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# Formal Methods

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## Assignment #3

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## ***Q1: Prepare and Enhance in the example of Light with various levels of brightness.***

### **Light model:**

Light model has three levels (light, medium, bright). I have also included mutual exclusion principle in that is defined below.

### **Mutual exclusion:**

Mutual exclusion model is a process which prevents two processes to access shared resources. The concept is used in concurrent programming which has a critical section in which there are shared resources.

### **Locations of Light1, Light2:**

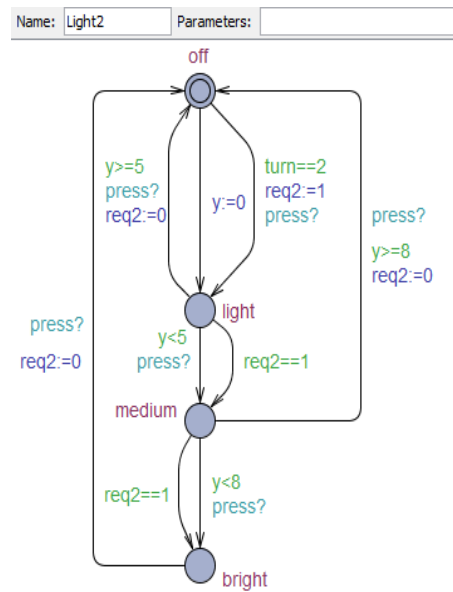
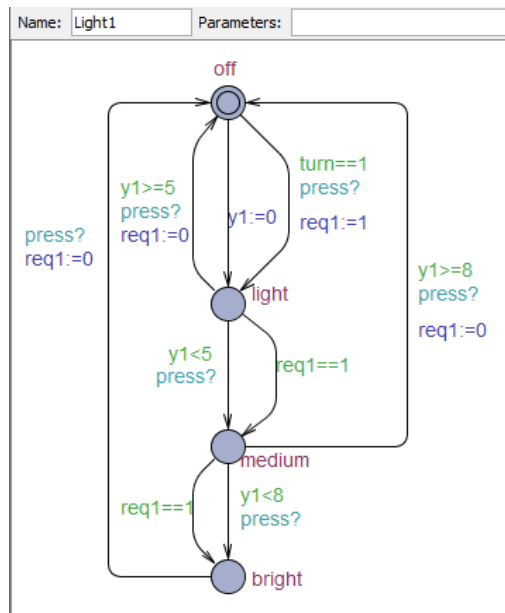
Off, light, medium, bright

