

EXERCISE 1.5

① Given that

$$f(x) = \begin{cases} \frac{\sqrt{2x+5} - \sqrt{x+7}}{x-2}, & x \neq 2 \\ k, & x = 2 \end{cases}$$

$$k = ?$$

Here  $f(2) = k$  (given)

$\therefore f(x)$  is continuous at  $x=2$

$$\therefore \lim_{x \rightarrow 2} f(x) = f(2) \quad \left( \frac{0}{0} \right) \text{ form}$$

$$\Rightarrow \lim_{x \rightarrow 2} \frac{\sqrt{2x+5} - \sqrt{x+7}}{x-2} = k$$

$$\Rightarrow \lim_{x \rightarrow 2} \frac{\sqrt{2x+5} - \sqrt{x+7}}{x-2} \times \frac{\sqrt{2x+5} + \sqrt{x+7}}{\sqrt{2x+5} + \sqrt{x+7}} = k$$

$$\Rightarrow \lim_{x \rightarrow 2} \frac{(\sqrt{2x+5})^2 - (\sqrt{x+7})^2}{(x-2)(\sqrt{2x+5} + \sqrt{x+7})} = k$$

$$\Rightarrow \lim_{x \rightarrow 2} \frac{(2x+5) - (x+7)}{(x-2)(\sqrt{2x+5} + \sqrt{x+7})} = k$$

$$\Rightarrow \lim_{x \rightarrow 2} \frac{2x+5-x-7}{(x-2)(\sqrt{2x+5} + \sqrt{x+7})} = k$$

$$\Rightarrow \lim_{x \rightarrow 2} \frac{(x-2)}{(x-2)(\sqrt{2x+5} + \sqrt{x+7})} = k$$

$$\Rightarrow \lim_{x \rightarrow 2} \frac{1}{\sqrt{2x+5} + \sqrt{x+7}} = k$$

$$\Rightarrow \frac{1}{\lim_{x \rightarrow 2} [\sqrt{2x+5} + \sqrt{x+7}]} = k$$

$$\Rightarrow \frac{1}{\sqrt{2(2)+5} + \sqrt{2+7}} = k$$

$$\Rightarrow \frac{1}{\sqrt{9} + \sqrt{9}} = k \Rightarrow \frac{1}{3+3} = k \Rightarrow \frac{1}{6} = k$$

Ans.

