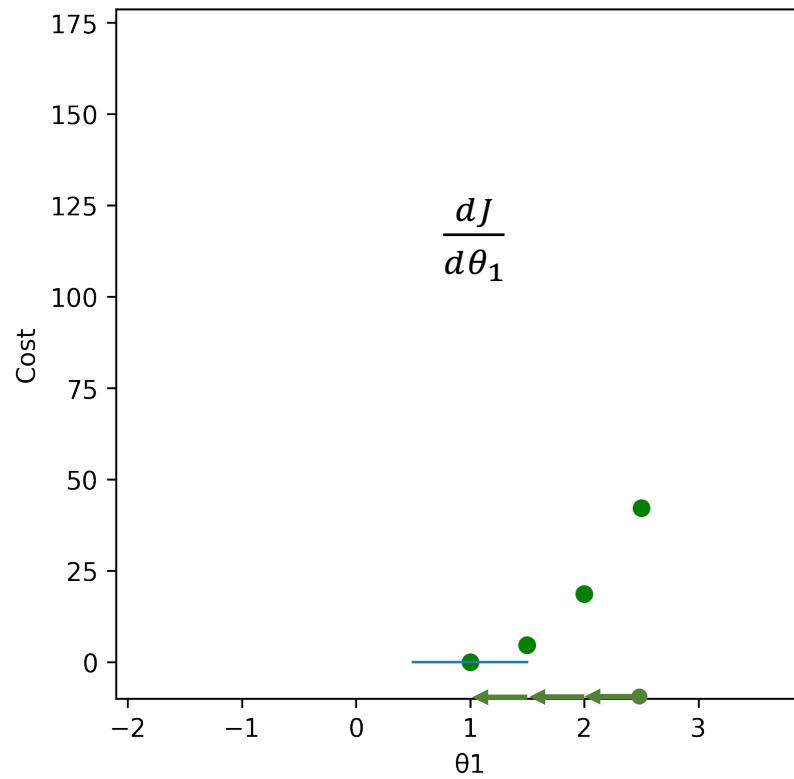
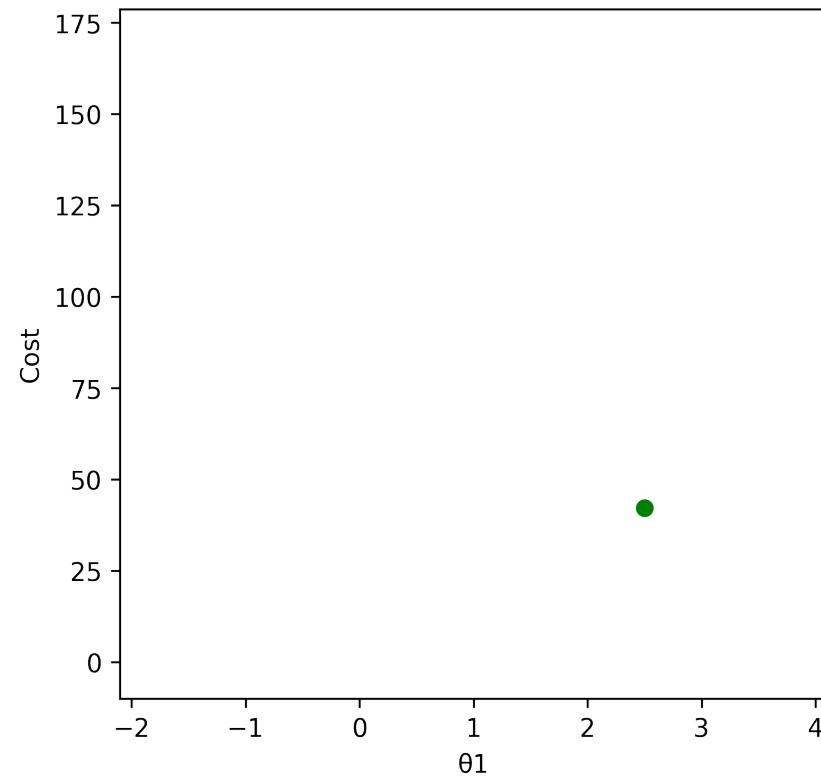


