6. A Stack Architecture as Target

Emil Sekerinski, McMaster University, updated April 2022

This notebook depends on three packages that need to be installed if the notebook is run locally:

- WABT, the WebAssembly Binary Toolkit
- pywasm, a WebAssembly interpreter written in Python
- · Wasmer, a collection of WebAssembly compilers with a Python embedding

This chapter extends the P0 compiler with code generation for WebAssembly. Like CLI (Common Language Infrastructure, the standard used for .NET) and JVM (Java Virtual Machine), WebAssembly is a *virtual* architecture: WebAssembly code needs either to be interpreted or compiled to *native* code. At the time of writing, WebAssembly can be interpreted with pywasm, can be compiled through Wasmer with a number of compilers, and can be executed in all common web browsers by *just-in-time* compilation. However, there is nothing web-specific about WebAssembly: its purpose is to allow safe and efficient execution of code that can originate from untrusted sources.

WebAssembly differs from the currently dominant RISC (Reduced Instruction Set Computer) architectures in a number of ways:

- Stack architecture: all operands of operations have to be pushed on a stack, there are no registers.
- Byte code: Instructions are encoded as single bytes, rather than whole words.
- Statically typed: type-checking ensures that the types of operands and operations match.
- Block-structured: there are constructs for if-statements and loops; jumps to arbitrary locations are not possible.
- Non-uniform store: rather than having memory as a flat sequenced of addressable bytes, there are several stores that are all
 addressed differently.

These notes introduce WebAssembly to the extent needed for P0.

WebAssembly programs are composed of *modules* that may depend on other modules and may interact with a *host environment*, like a web browser or another programming language. Modules are stored in two equivalent and mutually convertible forms,

- in binary .wasm files, with a flat sequences of instructions that each takes one byte,
- in textual .wat files with instructions in textual form where some locations can be names rather than numbers.

For readability we use the textual form and return to the details of the binary form.

WebAssembly Stores

WebAssembly programs distinguish different kind of stores,

- the code, where the program resides,
- the memory, where variables with computed locations (e.g. arrays) are stored,
- the global store, where initialized global variables and constants are stored,
- the stack, where operands of instructions, call frames with local variables, and certain labels are stored.

The code is *immutable*: there is no way to manipulate the code once it is loaded by the virtual machine. While we think of the code as being the WebAssembly program itself, an implementation is free to represent the programs in another form or to compile the program to machine code; except for efficiency, this would not be observable.

The code is made up of a collection of procedures, called *functions*. Functions are numbered and each function is a sequence of instructions. If a program has FN functions, the code is abstractly represented by:

```
var c: [0 ... FN) \rightarrow seq(byte)
```

The memory is a contiguously addressed array of bytes; its size is specified in multiples of *pages* of 2¹⁶ bytes. Its initial size is specified in a WebAssembly file but can explicitly grow. Bytes in the memory can be accessed arbitrarily. Abstractly, the memory is:

```
var m: [0 .. MemSize) \rightarrow byte
```

In WebAssembly, the value and result parameters of functions are typed as are local variables, global variables, and intermediate results on the stack. The only exception is the memory, which allows bytes to be interpreted as needed. The only types are 32 and 64 bit integer and floating-point numbers: i32, i64, f32, f64. There are no booleans, enumerations, arrays, tuples, lists, records, unions, or classes. These have to be either expressed in terms of supported types or mapped to the memory.

The global store is an array of typed values, which are one of i32, i64, f32, f64.

```
var q: [0 .. GlobalVars) → Value
```

The stack can only be accessed through specific arithmetic instructions and control flow instructions. Abstractly, the stack is an array of values; the *stack pointer* sp points to the next available entry:

```
var s: [0 .. StackSize) → Value var sp: [0 .. StackSize] = 0
```

WebAssembly Instructions

Operands of instructions have first to be pushed on the stack. The instructions to push a constant on the stack are $i32.const\ n$, $i64.const\ n$, $f32.const\ f$, $f64.const\ f$. Arithmetic instructions specify the type of the operands, for example for addition i32.add, i64.add, f32.add, f64.add. For P0 the sole WebAssembly type in the generated code is i32, so the P0 expression 3+4 corresponds to:

```
i32.const 3
i32.const 4
i32.add
```

To illustrate typing, the code

```
i32.const 3
i64.const 4
i32.add
```

is not type-correct: the *validation* of a WebAssembly program ensures that entries of the same type are popped as were pushed, which WebAssembly allows to do statically. That is, above code will be rejected when loaded into the virtual machine. Likewise, trying to pop from the empty stack is also detected during validation, e.g. if a program starts with:

```
i32.const 3 i32.add
```

The if ... else ... end instruction pops the top element from the stack as the condition. If it is not zero, the instructions following if are executed, otherwise those following else. For example, if x, y, m are local variable, following P0 statement can be translated as to the right.

```
if x > y then
    m := x
else
    m := y
```