① (i)  $x^2 + y^2 = 9$

$$\Rightarrow y^2 = 9 - x^2$$

$$\Rightarrow y = \pm \sqrt{9 - x^2}$$

$$\Rightarrow y \text{ will be real if } 9 - x^2 \geq 0$$

$$\Rightarrow 9 \geq x^2 \Rightarrow x^2 \leq 9$$

$$\Rightarrow \pm x \leq 3$$

$$\Rightarrow x \leq 3, -x \leq 3$$

$$\Rightarrow x \leq 3, x \geq -3$$

$$\Rightarrow x \leq 3, -3 \leq x$$

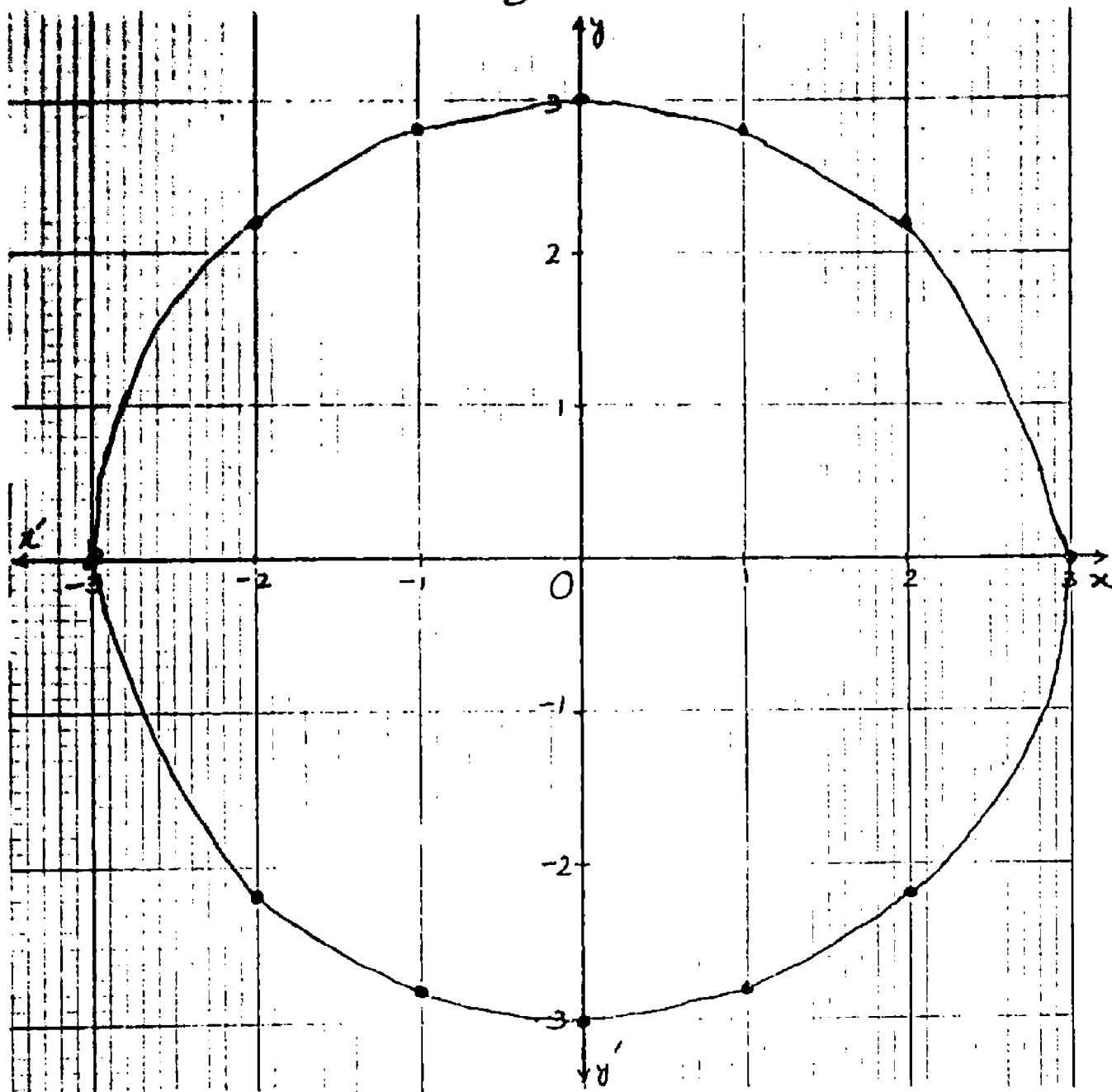
$$\Rightarrow -3 \leq x \leq 3$$

Table :

x	-3	-2	-1	0	1	2	3
y	0	$\pm 2.2$	$\pm 2.8$	$\pm 3$	$\pm 2.8$	$\pm 2.2$	0