$$2 = 2.5 - 0.5$$

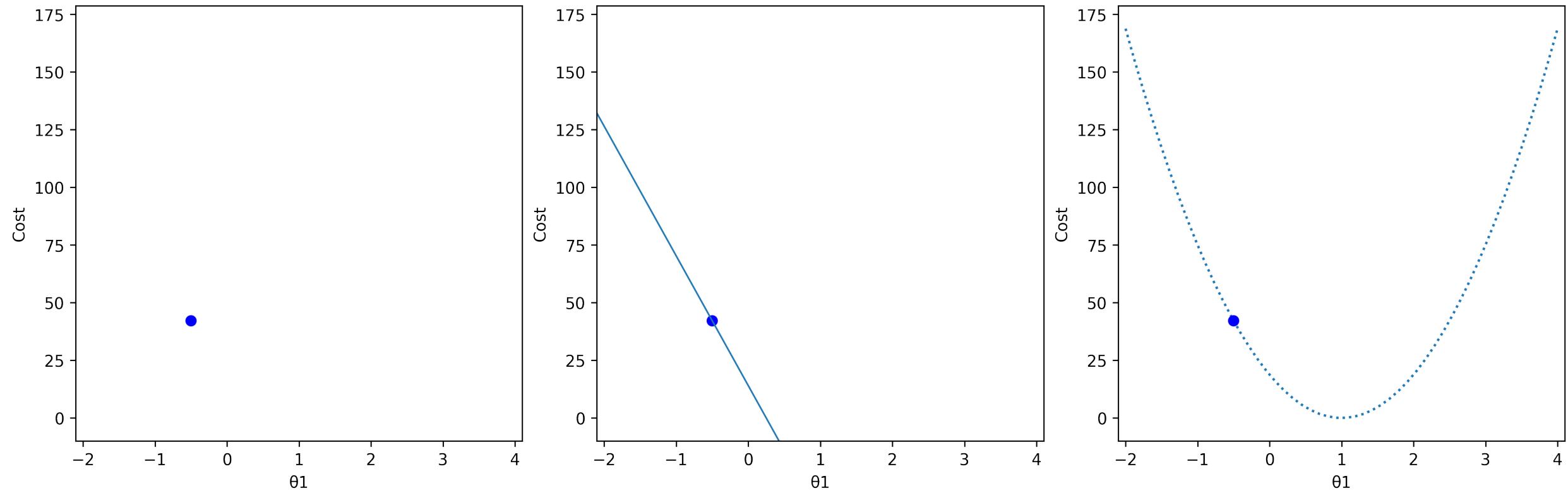
$$1.5 = 2 - 0.5$$

$$1 = 1.5 - 0.5$$

# Gradient Descent



## Gradient Descent



Repeat until convergence

$$\theta_1 = \theta_1 - \alpha \frac{dJ}{d\theta_1}$$

## Gradient Descent

$$\theta_0 = \theta_0 - \alpha \frac{\partial J}{\partial \theta_0}$$

$$\theta_1 = \theta_1 - \alpha \frac{\partial J}{\partial \theta_1}$$

$$\theta_2 = \theta_2 - \alpha \frac{\partial J}{\partial \theta_2}$$

Repeat until convergence

$$\theta_j = \theta_j - \alpha \frac{\partial J}{\partial \theta_j} \quad j = 0, 1, 2, \dots$$

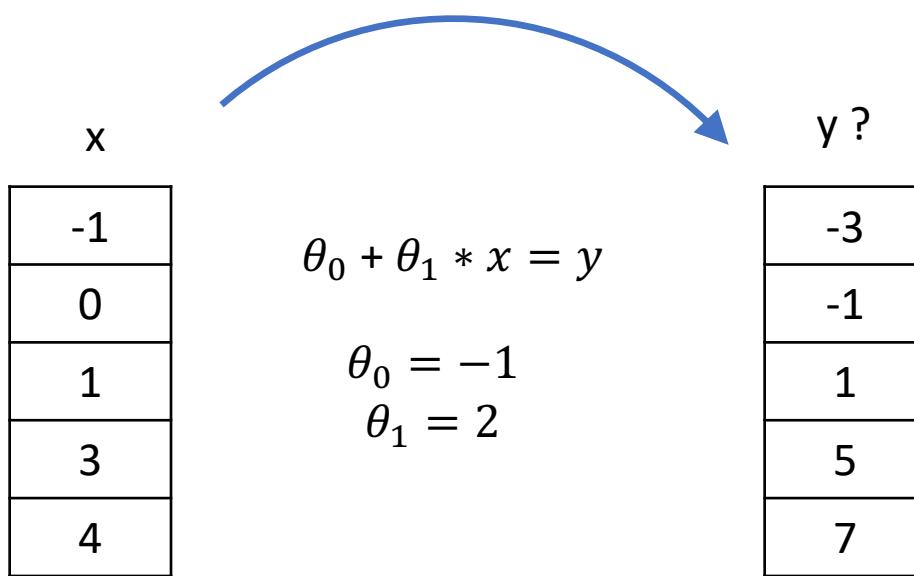
$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)})^2$$