### **Locations of User:**

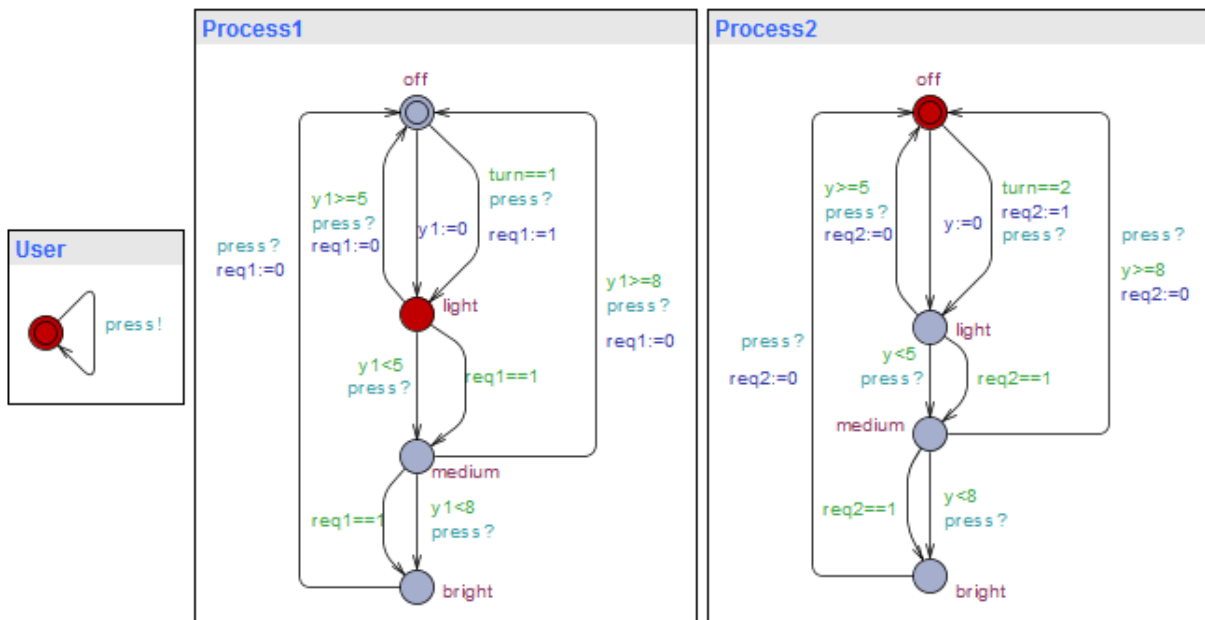
idle

<b>Process 1:</b>	<b>Process 2:</b>	<b>User:</b>
<b>off:</b> req1=1; while(turn!=1); press? Y1==0; <b>light:</b> while(req1!=1 && y1<5); press? <b>medium:</b> while(req1!=1 && y1<8); press? <b>bright:</b> press? req1=0; //and return to off	<b>off:</b> req2=1; while(turn!=2); press? y==0; <b>light:</b> while(req2!=1 && y<5); press? <b>medium:</b> while(req2!=1 && y<8); press? <b>bright:</b> press? req2=0; //and return to off and return to idle	<b>Idle:</b> press!

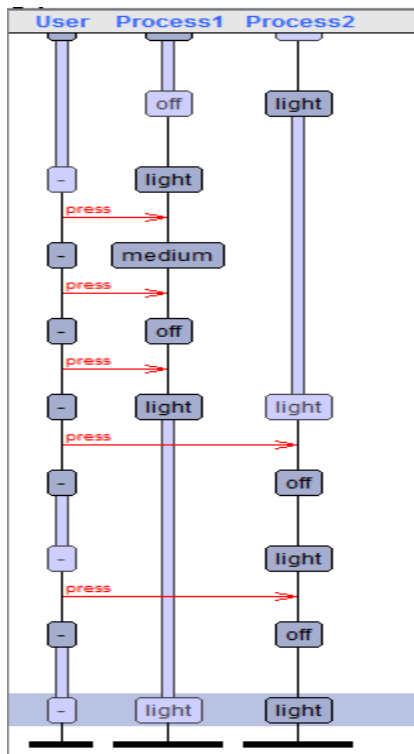
## Automaton:



## Simulation:



### Simulation Trace:



### Simulation Trace

```
(-, bright, off)
press: User → Process1
(-, off, off)
Process2
(-, off, light)
press: User → Process2
(-, off, off)
Process2
(-, off, light)
press: User → Process2
(-, off, off)
press: User → Process1
(-, light, off)
```

**System declarations:**

```
// Place template instantiations here.
User = user();
Process1 = Light1();
Process2 = Light2();
// List one or more processes to be composed into a system.
system User, Process1, Process2;
```

### Declarations:

```
// Place global declarations here.
chan press;
int [1,2] turn;
int [0,1] req1, req2;
```

Name: Light1

```
clock y1;
```

Name: Light2

```
clock y;
```

## Verification:

### Overview

E<> (Process2.bright and Process2.y<8)  
E<> (Process1.bright and Process1.y1<8)  
E<> not deadlock  
A[] not deadlock



### Query

E<> (Process2.bright and Process2.y<8)

### Comment

when process2 is at bright y is less than 8

### Status

E<> (Process2.bright and Process2.y<8)  
Verification/kernel/elapsed time used: 0.016s / 0s / 0.016s.  
Resident/virtual memory usage peaks: 6,448KB / 25,180KB.  
Property is satisfied.