Scale : One big square along x-axis = 1 unit

One big square along y-axis = 1 unit



(ii)  $\frac{x^2}{16} + \frac{y^2}{4} = 1$

Multiplying by 16, we get

$$x^2 + 4y^2 = 16 \Rightarrow 4y^2 = 16 - x^2 \Rightarrow y^2 = \frac{16 - x^2}{4} \Rightarrow y = \pm \frac{\sqrt{16 - x^2}}{2}$$

$$\Rightarrow y \text{ will be real if } 16 - x^2 \geq 0 \Rightarrow 16 \geq x^2 \Rightarrow x^2 \leq 16$$

$$\Rightarrow -4 \leq x \leq 4$$

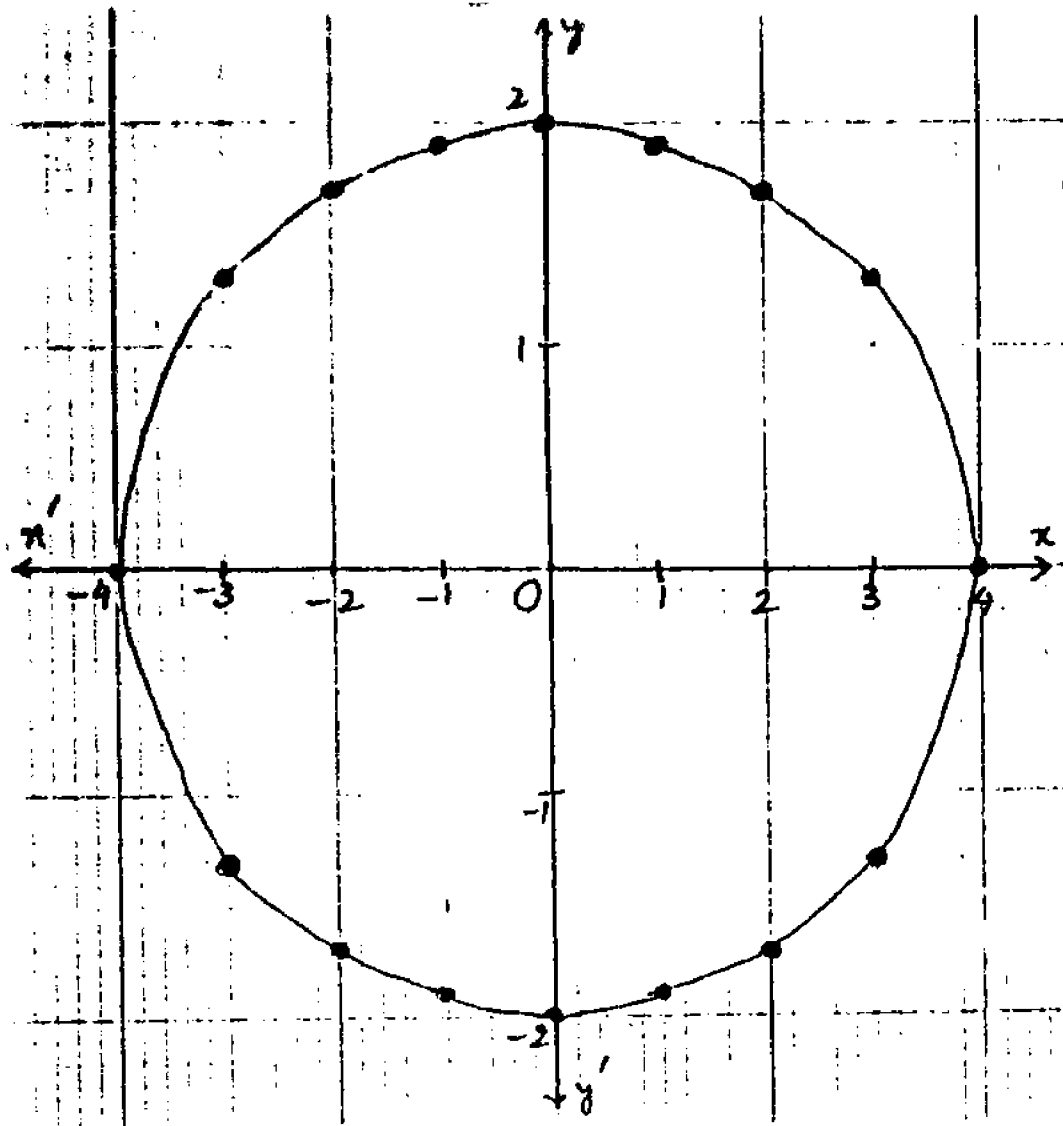
Table:

x	-4	-3	-2	-1	0	1	2	3	4
y	0	$\pm 1.3$	$\pm 1.7$	$\pm 1.9$	$\pm 2$	$\pm 1.9$	$\pm 1.7$	$\pm 1.3$	0

Scale:

One big square along x-axis = 2 units

One big square along y-axis = 1 unit.



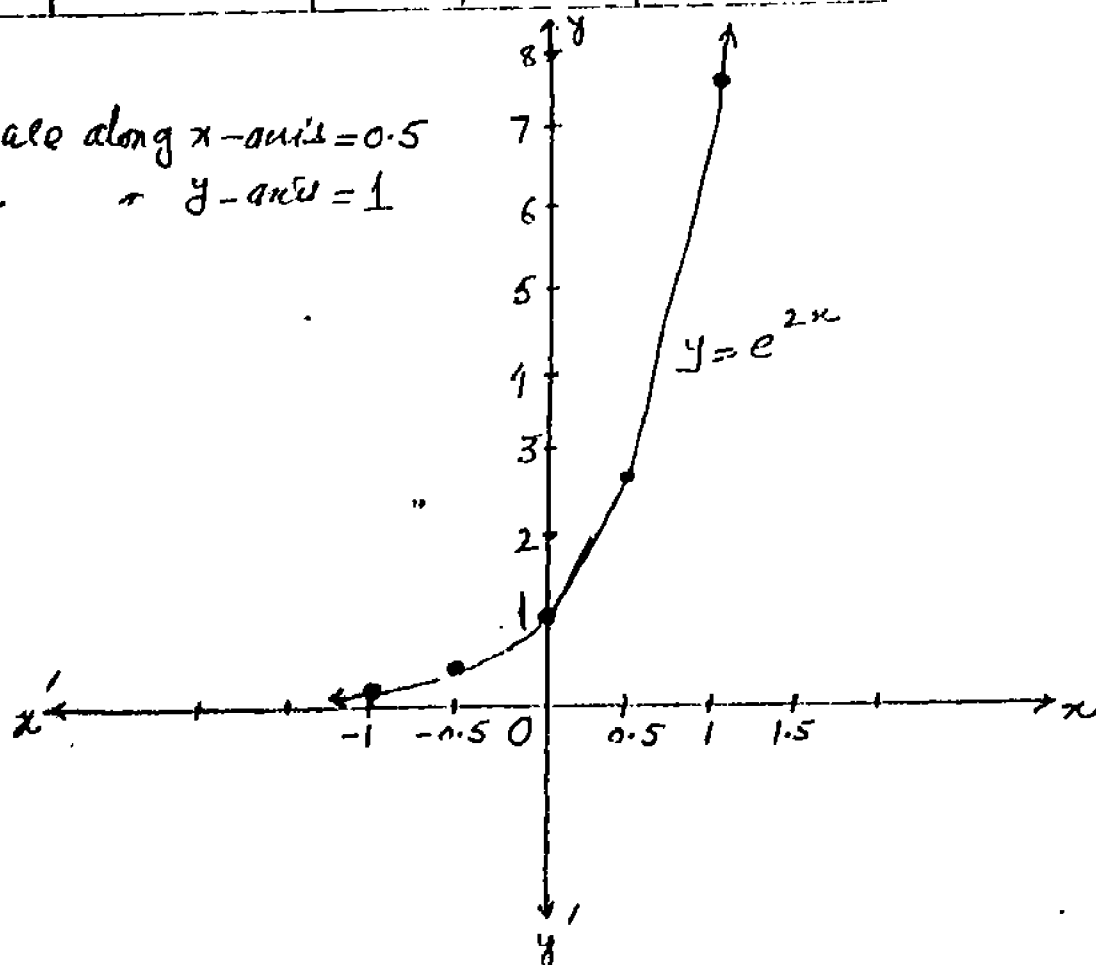
(iii)  $y = e^{2x}$

$x$	-1	-0.5	0	0.5	1
$y$	0.1	0.4	1	2.7	7.4

Scales:-

One big square along  $x$ -axis = 0.5

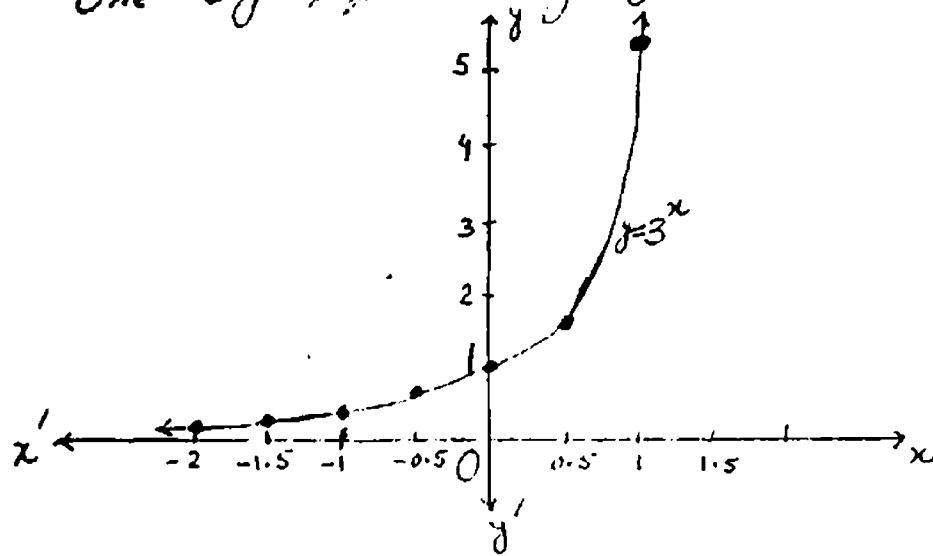
" " " " "  $y$ -axis = 1



Q.  $y = 3^x$

$x$	-2	-1.5	-1	-0.5	0	0.5	1	1.5
$y$	0.1	0.2	0.3	0.6	1	1.7	3	5.2

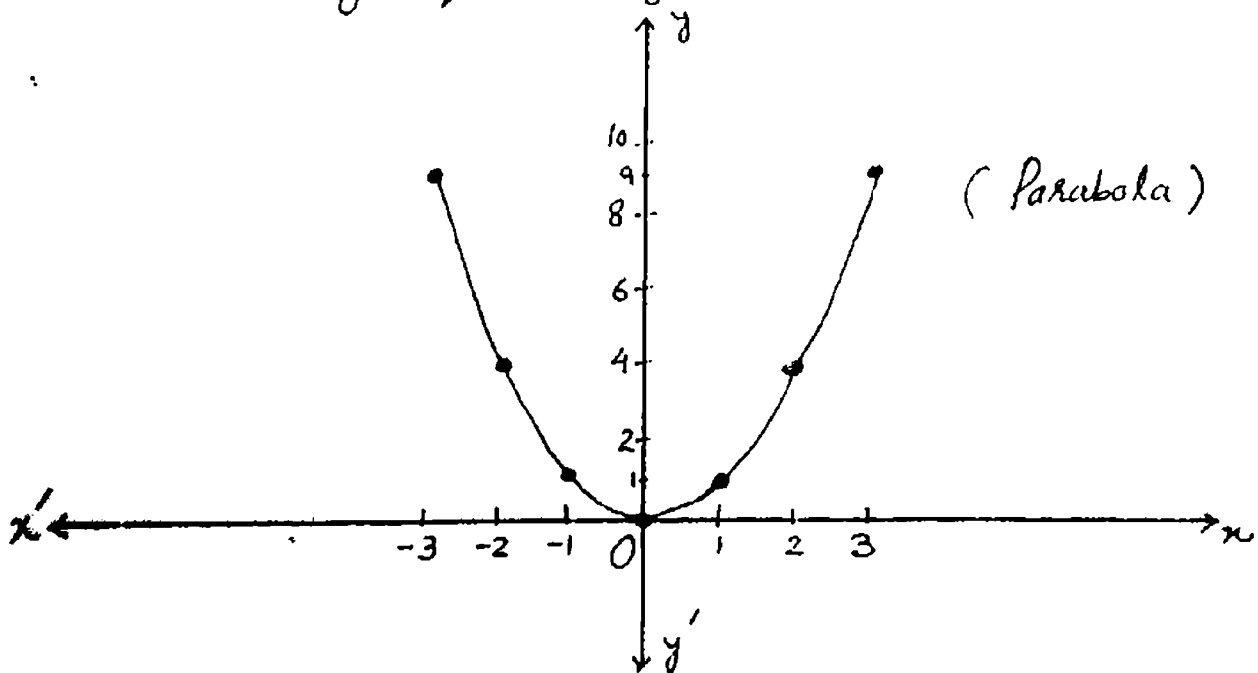
Scale: One big square along  $x$ -axis = 0.5 units  
One big square along  $y$ -axis = 1 unit



② (i)  $x = t, y = t^2, -3 \leq t \leq 3$

$t$	-3	-2	-1	0	1	2	3
$x$	-3	-2	-1	0	1	2	3
$y$	9	4	1	0	1	4	9

Scale: One big square along  $x$ -axis = 1 unit  
One big square along  $y$ -axis = 2 units

