

Solve the absolute value problems.

1. $|x - 2| < 8$

Solution:

$$\begin{aligned} |x - 2| < 8 &\implies -8 < x - 2 < 8 \\ &\implies -6 < x < 10 \end{aligned}$$

In interval form, this is $\boxed{(-6, 10)}$.

2. $|8x - 2| > 9$

Solution:

$$\begin{aligned} |8x - 2| > 9 &\implies 8x - 2 > 9 \quad \text{or} \quad 8x - 2 < -9 \\ &\implies x > \frac{11}{8} \quad \text{or} \quad x < -\frac{7}{8} \end{aligned}$$

In interval form, this is $\boxed{\left(-\infty, -\frac{7}{8}\right) \cup \left(\frac{11}{8}, \infty\right)}$.

3. $\sqrt{16x^2} \leq 24$

Solution:

Notice: $\sqrt{a^2} = |a| \implies \sqrt{16x^2} = |4x|$

$$\begin{aligned} |4x| \leq 24 &\implies -24 \leq 4x \leq 24 \\ &\implies -6 \leq x \leq 6 \end{aligned}$$

In interval form, this is $\boxed{[-6, 6]}$.

4. $|7 - x| > 60$

Solution:

$$\begin{aligned} |7 - x| > 60 &\implies 7 - x > 60 \quad \text{or} \quad 7 - x < -60 \\ &\implies x < -53 \quad \text{or} \quad x > 67 \end{aligned}$$

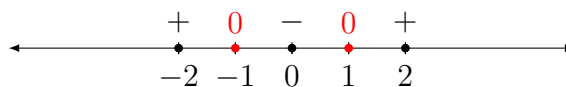
In interval form, this is $\boxed{(-\infty, -53) \cup (67, \infty)}$.

5. $|x^2 - 5| < 4$

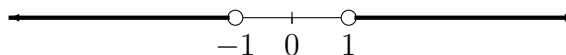
Solution:

$$|x^2 - 5| < 4 \implies -4 < x^2 - 5 < 4 \implies 1 < x^2 \text{ and } x^2 < 9$$

Since $x^2 > 1 \implies x^2 - 1 > 0 \implies (x - 1)(x + 1) > 0$, we can set up a sign chart with $x = \pm 1$ and test to see on which intervals the product $(x - 1)(x + 1)$ is positive.

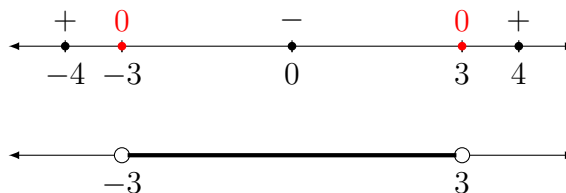


This gives us the following number line:



In interval notation, this is $(-\infty, -1) \cup (1, \infty)$.

Since $x^2 < 9 \implies x^2 - 9 < 0 \implies (x - 3)(x + 3) < 0$, we can set up another sign chart.



Since x needs to satisfy **both** inequalities, we consider the intersection of these two intervals:

$$\boxed{(-3, -1) \cup (1, 3)}$$