Consider following P0 procedure and its WebAssembly translation to the right:

```
procedure QuotRem(x, y: integer)
    var q, r: integer
    q := 0; r := x
    while r ≥ y do
        r := r - y; q := q + 1
    write(q); write(r)
```

WebAssembly functions can take value and result parameters. Names have to be prefixed with \$. The code declares function \$QuotRem with value parameters \$x and \$y and local variables \$q and \$r , all of type i32 . Parameters and local variable are accessed identically with local.set and local.get instructions: local.set x removes the top element from the stack and stores it at the location named x on the stack, which must have been declared to be of the same type; local.get x reads the local variable from the location named x on the stack and pushed it on top of the stack.

```
local.set $m
(func $QuotRem (param $x i32) (param $y i32)
  (local $q i32)
  (local $r i32)
  i32.const 0
  local.set $q
  local.get $x
  local.set $r
  loop $label0
    local.get $r
    local.get $y
    i32.ge_s
    if
      local.get $r
      local.get $y
      i32.sub
      local.set $r
      local.get $q
      i32.const 1
      i32.add
      local.set $q
      br $label0
    end
  end
  local.get $q
  call $write
  local.get $r
  call $write
```

local.get \$x

local.get \$y

local.get \$x

local.set \$m

local.get \$y

i32.gt s

if

- within block l ... end a branch instruction br l will transfer control to the end of the construct, i.e. the instruction following end;
- within loop l ... end a branch instruction br l will transfer control to the beginning of the construct, i.e. the instruction following loop l.

WebAssembly allows i32 values to be interpreted as either signed or unsigned 32-bit integers: the instruction i32.lt_s performs a signed comparison and pushes 1 or the stack if the result is true and 0 otherwise. The instruction br_if l transfers control to the block or loop instruction labelled l if the top of the stack is not zero. Note that it is impossible to branch inside a block or loop, branches can only go outwards.

Functions are called by pushing first all arguments on the stack, calling the function, and the popping the results from the stack. Thus the call write(q) first pushes q and then calls \$write, which is assumed to be defined elsewhere.

The grammar for WebAssembly function definitions, to the extent needed for P0, is:

```
num ::= digit {digit}
int ::= [ '-' ] num
name ::= '$' (letter | digit) {letter | digit}
num_type ::= "i32" | "i64"
func ::= "(" "func" name func_type { local } { instr } ")"
func_type ::= { "(" "param" name num_type ")" } { "(" "result" num_type ")" }
local ::= "(" "local" name num type ")"
instr ::= "i32.const" int | "i64.const" int |
           "i32.add" | "i64.add" | "i32.sub" | "i64.sub" | "i32.mul" | "i64.mul" |
           "i32.div_s" | "i64.div_s" | "i32.rem_s" | "i64.rem_s" |
"i32.eqz" | "i64.eqz" | "i32.eq" | "i64.eq" | "i32.ne" | "i64.ne" |
           "i32.lt_s" | "i64.lt_s" | "i32.gt_s" | "i64.gt_s"
           "i32.le s" | "i64.le s" | "i32.ge s" | "i64.ge s"
           "i32.load" "offset" "=" num | "i32.load" "offset" "=" num |
           "i32.store" "offset" "=" num | "i32.store" "offset" "=" num |
           "global.get" name
           "global.set" name |
           "local.get" name |
           "local.set" name
           "block" name { instr } "end" |
           "loop" name { instr } "end" |
           "if" { instr } [ "else" { instr } ] "end" |
           "br" name |
           "br if" name |
           "return" |
           "call" name
```

The effect of arithmetic instructions and load/store instructions on m, g, s can be described by assignment statements. Let i be an integer, x is the name of a local or global variable, and loc(x) the index of variable x on the stack, to be made precise later:

instruction	effect	trap condition
i32/64.const i	s[sp], $sp := i$, $sp + 1$	<pre>sp < StackSize</pre>
i32/64.add	s[sp - 2], sp := s[sp - 2] + s[sp - 1], sp - 1	
i32/64.sub	s[sp - 2], sp := s[sp - 2] - s[sp - 1], sp - 1	
i32/64.mul	$s[sp - 2], sp := s[sp - 2] \times s[sp - 1], sp - 1$	
i32/64.div_s	s[sp - 2], sp := s[sp - 2] div s[sp - 1], sp - 1	s[sp - 1] = 0
i32/64.rem_s	$s[sp - 2], sp := s[sp - 2] \mod s[sp - 1], sp - 1$	s[sp - 1] = 0
i32/64.eqz	s[sp - 1] := s[sp - 1] = 0	
i32/64.eq	s[sp - 2], sp := s[sp - 2] = s[sp - 1], sp - 1	
i32/64.ne	$s[sp - 2], sp := s[sp - 2] \neq s[sp - 1], sp - 1$	
i32/64.lt_s	s[sp - 2], sp := s[sp - 2] < s[sp - 1], sp - 1	
i32/64.gt_s	s[sp - 2], sp := s[sp - 2] > s[sp - 1], sp - 1	
i32/64.le_s	$s[sp - 2], sp := s[sp - 2] \le s[sp - 1], sp - 1$	
i32/64.ge_s	$s[sp - 2], sp := s[sp - 2] \ge s[sp - 1], sp - 1$	
i32/64.load offset = n	s[sp - 1] := m[s[sp - 1] + n]	$0 \le s[sp - 1] + n < MemSize$
i32/64.store offset = n	m[s[sp - 2] + n], sp := s[sp - 1], sp - 2	$0 \le s[sp - 1] + n < MemSize$
local.get x	s[sp], sp := s[loc(x)], sp + 1	
local.set x	s[loc(x)], sp := s[sp - 1], sp - 1	
global.get x	s[sp], sp := g[loc(x)], sp + 1	
global.set x	g[loc(x)], sp := s[sp - 1], sp - 1	