### Query

E<> (Process1.bright and Process1.y1<8)

### Comment

when process1 is at bright y1 is less than 8

### Status

E<> (Process2.bright and Process2.y<8)  
Verification/kernel/elapsed time used: 0.016s / 0s / 0.016s.  
Resident/virtual memory usage peaks: 6,448KB / 25,180KB.  
Property is satisfied.

### Query

E<> not deadlock

### Comment

there does exist a deadlock

### Status

E<> not deadlock  
Verification/kernel/elapsed time used: 0s / 0.016s / 0.046s.  
Resident/virtual memory usage peaks: 6,452KB / 25,180KB.  
Property is satisfied.

### Query

A[] not deadlock

### Comment

system does not have a deadlock

### Status

A[] not deadlock  
Verification/kernel/elapsed time used: 0.016s / 0s / 0.016s.  
Resident/virtual memory usage peaks: 6,436KB / 25,156KB.  
Property is satisfied.

## Q2: Write an example of your own.

### Train gate example:

Train gate automaton is a railway control automaton in which 6 trains pass through a single gate and no one collides. There are timing constraints for trains before entering the bridge. When approaching a train sends a appr! signal. Thereafter, it has 10 time units to receive a stop signal. This allows it to stop safely before the bridge. After these 10 time units, it takes further 10 time units to reach the bridge if the train is not stopped. If a train is stopped, it resumes its course when the controller sends a go! signal to it after a previous train has left the bridge and sent a leave! signal.

Train	Gate
<b>safe:</b> appr[id]! x=0 <b>cross:</b> while(x>=3) leave[id]! <b>start:</b> while(x>=7); x=0 <b>Appr:</b> x>=10 x=0 <b>Stop:</b> go[id]? x=0	<b>free:</b> appr[e]? len==0 enqueue(e) <b>Occ:</b> appr[e]? e:id_t enqueue(e) <b>C:</b> stop[tail()]!

There are two templates:

#### 1. Train :

##### a. Locations:

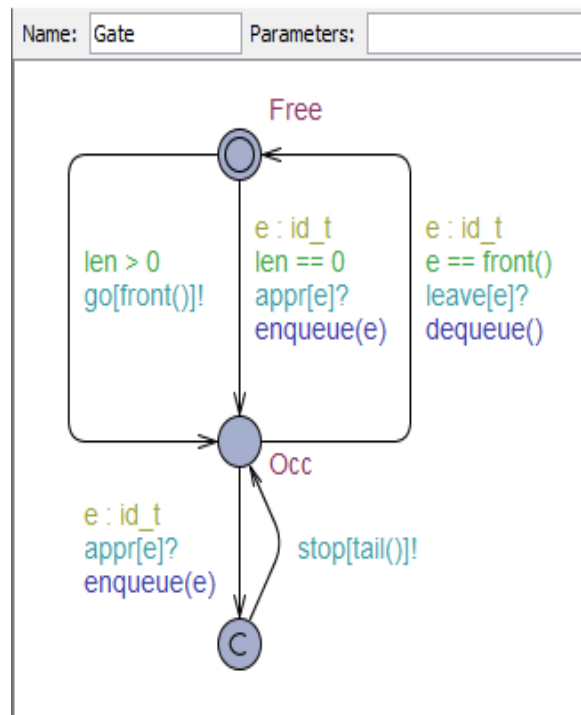
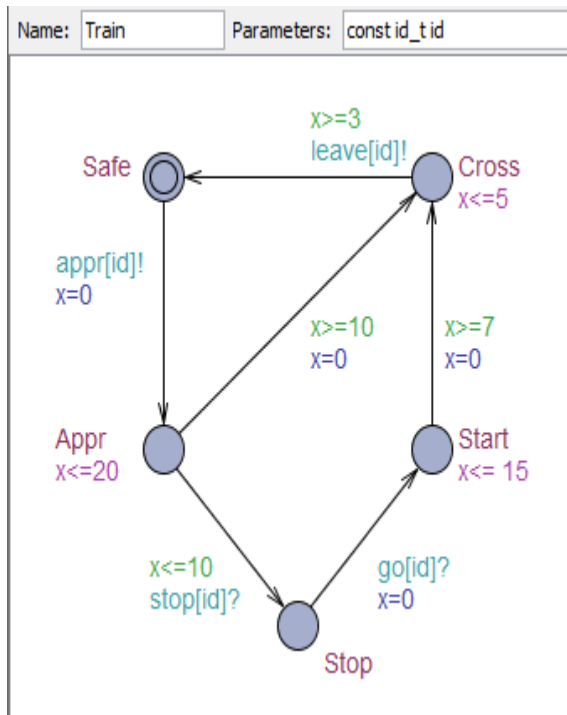
- i. Safe
- ii. Cross
- iii. Start
- iv. Appr
- v. Stop

