

In the name of God

Producer:
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Subject:
different of Bysection method whith using monte
carlo and normal bysection method.

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Issue: We have to execute the two-part method of rooting with the help of Monte Carlo method 100 times and save the number of repetitive steps and a random number until we finally reach the root with the desired accuracy each time we execute and then get the average of these 100 repetitions.

Our error is 10^{-5} .

Solve:

At the first we have a function with an interval.

Then we should make the c have a uniform distribution with $a = \min$ of interval, $b = \max$ of interval.

Then we should check this:

Step1: if $f(c) = 0$ or $f(c) \leq \text{error}$, set $\alpha = c$, else check step2&3.

Step2: if $f(c)*f(a) < 0$, set $b = c$,

Step3: if $f(c)*f(a) > 0$, set $a = c$, then go to step1.

We do above algorithm until step1 condition is True.

And we do this for bisection method with select $c = (a+b)/2$ in each round.

Now we can run our simulation for the above algorithm.

```
> rm(list=ls())
> n=100
> q=8
> M<-c()
> e<-10^-q
> for(i in 1:n){
+   baze<-c(0,1)
+   a<-baze[1];b<-baze[2]
+   f<-function(c){
+     f=c-(1/2)*cos(c)
+   }
+   c<-runif(1,a,b)
+ }
```

```

+   m=1
+   while((abs(b-a))>=(e)){
+       c<-runif(1,a,b)
+       if(f(c)*f(a)<0){b<-c
+       }else{
+           a<-c}
+       m<-m+1}
+   M[i]<-m}
>
> print(paste("the last value c in our function
is :",f(c)))
[1] "the last value c in our function is : 7.424
29451250359e-11"
> print(paste("the mean of M is :",mean(M)))
[1] "the mean of M is : 38.81"
>
>
> e<-10^-q
> r=0
> baze<-c(0,1)
> a<-baze[1];b<-baze[2]
> c<-(a+b)/2
> while((abs(b-a))>=(e)){
+   c<-(a+b)/2
+   if(f(c)*f(a)<0){b<-c
+   }else{
+       a<-c}
+   r<-r+1}
> print(r)
[1] 27

```

Conclusion:

As we have seen, the number of steps in bysection with the help of Mont Carlo has more steps than the simple bysection method($r < \text{mean}(m)$)