exercise.4.4

Solve by FACTORIZATION.

12 x.

$$\begin{array}{lll}
\mathbf{Q} & \mathbf{3} & \mathbf{9} & \mathbf{x} & -4 & \{-3, -4\} \\
\mathbf{Q} & \mathbf{3} & \mathbf{9} & \mathbf{x} & -12 & \mathbf{x} & -5 & = 0 \\
\mathbf{9} & \mathbf{x} & +3 & \mathbf{x} & -15 & \mathbf{x} & -5 & = 0 \\
3 & \mathbf{x} & (3 & \mathbf{x} + 1) & -5 & (3 & \mathbf{x} + 1) & = 0 \\
& & (3 & \mathbf{x} + 1) & (3 & \mathbf{x} - 5) & = 0
\end{array}$$

$$3x+1=0$$
, $3x-5=0$
 $3x=-1$, $3x=5$
 $x=-1/3$, $x=\frac{5}{3}$

$$x^{2} - x - 2 = 0$$

 $x^{2} + x - 2 = 0$
 $x^{2} +$

$$(x-1)-2(x+1)=0 \Rightarrow x=2, x=-1$$

$$(x-1)=0, x+1=0 \qquad \{2,-1\}$$

1.5
$$\times (x+7) = (2x-1)(x+4)$$

 $x^{2} + 7x = 2x^{2} + 8x - x - 4$
 $x^{3} + 7x = 2x^{3} + 8x - x - 4$
 $x^{4} + 7x = 2x^{3} + 7x - 4$
 $2x^{3} - x^{4} + 7x - 7x - 4 = 0$
 $x^{4} - 4 = 0$
 $x^{4} - (2)^{4} = 0$
 $(x+2)(x-2) = 0$

 $\mathbf{Q6} \quad \frac{x}{x+1} + \frac{x+1}{x} = \frac{5}{2}$ Multiplying by 2x (x+1) $2 \times (x+1) \cdot \frac{x}{x+1} + 2 \times (x+1) \cdot \frac{x+1}{x} = 2 \times (x+1) \cdot \frac{5}{x}$ $2x^{2} + 2(x+1)(x+1) = 5x(x+1)$ $2x^{2} + 2(x^{2} + 2x + 1) = 5x^{2} + 5x$ 2x + 2x +4x +2 = 5x +5x $4x^{2} + 4x + 2 = 5x^{2} + 5x$ $5x^{2}-4x^{2}+5x-4x-2=0$ x + x - 2 = 0 $x^2 - x + 2x - 2 = 0$ $o = (1-\kappa) + (1-\kappa) \kappa$ $(\chi-i)(\chi+L)=0$ ⇒ X= | , X=-2 { 1,-2} $Q.7_{\frac{1}{\chi+1}} + \frac{2}{\chi+2} = \frac{7}{\chi+5}$ Mulliplying by (x+1)(x+2)(x+5) $(x+1)(x+2)(x+5)\frac{1}{x+1}+(x+1)(x+2)(x+5)\frac{2}{x+2}$ (x+1)(x+5)+1(x+1)(x+5)=7(x+1)(x+2)x+5x+2x+10+2(x+5x+x+5)=7(x+2x+x+2) x+7x+10+2x+12x+10=7x+21x+14 3x+19x+20=7x+21x+14 7x-3x+21x-19x+14-20=0 $4x^{2} + 2x - 6 = 0$ $2x^{2} + x - 3 = 0$ -6x2 2x - 2x + 3x -3 =0 -LN 3x 2x(x-1)+3(x-1)=0 (x-1) (1x+3) = 0

X-1=0, 2X+3 = 0

x = -3, $\{1, -\frac{3}{2}\}$

N=1 , 2 x=-3

 $\mathbf{0.8} \frac{a}{ax-1} + \frac{b}{bx-1} = a+b$ $\frac{a}{ax-1}-b+\frac{b}{bx-1}-a=0$ $\frac{a-b(ax-1)}{ax-1} + \frac{b-a(bx-1)}{b} = 0$ $\frac{a-abx+b}{ax-1} + \frac{b-abx+a}{bx-1} = 0$ $\frac{a+b-abx}{ax-1} + \frac{a+b-abx}{bx-1} = 0$ $(a+b-abx)\left\{\frac{1}{ax-1}+\frac{1}{bx-1}\right\}=0$ $\frac{-2x^{2}}{(a+b-abx)} \left\{ \frac{ax-1}{ax-1} + \frac{bx-1}{bx-1} \right\} = 0$ $-x \ge x$ $(a+b-abx) \left\{ \frac{bx-1+ax-1}{(ax-1)(bx-1)} \right\} = 0$ (a+b-abx) (ax+bx-1)=o(ax-1)(bx-1) (a+b-abx)(ax+bx-2)=0Eilher a+b-abx = 0 or ax+bx-1=0 => abx = a+b , (a+b)x = 2 $\Rightarrow \quad \chi = \frac{a+b}{ab} \; , \quad \chi = \frac{2}{a+b}$ $\left\{ \frac{a+b}{ab}, \frac{2}{a+L} \right\}$ = $(x+1)(x+2)(x+5)\frac{7}{x+5}$ # Solve By Completing Square. **Q.9** $x^2 - 2x - 899 = 0$ $x^{1}-\lambda x = R99$ Adding (=) = (1) on both sides $x^{2}-2x+(-1)^{2}=899+(-1)^{2}$ $(x-1)^{-} = 899+1$ (x-1) = 900 ⇒ x-1 =±30 X-1 = 30, X-1 = -30 N = 30+1) N =-30+1 x = 31, x = -29{ 31,-29} Q.10 x+4x-1085=0 x+4x = 1085 Adding (4/2) = (2) on both sides

