

I-CHIP PS-1

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→ ~~We will not~~ as we also have to find the negatives of ~~sum~~ some numbers and also find difference of ~~su~~ 2 numbers. So we will write the negative numbers in 2's complement form let our 8 bit number be x . So its negative in 2's complement form is

$$-x = \sim x + 0000-0001$$

→ Now we will see the proof of all the functions according to their opcode.

① $\theta = 0$ opcode = 101010

$$zn = 1 \Rightarrow x = 0000-0000 \quad ny = 0 \Rightarrow y = 0000-0000$$

$$nx = 0 \Rightarrow x = 0000-0000 \quad f = 1 \Rightarrow x+y = 0000-0000$$

$$zy = 1 \Rightarrow y = 0000-0000 \quad no = 0 \Rightarrow \boxed{\theta = x+y = 0000-0000}$$

② $\theta = 1$ opcode = 111111

$$zn = 1 \Rightarrow x = 0000-0000$$

$$nx = 1 \Rightarrow x = 1111-1111$$

$$zy = 1 \Rightarrow y = 0000-0000$$

$$ny = 1 \Rightarrow y = 1111-1111$$

$$f = 1 \Rightarrow x+y = \overset{\text{neglect}}{1}-1111-1110$$

$$no = 1 \Rightarrow \sim(x+y) = 0000-0001$$

$$\boxed{\theta = 0000-0001}$$

③ ~~$\theta = -1$~~ opcode = 111 010

$zx = 1 \Rightarrow x = 0000_0000$

$nx = 1 \Rightarrow x = 1111_1111$

$zy = 1 \Rightarrow y = 0000_0000$

$ny = 0 \Rightarrow y = 0000_0000$

$f = 1 \Rightarrow x + y = 1111_1111$

$no = 0 \Rightarrow \boxed{\theta = 1111_1111}$

↳ which is -1 in 2's complement form

④ $\theta = x$ opcode = 001100

$zx = 0 \Rightarrow x = x$

$f = 0 \Rightarrow x \& y = x$

$nx = 0 \Rightarrow x = x$

$no = 0 \Rightarrow \boxed{\theta = x}$

$zy = 1 \Rightarrow y = 0000_0000$

$ny = 1 \Rightarrow y = 1111_1111$

⑤ $\theta = y$ opcode = 110000

$zx = 1 \Rightarrow x = 0000_0000$

$f = 0 \Rightarrow x \& y = y$

$nx = 1 \Rightarrow x = 1111_1111$

$no = 0 \Rightarrow \boxed{\theta = y}$

$zy = 0 \Rightarrow y = y$

$ny = 0 \Rightarrow y = y$

⑥ $\theta = \sim x$ opcode = 001101

As derived in ④ for x we only have to complement it. So we only have to change no bit to 1

⑦ $\theta = \sim y$ opcode = 110001

Similar to 6 we only have to change no bit to 1 in opcode of ⑤

⑧ $\theta = -x$ opcode = 001111

$zx = 0 \Rightarrow x = x$

$f = 1 \Rightarrow x + y = x + 1111 - 1111$

$nx = 0 \Rightarrow x = x$

$no = 1 \Rightarrow \theta = \sim(x + 1111 - 1111)$

$zy = 1 \Rightarrow y = 0000 - 0000$

$ny = 1 \Rightarrow y = 1111 - 1111$

Now $1111 - 1111$ is -1 in 2's complement form.

$\theta = \sim(x - 1)$

Now using identity defined in beginning

$-x = \sim x + 1$

Put $x = x - 1$

$\Rightarrow -(x - 1) = \sim(x - 1) + 1$

$-x + 1 = \sim(x - 1) + 1$

$\sim(x - 1) = -x$

$\Rightarrow \boxed{\theta = -x}$

⑨ $\theta = -y$ opcode = 110011

Similar as done in ⑧ only we have to get y in place of x . So we have to set $zx = 0$, $nx = 0$, $zy = 1$, $ny = 1$ and the rest will be same ($f = 1$, $no = 1$).