$$\frac{\partial J}{\partial \theta_0} = \frac{1}{m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)}) * 1$$

$$\frac{\partial J}{\partial \theta_1} = \frac{1}{m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)}) * x^{(i)}$$

$$\boxed{\begin{aligned}\theta_0 &= \theta_0 - \frac{\alpha}{m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)}) \\ \theta_1 &= \theta_1 - \frac{\alpha}{m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)}) * x^{(i)}\end{aligned}}$$

## Dot product



$$X \cdot \theta = y$$

x

```
array([[ 1., -1.],
       [ 1.,  0.],
       [ 1.,  1.],
       [ 1.,  3.],
       [ 1.,  4.]])
```

theta

```
array([[-1],
       [ 2]])
```

np.dot(x, theta)

```
array([-3.,
       [-1.],
       [ 1.],
       [ 5.],
       [ 7.]])
```

x.shape

```
(5, 2)
```

theta.shape

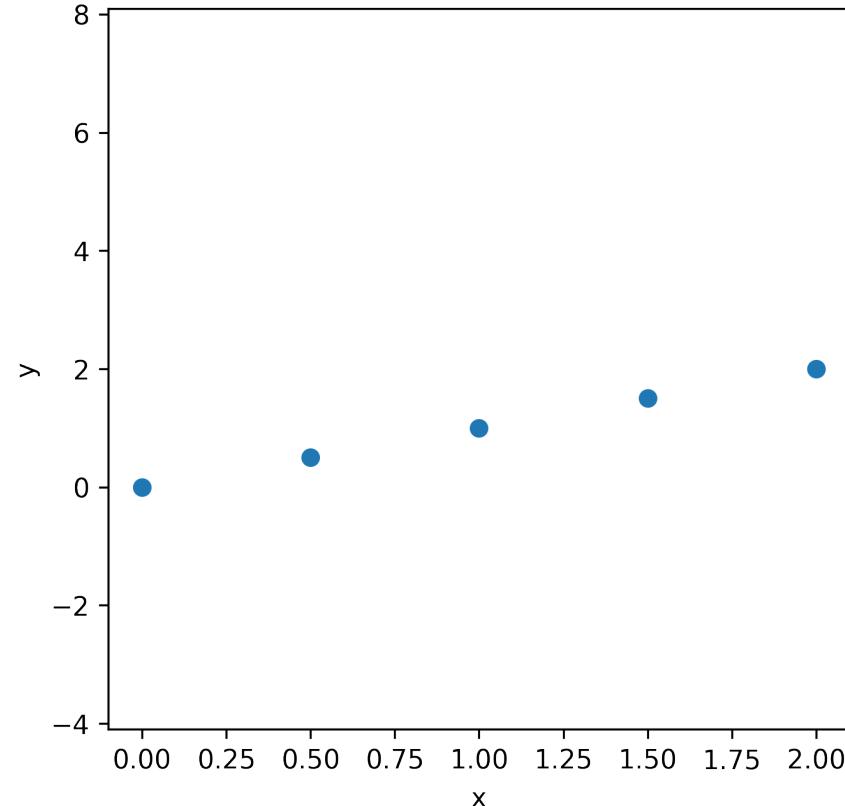
```
(2, 1)
```

np.reshape()  
np.newaxis

theta.shape

~~```
(2, )
```~~

# The Challenge



```
def cost_function(X, y, theta):  
    J(theta_0, theta_1) =  $\frac{1}{2m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)})^2$ 
```

```
def GD_one_step(X, y, theta, lr):  
     $\theta_0 = \theta_0 - \frac{\alpha}{m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)})$   
     $\theta_1 = \theta_1 - \frac{\alpha}{m} \sum_{i=1}^m (\theta_0 + \theta_1 x^{(i)} - y^{(i)}) * x^{(i)}$ 
```

```
def GD(X, y, lr, epoch):  
    Repeat until convergence
```

## Challenge 1 Linear regression

scikit  
*learn*

Good luck!

 @malicannoyan



## Challenge 2

Aleatoric  
Epistemic

## Challenge 4 Implement Linear regression

$$\theta_j = \theta_j - \alpha \frac{\partial J}{\partial \theta_j}$$

## Challenge 3 Overfitting