Pushing on a full stack, dividing by zero, or accessing the memory outside its bounds is an error. In that case, the program traps,

meaning that it terminates and passes control to its environment.

A WebAssembly module can import functions, declare initialized global variables, define functions, declare the initial size of the memory, and designate one function as the start function that is executed when the module is loaded. The grammar is:

```
string ::= \" {char} \"
module ::= "(" "module" {import} {global} {func} [memory] [start] ")"
import ::= "(" "import" string string "(" "func" name func_type ")" ")"
global ::= "(" "global" name "(" "mut" num_type ")" instr ")"
memory ::= "(" "memory" num ")"
start ::= "(" "start" name ")"
```

In global variable declarations, the keyword mut specifies that the variable is mutable, otherwise it is a constant. The subsequent instructions have to initialize the variable with a value of matching type.

(module

)

(func \$program
 (local \$x i32)

(local \$y i32)

(import "P0lib" "write" (func \$write (param i32)))

(import "P0lib" "writeln" (func \$writeln))
(import "P0lib" "read" (func \$read (result i32)))

(func \$QuotRem (param \$x i32) (param \$y i32)

Executing WebAssembly

For P0 programs, we specify the following in WebAssembly modules:

- The standard library consists of the procedures write, writeln, and read; these have to be imported from the host environment.
- The size of the memory is specified as 1 page with 2¹⁶ bytes.
- The main program in P0 translates to a function \$program in WebAssembly and is designated as a the start function.

```
call $read
                                                           local.set $x
procedure QuotRem(x, y: integer)
                                                           call $read
    var q, r: integer
                                                           local.set $y
         q := 0; r := x
                                                           local.get $x
        while r \ge y do // q \times y + r = x \wedge r \ge y
                                                           local.get $y
             r := r - y; q := q + 1
                                                           call $QuotRem
        write(q); write(r)
                                                         (memory 1)
program arithmetic
                                                         (start $program)
  var x, y: integer
    x \leftarrow read(); y \leftarrow read()
    QuotRem(x, y)
```

WebAssembly programs can be run in a web browser through a JavaScript extension that is currently supported by all main web browsers. For this, the P0 standard library has to be implemented in JavaScript so it can be imported in WebAssembly. The library is a JavaScript structure P0lib with fields write, writeln, and read, which are all JavaScript functions. That structure is then collected with potentially other parameters (e.g. other libraries) in one JavaScript structure params:

```
const params = {
    P0lib: {
        write: i => this.append_stream({text: '' + i, name: 'stdout'}),
        writeln: () => this.append_stream({text: '\\n', name: 'stdout'}),
        read: () => window.prompt()
    }
}
```

The WebAssembly code is assumed to be in a binary WebAssembly file with url in JavaScript variable wasmfile. The JavaScript function fetch(wasmfile) reads that file, but does so asynchronously in the background, i.e. does not return the content of the file but rather a Promise<Response> that eventually resolves to the Response of the http request. To read the whole file as a binary sequence, the response has to be converted to an ArrayBuffer, as needed for execution with WebAssembly. The Promise method .then takes a function as a parameter; that function is called with the resolved value of the promise, response below, when the promise is resolved successfully (for treatment of errors, a .catch method is provided, which won't be used here). The function WebAssembly.compile takes an ArrayBuffer object, code below, and returns the executable module. That module is without state, i.e. can in principle be shared among multiple executions. The function WebAssembly.instantiate allocates the memory, sets up the stack, binds imported functions, and calls the start function of the module:

```
fetch(wasmfile)
    .then(response => response.arrayBuffer())
    .then(code => WebAssembly.compile(code))
    .then(module => WebAssembly.instantiate(module, params))
```