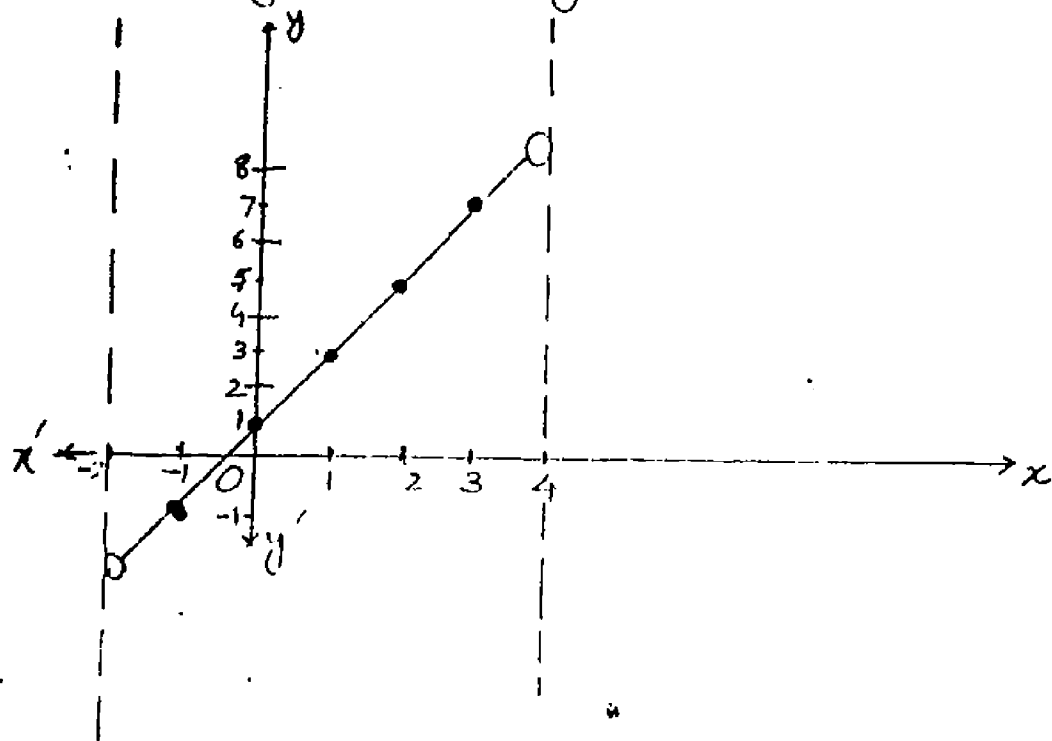


(ii)  $x = t-1$ ,  $y = 2t-1$ ,  $-1 < t < 5$

$t$	0	1	2	3	4
$x$	-1	0	1	2	3
$y$	-1	1	3	5	7

Scale: One big square along  $x$ -axis = 1 unit

One big square along  $y$ -axis = 2 units



(iii)  $x = \sec \theta$ ,  $y = \tan \theta$ , where  $\theta$  is a parameter.

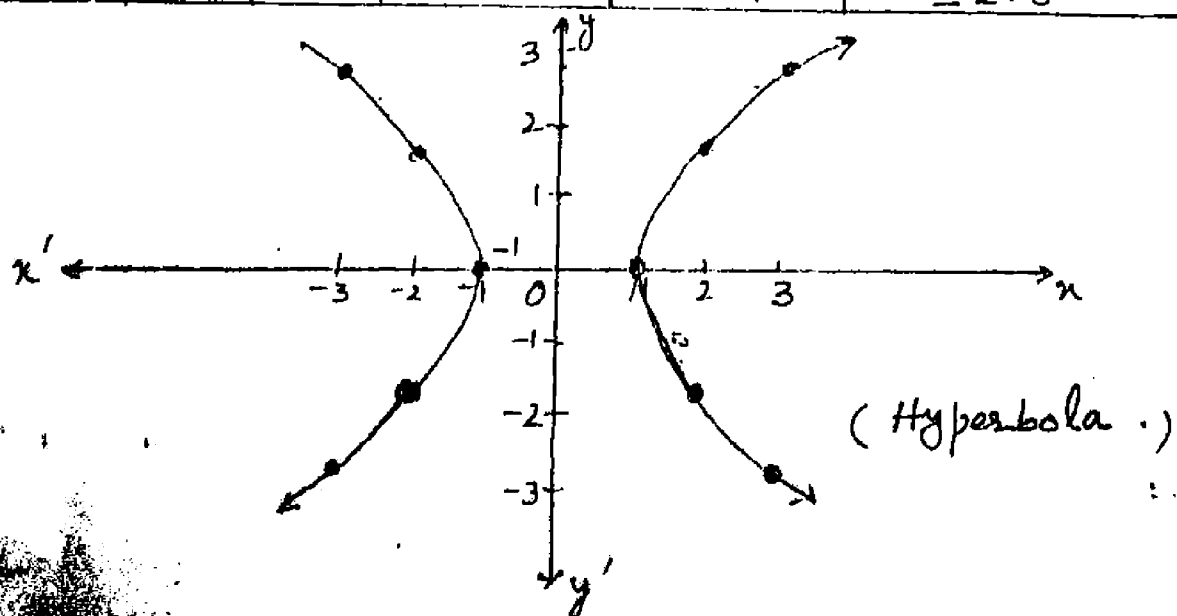
$$1 + \tan^2 \theta = \sec^2 \theta \Rightarrow 1 = \sec^2 \theta - \tan^2 \theta$$

$$\Rightarrow 1 = x^2 - y^2 \Rightarrow y^2 = x^2 - 1 \Rightarrow y = \pm \sqrt{x^2 - 1}$$

$$\Rightarrow y \text{ will be real if } x^2 - 1 \geq 0 \Rightarrow x^2 \geq 1$$

$$\Rightarrow \pm x \geq 1 \Rightarrow x \geq 1, -x \geq 1 \Rightarrow x \geq 1, x \leq -1$$