#### 2. Gate

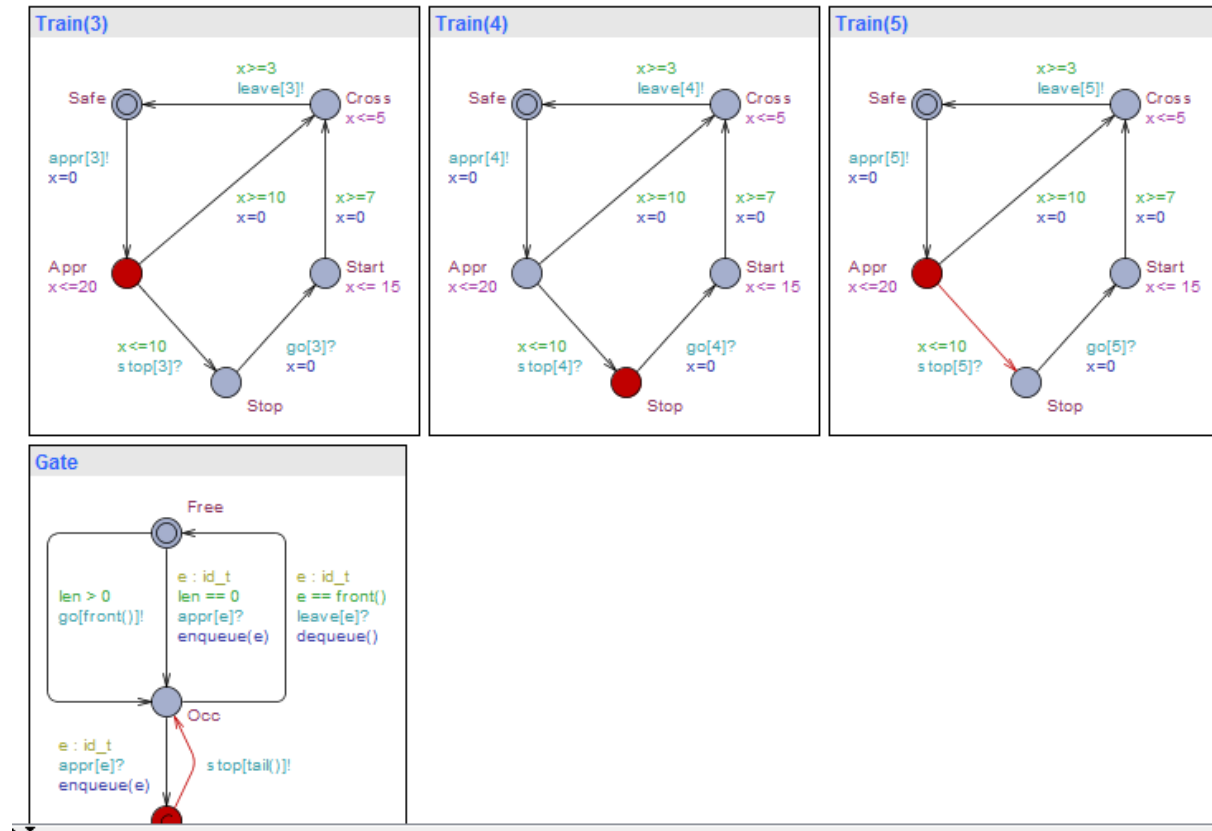
##### a. Locations:

- i. Free
- ii. Occ
- iii. C

## Automaton:

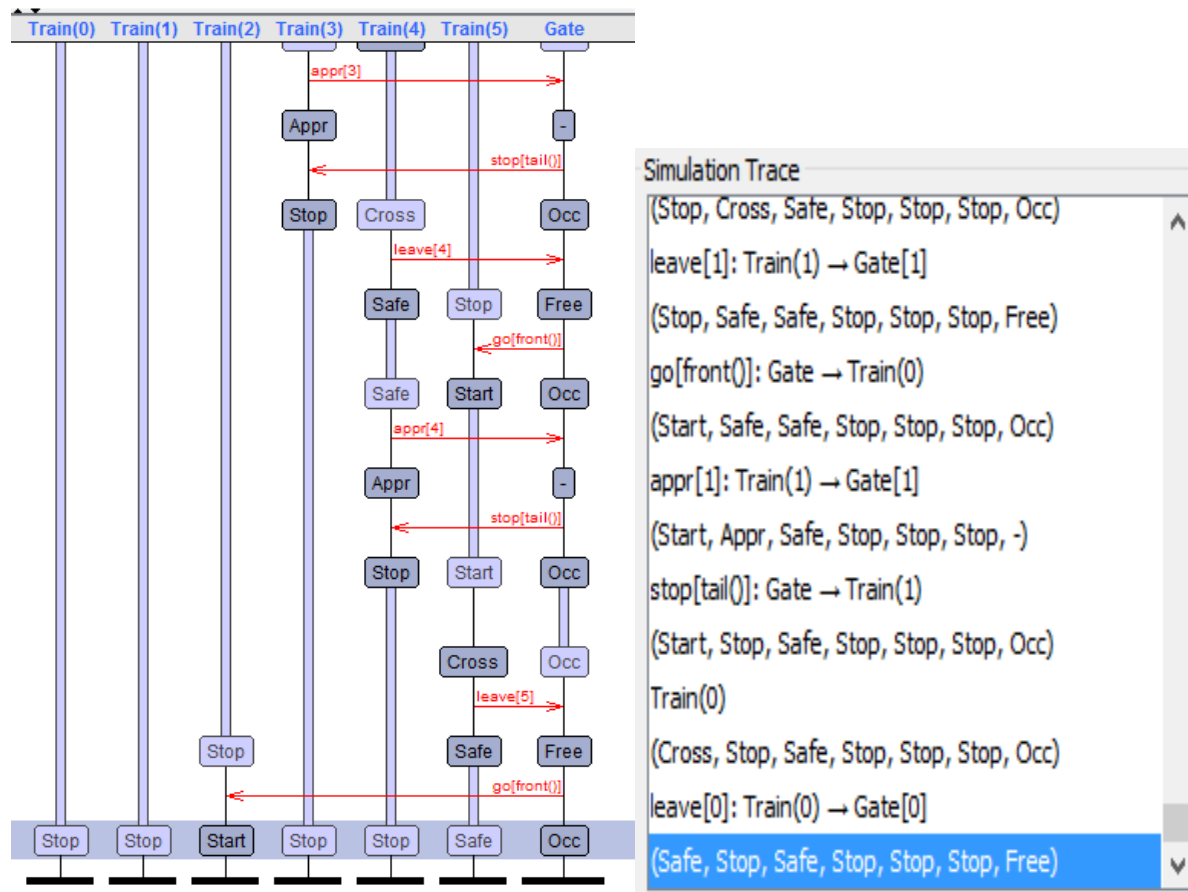


## Simulation:





### Simulation trace:



### System declarations:

```
system Train, Gate;
```

## Declarations:

```
const int N = 6;           // # trains
typedef int[0,N-1] id_t;

chan      appr[N], stop[N], leave[N];
urgent chan go[N];
```