JavaScript can be executed in Jupyter notebooks by displaying HTML code with JavaScript in the web browser. The library IPython.core.display provides a Python function to that end. The JavaScript code for fetching a WebAssembly file and executing it with the standard P0 library are placed in the Python function runwasm(wasmfile):

```
In [ ]: def runwasm(wasmfile):
    from IPython.display import display, Javascript
    display(Javascript("""
```

```
const params = {
    P0lib: {
        write: i => this.append_stream({text: '' + i, name: 'stdout'}),
        writeln: () => this.append_stream({text: '\\n', name: 'stdout'}),
        read: () => window.prompt()
    }
}
fetch('""" + wasmfile + """') // asynchronously fetch file, return Response object
    .then(response => response.arrayBuffer()) // read the response to completion and stores it in an ArrayBuff.
    .then(code => WebAssembly.compile(code)) // compile (sharable) code.wasm
    .then(module => WebAssembly.instantiate(module, params)) // create an instance with memory
    // .then(instance => instance.exports.program()); // run the main program; not needed if start function specified.
```

For example, the complete textual WebAssembly file corresponding to the P0 program arithmetic is:

```
In [ ]: %writefile arithmetic.wat
        (module
           (import "Polib" "write" (func $write (param i32)))
           (import "POlib" "writeln" (func $writeln))
           (import "P0lib" "read" (func $read (result i32)))
           (func $QuotRem (param $x i32) (param $y i32)
            (local $q i32)
             (local $r i32)
            i32.const 0
            local.set $q
            local.get $x
            local.set $r
            loop $label0
              local.get $r
              local.get $y
              i32.ge_s
                local.get $r
                local.get $y
                i32.sub
                local.set $r
                local.get $q
                i32.const 1
                i32.add
                local.set $q
                br $label0
            end
            local.get $q
            call $write
            local.get $r
            call $write
          (func $program
             (local $x i32)
            (local $y i32)
            call $read
            local.set $x
            call $read
            local.set $y
            local.get $x
            local.get $y
            call $QuotRem
           (memory 1)
           (start $program)
```

That has to be converted to a binary form for execution:

```
In [ ]: !wat2wasm arithmetic.wat
```

Now the generate code can be executed. Note that the WebAssembly code runs natively on the computer on which the web browser runs, not on the Jupyter server, where the Python kernel runs:

```
In [ ]: runwasm("arithmetic.wasm")
```

Alternatively to running WebAssembly programs in the browser, programs can be interpreted by pywasm. In this case, Python is the host environment and provides an implementation of the standard library:

```
In [ ]: def runpywasm(wasmfile):
    def write(s, i): print(i)
    def writeln(s): print()
    def read(s): return int(input())
```

```
import pywasm
vm = pywasm.load(wasmfile, {'P0lib': {'write': write, 'writeln': writeln, 'read': read}})
In []: runpywasm("arithmetic.wasm")
```

The third option is to use Wasmer, which supports several compilers for compiling wasm to native code, including LLVM. The cell below uses the cranelift compiler, which reportedly run faster than LLVM, but does not generate as efficient code. With the Python binding of Wasmer, Python can the be host environment:

Translation Scheme for Expressions

The translation scheme for arithmetic expressions is:

E	code(E)	condition
X	local.get \$x	if x local variable
X	global.get \$x	if x global variable
n	i32.const n	if n integer constant
$E_1 \times E_2$	<pre>code(E₁) code(E₂) i32.mul</pre>	
E ₁ div E ₂	<pre>code(E₁) code(E₂) i32.div_s</pre>	
E ₁ mod E ₂	<pre>code(E₁) code(E₂) i32.rem_s</pre>	
+ E	code(E)	
- E	i32.const 0 code(E) i32.sub	
E ₁ + E ₂	<pre>code(E₁) code(E₂) i32.add</pre>	
E ₁ - E ₂	<pre>code(E₁) code(E₂) i32.sub</pre>	

For boolean expression, the translation scheme is analogous, except that no code is generated for the negation of a relational operation, only the relation is negated:

E	code(E)	E	cond(E)
Х	code(x)	not x	i32.const 1 code(x) i32.sub
$E_1 = E_2$	<pre>code(E₁) code(E₂) i32.eq</pre>	$not(E_1 = E_2)$	<pre>code(E₁) code(E₂) i32.ne</pre>
$E_1 \neq E_2$	<pre>code(E₁) code(E₂) i32.ne</pre>	$not(E_1 \neq E_2)$	<pre>code(E₁) code(E₂) i32.eq</pre>
$E_1 < E_2$	<pre>code(E₁) code(E₂) i32.lt_s</pre>	$not(E_1 < E_2)$	<pre>code(E₁) code(E₂) i32.ge_s</pre>
$E_1 \leq E_2$	<pre>code(E₁) code(E₂) i32.le_s</pre>	$not(E_1 \leq E_2)$	<pre>code(E₁) code(E₂) i32.gt_s</pre>
	code(E ₁)		code(E ₁)

Translation Scheme for Statements and Declarations

The translation scheme for P0 statements is:

S	code(S)	
X1,, Xn := E1,, En	code(E ₁) code(E _n) set \$x _n set \$x ₁	set is local.set for local variable and global.set for global variable
$x_1,, x_m \leftarrow p(E_1,, E_n)$	<pre>code(E₁) code(E_n) call \$p set \$x_m set \$x₁</pre>	set is local.set for local variable and global.set for global variable
S1;; Sn	code(S ₁) code(S _n)	
if E then S	<pre>code(E) if code(S) end</pre>	
if E then S_1 else S_2	<pre>code(E) if code(S1) else code(S2) end</pre>	
while E do S	<pre>loop \$L code(E) if code(S) br \$L end end</pre>	

The translation scheme for declarations is:

```
code(D)
var x: integer
                                                                 (local $x i32)
                                                                                                                     for local declaration
                                                                  (local $x i32)
var x: boolean
                                                                                                                     for local declaration
var x: integer
                                                                  (global $x (mut i32) i32.const 0)
                                                                                                                     for global declaration
var x: boolean
                                                                  (global x (mut i32) i32.const 0)
                                                                                                                     for global declaration
                                                                  (func $p (param $v<sub>1</sub> i32) ... (param
                                                                 $v<sub>n</sub> i32)
                                                                    (result i32) ... (result i32) (local $r<sub>1</sub> i32)
procedure p(v<sub>1</sub>: T<sub>1</sub>, ... , v<sub>n</sub>: T<sub>n</sub>) \rightarrow (r<sub>1</sub>: U<sub>1</sub>, ... ,
rm: Um)
D
S
                                                                                                                     if all T_i , U_j are integer or
                                                                    (local $rm i32)
                                                                    code(D)
                                                                                                                     boolean
                                                                    code(S)
                                                                    local.get $r1
                                                                    local.get $rm
                                                                  (module
                                                                    stdlibimport
                                                                    (func $program
program n
  D
                                                                      code(D)
  S
                                                                      code(S)
```

Above, stdlibimports stands for the import of the P0 standard library, which is:

```
(import "P0lib" "write" (func $write (param i32)))
(import "P0lib" "writeln" (func $writeln))
(import "P0lib" "read" (func $read (result i32)))
```

Binary WebAssembly Files

It is instructive to "reverse engineer" the binary WebAssembly file by converting it back to the textual form. In WebAssembly, comments are written as (;comment;) and by ;;comment for comments that extend until the end of the line:

```
In [ ]: !wasm2wat arithmetic.wasm
```

A copy of the output is to the right; it reveals what is stored in the binary format:

• Function parameters and local variables are referred to by numbers starting with 0, rather than by names. That is, in

```
procedure QuotRem(x, y: integer)
    var q, r: integer
    q := 0; r := x
    while r ≥ y do
        r := r - y; q := q + 1
    write(q); write(r)
```

variables $\ x$, $\ y$, $\ q$, $\ r$ are referred to by $\ 0$ to $\ 3$, respectively.

- Functions are referred to by numbers rather than names: functions write, writeln, read, QuotRem, program are referred to by 0 to 4, respectively.
- The function types are also numbered and referred to by their position number.
- The targets of br and br_if refer to the enclosing block
 ... end , loop ... end , if ... end by number: the closest one is 0 , the next closest one is 1 , etc. Recall that the only branches allowed to outer block and end instructions.

```
(module
  (type (;0;) (func (param i32)))
 (type (;1;) (func))
  (type (;2;) (func (result i32)))
  (type (;3;) (func (param i32 i32)))
  (import "P0lib" "write" (func (;0;) (type 0)))
  (import "P0lib" "writeln" (func (;1;) (type 1)))
 (import "P0lib" "read" (func (;2;) (type 2)))
  (global (;0;) (mut i32) (i32.const 0))
  (global (;1;) (mut i32) (i32.const 0))
  (func (;3;) (type 3) (param i32 i32)
   (local i32 i32)
   i32.const 0
   local.set 2
   local.get 0
   local.set 3
   loop ;; label = @1
     local.get 3
     local.get 1
     i32.ge_s
     if ;; label = @2
       local.get 3
       local.get 1
       i32.sub
       local.set 3
       local.get 2
       i32.const 1
       i32.add
       local.set 2
       br 1 (;@1;)
     end
   end
   local.get 2
   call 0
   local.get 3
   call 0)
 (func (;4;) (type 1)
   call 2
   global.set 0
   call 2
   qlobal.set 1
   global.get 0
   global.get 1
   call 3)
  (memory (;0;) 1)
  (start 4))
```

Translation Scheme for Boolean Operators

In P0 boolean operators and and or evaluate conditionally:

```
p and q = if p then q else false p or q = if p then true else q
```

As soon as the result is determined, the remaining operands are not evaluated. This way, expressions like

```
(i < N) and (a[i] \neq x)

(y = 0) or (x \text{ div } y = m)
```

will not evaluate the second half if the first half determines the result.