$x$	-3	-2	-1	1	2	3
$y$	$\pm 2.8$	$\pm 1.7$	0	0	$\pm 1.7$	$\pm 2.8$



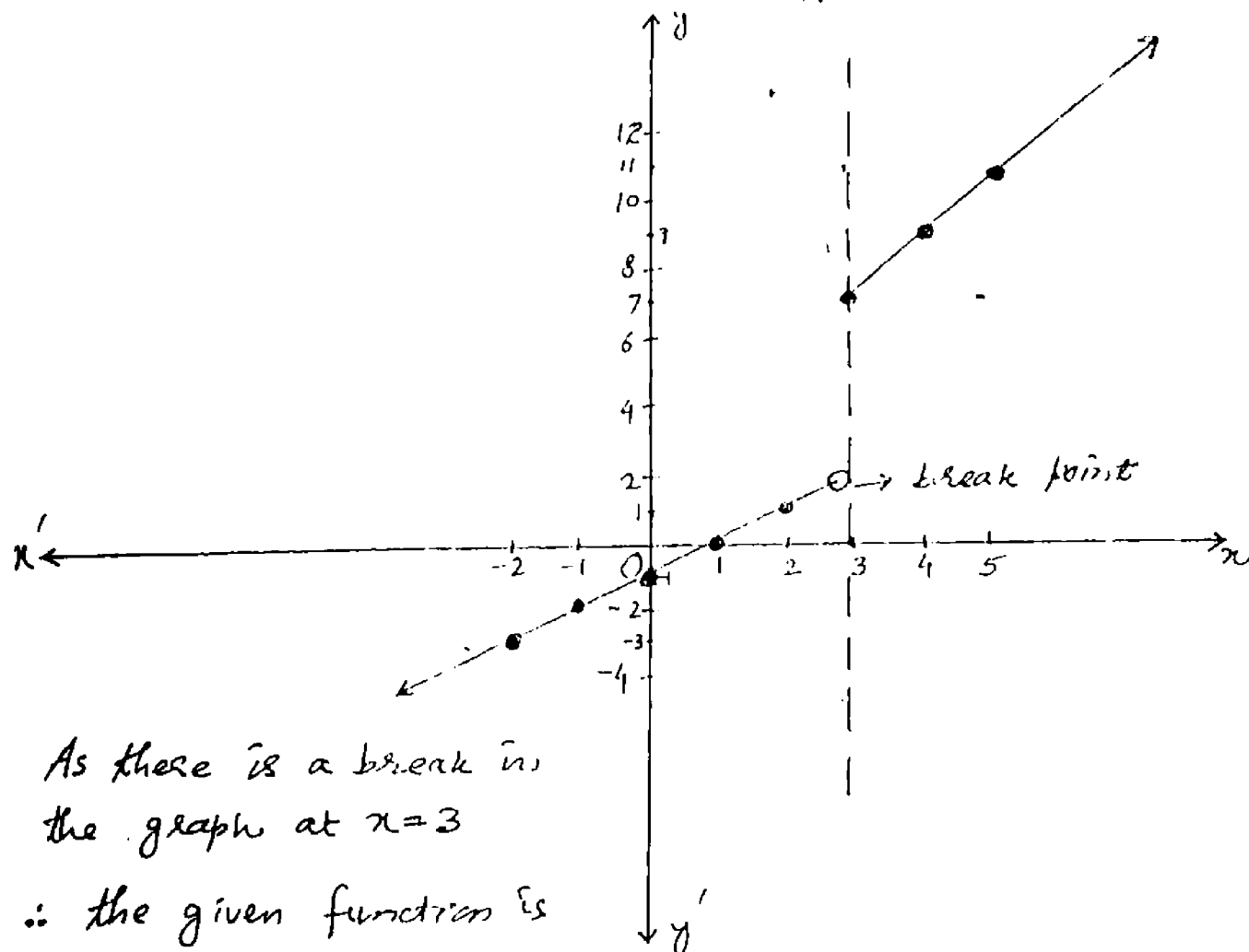
③ (i)  $y = \begin{cases} x-1 & \text{if } x < 3 \\ 2x+1 & \text{if } x \geq 3 \end{cases}$

Table for  $y = x-1$ ,  $x < 3$  is

$x$	-2	-1	0	1	2
$y$	-3	-2	-1	0	1

Table for  $y = 2x+1$ ,  $x \geq 3$  is

$x$	3	4	5
$y$	7	9	11



As there is a break in the graph at  $x=3$   
 $\therefore$  the given function is discontinuous at  $x=3$

(ii)  $y = \frac{x^2 - 4}{x - 2}$ ,  $x \neq 2$   
 $= \frac{(x-2)(x+2)}{x-2}$ ,  $x \neq 2$   
 $= x+2$ ,  $x \neq 2$

The given function is not defined at  $x=2$

$x$	-3	-2	-1	0	1	3	4	5
$y$	-1	0	1	2	3	5	6	7

Scale: One big square along  $x$ -axis = 2 units  
 One big square along  $y$ -axis = 2 units.

Q.1)  $y = \sin 2x$ ,  $-\pi \leq x \leq \pi$

We draw the graphs of

$y = x$  and  $y = \sin 2x$ .