 $x^{2}+4x+(2)^{2}=1085+(2)^{2}$

$$(x+2)^{2} = 1089$$

$$\Rightarrow x+1 = \pm 33.$$

$$x+2 = 33-2, \quad x = -33-2$$

$$x = 31, \quad x = -35$$

$$\begin{cases} 31, -35 \end{cases}$$

$$x^{2} + 6x = 567 = 0 \end{cases}$$

$$x^{2} + 6x = 567$$

$$x^{3} + 6x + (3)^{2} = 567 + (3)^{3}$$

$$(x+3)^{2} = 567 + 9$$

$$(x+3)^{2} = 576$$

$$x+3 = \pm 24$$

$$x = 24-3, \quad x = -24$$

$$x = 24-3, \quad x = -27$$

$$\begin{cases} 21, -27 \end{cases}$$

$$(x-3)^{2} = 648 + (\frac{3}{2})^{2}$$

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$$(x-3)^{2} = \frac{2592+9}{4}$$

$$(x-3)^{2} = \frac{51}{4}, \quad x-3 = -\frac{51}{4}$$

$$x = \frac{51}{4}, \quad x = -\frac{51}{4}, \quad x = -\frac{51}{4}$$

$$x = \frac{51}{4}, \quad x = -\frac{48}{4}$$

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$$x = \frac{51}{4}, \quad x = -\frac{24}{4}$$

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Q.13 x - x - 1806 = 0 $\chi^2 - \chi = /806$ Adding (1/2) on both sides x2-x+(1/2)=1806+(1/2) $(x - \frac{1}{2})^2 = 1806 + \frac{1}{2}$ $(x - \frac{1}{2})^{2} = \frac{7214+1}{2}$ $(x - \frac{1}{2})^{2} = \frac{7225}{2}$ > x-1/2 = ± 85/ x-1/2 = 85/2 , x-1/2 = -85/2 x = 85/ + 1/2 , x = -85/ + 1/2 $\mathcal{H} = \frac{85+1}{2} \quad , \quad \mathcal{H} = \frac{-85+1}{2}$ x = 86/2, x = -84/2x = 43, x = -42 $\{45, -42\}$ Q.14 2x+12x-110=0 Dividing by 2. x2+6x-55=0 Adding $(\frac{6}{4})^{2} = (3)^{2}$ on both sides $x^{2}+6x+(3)^{2}=55+(3)^{2}$ (x + 3) = 55+9 $(n + 3)^2 = 64$ X+3 = ± 8 N+3=8) N+3=-8 N=8-3 , N=-8-3 x = 5, x = -H\$ 5,-11} * Find roots by using . Q. Formula. Q.15 5x-13x+6=0 Compairing ax+bx + c = 0 We have $\alpha = 5, b = -13, c = 6$ Using $x = -b \pm \sqrt{b^2 - 4ac}$ $X = \frac{-(-13) \pm \sqrt{(-13)^2 - 4(5)(6)}}{2(5)}$ $X = \frac{13 \pm \sqrt{169 - 120}}{10}$

$$x = \frac{13 \pm \sqrt{49}}{10} \Rightarrow x = \frac{13 \pm 7}{10}$$

$$x = \frac{13 + 7}{10}, \quad x = \frac{13 - 7}{10}$$

$$x = \frac{20}{10}, \quad x = \frac{6}{10}$$

$$x = 2, \quad x = \frac{3}{5}, \quad \left\{2, \frac{3}{5}\right\}$$

$$\mathbf{Q.16} \quad 4x + 7x - 1 = 0$$
Compairing $ax + bx + c = 0$
We get $a = 4, b = 7, c = -1$
Using $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$$x = \frac{-7 \pm \sqrt{(7)^{2} - 4(4)(-1)}}{2(4)}$$

$$x = \frac{-7 \pm \sqrt{49 + 16}}{8}$$

$$x = \frac{-7 \pm \sqrt{65}}{8} \qquad \left\{ -\frac{7 \pm \sqrt{65}}{8} \right\}$$