The WebAssembly if instruction is used for conditional evaluation:

```
if (a < b)
                 code(a)
                                    if (a < b)
                                                     code(a)
and (c = d)
                 code(b)
                                    or (c = d)
                                                     code(b)
                 i32.lt s
                                    or (e \ge f)
and (e \ge f)
                                                     i32.lt s
                 if (result i32)
                                                     if (result i32)
then S
                                    then S
                  code(c)
                                                     i32.const 1
                  code(d)
                                                     else
                  i32.eq
                                                      code(c)
```

```
else
                                     code(d)
i32.const 0
                                     i32.eq
                                    end
end
if (result i32)
                                    if (result i32)
code(e)
                                     i32.const 1
code(f)
                                    else
i32.ge_s
                                     code(e)
else
                                     code(f)
u32.const 0
                                     i32.ge_s
end
                                    end
if
                                    if
 code(S)
                                     code(S)
end
                                    end
```

E	code(E)
not E	<pre>code(E) i32.eqz</pre>
E ₁ and E ₂	<pre>code(E₁) if (result i32) code(E₂) else i32.const θ end</pre>
E ₁ or E ₂	<pre>code(E1) if (result i32) i32.const 1 else code(E2) end</pre>

This translation scheme generates for if a = b and c > d then S equivalent code as for if a = b then if c > d then S:

```
get a
             get b
             i32.eq
             if
               get c
if a = b
              get d
and c > d
               i32.gt_s
then S
             else
              i32.const 0
             end
             if
              code(S)
             end
             get a
             get b
             i32.eq
             if
if a = b
               aet c
then
               get d
 if c > d
               i32.gt_s
 then S
               if
                code(S)
               end
             end
```

This translation scheme leads 0 (for false) and 1 (for true) to be explicitly pushed on the stack. Alternatively, using the WebAssembly block instruction, conditional evaluation can be expressed with forward branches. Note how for conjunctions each condition is negated, for disjunctions only the last condition is negated. For while-statements, the loop instruction is used; branches in conditions go to the outer block instruction:

```
if (a < b)
                               if (a < b) block
                                                         while a < b
                                                                         block
             block
                                                          do S
and (c = d)
              code(a)
                               or (c = d)
                                            block
                                                                           loop
and (e \ge f)
              code(b)
                               or (e \ge f)
                                             code(a)
                                                                              code(a)
then S
                               then S
                                             code(b)
              i32.ge s
                                                                              code(b)
              br if 0
                                             i32.lt s
                                                                              i32.ge s
                                             br if 0
                                                                              br if 1
              code(c)
              code(d)
                                             code(c)
                                                                              code(S)
              i32.ne
                                             code(d)
                                                                              br 0
              br if 0
                                             i32.eq
                                                                           end
                                             br_if 0
                                                                         end
              code(e)
              code(f)
                                             code(e)
              i32.lt_s
                                             code(f)
              br if 0
                                             i32.lt s
              code(S)
                                             br_if 1
             end
                                            end
```

```
code(S)
```

These observations motivate following translation scheme: for boolean expression B that does not contain conditional boolean operators, code(B) specifies the WebAssembly instructions; for an expression B with a conditional boolean operator, condcode(B, L) specifies the WebAssembly instructions that branch to label L if the condition is false and "fall through" otherwise:

```
s
            code(S)
            block
if B
              condcode(B, 0)
then S
              code(S)
             block
              block
                 condcode(B, 0)
if B
                 code(S_1)
then S<sub>1</sub>
                br 1
else S<sub>2</sub>
              end
              code(S<sub>2</sub>)
             end
            block
              loop
                 condcode(B, 1)
while B
                 code(S)
do S
              end
            end
```

```
В
             condcode(B, L)
              condcode(not B<sub>1</sub>, L)
 Вı
              \quad \text{br if } L
 and ...
              condcode(not Bn, L)
and B_n
              br_if L
              block
                condcode(B<sub>1</sub>, 0)
                br if 0
 Вı
 or ...
                condcode(B_{n-1}, 0)
 \text{or } B_n
                br if 0
                condcode(not B_n, L + 1)
                br_if L + 1
```

Translation Scheme for Arrays

Global arrays are statically allocated consecutively in memory. Below, adr(x) = 0 and $adr(y) = adr(x) + size(A) = 0 + 7 \times 4 = 28$:

```
type A = [1..7] \rightarrow integer
                              (global $i (mut i32) i32.const 0)
var x: A
                              (global $h (mut i32) i32.const 0)
var y: A
                              (func $program
var i: integer
                                  i32.const 3
var h: integer
                                  global.set $i
                                  global.get $i
program p
    i := 3
                                  i32.const 1
                                                  ;; x.lower
    h := y[i]
                                  i32.sub
                                  i32.const 4
    x[i] := 5
                                                  ;; size(integer)
                                  i32.mul
                                  i32.const 28
                                                  ;; adr(y)
                                  i32.add
                                  i32.load
                                  global.set $h
                                  global.get i ;; x[i] := 5
                                   i32.const 1
                                  i32.sub
                                  i32.const 4
                                  i32.mul
                                  i32.const 0
                                  i32.add
                                  i32.const 5
                                   i32.store
                              )
```