For  $y = \sin 2x$

$x$	$-180^\circ$	$-150^\circ$	$-120^\circ$	$-90^\circ$	$-60^\circ$	$-30^\circ$	$0^\circ$	$30^\circ$	$60^\circ$	$90^\circ$	$120^\circ$	$150^\circ$	$180^\circ$
$y$	0	0.9	+0.9	0	-0.9	-0.9	0	0.9	0.9	0	-0.9	-0.9	0

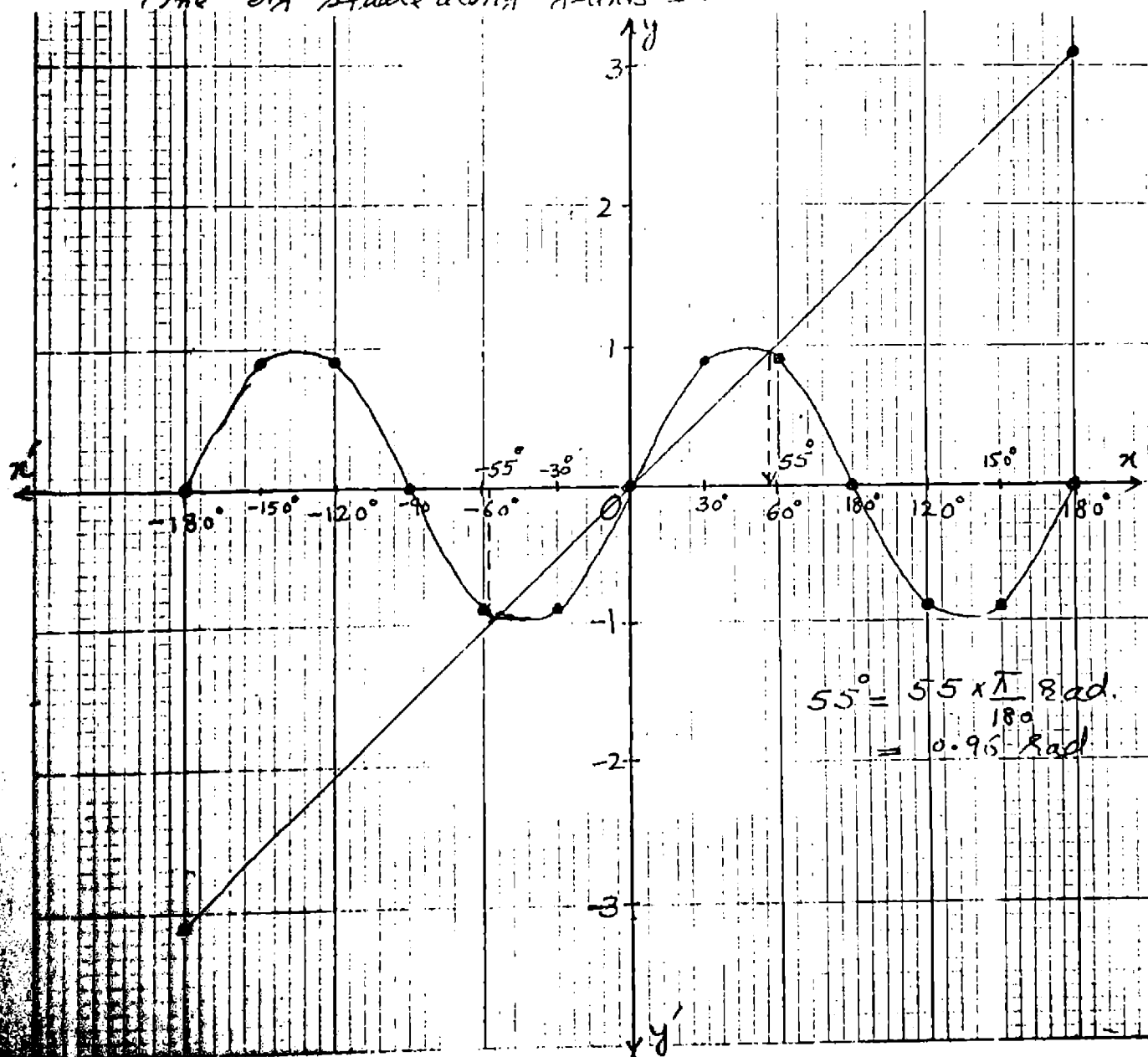
For  $y = x$

$x$	$-180^\circ$	0	$180^\circ$
$y$	-3.1	0	3.1

$180^\circ = \pi \text{ Rad} = 3.14 \text{ Rad}$ .

Scale One big square along  $x$ -axis =  $60^\circ$

One big square along  $y$ -axis = 1 unit.