⑩ $\theta = x + 1$ opcode = 011111

$zx = 0 \Rightarrow x = x$

$ny = 1 \Rightarrow y = 1111 - 1111$

$nx = 1 \Rightarrow x = \sim x$

$f = 1 \Rightarrow x + y = \sim x + 1111 - 1111$

$zy = 1 \Rightarrow y = 0000 - 0000$

$no = 1 \Rightarrow \theta = \sim(\sim x + 1111 - 1111)$

Now $1111 - 1111$ is -1 in 2's complement form

So $\theta = \sim(\sim x - 1)$

Now $-x = \sim x + 1 \Rightarrow \sim x = -x - 1$

$\Rightarrow \theta = \sim(-x - 1 - 1) = \sim(-x - 2)$

Put $x = -x - 2$ in the identity

$-(-x - 2) = \sim(-x - 2) + 1$

$x + 2 = \sim(-x - 2) + 1$

$\sim(-x - 2) = \boxed{x + 1}$

(11) $\theta = y + 1$ opcode = 110111

This function is similar to the function in part (10) just we have to change the z_x, n_x, z_y and n_y control input to get y in place of x .
So $z_x = 1, n_x = 1, z_y = 0, n_y = 1$

(12) $\theta = x + 1$ opcode = 0001110

$z_x = 0 \Rightarrow x = x$

$n_x = 0 \Rightarrow x = x$

$f = 1 \Rightarrow n + y = x + 1111 - 1111$

$n_0 = 0 \Rightarrow \theta = x + 1111 - 1111$

$z_y = 1 \Rightarrow y = 0000 - 0000$

$n_y = 1 \Rightarrow y = 1111 - 1111$

• Now $1111 - 1111$ is -1 in 2's complement form
So $\boxed{\theta = x - 1}$

(13) $\theta = y - 1$ opcode = 110010

$z_x = 1 \Rightarrow x = 0000 - 0000$

$n_x = 1 \Rightarrow x = 1111 - 1111$

$n_y = 0 \Rightarrow y = y$

$f = 1 \Rightarrow n + y = y + 1111 - 1111$

$z_y = 0 \Rightarrow y = y$

$n_0 = 0 \Rightarrow \theta = y + 1111 - 1111$

• Now $1111 - 1111$ is -1 in 2's complement form
So $\boxed{\theta = y - 1}$

(14) $\theta = n + y$ opcode = 000010

$z_x = 0 \Rightarrow x = x$

$n_x = 0 \Rightarrow x = x$

$n_y = 0 \Rightarrow y = y$

$f = 1 \Rightarrow n + y = n + y$

$z_y = 0 \Rightarrow y = y$

$n_0 = 0 \Rightarrow \boxed{\theta = n + y}$

(15) $\theta = x - y$ opcode = 010011

$z_x = 0 \Rightarrow x = x$

$n_x = 1 \Rightarrow x = \sim x$

$f = 1 \Rightarrow n + y = \sim x + y$

$n_0 = 1 \Rightarrow \theta = \sim(\sim x + y)$

$z_y = 0 \Rightarrow y = y$

$n_y = 0 \Rightarrow y = y$

- Now using the identity $\neg x = \neg x + 1$
 $\neg x = -x - 1$

$$0 = \neg(-x - 1 + y)$$

Again using the identity

$$\neg(-x - 1 + y) = -(-x - 1 + y) - 1$$

$$= x + 1 - y - 1$$

$$\boxed{0 = x - y}$$

(16) $0 = y - x$ opcode = 000111

$$zn = 0 \Rightarrow x = x$$

$$ny = 1 \Rightarrow y = \neg y$$

$$nx = 0 \Rightarrow x = x$$

$$f = 1 \Rightarrow x + y = x + \neg y$$

$$zy = 0 \Rightarrow y = y$$

$$no = 1 \Rightarrow 0 = \neg(x + \neg y)$$

- Now using the identity
 $\neg x = \neg x + 1$

$$\neg y = -y - 1$$

Putting $x = x + (-y - 1)$ in identity

$$\neg(x + (-y - 1)) = \neg(x - y - 1) + 1$$

$$\neg(x - y - 1) = -x + y + 1$$

$$\boxed{0 = y - x}$$

(17) $0 = x \& y$ opcode = 000000

$$zn = 0 \Rightarrow x = x$$

$$ny = 0 \Rightarrow y = y$$

$$nx = 0 \Rightarrow x = x$$

$$f = 0 \Rightarrow x \& y = x \& y$$

$$zy = 0 \Rightarrow y = y$$

$$no = 0 \Rightarrow \boxed{0 = x \& y}$$

(18) $0 = x | y$ opcode = 010101

$$zn = 0 \Rightarrow x = x$$

$$ny = 1 \Rightarrow y = \neg y$$

$$nx = 1 \Rightarrow x = \neg x$$

$$f = 0 \Rightarrow x \& y = \neg x \& \neg y$$

$$zy = 0 \Rightarrow y = y$$

$$no = 1 \Rightarrow 0 = \neg(\neg x \& \neg y)$$

So using De Morgan's Law

$$\boxed{0 = x | y}$$