The compiler uses variable memsize to keep track of statically allocated memory; it is initially 0. No code is generated for a variable declaration, rather the address is stored in field adr of the symbol table entry for the variable. With $A = [1 ... u] \rightarrow T$:

Local arrays are dynamically allocated in memory in a stack that mimics the calling stack. For local array x, local variable \$x of type i32 points to the address of x in memory. Global WebAssembly variable \$memsize points to the top of the stack. Each procedure has a local variable \$mp with the pointer the top of the stack before the allocation of local variables. In the procedure prologue, \$memsize is saved in \$mp and restored in the epilogue. Variable \$memsize is initially the size of all statically allocated arrays:

```
type A = [1..7] \rightarrow integer
                              (func $q
                                   (local $y i32)
var x: A
procedure q()
                                   (local $mp i32)
  var y: A
                                   global.get $memsize
    y[3] := 5
                                   local.set $mp
program p
                                   global.get $memsize
  var z: A
                                   local.tee $y
    q()
                                   i32.const 28
                                   i32.add
                                   global.set $memsize
                                   i32.const 3
                                  i32.const 1
                                   i32.sub
                                   i32.const 4
                                   i32.mul
                                   local.get $y
                                   i32.add
                                   i32.const 5
                                   i32.store
                                   local.get $mp
                                   global.set $memsize
                              (global $memsize (mut i32) i32.const 28)
                               (func $program
                                   (local $z i32)
                                   (local $mp i32)
                                   global.get $memsize
                                   local.set $mp
                                   global.get $memsize
                                   i32.const 28
                                   i32.add
                                   local.tee $z
                                   global.set $memsize
                                   call $q
                                   local.get $mp
                                   global.set $memsize
```

With $A = [1 ... u] \rightarrow T$, the translation scheme for programs with local array declarations is:

S

```
D
                                                                         code(D)
                                                                           (local $x i32)
                                                                           global.get $memsize
                                                                                                                                          local
var x: A
                                                                           local.tee $x
                                                                                                                                          declaration
                                                                           i32.const size(A)
                                                                           i32.add
                                                                          global.set $memsize
                                                                           (func $p (param $v<sub>1</sub> i32) ... (param $v<sub>n</sub> i32)
                                                                             (result i32) ... (result i32)
                                                                             (local $r1 i32)
                                                                             (local $rm i32)
                                                                             code(D)
procedure p(v<sub>1</sub>: T<sub>1</sub>, ..., v<sub>n</sub>: T<sub>n</sub>) \rightarrow (r<sub>1</sub>: U<sub>1</sub>, ..., r<sub>m</sub>:
                                                                             (local $mp i32)
U_m)
                                                                             global.get $memsize
   D
                                                                             local.set $mp
   S
                                                                             code(S)
                                                                             local.get $r1
                                                                             local.get $rm
                                                                             local.get $mp
                                                                             global.set $memsize
                                                                             stdlibimport
                                                                             code(D<sub>1</sub>)
                                                                             (global $memsize (mut i32) i32.const
                                                                         memsize)
                                                                             (func $program
                                                                               code(D<sub>2</sub>)
program n
                                                                               (local $mp i32)
  D<sub>2</sub>
```

global.get \$memsize

```
code(S)
local.get $mp
global.set $memsize
)
)
```

With $A = [1 .. u] \rightarrow T$, the translation scheme for array indexing and array assignment is:

```
code(E)
                            if x global variable
       i32.const x.adr
Х
        local.get $x
                            if x local variable
        code(E)
        i32.const x.lower
        i32.sub
i32.const size(A)
i32.mul
       code(x)
        i32.add
       i32.load
     s
                 code(S)
                  code(E)
                  i32.const x.lower
                  i32.sub
                  i32.const size(T)
     x[E] := F
                  i32.mul
                  code(x)
                  i32.add
                  code(F)
                  i32.store
                  code(x1)
                  code(x2)
     X_1 := X_2
                  i32.const size(T)
                  memory.copy
```

If s, d, n of type i32 are the top elements of the stack, the instruction memory.copy copies n bytes in memory starting at index s to index d.

When arrays are passed as value and result parameters, only a pointer to the array in memory is passed:

```
type A = [1..7] \rightarrow integer
                                (func $q (param $x i32) (result i32)
type B = [0 .. 1] \rightarrow A
                                   (local $y i32)
var b: B
                                    (local $mp i32)
procedure q(x: A) \rightarrow (y: A)
                                    global.get $memsize
   y := x
                                    local.set $mp
program p
                                    global.get $memsize
  b[0] \leftarrow q(b[1])
                                    local.tee $y
                                    i32.const 28
                                    i32.add
                                    global.set $memsize
                                    local.get $y
                                    local.get $x
                                    i32.const 28
                                    memory.copy
                                    local.get $mp
                                    global.set $memsize
                                    local.get $y
                                (global $memsize (mut i32) i32.const 56)
                                (func $program
                                    i32.const 0
                                    i32.const 28
                                    call $q
                                    i32.const 28
                                    memory.copy
```

Passing pointers leads to *aliasing* when two pointers point to the same address and modifications through one pointer are visible through the other pointer. To avoid aliasing,

- an array parameter passed by value is a local constant, rather than local variable; it has to be copied to a local variable before it can be updated,
- a global variable that is passed as a parameter must not be accessed as a global variable; this can be simply enforced by not allowing global variables altogether.

```
type A = [1..7] \rightarrow integer
```

Currently, P0 does not check for aliasing.