Q.17/5x+2ax-a=0

Compairing
$$ax^2 + bx + c = 0$$

 $a = 15, b = 2a, c = -a^2$

Using
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-1a \pm \sqrt{(1a)^2 - 4(15)(-a^2)}}{2(15)}$$

$$X = \frac{-1a \pm \sqrt{4a^2 + 60a^2}}{30}$$

$$\chi = \frac{-2a \pm \sqrt{64a^2}}{30} \Rightarrow \chi = \frac{-2a \pm 8a}{30}$$

$$x = \frac{-2a + 8a}{30}$$
, $x = \frac{-1a - 8a}{30}$

$$x = \frac{6a}{30}, x = \frac{-10a}{30}$$

$$x = \frac{a}{5}, x = -\frac{a}{3}$$
 $\{\frac{a}{5}, -\frac{a}{3}\}$

Q.18 16x+8x+1=0

Using.
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-8 \pm \sqrt{(8)^2 - 4(16)(1)}}{2(16)}$$

$$X = \frac{-8 \pm \sqrt{64 - 64}}{32} \Rightarrow X = \frac{-8 \pm \sqrt{6}}{32}$$

$$x = \frac{-8}{31} \Rightarrow x = -\frac{1}{4} \left\{ -\frac{1}{4} \right\}$$

Q.19

(x-a)(x-b)+(x-b)(x-c)+(x-c)(x-a)=0Simplyfying

 $x^{2}-bx-ax+ab+x^{2}-cx-bx+bc+x^{2}-ax-cx+ac=0$ $3x^{2}-2ax-2bx-2cx+ab+bc+ac=0$

3x -2 (a+b+c) x + ab+bc+ac=0

Using
$$x = -b \pm \sqrt{b^2 - 4ac}$$

$$\chi = \frac{-[-2(a+b+c)] \pm \sqrt{[2(a+b+c)]^{2} - 4(3)(ab+bc+ac)}}{2(3)}$$

$$X = \frac{2(a+b+c) \pm 2\sqrt{(a+b+c)^2 - 3(ab+bc+ac)}}{6}$$

$$X = \frac{(a+b+c) \pm \sqrt{a^2+b^2+c^2+2ab+2bc+2ca-3ab-3bc}}{3}$$

$$X = \frac{(a+b+c) \pm \sqrt{a^2 + b^2 + c^2 - ab - bc - ca}}{3}$$

$$\left\{ \frac{(a+b+c)\pm\sqrt{a^2+b^2+c^2-ab-bc-ca}}{3} \right\}$$

1.20(a+b) x+(a+2b+c)x+b+c=0

Using
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$X = \frac{-(a+2b+c) \pm \sqrt{(a+2b+c)^2 + (a+b)(b+c)}}{2(a+b)}$$

$$x = \frac{-(a+2b+c)\pm\sqrt{(a+2b+c)^2-4(ab+ac+b+bc)}}{2(a+b)}$$

$$X = \frac{-(a+2b+c) \pm \sqrt{a^2+4b^2+c^2+4ab+4bc+2ac}}{-4ab-4ac-4b^2-4bc}$$

$$\chi = \frac{-(a+1b+c) \pm \sqrt{a^{2}+c^{2}-2ac}}{2(a+b)}$$

$$X = \frac{-(a+1b+c) \pm \sqrt{(a-c)^{2}}}{2(a+b)}$$

$$x = \frac{-(a+1b+c) \pm (a-c)}{2(a+b)}$$

$$X = \frac{-(a+2b+c)+a-c}{2(a+b)}, X = \frac{-(a+2b+c)-a+c}{2(a+b)}$$

$$y = \frac{-(a+2b+c)+a-c}{2(a+b)}$$

$$y = \frac{-(a+2b+c)+a-c}{2(a+b)}$$

$$X = \frac{-a-1b-c+a-c}{2(a+b)}, \quad X = \frac{-a-1b-c-a+c}{2(a+b)}$$

$$(3+2)(3-3) = 0$$

$$y + 2 = 0, \quad y - 3 = 0$$

$$y = -2b-2c$$

$$y = -2b-2c$$

$$x = \frac{-2b-2c}{2(a+b)}$$
, $x = \frac{-2b-1a}{2(a+b)}$ $y = -2$, $y = 3$

$$x = \frac{-2(b+c)}{2(a+b)}$$
, $x = \frac{-2(a+b)}{2(a+b)}$ Then $x'' = -2$ Then $x'' = 3$

$$X = -\frac{(b+c)}{a+b}, \quad X = -1$$

$$\left\{ -\frac{(b+c)}{a+b}, -1 \right\}$$

put
$$x^{4} = y$$
 then
$$y^{2} - y - 6 = 0$$
Factorizing

$$y^{2} + 2y - 3y - 6 = 0$$

$$y(y+2) - 3(y+2) = 0$$

$$y(y+2) - 3(y+2) = 0$$

$$(y+2)(y-3) = 0$$

$$y+2=0, y-3=0$$

$$y=-2, y=3$$

If
$$y = -2$$
, $y = 3$
Then $x^{4} = -2$ Then $x^{4} = 3$
 $(x^{4})^{4} = (-2)^{4}$, $(x^{4})^{4} = (3)^{4}$

$$x = 16$$
, $x = 81$
 $\{16, 81\}$

Tama Na 2