$y = x$  cuts the curve  $y = \sin 2x$  at  $x = -55^\circ, 0, 55^\circ$   
 $\therefore \text{S.S.} = \{-55^\circ, 0, 55^\circ\} = \{-0.96, 0, 0.96\}$

gwp  
(ii)  $\frac{x}{2} = \cos x$  ,  $-\pi \leq x \leq \pi$

We draw the graphs of  $y = \frac{x}{2}$  and  $y = \cos x$

For  $y = \cos x$

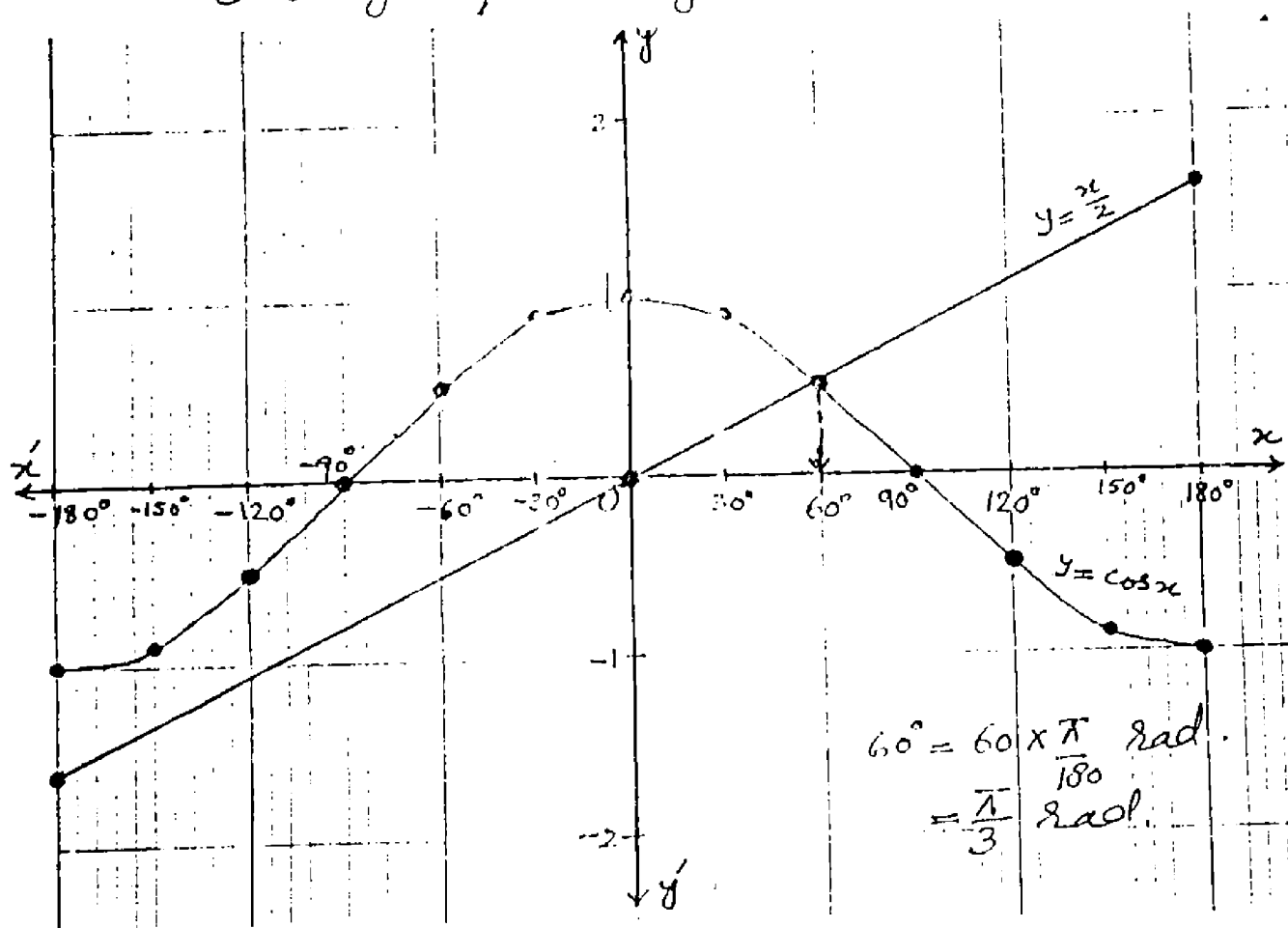
$x$	$-180^\circ$	$-150^\circ$	$-120^\circ$	$-90^\circ$	$-60^\circ$	$-30^\circ$	$0^\circ$	$30^\circ$	$60^\circ$	$90^\circ$	$120^\circ$	$150^\circ$	$180^\circ$
$y$	-1	-0.9	-0.5	0	0.5	0.9	1	0.9	0.5	0	-0.5	-0.9	-1

For  $y = \frac{x}{2}$

$x$	$-180^\circ$	$0^\circ$	$180^\circ$
$y$	-1.6	0	1.6

Scale: One big square along  $x$ -axis =  $60^\circ$

One big square along  $y$ -axis = 1 unit.



The line  $y = \frac{x}{2}$  cuts the curve  $y = \cos x$  at  $x = 60^\circ$

$$\therefore \text{S.S.} = \{60^\circ\} = \left\{ \frac{\pi}{3} \right\} \quad \text{Ans.}$$

(iii)  $2x = \tan x$  ,  $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$

We draw the graphs of  $y = 2x$  and  $y = \tan x$

For  $y = \tan x$

$x$	$-90^\circ$	$-75^\circ$	$-60^\circ$	$-45^\circ$	$-30^\circ$	$-15^\circ$	$0^\circ$	$15^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$75^\circ$	$90^\circ$
$y$	$\infty$	-3.7	-1.7	-1	-0.6	-0.3	0	0.3	0.6	1	1.7	3.7	$\infty$



For  $y = 2x$

$x$	$-90^\circ$	$0$	$90^\circ$
$y$	$-3.1$	$0$	$3.1$

Scale: One big square along  $x$ -axis  $= 30^\circ$

One big square along  $y$ -axis  $= 1$  unit

