Solve the inequalities for x.

1.
$$6 - 7x > 4$$

Solution:

Rearranging, we have

$$-7x > -2 \implies x < \frac{2}{7}.$$

In interval notation, this is $\left(-\infty, \frac{2}{7}\right)$.

2.
$$5x + 2 > -3x - 4$$

Solution:

Rearranging, we have

$$8x > -6 \implies x > -\frac{3}{4}$$

In interval notation, this is $\left(-\frac{3}{4}, \infty\right)$.

3.
$$x^2 - 3x - 4 \le 0$$

Solution:

Factoring,

$$x^2 - 3x - 4 \le 0 \implies (x - 3)(x + 2) \le 0$$

Creating a sign chart, we look for intervals around x=-2 and x=3 where the product is positive:

The correct interval is then [-2,3].

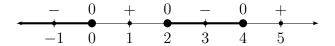
4.
$$x^3 < 6x^2 - 8x$$

Solution:

Rearranging,

$$x^{3} \leq 6x^{2} - 8x \implies x^{3} - 6x^{2} + 8x \leq 0$$
$$\implies x(x - 2)(x - 4) \leq 0$$

Creating a sign chart, we have



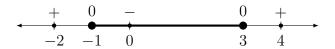
The correct interval is then $(-\infty, 0] \cup [2, 4]$

5.
$$\frac{(x-2)(x-1)}{5-x} \le 1$$

Solution:

If 5 - x > 0 (i.e. x < 5), we have

$$x^{2} - 3x + 2 \le (5 - x)$$
 \implies $x^{2} - 2x - 3 \le 0$
 \implies $(x - 3)(x + 1) \le 0$



This gives us the interval [-1,3].

If 5 - x < 0 (i.e. x > 5), we have

$$x^{2} - 3x + 2 \ge 5 - x \implies x^{2} - 2x - 3 \ge 0$$
$$\implies (x - 3)(x + 1) \ge 0$$

The interval $(-\infty, -1) \cup (3, \infty)$ satisfies $(x-3)(x+1) \ge 0$. Incorporating our assumption that x > 5, we have $(5, \infty)$.

Putting these together, we have $[-1,3] \cup (5,\infty)$.