As a note, variations of above scheme are possible:

- If the size of all local arrays can be statically determined, \$memsize can be incremented by that amount in the procedure prologue and decremented in the epilogue without a need for local variable \$mp . While not strictly needed in P0, having \$mp allows more easily extensions with arrays of dynamic size and other dynamic data structures.
- If x is an array, in the call $x \leftarrow p()$ only the address of the result is returned and the caller copies the result to x. Alternatively, the callee can perform that copy, leading to less duplication of copying code. For this, the address of x has to be passed as an additional parameter, as in the call p(x).

Translation Scheme for Records

Like arrays, records are allocated consecutively in memory. Below, adr(x) = 0 and $adr(y) = adr(x) + size([1 .. 7] \rightarrow R) = 7 \times size(R) = 7 \times 8 = 56$:

```
type R = (f: integer, g: integer)
                                     (func $program
var x: [1 ... 7] \rightarrow R
                                         (local $i i32)
var y: R
                                         i32.const 3 ;; 3
program p
                                         local.set $i
    var i: integer
                                         local.get $i
        i := 3
                                         i32.const 1 ;; x.lower
        x[i].g := 5
                                         i32.sub
        y.f := 7
                                         i32.const 8
                                                        ;; size(R)
                                         i32.mul
                                         i32.const 0
                                                        ;; adr(x)
                                         i32.add
                                         i32.const 4
                                                        ;; offset(g)
                                         i32.add
                                         i32.const 5
                                                        ;; 5
                                         i32.store
                                         i32.const 56
                                                        ;; adr(y) + offset(f)
                                         i32.const 7
                                                         ;; 7
                                         i32.store
```

No code is generated for a variable declaration, but the address is stored as a field of the symbol table entry for the variable. With $R = (f_1: T_1, f_2: T_2, ...)$:

```
D code(D) effect

var x: R x.adr := memsize; memsize := memsize + size(R)
```

Assume that the address of x is on the stack. The the code for x.f updates that address:

```
code(E)
x.f i32.const offset(f)
i32.add
```

Translation Scheme for Exceptions

```
try
                    try $10
    write(3)
                      i32.const 3
    throw
                      call $write
                      throw $10
    write(5)
                      i32.const 5
    write(7)
                      call $write
write(9)
                    catch
                      drop
                      i32.const 7
                      call $write
                    end
                    i32.const 9
                    call $write
```

```
(module
          (import "POlib" "write" (func $write (param i32)))
          (import "POlib" "writeln" (func $writeln))
          (import "P0lib" "read" (func $read (result i32)))
          (tag $e)
          (func $q (param $x i32) (result i32)
            throw $e
            local.get $x
          (func $program
            try
              i32.const 3
              call $q
              call $write
            catch $e
              i32.const 7
              call $write
            end
          (memory 1)
          (start $program)
In []: !wat2wasm --enable-exceptions exception.wat
        To run this in Chrome, Experimental WebAssembly has to be enabled under chrome://flags:
            try
                                     try $10
                try
                                       i32.const 3
                    write(3)
                                       call $write
                    throw
                                       throw $10
                                       i32.const 5
                    write(5)
```

In []: runwasm("exception.wasm")

```
catch
                         call $write
       write(7)
                       catch
    write(9)
                         drop
                         i32.const 7
    throw
    write(11)
                         call $write
catch
                       end
   write(13)
                       i32.const 9
write(15)
                       call $write
```

```
In [ ]: %writefile exception.wat
        (module
          (import "P0lib" "write" (func $write (param i32)))
           (import "POlib" "writeln" (func $writeln))
          (import "P0lib" "read" (func $read (result i32)))
           (tag $e)
         (func $q (param $x i32) (result i32)
            (local $y i32)
            i32.const 1
            call $write
            try
              try
                i32.const 3
                call $write
                throw $e
                i32.const 5
                call $write
              catch $e
                i32.const 7
                call $write
              end
              i32.const 9
              call $write
              throw $e
              i32.const 11
              call $write
            catch $e
              i32.const 13
              call $write
            end
            i32.const 15
          (func $program
            i32.const 1
            call $q
            call $write
```

```
(memory 1)
  (start $program)
)

In []: !wat2wasm --enable-exceptions exception.wat

To run this in Chrome, Experimental WebAssembly has to be enabled under chrome://flags:

In []: runwasm("exception.wasm")

In []: runwasmer("exception.wasm")
```

SIMD Operations

Bulk Memory Operations

Loading [MathJax]/jax/output/CommonHTML/fonts/TeX/fontdata.js