Name: Train	Parameters: const id_t id
-------------	---------------------------

```
clock x;
```

Name: Gate	Parameters:
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```
id_t list[N+1];
int[0,N] len;
// Put an element at the end of the queue
void enqueue(id_t element)
{
    list[len++] = element;
}
// Remove the front element of the queue
void dequeue()
{
    int i = 0;
    len -= 1;
    while (i < len)
    {
        list[i] = list[i + 1];
        i++;
    }
    list[i] = 0;
}
// Returns the front element of the queue
id_t front()
{
    return list[0];
}
// Returns the last element of the queue
id_t tail()
{
    return list[len - 1];
}
```

## Verification:

Overview
<div>E&lt;&gt; Gate.Occ</div> <div>E&lt;&gt; Train(0).Cross</div> <div>E&lt;&gt; Train(1).Cross</div> <div>E&lt;&gt; Train(0).Cross and Train(1).Stop</div> <div>E&lt;&gt; Train(0).Cross and (forall (i : id_t) i != 0 imply Train(i).Stop)</div> <div>A[] forall (i : id_t) forall (j : id_t) Train(i).Cross &amp;&amp; Train(j).Cross imply i == j</div> <div>A[] Gate.list[N] == 0</div> <div>Train(0).Appr --&gt; Train(0).Cross</div> <div>Train(1).Appr --&gt; Train(1).Cross</div> <div>Train(2).Appr --&gt; Train(2).Cross</div> <div>Train(3).Appr --&gt; Train(3).Cross</div> <div>Train(4).Appr --&gt; Train(4).Cross</div> <div>Train(5).Appr --&gt; Train(5).Cross</div> <div>A[] not deadlock</div>

Query
E<> Gate.Occ
Comment
Gate can receive (and store in queue) msg's from approaching trains.
Status
E<> Gate.Occ Verification/kernel/elapsed time used: 0s / 0s / 0s. Resident/virtual memory usage peaks: 7,872KB / 27,924KB. Property is satisfied.

Query
E<> Train(0).Cross
Comment
Train 0 can reach crossing.
Status
E<> Train(0).Cross Verification/kernel/elapsed time used: 0s / 0s / 0s. Resident/virtual memory usage peaks: 7,300KB / 26,928KB. Property is satisfied.

Query
E<> Train(0).Cross and (forall (i : id_t) i != 0 imply Train(i).Stop)
Comment
Train 0 can cross bridge while the other trains are waiting to cross.
Status
E<> Train(0).Cross and (forall (i : id_t) i != 0 imply Train(i).Stop) Verification/kernel/elapsed time used: 0.218s / 0s / 0.21s. Resident/virtual memory usage peaks: 7,620KB / 27,516KB. Property is satisfied.

Query
A[] forall (i : id_t) forall (j : id_t) Train(i).Cross && Train(j).Cross imply i == j
Comment
There is never more than one train crossing the bridge (at any time instance).
Status
A[] forall (i : id_t) forall (j : id_t) Train(i).Cross && Train(j).Cross imply i == j Verification/kernel/elapsed time used: 0.672s / 0.016s / 0.678s. Resident/virtual memory usage peaks: 8,264KB / 29,108KB. Property is satisfied.

Query	Query
A[] not deadlock	E<> Train(0).Cross and Train(1).Stop
Comment	Comment
The system is deadlock-free.	Train 0 can be crossing bridge while Train 1 is waiting to cross.
Status	Status
A[] not deadlock Verification/kernel/elapsed time used: 0.656s / 0.031s / 0.701s. Resident/virtual memory usage peaks: 8,016KB / 28,304KB. Property is satisfied.	E<> Train(0).Cross and Train(1).Stop Verification/kernel/elapsed time used: 0s / 0.015s / 0.015s. Resident/virtual memory usage peaks: 6,836KB / 26,052KB. Property is satisfied.

## Github Link:

<https://github.com/Mehmoona-bibi/Automaton/>